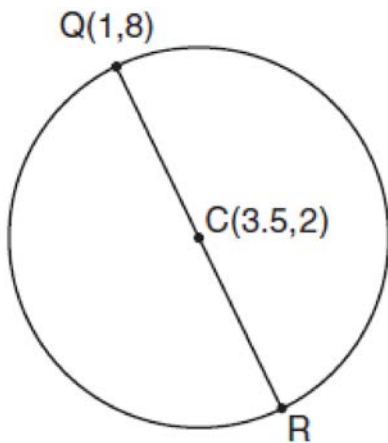


**G.GPE.B.4: Circles in the Coordinate Plane**

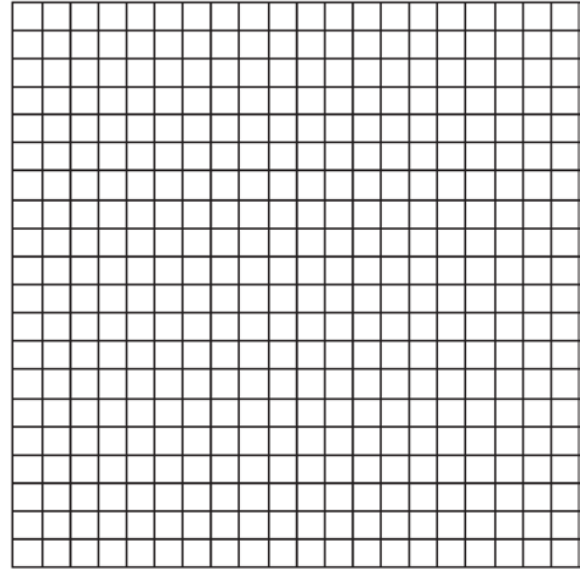
- 1 What are the coordinates of the center of a circle if the endpoints of its diameter are  $A(8,-4)$  and  $B(-3,2)$ ?
  - 1)  $(2.5, 1)$
  - 2)  $(2.5, -1)$
  - 3)  $(5.5, -3)$
  - 4)  $(5.5, 3)$
  
- 2 Segment  $AB$  is the diameter of circle  $M$ . The coordinates of  $A$  are  $(-4, 3)$ . The coordinates of  $M$  are  $(1, 5)$ . What are the coordinates of  $B$ ?
  - 1)  $(6, 7)$
  - 2)  $(5, 8)$
  - 3)  $(-3, 8)$
  - 4)  $(-5, 2)$
  
- 3 Line segment  $AB$  is a diameter of circle  $O$  whose center has coordinates  $(6, 8)$ . What are the coordinates of point  $B$  if the coordinates of point  $A$  are  $(4, 2)$ ?
  - 1)  $(1, 3)$
  - 2)  $(5, 5)$
  - 3)  $(8, 14)$
  - 4)  $(10, 10)$
  
- 4 The center of circle  $Q$  has coordinates  $(3, -2)$ . If circle  $Q$  passes through  $R(7, 1)$ , what is the length of its diameter?
  - 1) 50
  - 2) 25
  - 3) 10
  - 4) 5
  
- 5 In circle  $O$ , a diameter has endpoints  $(-5, 4)$  and  $(3, -6)$ . What is the length of the diameter?
  - 1)  $\sqrt{2}$
  - 2)  $2\sqrt{2}$
  - 3)  $\sqrt{10}$
  - 4)  $2\sqrt{41}$
  
- 6 In the coordinate plane, the points  $(2, 2)$  and  $(2, 12)$  are the endpoints of a diameter of a circle. What is the length of the radius of the circle?
  - 1) 5
  - 2) 6
  - 3) 7
  - 4) 10
  
- 7 A circle whose center is the origin passes through the point  $(-5, 12)$ . Which point also lies on this circle?
  - 1)  $(10, 3)$
  - 2)  $(-12, 13)$
  - 3)  $(11, 2\sqrt{12})$
  - 4)  $(-8, 5\sqrt{21})$
  
- 8 A circle has a center at  $(1, -2)$  and radius of 4. Does the point  $(3.4, 1.2)$  lie on the circle? Justify your answer.

- 9 In circle  $O$ , diameter  $\overline{RS}$  has endpoints  $R(3a, 2b - 1)$  and  $S(a - 6, 4b + 5)$ . Find the coordinates of point  $O$ , in terms of  $a$  and  $b$ . Express your answer in simplest form.

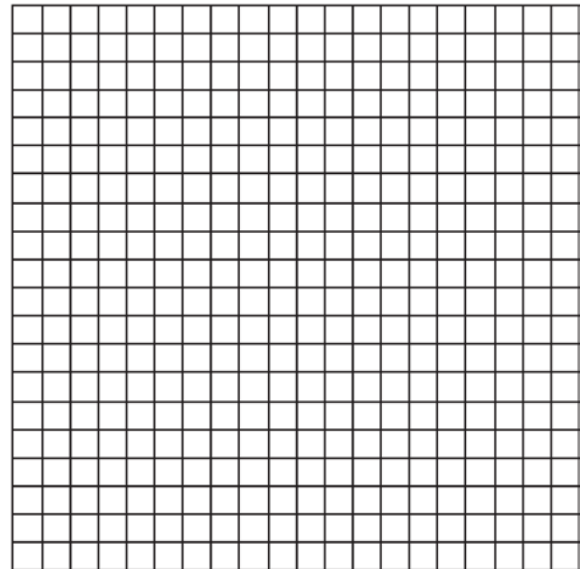
- 10 In the diagram below of circle  $C$ ,  $\overline{QR}$  is a diameter, and  $Q(1, 8)$  and  $C(3.5, 2)$  are points on a coordinate plane. Find and state the coordinates of point  $R$ .



- 11 In a circle whose center is  $(2, 3)$ , one endpoint of a diameter is  $(-1, 5)$ . Find the coordinates of the other endpoint of that diameter. [The use of the accompanying grid is optional.]



- 12 On the accompanying grid, graph a circle whose center is at  $(0, 0)$  and whose radius is 5. Determine if the point  $(5, -2)$  lies on the circle.



**G.GPE.B.4: Circles in the Coordinate Plane**  
**Answer Section**

1 ANS: 2

$$M_x = \frac{8+(-3)}{2} = 2.5. \quad M_y = \frac{-4+2}{2} = -1.$$

REF: 061312ge

2 ANS: 1

$$1 = \frac{-4+x}{2}. \quad 5 = \frac{3+y}{2}.$$

$$-4+x = 2 \quad 3+y = 10$$

$$x = 6 \quad y = 7$$

REF: 081115ge

3 ANS: 3

$$6 = \frac{4+x}{2}. \quad 8 = \frac{2+y}{2}.$$

$$4+x = 12 \quad 2+y = 16$$

$$x = 8 \quad y = 14$$

REF: 011305ge

4 ANS: 3

$$r = \sqrt{(7-3)^2 + (1-(-2))^2} = \sqrt{16+9} = 5$$

REF: 061503geo

5 ANS: 4

$$d = \sqrt{(-5-3)^2 + (4-(-6))^2} = \sqrt{64+100} = \sqrt{164} = \sqrt{4} \sqrt{41} = 2\sqrt{41}$$

REF: 011121ge

6 ANS: 1

Because the diameter is parallel to the  $y$ -axis, the length of the diameter may be calculated by subtracting the  $y$  values. If the diameter is  $12 - 2 = 10$ , the radius is 5.

REF: 010426a

7 ANS: 3

$$\sqrt{(-5)^2 + 12^2} = \sqrt{169} \quad \sqrt{11^2 + (2\sqrt{12})^2} = \sqrt{121 + 48} = \sqrt{169}$$

REF: 011722geo

8 ANS:

$$\text{Yes. } (x-1)^2 + (y+2)^2 = 4^2$$

$$(3.4-1)^2 + (1.2+2)^2 = 16$$

$$5.76 + 10.24 = 16$$

$$16 = 16$$

REF: 081630geo

9 ANS:

$$(2a-3, 3b+2) \cdot \left( \frac{3a+a-6}{2}, \frac{2b-1+4b+5}{2} \right) = \left( \frac{4a-6}{2}, \frac{6b+4}{2} \right) = (2a-3, 3b+2)$$

REF: 061134ge

10 ANS:

$$(6, -4) \cdot C_x = \frac{Q_x + R_x}{2} \cdot C_y = \frac{Q_y + R_y}{2}$$

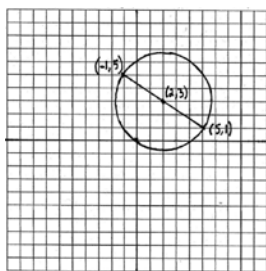
$$3.5 = \frac{1 + R_x}{2} \quad 2 = \frac{8 + R_y}{2}$$

$$7 = 1 + R_x \quad 4 = 8 + R_y$$

$$6 = R_x \quad -4 = R_y$$

REF: 011031ge

11 ANS:



$$(5, 1) \cdot C_x = \frac{A_x + B_x}{2} \cdot C_y = \frac{A_y + B_y}{2}$$

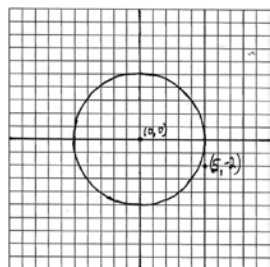
$$2 = \frac{-1 + R_x}{2} \quad 3 = \frac{5 + R_y}{2}$$

$$4 = -1 + R_x \quad 6 = 5 + R_y$$

$$5 = R_x \quad 1 = R_y$$

REF: 010633a

12 ANS:



The point  $(5, -2)$  does not lie on the circle.

REF: 080230a