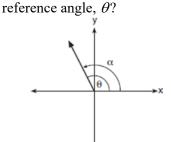
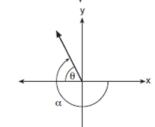
## F.TF.A.2: Reference Angles

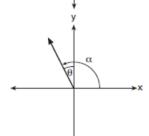
1 Which diagram represents an angle,  $\alpha$ , measuring  $\frac{13\pi}{20}$  radians drawn in standard position, and its



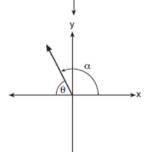
1)



2)



3)



- 4)
- 2 Sin 190° is equal to
  - 1) sin 10°
  - 2) cos 10°
  - 3) -sin 10°
  - 4) -cos 10°

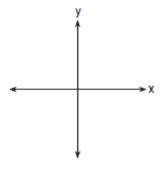
- 3 Which expression is equivalent to  $\sin(200^\circ)$ ?
  - $-\sin 20^{\circ}$
  - 2) cos 20°
  - 3)  $\cos 70^{\circ}$
  - 4)  $-\sin 70^{\circ}$
- 4 Expressed as a function of a positive acute angle, sin 230° is equal to
  - $-\sin 40^{\circ}$
  - $-\sin 50^{\circ}$
  - 3) sin 40°
  - 4)  $\sin 50^{\circ}$
- 5 The expression sin 240° is equivalent to
  - 1) sin 60°
  - 2)  $\cos 60^{\circ}$
  - $-\sin 60^{\circ}$
  - 4)  $-\cos 60^{\circ}$
- 6 Which expression is equivalent to  $\sin(-120^{\circ})$ ?
  - 1) sin 60°
  - $-\sin 60^{\circ}$
  - 3)  $\cos 30^{\circ}$
  - 4)  $-\cos 60^{\circ}$
- 7 Expressed as a function of a positive acute angle,  $\sin(-230^\circ)$  is equal to
  - 1)  $\sin 50^{\circ}$
  - $-\sin 50^{\circ}$
  - 3)  $\cos 50^{\circ}$
  - 4)  $-\cos 50^{\circ}$
- 8 Which expression is *not* equivalent to sin 150°?
  - 1) sin 30°
  - 2) -sin 210°
  - 3)  $\cos 60^{\circ}$
  - 4)  $-\cos 60^{\circ}$

Regents Exam Questions F.TF.A.2: Reference Angles www.jmap.org

Name: \_\_\_\_\_

- 9 Which expression is equivalent to cos 120°?
  - 1)  $\cos 60^{\circ}$
  - 2) cos 30°
  - $-\sin 60^{\circ}$
  - 4)  $-\sin 30^{\circ}$
- 10 Two straight roads intersect at an angle whose measure is 125°. Which expression is equivalent to the cosine of this angle?
  - 1) cos 35°
  - 2)  $-\cos 35^{\circ}$
  - 3)  $\cos 55^{\circ}$
  - 4)  $-\cos 55^{\circ}$
- 11 Expressed as a function of a positive acute angle,  $cos(-305^{\circ})$  is equal to
  - 1) -cos 55°
  - 2) cos 55°
  - 3)  $-\sin 55^{\circ}$
  - 4)  $\sin 55^{\circ}$
- 12 The expression tan(-240°) is equivalent to
  - 1) tan 60°
  - 2) -tan 30°
  - $-\tan 60^{\circ}$
  - 4) tan 30°
- 13 Expressed as a function of a positive acute angle, cot(-120)° is equivalent to
  - 1) -tan 60°
  - 2) cot 60°
  - 3)  $-\cot 30^{\circ}$
  - 4) cot 30°
- 14 The expression cot(-200°) is equivalent to
  - 1) -tan 20°
  - 2) tan 70°
  - 3) -cot 20°
  - 4) cot 70°

- 15 Express  $\sin(-170^\circ)$  as a function of a positive acute angle.
- 16 Express sin(-215°) as a function of a positive acute angle.
- 17 Express  $\cos(-155^{\circ})$  as a function of a positive acute angle.
- 18 Express cos(-220°) as a function of a positive acute angle.
- 19 Express tan 230° as a function of a positive acute angle.
- 20 Express tan(-140°) as a function of a positive acute angle.
- 21 Sketch an angle of 250° in standard position and then express cos 250° as a cosine function of a positive acute angle.



## F.TF.A.2: Reference Angles Answer Section

1 ANS: 4 REF: 081707aii 2 ANS: 3 REF: 068429siii 3 ANS: 1 REF: 088915siii 4 ANS: 2 REF: 081515a2 5 ANS: 3 REF: 010418siii

6 ANS: 2

The choices were originally: 1)  $\sin 60^\circ$ ; 2)  $-\sin 60^\circ$ ; 3)  $\cos 30^\circ$ ; 4)  $-\cos 30^\circ$ , so that (2) and (4) were correct responses.

REF: 018919siii

7 ANS: 1

Expressed as a positive angle,  $\sin(-230) = \sin 130$ . -230 + 360 = 130. For the reference angle of a Quadrant II angle,  $\sin \theta = \sin(180 - \theta) = \sin(180 - 130) = \sin 50$ .

REF: 060503b

8 ANS: 4 REF: 010120siii 9 ANS: 4 REF: 060215siii

10 ANS: 4

$$\cos \theta = -\cos(180^{\circ} - \theta)$$

The terminal side of the angle lies in Quadrant II.  $\cos 125 = -\cos(180 - 125)$ 

$$= -\cos 55^{\circ}$$

REF: 080511b

11 ANS: 2

$$\cos(-305^{\circ} + 360^{\circ}) = \cos(55^{\circ})$$

REF: 061104a2

12 ANS: 3 REF: 068535siii 13 ANS: 2 REF: 080330siii 14 ANS: 3 REF: 069933siii

15 ANS:

 $-\sin 10^{\circ} \text{ or } -\cos 80^{\circ}$ 

REF: 068014siii

16 ANS:

sin 35° or cos 55°

REF: 068617siii

17 ANS:

 $-\sin 65^{\circ}$  or  $-\cos 25^{\circ}$ 

REF: 088416siii

18 ANS:

 $-\cos 40^{\circ} \text{ or } -\sin 50^{\circ}$ 

REF: 018406siii

19 ANS:

tan 50° or cot 40°

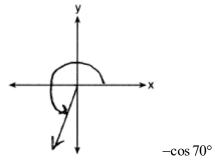
REF: 068811siii

20 ANS:

 $\tan 40^{\circ} \text{ or } \cot 50^{\circ}$ 

REF: 068912siii

21 ANS:



REF: 011734a2