

**F.IF.B.4: Evaluating Logarithmic Expressions**

1 The expression  $\log_8 64$  is equivalent to

- 1) 8
- 2) 2
- 3)  $\frac{1}{2}$
- 4)  $\frac{1}{8}$

2 The expression  $\log_5 \left( \frac{1}{25} \right)$  is equivalent to

- 1)  $\frac{1}{2}$
- 2) 2
- 3)  $-\frac{1}{2}$
- 4) -2

3 The loudness of sound is measured in units called decibels (dB). These units are measured by first assigning an intensity  $I_0$  to a very soft sound that is called the threshold sound. The sound to be measured is assigned an intensity,  $I$ , and the decibel rating,  $d$ , of this sound is found using  $d = 10 \log \frac{I}{I_0}$ . The threshold sound audible to the average person is  $1.0 \times 10^{-12}$  W/m<sup>2</sup> (watts per square meter). Consider the following sound level classifications:

Moderate	45-69 dB
Loud	70-89 dB
Very Loud	90-109 dB
Defeating	>110 dB

How would a sound with intensity  $6.3 \times 10^{-3}$  W/m<sup>2</sup> be classified?

- 1) moderate
- 2) loud
- 3) very loud
- 4) deafening

4 If  $\log_9 81 = x$ , find  $x$ .

5 Find the value of  $n$ :  $\log_{100} 10,000 = n$

6 For what value of  $k$  will the graph of  $y = \log_{10} x$  contain the point  $(1, k)$ ?

7 Complete the table below for the values of  $y$  for the equation  $y = \log_2 x$ .

$x$	$\frac{1}{4}$	$\frac{1}{2}$	1	2	4
$y$					

- 8 If  $x = \log_2 9$ , find, to the *nearest tenth*, the value of  $x$ .
- 9 If  $\log_3 5 = x$ , find  $x$  to the *nearest tenth*.
- 10 Solve for  $x$  to the *nearest hundredth*:  $\log_7 75 = x$
- 11 Find the value of  $\log 58.43$  to four decimal places.
- 12 Find the value of  $\log 429.7$  correct to *four decimal places*.
- 13 Find  $\log 742.6$  to the *nearest ten-thousandth*.
- 14 Find  $\log 1985$  to *four* decimal places.
- 15 Find  $\log 2001$  to the *nearest ten-thousandth*.
- 16 The scientists in a laboratory company raise amebas to sell to schools for use in biology classes. They know that one ameba divides into two amebas every hour and that the formula  $t = \log_2 N$  can be used to determine how long in hours,  $t$ , it takes to produce a certain number of amebas,  $N$ . Determine, to the *nearest tenth of an hour*, how long it takes to produce 10,000 amebas if they start with one ameba.
- 17 Evaluate  $e^{x \ln y}$  when  $x = 3$  and  $y = 2$ .
- 18 The expression  $\log_2(x - 4)$  is undefined for all values of  $x$  such that
- |            |               |
|------------|---------------|
| 1) $x > 1$ | 3) $x \leq 4$ |
| 2) $x > 0$ | 4) $x \leq 0$ |
- 19 The expression  $\log_3(8 - x)$  is defined for all values of  $x$  such that
- |               |               |
|---------------|---------------|
| 1) $x > 8$    | 3) $x < 8$    |
| 2) $x \geq 8$ | 4) $x \leq 8$ |

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### Answer Section

1 ANS: 2

$$8^2 = 64$$

REF: fall0909a2

2 ANS: 4 REF: 011124a2

3 ANS: 3

$$d = 10 \log \frac{6.3 \times 10^{-3}}{1.0 \times 10^{-12}} \approx 98$$

REF: 011715a2

4 ANS:

2

REF: 068110siii

5 ANS:

2

REF: 019407siii

6 ANS:

0

REF: 088508siii

7 ANS:

$x$	$\frac{1}{4}$	$\frac{1}{2}$	1	2	4
$y$	-2	-1	0	1	2

REF: 019742siii

8 ANS:

3.2

REF: 018941siii

9 ANS:

1.5

REF: 088637siii

10 ANS:

2.22

REF: 089940siii

11 ANS:

1.7666

REF: 018412siii

12 ANS:  
2.6332

REF: 068114siii

13 ANS:  
2.8708

REF: 018503siii

14 ANS:  
3.2978

REF: 068507siii

15 ANS:  
3.3012

REF: 088613siii

16 ANS:  
 $t = \log_2 10000$

$$2^t = 10000$$

$$13.3. \log 2^t = \log 10000$$

$$t \log 2 = \log 10000$$

$$t = \frac{\log 10000}{\log 2} \approx 13.3$$

REF: 060125b

17 ANS:  
 $e^{3 \ln 2} = e^{\ln 2^3} = e^{\ln 8} = 8$

REF: 061131a2

18 ANS: 3                      REF: fall9904b

19 ANS: 3                      REF: 010412b