

Calculus Practice: Use Derivatives to Analyze Functions 6b**For each problem, find the x-coordinates of all points of inflection.**

1) $f(x) = x^5 - 2x^3 + 3$

2) $y = -2x^2 + 12x - 17$

3) $f(x) = -x^5 + 2x^3 - 2$

4) $y = x^2 + 4x + 1$

5) $y = -x^5 + 2x^3 + 3$

6) $y = x^5 - 2x^3$

7) $f(x) = -x^3 + 2x^2 - 4$

8) $y = x^5 - 3x^3 - 2$

$$9) \ f(x) = x^4 - 4x^2 + 1$$

$$10) \ f(x) = x^3 - 11x^2 + 39x - 41$$

$$11) \ f(x) = -x^3 - 4x^2 - 4x$$

$$12) \ y = x^3 - 15x^2 + 72x - 113$$

$$13) \ f(x) = -x^3 + 15x^2 - 72x + 111$$

$$14) \ y = \frac{x^2}{2} - 2x - 2$$

$$15) \ y = -x^5 + 3x^3 + 1$$

$$16) \ y = x^3 - 4x^2 + 4$$

Calculus Practice: Use Derivatives to Analyze Functions 6b**For each problem, find the x-coordinates of all points of inflection.**

1) $f(x) = x^5 - 2x^3 + 3$

Inflection points at: $x = -\frac{\sqrt{15}}{5}, 0, \frac{\sqrt{15}}{5}$

2) $y = -2x^2 + 12x - 17$

No inflection points exist.

3) $f(x) = -x^5 + 2x^3 - 2$

Inflection points at: $x = -\frac{\sqrt{15}}{5}, 0, \frac{\sqrt{15}}{5}$

4) $y = x^2 + 4x + 1$

No inflection points exist.

5) $y = -x^5 + 2x^3 + 3$

Inflection points at: $x = -\frac{\sqrt{15}}{5}, 0, \frac{\sqrt{15}}{5}$

6) $y = x^5 - 2x^3$

Inflection points at: $x = -\frac{\sqrt{15}}{5}, 0, \frac{\sqrt{15}}{5}$

7) $f(x) = -x^3 + 2x^2 - 4$

Inflection point at: $x = \frac{2}{3}$

8) $y = x^5 - 3x^3 - 2$

Inflection points at: $x = -\frac{3\sqrt{10}}{10}, 0, \frac{3\sqrt{10}}{10}$

$$9) \ f(x) = x^4 - 4x^2 + 1$$

Inflection points at: $x = -\frac{\sqrt{6}}{3}, \frac{\sqrt{6}}{3}$

$$10) \ f(x) = x^3 - 11x^2 + 39x - 41$$

Inflection point at: $x = \frac{11}{3}$

$$11) \ f(x) = -x^3 - 4x^2 - 4x$$

Inflection point at: $x = -\frac{4}{3}$

$$12) \ y = x^3 - 15x^2 + 72x - 113$$

Inflection point at: $x = 5$

$$13) \ f(x) = -x^3 + 15x^2 - 72x + 111$$

Inflection point at: $x = 5$

$$14) \ y = \frac{x^2}{2} - 2x - 2$$

No inflection points exist.

$$15) \ y = -x^5 + 3x^3 + 1$$

Inflection points at: $x = -\frac{3\sqrt{10}}{10}, 0, \frac{3\sqrt{10}}{10}$

$$16) \ y = x^3 - 4x^2 + 4$$

Inflection point at: $x = \frac{4}{3}$