

Calculus Practice: Use Derivatives to Analyze Functions 5a

For each problem, find the open intervals where the function is increasing and decreasing.

1) $y = (-3x + 15)^{\frac{1}{2}}$

- A) Increasing: $(-\infty, 5)$ Decreasing: No intervals exist
 B) Increasing: $(-\infty, 3)$ Decreasing: $(3, \infty)$
 C) Increasing: No intervals exist. Decreasing: $(-\infty, 5)$
 D) Increasing: $(-\infty, 2)$ Decreasing: $(2, \infty)$

2) $y = -\frac{x^2}{4x - 8}$

- A) Increasing: $(-\infty, \frac{1}{3}), (\frac{4}{3}, \infty)$ Decreasing: $(\frac{1}{3}, \frac{2}{3}), (\frac{2}{3}, \frac{4}{3})$
 B) Increasing: $(4, 8), (8, 16)$ Decreasing: $(-\infty, 4), (16, \infty)$
 C) Increasing: $(0, 2), (2, 4)$ Decreasing: $(-\infty, 0), (4, \infty)$
 D) Increasing: $(-\infty, 0), (4, \infty)$ Decreasing: $(0, 2), (2, 4)$

3) $y = \frac{1}{6}x^{\frac{7}{3}} - \frac{14}{3}x^{\frac{1}{3}} - 2$

- A) Increasing: $(-\infty, -8), (8, \infty)$ Decreasing: $(-8, 8)$
 B) Increasing: $(-\frac{2}{3}, \frac{2}{3})$ Decreasing: $(-\infty, -\frac{2}{3}), (\frac{2}{3}, \infty)$
 C) Increasing: $(-\infty, -2), (2, \infty)$ Decreasing: $(-2, 2)$
 D) Increasing: $(-2, 2)$ Decreasing: $(-\infty, -2), (2, \infty)$

4) $f(x) = -\frac{9x^2 - 9}{x^3}$

- A) Increasing: $(-\frac{\sqrt{3}}{3}, \frac{1}{3}), (\frac{1}{3}, \frac{\sqrt{3}}{3})$ Decreasing: $(-\infty, -\frac{\sqrt{3}}{3}), (\frac{\sqrt{3}}{3}, \infty)$
 B) Increasing: $(-\infty, -4\sqrt{3}), (4\sqrt{3}, \infty)$ Decreasing: $(-4\sqrt{3}, 4), (4, 4\sqrt{3})$
 C) Increasing: $(-\infty, -\sqrt{3}), (\sqrt{3}, \infty)$ Decreasing: $(-\sqrt{3}, 0), (0, \sqrt{3})$
 D) Increasing: $(-\sqrt{3}, 0), (0, \sqrt{3})$ Decreasing: $(-\infty, -\sqrt{3}), (\sqrt{3}, \infty)$

5) $f(x) = -2\sec(x); [-\pi, \pi]$

- A) Increasing: $(-\pi, -\frac{\pi}{2}), (-\frac{\pi}{2}, 0), (0, \frac{\pi}{2}), (\frac{\pi}{2}, \pi)$ Decreasing: No intervals exist
 B) Increasing: $(-\frac{3\pi}{2}, -\frac{\pi}{2}), (\frac{\pi}{2}, \frac{3\pi}{2})$ Decreasing: $(-\frac{\pi}{2}, \frac{\pi}{2}), (\frac{3\pi}{2}, 2\pi)$
 C) Increasing: $(-\pi, -\frac{\pi}{2}), (-\frac{\pi}{2}, 0)$ Decreasing: $(0, \frac{\pi}{2}), (\frac{\pi}{2}, \pi)$
 D) Increasing: $(0, \pi)$ Decreasing: $(-\pi, 0)$

6) $y = \tan(2x)$; $[-\pi, \pi]$

A) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right)$ Decreasing: $\left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$

B) Increasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$ Decreasing: No intervals exist.

C) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

D) Increasing: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(0, \frac{\pi}{2}\right)$

7) $f(x) = -\cos(2x)$; $[-\pi, \pi]$

A) Increasing: $(-\pi, 0)$ Decreasing: $(0, \pi)$

B) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

C) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

D) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(0, \frac{\pi}{2}\right)$ Decreasing: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, \pi\right)$

8) $f(x) = \sin(x)$; $[-\pi, \pi]$

A) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

B) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: No intervals exist

C) Increasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$ Decreasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$

D) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$

9) $y = -2\csc(2x)$; $[-\pi, \pi]$

A) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

B) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: No intervals exist

C) Increasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{\pi}{4}, 0\right), \left(0, \frac{\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$ Decreasing: $\left(-\frac{3\pi}{4}, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, -\frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{4}\right)$

D) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

10) $f(x) = -\cot(2x)$; $[-\pi, \pi]$

A) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

B) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(0, \frac{\pi}{2}\right)$ Decreasing: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, \pi\right)$

C) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: No intervals exist.

D) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

Calculus Practice: Use Derivatives to Analyze Functions 5a

For each problem, find the open intervals where the function is increasing and decreasing.

1) $y = (-3x + 15)^{\frac{1}{2}}$

- A) Increasing: $(-\infty, 5)$ Decreasing: No intervals exist
 B) Increasing: $(-\infty, 3)$ Decreasing: $(3, \infty)$
 *C) Increasing: No intervals exist. Decreasing: $(-\infty, 5)$
 D) Increasing: $(-\infty, 2)$ Decreasing: $(2, \infty)$

2) $y = -\frac{x^2}{4x - 8}$

- A) Increasing: $(-\infty, \frac{1}{3}), (\frac{4}{3}, \infty)$ Decreasing: $(\frac{1}{3}, \frac{2}{3}), (\frac{2}{3}, \frac{4}{3})$
 B) Increasing: $(4, 8), (8, 16)$ Decreasing: $(-\infty, 4), (16, \infty)$
 *C) Increasing: $(0, 2), (2, 4)$ Decreasing: $(-\infty, 0), (4, \infty)$
 D) Increasing: $(-\infty, 0), (4, \infty)$ Decreasing: $(0, 2), (2, 4)$

3) $y = \frac{1}{6}x^{\frac{7}{3}} - \frac{14}{3}x^{\frac{1}{3}} - 2$

- A) Increasing: $(-\infty, -8), (8, \infty)$ Decreasing: $(-8, 8)$
 B) Increasing: $(-\frac{2}{3}, \frac{2}{3})$ Decreasing: $(-\infty, -\frac{2}{3}), (\frac{2}{3}, \infty)$
 *C) Increasing: $(-\infty, -2), (2, \infty)$ Decreasing: $(-2, 2)$
 D) Increasing: $(-2, 2)$ Decreasing: $(-\infty, -2), (2, \infty)$

4) $f(x) = -\frac{9x^2 - 9}{x^3}$

- A) Increasing: $(-\frac{\sqrt{3}}{3}, \frac{1}{3}), (\frac{1}{3}, \frac{\sqrt{3}}{3})$ Decreasing: $(-\infty, -\frac{\sqrt{3}}{3}), (\frac{\sqrt{3}}{3}, \infty)$
 B) Increasing: $(-\infty, -4\sqrt{3}), (4\sqrt{3}, \infty)$ Decreasing: $(-4\sqrt{3}, 4), (4, 4\sqrt{3})$
 *C) Increasing: $(-\infty, -\sqrt{3}), (\sqrt{3}, \infty)$ Decreasing: $(-\sqrt{3}, 0), (0, \sqrt{3})$
 D) Increasing: $(-\sqrt{3}, 0), (0, \sqrt{3})$ Decreasing: $(-\infty, -\sqrt{3}), (\sqrt{3}, \infty)$

5) $f(x) = -2\sec(x); [-\pi, \pi]$

- A) Increasing: $(-\pi, -\frac{\pi}{2}), (-\frac{\pi}{2}, 0), (0, \frac{\pi}{2}), (\frac{\pi}{2}, \pi)$ Decreasing: No intervals exist
 B) Increasing: $(-\frac{3\pi}{2}, -\frac{\pi}{2}), (\frac{\pi}{2}, \frac{3\pi}{2})$ Decreasing: $(-\frac{\pi}{2}, \frac{\pi}{2}), (\frac{3\pi}{2}, 2\pi)$
 *C) Increasing: $(-\pi, -\frac{\pi}{2}), (-\frac{\pi}{2}, 0)$ Decreasing: $(0, \frac{\pi}{2}), (\frac{\pi}{2}, \pi)$
 D) Increasing: $(0, \pi)$ Decreasing: $(-\pi, 0)$

6) $y = \tan(2x)$; $[-\pi, \pi]$

A) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right)$ Decreasing: $\left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$

*B) Increasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$ Decreasing: No intervals exist.

C) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

D) Increasing: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(0, \frac{\pi}{2}\right)$

7) $f(x) = -\cos(2x)$; $[-\pi, \pi]$

A) Increasing: $(-\pi, 0)$ Decreasing: $(0, \pi)$

B) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

C) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

*D) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(0, \frac{\pi}{2}\right)$ Decreasing: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, \pi\right)$

8) $f(x) = \sin(x)$; $[-\pi, \pi]$

*A) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

B) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: No intervals exist

C) Increasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$ Decreasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$

D) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$

9) $y = -2\csc(2x)$; $[-\pi, \pi]$

A) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$

B) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: No intervals exist

*C) Increasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{\pi}{4}, 0\right), \left(0, \frac{\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$ Decreasing: $\left(-\frac{3\pi}{4}, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, -\frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{4}\right)$

D) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

10) $f(x) = -\cot(2x)$; $[-\pi, \pi]$

A) Increasing: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$ Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

B) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(0, \frac{\pi}{2}\right)$ Decreasing: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, \pi\right)$

*C) Increasing: $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$ Decreasing: No intervals exist.

D) Increasing: No intervals exist Decreasing: $\left(-\pi, -\frac{3\pi}{4}\right), \left(-\frac{3\pi}{4}, -\frac{\pi}{4}\right), \left(-\frac{\pi}{4}, \frac{\pi}{4}\right), \left(\frac{\pi}{4}, \frac{3\pi}{4}\right), \left(\frac{3\pi}{4}, \pi\right)$