

Calculus Practice: Use Derivatives to Analyze Functions 3a

For each problem, find all discontinuities.

1) $f(x) = -\frac{9x}{x^2 + 9}$

- A) No discontinuities exist. B) Discontinuity at: $x = -1$
C) Discontinuity at: $x = 5$ D) Discontinuity at: $x = -5$

2) $y = \frac{1}{x + 2}$

- A) Discontinuity at: $x = 0$ B) Discontinuity at: $x = 6$
C) Discontinuity at: $x = 1$ D) Discontinuity at: $x = -2$

3) $y = -\frac{x^2}{4x - 8}$

- A) Discontinuity at: $x = 3$ B) Discontinuity at: $x = -7$
C) Discontinuity at: $x = 0$ D) Discontinuity at: $x = 2$

4) $y = -\frac{x^2}{2x - 4}$

- A) Discontinuity at: $x = 6$ B) Discontinuity at: $x = -1$
C) Discontinuity at: $x = -5$ D) Discontinuity at: $x = 2$

5) $f(x) = -\frac{x^3}{x^2 - 4}$

- A) Discontinuity at: $x = 7$ B) Discontinuity at: $x = 1$
C) Discontinuity at: $x = -3$ D) Discontinuities at: $x = -2, 2$

6) $y = \left(\frac{x}{x - 3}\right)^2$

- A) Discontinuity at: $x = 0$ B) Discontinuity at: $x = -7$
C) Discontinuity at: $x = 3$ D) Discontinuity at: $x = 6$

7) $y = -\frac{x}{x^2 - 4}$

- A) Discontinuity at: $x = 0$ B) Discontinuity at: $x = 3$
C) Discontinuity at: $x = 4$ D) Discontinuities at: $x = -2, 2$

8) $f(x) = -\frac{x}{x^2 - 1}$

- A) Discontinuity at: $x = 6$ B) Discontinuity at: $x = 1$
C) Discontinuities at: $x = -1, 1$ D) Discontinuity at: $x = -5$

9) $f(x) = -\frac{2x}{x + 3}$

- A) Discontinuity at: $x = -3$ B) Discontinuity at: $x = 6$
C) Discontinuity at: $x = -6$ D) Discontinuity at: $x = -5$

10) $y = \cot(2x)$; $[-\pi, \pi]$

A) No discontinuities exist.

B) Discontinuities at: $x = -\pi, 0, \pi$

C) Discontinuities at: $x = -\pi, -\frac{\pi}{2}, 0, \frac{\pi}{2}, \pi$

D) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

11) $f(x) = 2\cos(2x)$; $[-\pi, \pi]$

A) No discontinuities exist.

B) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

C) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

12) $f(x) = \tan(x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\pi, 0, \pi$

B) No discontinuities exist.

C) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

13) $y = -\csc(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\pi, 0, \pi$

B) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

C) Discontinuities at: $x = -\pi, -\frac{\pi}{2}, 0, \frac{\pi}{2}, \pi$

D) No discontinuities exist.

14) $f(x) = \sin(2x)$; $[-\pi, \pi]$

A) No discontinuities exist.

B) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

C) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

15) $f(x) = -2\cos(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

B) No discontinuities exist.

C) Discontinuities at: $x = -\pi, 0, \pi$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

16) $f(x) = -2\sin(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

B) No discontinuities exist.

C) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

D) Discontinuities at: $x = -\pi, 0, \pi$

17) $y = \tan(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

B) Discontinuities at: $x = -\pi, -\frac{\pi}{2}, 0, \frac{\pi}{2}, \pi$

C) Discontinuities at: $x = -\pi, 0, \pi$

D) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

18) $y = -\cos(x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

B) No discontinuities exist.

C) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

D) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

Calculus Practice: Use Derivatives to Analyze Functions 3a

For each problem, find all discontinuities.

$$1) f(x) = -\frac{9x}{x^2 + 9}$$

- *A) No discontinuities exist. B) Discontinuity at: $x = -1$
 C) Discontinuity at: $x = 5$ D) Discontinuity at: $x = -5$

$$2) y = \frac{1}{x + 2}$$

- A) Discontinuity at: $x = 0$ B) Discontinuity at: $x = 6$
 C) Discontinuity at: $x = 1$ *D) Discontinuity at: $x = -2$

$$3) y = -\frac{x^2}{4x - 8}$$

- A) Discontinuity at: $x = 3$ B) Discontinuity at: $x = -7$
 C) Discontinuity at: $x = 0$ *D) Discontinuity at: $x = 2$

$$4) y = -\frac{x^2}{2x - 4}$$

- A) Discontinuity at: $x = 6$ B) Discontinuity at: $x = -1$
 C) Discontinuity at: $x = -5$ *D) Discontinuity at: $x = 2$

$$5) f(x) = -\frac{x^3}{x^2 - 4}$$

- A) Discontinuity at: $x = 7$ B) Discontinuity at: $x = 1$
 C) Discontinuity at: $x = -3$ *D) Discontinuities at: $x = -2, 2$

$$6) y = \left(\frac{x}{x - 3}\right)^2$$

- A) Discontinuity at: $x = 0$ B) Discontinuity at: $x = -7$
 *C) Discontinuity at: $x = 3$ D) Discontinuity at: $x = 6$

$$7) y = -\frac{x}{x^2 - 4}$$

- A) Discontinuity at: $x = 0$ B) Discontinuity at: $x = 3$
 C) Discontinuity at: $x = 4$ *D) Discontinuities at: $x = -2, 2$

$$8) f(x) = -\frac{x}{x^2 - 1}$$

- A) Discontinuity at: $x = 6$ B) Discontinuity at: $x = 1$
 *C) Discontinuities at: $x = -1, 1$ D) Discontinuity at: $x = -5$

$$9) f(x) = -\frac{2x}{x + 3}$$

- *A) Discontinuity at: $x = -3$ B) Discontinuity at: $x = 6$
 C) Discontinuity at: $x = -6$ D) Discontinuity at: $x = -5$

10) $y = \cot(2x)$; $[-\pi, \pi]$

A) No discontinuities exist.

B) Discontinuities at: $x = -\pi, 0, \pi$

*C) Discontinuities at: $x = -\pi, -\frac{\pi}{2}, 0, \frac{\pi}{2}, \pi$

D) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

11) $f(x) = 2\cos(2x)$; $[-\pi, \pi]$

*A) No discontinuities exist.

B) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

C) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

12) $f(x) = \tan(x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\pi, 0, \pi$

B) No discontinuities exist.

*C) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

13) $y = -\csc(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\pi, 0, \pi$

B) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

*C) Discontinuities at: $x = -\pi, -\frac{\pi}{2}, 0, \frac{\pi}{2}, \pi$

D) No discontinuities exist.

14) $f(x) = \sin(2x)$; $[-\pi, \pi]$

*A) No discontinuities exist.

B) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

C) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

15) $f(x) = -2\cos(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

*B) No discontinuities exist.

C) Discontinuities at: $x = -\pi, 0, \pi$

D) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

16) $f(x) = -2\sin(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

*B) No discontinuities exist.

C) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

D) Discontinuities at: $x = -\pi, 0, \pi$

17) $y = \tan(2x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$

B) Discontinuities at: $x = -\pi, -\frac{\pi}{2}, 0, \frac{\pi}{2}, \pi$

C) Discontinuities at: $x = -\pi, 0, \pi$

*D) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

18) $y = -\cos(x)$; $[-\pi, \pi]$

A) Discontinuities at: $x = -\pi, 0, \pi, -\frac{\pi}{2}, \frac{\pi}{2}$

*B) No discontinuities exist.

C) Discontinuities at: $x = -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$

D) Discontinuities at: $x = -\frac{\pi}{2}, \frac{\pi}{2}$