

## Calculus Practice: Techniques for Finding Antiderivatives 1a

Evaluate each indefinite integral. Use the provided substitution.

1)  $\int 40x^4(2x^5 + 1)^4 dx; \ u = 2x^5 + 1$

- A)  $\frac{4}{5}(2x^5 + 1)^5 + C$
- B)  $\frac{5}{6}(2x^5 + 1)^6 + C$
- C)  $\frac{3}{5}(2x^5 + 1)^5 + C$
- D)  $(2x^5 + 1)^5 + C$

2)  $\int (4x^5 - 1)^5 \cdot 40x^4 dx; \ u = 4x^5 - 1$

- A)  $(4x^5 - 1)^4 + C$
- B)  $\frac{2}{5}(4x^5 - 1)^5 + C$
- C)  $(4x^5 - 1)^5 + C$
- D)  $\frac{1}{3}(4x^5 - 1)^6 + C$

3)  $\int (x - 1)^3 \cdot 5x dx; \ u = x - 1$

- A)  $\frac{1}{7}(x - 1)^7 + \frac{1}{6}(x - 1)^6 + C$
- B)  $\frac{3}{5}(x - 1)^5 + \frac{3}{4}(x - 1)^4 + C$
- C)  $\frac{4}{7}(x - 1)^7 + \frac{2}{3}(x - 1)^6 + C$
- D)  $(x - 1)^5 + \frac{5}{4}(x - 1)^4 + C$

4)  $\int (x + 3)^4 \cdot x dx; \ u = x + 3$

- A)  $\frac{3}{5}(x + 3)^5 - \frac{9}{4}(x + 3)^4 + C$
- B)  $\frac{1}{6}(x + 3)^6 - \frac{3}{5}(x + 3)^5 + C$
- C)  $\frac{5}{7}(x + 3)^7 - \frac{5}{2}(x + 3)^6 + C$
- D)  $\frac{4}{5}(x + 3)^5 - 3(x + 3)^4 + C$

5)  $\int \frac{40x^4}{(2x^5 + 3)^3} dx; \ u = 2x^5 + 3$

- A)  $-\frac{1}{(2x^5 + 3)^3} + C$
- B)  $-\frac{3}{2(2x^5 + 3)^2} + C$
- C)  $-\frac{2}{(2x^5 + 3)^2} + C$
- D)  $-\frac{5}{4(2x^5 + 3)^4} + C$

6)  $\int \frac{80x^3}{(5x^4 - 2)^4} dx; \ u = 5x^4 - 2$

- A)  $-\frac{2}{3(5x^4 - 2)^3} + C$
- B)  $-\frac{5}{3(5x^4 - 2)^3} + C$
- C)  $-\frac{4}{3(5x^4 - 2)^3} + C$
- D)  $-\frac{1}{2(5x^4 - 2)^4} + C$

7)  $\int \frac{2x}{(3x-1)^4} dx; \ u = 3x-1$

- A)  $-\frac{1}{9(3x-1)^2} - \frac{2}{27(3x-1)^3} + C$
- B)  $-\frac{5}{27(3x-1)^3} - \frac{5}{36(3x-1)^4} + C$
- C)  $-\frac{5}{18(3x-1)^2} - \frac{5}{27(3x-1)^3} + C$
- D)  $-\frac{1}{9(3x-1)^3} - \frac{1}{12(3x-1)^4} + C$

8)  $\int \frac{5x}{(x-1)^5} dx; \ u = x-1$

- A)  $-\frac{1}{3(x-1)^3} - \frac{1}{4(x-1)^4} + C$
- B)  $-\frac{5}{3(x-1)^3} - \frac{5}{4(x-1)^4} + C$
- C)  $-\frac{1}{(x-1)^3} - \frac{3}{4(x-1)^4} + C$
- D)  $-\frac{2}{3(x-1)^3} - \frac{1}{2(x-1)^4} + C$

9)  $\int 9x^2 \sqrt{x^3 - 3} dx; \ u = x^3 - 3$

- A)  $\frac{4}{3}(x^3 - 3)^{\frac{3}{2}} + C$
- B)  $\frac{15}{4}(x^3 - 3)^{\frac{4}{3}} + C$
- C)  $2(x^3 - 3)^{\frac{3}{2}} + C$
- D)  $\frac{8}{3}(x^3 - 3)^{\frac{3}{2}} + C$

10)  $\int 12x^3 \sqrt{x^4 + 5} dx; \ u = x^4 + 5$

- A)  $\frac{4}{3}(x^4 + 5)^{\frac{3}{2}} + C$
- B)  $\frac{10}{3}(x^4 + 5)^{\frac{3}{2}} + C$
- C)  $2(x^4 + 5)^{\frac{3}{2}} + C$
- D)  $\frac{15}{4}(x^4 + 5)^{\frac{3}{2}} + C$

11)  $\int x(3x-2)^{\frac{1}{5}} dx; \ u = 3x-2$

- A)  $\frac{2}{21}(3x-2)^{\frac{7}{3}} + \frac{1}{3}(3x-2)^{\frac{4}{3}} + C$
- B)  $\frac{4}{21}(3x-2)^{\frac{7}{3}} + \frac{2}{3}(3x-2)^{\frac{4}{3}} + C$
- C)  $\frac{20}{99}(3x-2)^{\frac{11}{5}} + \frac{20}{27}(3x-2)^{\frac{6}{5}} + C$
- D)  $\frac{5}{99}(3x-2)^{\frac{11}{5}} + \frac{5}{27}(3x-2)^{\frac{6}{5}} + C$

12)  $\int 2x \sqrt[3]{x-4} dx; \ u = x-4$

- A)  $\frac{2}{5}(x-4)^{\frac{5}{2}} + \frac{8}{3}(x-4)^{\frac{3}{2}} + C$
- B)  $\frac{12}{7}(x-4)^{\frac{7}{3}} + 12(x-4)^{\frac{4}{3}} + C$
- C)  $2(x-4)^{\frac{5}{2}} + \frac{40}{3}(x-4)^{\frac{3}{2}} + C$
- D)  $\frac{6}{7}(x-4)^{\frac{7}{3}} + 6(x-4)^{\frac{4}{3}} + C$

## Calculus Practice: Techniques for Finding Antiderivatives 1a

Evaluate each indefinite integral. Use the provided substitution.

1)  $\int 40x^4(2x^5 + 1)^4 dx; \ u = 2x^5 + 1$

- \*A)  $\frac{4}{5}(2x^5 + 1)^5 + C$
- B)  $\frac{5}{6}(2x^5 + 1)^6 + C$
- C)  $\frac{3}{5}(2x^5 + 1)^5 + C$
- D)  $(2x^5 + 1)^5 + C$

2)  $\int (4x^5 - 1)^5 \cdot 40x^4 dx; \ u = 4x^5 - 1$

- A)  $(4x^5 - 1)^4 + C$
- B)  $\frac{2}{5}(4x^5 - 1)^5 + C$
- C)  $(4x^5 - 1)^5 + C$
- \*D)  $\frac{1}{3}(4x^5 - 1)^6 + C$

3)  $\int (x - 1)^3 \cdot 5x dx; \ u = x - 1$

- A)  $\frac{1}{7}(x - 1)^7 + \frac{1}{6}(x - 1)^6 + C$
- B)  $\frac{3}{5}(x - 1)^5 + \frac{3}{4}(x - 1)^4 + C$
- C)  $\frac{4}{7}(x - 1)^7 + \frac{2}{3}(x - 1)^6 + C$
- \*D)  $(x - 1)^5 + \frac{5}{4}(x - 1)^4 + C$

4)  $\int (x + 3)^4 \cdot x dx; \ u = x + 3$

- A)  $\frac{3}{5}(x + 3)^5 - \frac{9}{4}(x + 3)^4 + C$
- \*B)  $\frac{1}{6}(x + 3)^6 - \frac{3}{5}(x + 3)^5 + C$
- C)  $\frac{5}{7}(x + 3)^7 - \frac{5}{2}(x + 3)^6 + C$
- D)  $\frac{4}{5}(x + 3)^5 - 3(x + 3)^4 + C$

5)  $\int \frac{40x^4}{(2x^5 + 3)^3} dx; \ u = 2x^5 + 3$

- A)  $-\frac{1}{(2x^5 + 3)^3} + C$
- B)  $-\frac{3}{2(2x^5 + 3)^2} + C$
- \*C)  $-\frac{2}{(2x^5 + 3)^2} + C$
- D)  $-\frac{5}{4(2x^5 + 3)^4} + C$

6)  $\int \frac{80x^3}{(5x^4 - 2)^4} dx; \ u = 5x^4 - 2$

- A)  $-\frac{2}{3(5x^4 - 2)^3} + C$
- B)  $-\frac{5}{3(5x^4 - 2)^3} + C$
- \*C)  $-\frac{4}{3(5x^4 - 2)^3} + C$
- D)  $-\frac{1}{2(5x^4 - 2)^4} + C$

7)  $\int \frac{2x}{(3x-1)^4} dx; \ u = 3x-1$

- \*A)  $-\frac{1}{9(3x-1)^2} - \frac{2}{27(3x-1)^3} + C$
- B)  $-\frac{5}{27(3x-1)^3} - \frac{5}{36(3x-1)^4} + C$
- C)  $-\frac{5}{18(3x-1)^2} - \frac{5}{27(3x-1)^3} + C$
- D)  $-\frac{1}{9(3x-1)^3} - \frac{1}{12(3x-1)^4} + C$

8)  $\int \frac{5x}{(x-1)^5} dx; \ u = x-1$

- A)  $-\frac{1}{3(x-1)^3} - \frac{1}{4(x-1)^4} + C$
- \*B)  $-\frac{5}{3(x-1)^3} - \frac{5}{4(x-1)^4} + C$
- C)  $-\frac{1}{(x-1)^3} - \frac{3}{4(x-1)^4} + C$
- D)  $-\frac{2}{3(x-1)^3} - \frac{1}{2(x-1)^4} + C$

9)  $\int 9x^2 \sqrt{x^3 - 3} dx; \ u = x^3 - 3$

- A)  $\frac{4}{3}(x^3 - 3)^{\frac{3}{2}} + C$
- B)  $\frac{15}{4}(x^3 - 3)^{\frac{4}{3}} + C$
- \*C)  $2(x^3 - 3)^{\frac{3}{2}} + C$
- D)  $\frac{8}{3}(x^3 - 3)^{\frac{3}{2}} + C$

10)  $\int 12x^3 \sqrt{x^4 + 5} dx; \ u = x^4 + 5$

- A)  $\frac{4}{3}(x^4 + 5)^{\frac{3}{2}} + C$
- B)  $\frac{10}{3}(x^4 + 5)^{\frac{3}{2}} + C$
- \*C)  $2(x^4 + 5)^{\frac{3}{2}} + C$
- D)  $\frac{15}{4}(x^4 + 5)^{\frac{4}{3}} + C$

11)  $\int x(3x-2)^{\frac{1}{5}} dx; \ u = 3x-2$

- A)  $\frac{2}{21}(3x-2)^{\frac{7}{3}} + \frac{1}{3}(3x-2)^{\frac{4}{3}} + C$
- B)  $\frac{4}{21}(3x-2)^{\frac{7}{3}} + \frac{2}{3}(3x-2)^{\frac{4}{3}} + C$
- C)  $\frac{20}{99}(3x-2)^{\frac{11}{5}} + \frac{20}{27}(3x-2)^{\frac{6}{5}} + C$
- \*D)  $\frac{5}{99}(3x-2)^{\frac{11}{5}} + \frac{5}{27}(3x-2)^{\frac{6}{5}} + C$

12)  $\int 2x \sqrt[3]{x-4} dx; \ u = x-4$

- A)  $\frac{2}{5}(x-4)^{\frac{5}{2}} + \frac{8}{3}(x-4)^{\frac{3}{2}} + C$
- B)  $\frac{12}{7}(x-4)^{\frac{7}{3}} + 12(x-4)^{\frac{4}{3}} + C$
- C)  $2(x-4)^{\frac{5}{2}} + \frac{40}{3}(x-4)^{\frac{3}{2}} + C$
- \*D)  $\frac{6}{7}(x-4)^{\frac{7}{3}} + 6(x-4)^{\frac{4}{3}} + C$