

Calculus Practice: Calculating Derivatives 2a

Differentiate each function with respect to x .

1) $f(x) = -\frac{5}{x} + \frac{3}{x^4} + \frac{3}{x^5}$

A) $f'(x) = -5x^{-2} + 3x^{-5} + 3x^{-6}$
 $= -\frac{5}{x^2} + \frac{3}{x^5} + \frac{3}{x^6}$

B) $f'(x) = 5x^{-1} - 12x^{-4} - 15x^{-5}$
 $= \frac{5}{x} - \frac{12}{x^4} - \frac{15}{x^5}$

C) $f'(x) = 5x^{-2} - 12x^{-5} - 15x^{-6}$
 $= \frac{5}{x^2} - \frac{12}{x^5} - \frac{15}{x^6}$

D) $f'(x) = 5x - 12x - 15x$
 $= -22x$

2) $f(x) = \frac{5}{x^3} - \frac{4}{3x^4} + \frac{2}{x^5}$

A) $f'(x) = -15x^{-4} + \frac{16x^{-5}}{3} - 10x^{-6}$
 $= -\frac{15}{x^4} + \frac{16}{3x^5} - \frac{10}{x^6}$

B) $f'(x) = 5x^{-4} - \frac{4x^{-5}}{3} + 2x^{-6}$
 $= \frac{5}{x^4} - \frac{4}{3x^5} + \frac{2}{x^6}$

C) $f'(x) = -15x + \frac{16x}{3} - 10x$
 $= -25x + \frac{16x}{3}$

D) $f'(x) = -15x^{-3} + \frac{16x^{-4}}{3} - 10x^{-5}$
 $= -\frac{15}{x^3} + \frac{16}{3x^4} - \frac{10}{x^5}$

3) $y = \frac{2}{5x^3} - \frac{3}{x^4} + \frac{5}{x^5}$

A) $\frac{dy}{dx} = -\frac{6x}{5} + 12x - 25x$
 $= -\frac{6x}{5} - 13x$

B) $\frac{dy}{dx} = -\frac{6x^{-3}}{5} + 12x^{-4} - 25x^{-5}$
 $= -\frac{6}{5x^3} + \frac{12}{x^4} - \frac{25}{x^5}$

C) $\frac{dy}{dx} = \frac{2x^{-4}}{5} - 3x^{-5} + 5x^{-6}$
 $= \frac{2}{5x^4} - \frac{3}{x^5} + \frac{5}{x^6}$

D) $\frac{dy}{dx} = -\frac{6x^{-4}}{5} + 12x^{-5} - 25x^{-6}$
 $= -\frac{6}{5x^4} + \frac{12}{x^5} - \frac{25}{x^6}$

4) $y = -\frac{4}{x^2} - \frac{3}{5x^4}$

A) $\frac{dy}{dx} = 8x^{-3} + \frac{12x^{-5}}{5}$
 $= \frac{8}{x^3} + \frac{12}{5x^5}$

B) $\frac{dy}{dx} = -4x^{-3} - \frac{3x^{-5}}{5}$
 $= -\frac{4}{x^3} - \frac{3}{5x^5}$

C) $\frac{dy}{dx} = 8x^{-2} + \frac{12x^{-4}}{5}$
 $= \frac{8}{x^2} + \frac{12}{5x^4}$

D) $\frac{dy}{dx} = 8x + \frac{12x}{5}$

$$5) f(x) = \frac{4}{3x} + \frac{5}{x^4} + \frac{4}{x^5}$$

$$\begin{aligned} \text{A) } f'(x) &= -\frac{4x}{3} - 20x - 20x \\ &= -\frac{4x}{3} - 40x \end{aligned}$$

$$\begin{aligned} \text{B) } f'(x) &= \frac{4x^{-2}}{3} + 5x^{-5} + 4x^{-6} \\ &= \frac{4}{3x^2} + \frac{5}{x^5} + \frac{4}{x^6} \end{aligned}$$

$$\begin{aligned} \text{C) } f'(x) &= -\frac{4x^{-2}}{3} - 20x^{-5} - 20x^{-6} \\ &= -\frac{4}{3x^2} - \frac{20}{x^5} - \frac{20}{x^6} \end{aligned}$$

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$$6) y = \frac{4}{x^4}$$

$$\begin{aligned} \text{A) } \frac{dy}{dx} &= 4x^{-5} \\ &= \frac{4}{x^5} \end{aligned}$$

$$\text{B) } \frac{dy}{dx} = -16x$$

$$\begin{aligned} \text{C) } \frac{dy}{dx} &= -16x^{-4} \\ &= -\frac{16}{x^4} \end{aligned}$$

$$\begin{aligned} \text{D) } \frac{dy}{dx} &= -16x^{-5} \\ &= -\frac{16}{x^5} \end{aligned}$$

$$7) y = \frac{1}{x} + \frac{1}{2x^5}$$

$$\begin{aligned} \text{A) } \frac{dy}{dx} &= -x - \frac{5x}{2} \\ &= -x - \frac{5x}{2} \end{aligned}$$

$$\begin{aligned} \text{B) } \frac{dy}{dx} &= x^{-2} + \frac{x^{-6}}{2} \\ &= \frac{1}{x^2} + \frac{1}{2x^6} \end{aligned}$$

$$\begin{aligned} \text{C) } \frac{dy}{dx} &= -x^{-2} - \frac{5x^{-6}}{2} \\ &= -\frac{1}{x^2} - \frac{5}{2x^6} \end{aligned}$$

$$\begin{aligned} \text{D) } \frac{dy}{dx} &= -x^{-1} - \frac{5x^{-5}}{2} \\ &= -\frac{1}{x} - \frac{5}{2x^5} \end{aligned}$$

$$8) y = -\frac{1}{4x^2} - \frac{2}{5x^4}$$

$$\text{A) } \frac{dy}{dx} = \frac{2x}{4} + \frac{8x}{5}$$

$$\begin{aligned} \text{B) } \frac{dy}{dx} &= \frac{2x^{-3}}{4} + \frac{8x^{-5}}{5} \\ &= \frac{2}{4x^3} + \frac{8}{5x^5} \end{aligned}$$

$$\begin{aligned} \text{C) } \frac{dy}{dx} &= \frac{2x^{-2}}{4} + \frac{8x^{-4}}{5} \\ &= \frac{2}{4x^2} + \frac{8}{5x^4} \end{aligned}$$

$$\begin{aligned} \text{D) } \frac{dy}{dx} &= -\frac{x^{-3}}{4} - \frac{2x^{-5}}{5} \\ &= -\frac{1}{4x^3} - \frac{2}{5x^5} \end{aligned}$$

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