

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

TENTH YEAR MATHEMATICS

Friday, June 16, 1978 — 1:15 to 4:15 p.m., only

The last page of the booklet is the answer sheet. Fold the last page along the perforations and, slowly and carefully, tear off the answer sheet. Then fill in the heading of your answer sheet.

On page 5 you will find the "Tables of Natural Trigonometric Functions" which you may need to answer some questions in this examination. Fold this page along the perforations, and tear it off also slowly and carefully.

When you have completed the examination, you must sign the statement printed at the end of the answer paper, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer paper cannot be accepted if you fail to sign this declaration.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN

Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Unless otherwise specified, answers may be left in terms of π or in radical form. Write your answers in the spaces provided on the separate answer sheet.

1 The ratio of the circumferences of two circles is 1:4. If the length of the radius of the smaller circle is 3, find the length of the radius of the larger circle.

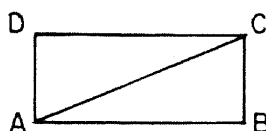
2 Triangle ABC is inscribed in circle O , \overline{AB} is the diameter of the circle, and $m\angle A = 40$. Which is the shortest side of the triangle?

3 The lengths of the sides of a triangle are 4, 6, and 8. If the midpoints of the three sides are joined to form a second triangle, find the perimeter of the second triangle.

4 Find the area of a right triangle whose legs have lengths 5 and 10.

5 In $\triangle ABC$, $\overline{AB} \cong \overline{BC}$ and $m\angle A = 30$. Find $m\angle B$.

6 In the accompanying diagram of rectangle $ABCD$, $AB = 10$ and $BC = 4$. Find, in radical form, the length of diagonal \overline{AC} .



7 A regular hexagon is inscribed in a circle whose radius has length 4. Find the length of a side of the hexagon.

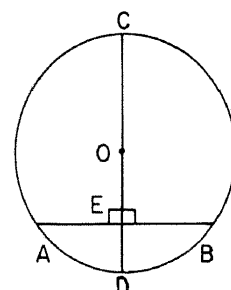
8 Circle O has center $(0,2)$ and diameter \overline{AB} . If the coordinates of A are $(-3,2)$, find the coordinates of B .

9 Find the radius of a circle whose area is 36π .

10 The area of parallelogram $ABCD$ is equal to the area of a square whose side is 6. If $AB = 12$, find the length of an altitude drawn to side \overline{AB} .

11 If the lengths of the bases of a trapezoid are 9 and 23, find the length of the median.

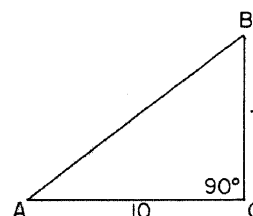
12 In the accompanying diagram, diameter \overline{CD} of circle O is drawn perpendicular to chord \overline{AB} at E . If $AB = 8$ and $CE = 8$, find ED .



13 Find the circumference of a circle if an arc whose measure is 120 degrees has a length of 8π .

14 The lengths of the bases of a trapezoid are 11 centimeters and 15 centimeters. If the area of the trapezoid is 78 square centimeters, find the number of centimeters in the length of the altitude.

15 In the accompanying figure, ABC is a right triangle with $m\angle C = 90$, $BC = 7$, and $AC = 10$. Find, to the nearest degree, the measure of $\angle A$.



Directions (16–29): Write in the space provided on the separate answer sheet the numeral preceding the expression that best completes each statement or answers each question.

16 If $\triangle ABC \cong \triangle DEF$ and $\triangle DEF \sim \triangle RST$, then which must be true?

- (1) $\triangle ABC \cong \triangle RST$
- (2) $\triangle ABC \sim \triangle RST$
- (3) area of $\triangle ABC =$ area of $\triangle RST$
- (4) perimeter of $\triangle ABC =$ perimeter of $\triangle RST$

17 In parallelogram $ABCD$, if $m\angle A = x$, then $m\angle B$ equals

- (1) $90 - x$
- (2) $180 - x$
- (3) $180 - 2x$
- (4) $2x$

- 18 If two polygons are similar, which statement must be true?
- (1) The polygons are congruent.
 - (2) The polygons are equiangular.
 - (3) The lengths of the corresponding sides of the polygons are in proportion.
 - (4) The polygons are equilateral.

- 19 Point P is 2 inches from \overleftrightarrow{CD} . What is the total number of points that are 1 inch from \overleftrightarrow{CD} and also 1 inch from P ?
- (1) 1
 - (2) 2
 - (3) 3
 - (4) 4

- 20 To prove by *indirect* proof that an angle x of a certain triangle is an obtuse angle, it could be shown that
- (1) the measure of angle x is greater than the measure of some other angle y which is known to be acute
 - (2) the two sides of the triangle which form angle x are not perpendicular
 - (3) the measure of angle x is equal to the measure of some other angle z which is known to be acute
 - (4) angle x is neither an acute angle nor a right angle

- 21 An equation of the locus of points whose ordinates are 3 less than twice their abscissas is
- (1) $y = 2x - 3$
 - (2) $y = 2x + 3$
 - (3) $x = 2y - 3$
 - (4) $x = 2y + 3$

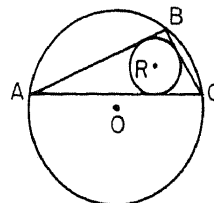
- 22 The measure of each exterior angle of a regular ten-sided polygon is
- (1) 36°
 - (2) 144°
 - (3) 180°
 - (4) 360°

- 23 If in triangle ABC , $m\angle A = 60$ and the measure of an exterior angle at B is 140° , then
- (1) \overline{BC} is the shortest side of the triangle
 - (2) \overline{AB} is the longest side of the triangle
 - (3) the triangle is obtuse
 - (4) the triangle is isosceles

- 24 Which set may be the lengths of the sides of an obtuse triangle?
- (1) $\{3, 3, 3\}$
 - (2) $\{3, 4, 8\}$
 - (3) $\{3, 4, 5\}$
 - (4) $\{3, 4, 6\}$

- 25 The distance between the points $(-2, 3)$ and $(6, -2)$ is
- (1) $\sqrt{17}$
 - (2) $\sqrt{65}$
 - (3) $\sqrt{89}$
 - (4) 10

- 26 In the accompanying diagram, O is the center of the circle circumscribed about scalene $\triangle ABC$ and R is the center of the circle inscribed in scalene $\triangle ABC$. Which statement is *false*?



- (1) Point R is equidistant from \overline{AC} and \overline{BC} .
 - (2) Point O is equidistant from points B and C .
 - (3) Point R lies on the bisectors of angles A and C .
 - (4) Point O lies on the bisectors of angles A and C .
- 27 An altitude drawn to the hypotenuse of a right triangle divides the hypotenuse into segments whose lengths are 4 and 16. The length of the altitude to the hypotenuse is
- (1) 8
 - (2) 10
 - (3) 20
 - (4) 64

- 28 Which statement is *not* always true?
- (1) A square is a rhombus.
 - (2) A square is a rectangle.
 - (3) A parallelogram is a polygon.
 - (4) A trapezoid is a parallelogram.

- 29 What is true of the line segment joining $(-5, 2)$ and $(-5, -7)$?
- (1) Its slope is -2 .
 - (2) Its slope is $\frac{7}{2}$.
 - (3) Its slope is undefined.
 - (4) Its slope is zero.

Directions (30): Leave all construction lines on the answer sheet.

- 30 *On the answer sheet*, construct a triangle similar to the given triangle RST , using the line segment \overline{AB} as the base corresponding to \overline{RS} .

GO RIGHT ON TO THE NEXT PAGE.

Answers to the following questions are to be written on paper provided by the school.

Part II

Answer four questions from this part. Show all work unless otherwise directed.

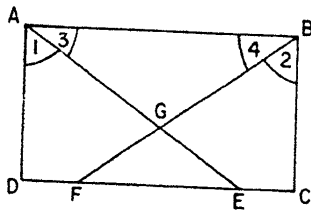
31 Prove either a or b, but not both:

a The sum of the measures of the angles of a triangle is 180 degrees. [10]

OR

b The measure of an angle formed by two chords intersecting inside the circle is equal to one-half the sum of the measures of the intercepted arcs. [10]

32 Given: rectangle $ABCD$, \overline{DFEC} , \overline{AGE} , \overline{BGF} , $\overline{DF} \cong \overline{EC}$

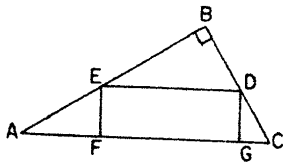


Prove: a $\angle 1 \cong \angle 2$ [6]

b $\angle 3 \cong \angle 4$ [2]

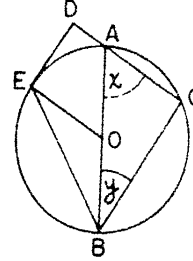
c $\overline{AG} \cong \overline{GB}$ [2]

33 Given: rectangle $DEFG$, triangle ABC with a right angle at B , \overline{AEB} , \overline{BDC} , \overline{AFGC}



Prove: $ED \times DG = DC \times EB$ [10]

34 Given: circle O , tangent \overline{DE} , secant \overline{DAC} , diameter \overline{AOB} , \overline{OE} , $\overline{BE} \cong \overline{BC}$, $m\angle x : m\angle y = 2:1$



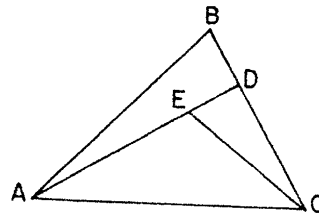
Find: a $m\angle y$ [2]

b $m\widehat{EB}$ [3]

c $m\angle EOA$ [2]

d $m\angle D$ [3]

35 Given: $\triangle ABC$ with \overline{BDC} , \overline{AED} , and \overline{EC} drawn



Prove: $m\angle AEC > m\angle ABC$ [10]

36 The vertices of quadrilateral $ABCD$ are $A(0, -3)$, $B(1, 0)$, $C(4, 0)$, and $D(3, -3)$.

a Show by means of coordinate geometry that $ABCD$ is a parallelogram and state a reason for your conclusion. [6]

b Find the area of the parallelogram. [4]

*37 The coordinates of points A , B , and C are $A(0, 2)$, $B(2, 6)$, and $C(4, 1)$.

a Write an equation of \overleftrightarrow{AB} . [4]

b Write an equation of the line through C perpendicular to \overleftrightarrow{AB} . [6]

* This question is based on an optional topic in the syllabus.

THE UNIVERSITY OF THE STATE OF NEW YORK
THE STATE EDUCATION DEPARTMENT
 BUREAU OF ELEMENTARY AND SECONDARY EDUCATIONAL TESTING

Tables of Natural Trigonometric Functions
 (For use with 9th and 10th Year Mathematics Regents Examinations)

Angle	Sine	Cosine	Tangent	Angle	Sine	Cosine	Tangent
1°	.0175	.9998	.0175	46°	.7193	.6947	1.0355
2°	.0349	.9994	.0349	47°	.7314	.6820	1.0724
3°	.0523	.9986	.0524	48°	.7431	.6691	1.1106
4°	.0698	.9976	.0699	49°	.7547	.6561	1.1504
5°	.0872	.9962	.0875	50°	.7660	.6428	1.1918
6°	.1045	.9945	.1051	51°	.7771	.6293	1.2349
7°	.1219	.9925	.1228	52°	.7880	.6157	1.2799
8°	.1392	.9903	.1405	53°	.7986	.6018	1.3270
9°	.1564	.9877	.1584	54°	.8090	.5878	1.3764
10°	.1736	.9848	.1763	55°	.8192	.5736	1.4281
11°	.1908	.9816	.1944	56°	.8290	.5592	1.4826
12°	.2079	.9781	.2126	57°	.8387	.5446	1.5399
13°	.2250	.9744	.2309	58°	.8480	.5299	1.6003
14°	.2419	.9703	.2493	59°	.8572	.5150	1.6643
15°	.2588	.9659	.2679	60°	.8660	.5000	1.7321
16°	.2756	.9613	.2867	61°	.8746	.4848	1.8040
17°	.2924	.9563	.3057	62°	.8829	.4695	1.8807
18°	.3090	.9511	.3249	63°	.8910	.4540	1.9626
19°	.3256	.9455	.3443	64°	.8988	.4384	2.0503
20°	.3420	.9397	.3640	65°	.9063	.4226	2.1445
21°	.3584	.9336	.3839	66°	.9135	.4067	2.2460
22°	.3746	.9272	.4040	67°	.9205	.3907	2.3559
23°	.3907	.9205	.4245	68°	.9272	.3746	2.4751
24°	.4067	.9135	.4452	69°	.9336	.3584	2.6051
25°	.4226	.9063	.4663	70°	.9397	.3420	2.7475
26°	.4384	.8988	.4877	71°	.9455	.3256	2.9042
27°	.4540	.8910	.5095	72°	.9511	.3090	3.0777
28°	.4695	.8829	.5317	73°	.9563	.2924	3.2709
29°	.4848	.8746	.5543	74°	.9613	.2756	3.4874
30°	.5000	.8660	.5774	75°	.9659	.2588	3.7321
31°	.5150	.8572	.6009	76°	.9703	.2419	4.0108
32°	.5299	.8480	.6249	77°	.9744	.2250	4.3315
33°	.5446	.8387	.6494	78°	.9781	.2079	4.7046
34°	.5592	.8290	.6745	79°	.9816	.1908	5.1446
35°	.5736	.8192	.7002	80°	.9848	.1736	5.6713
36°	.5878	.8090	.7265	81°	.9877	.1564	6.3138
37°	.6018	.7986	.7536	82°	.9903	.1392	7.1154
38°	.6157	.7880	.7813	83°	.9925	.1219	8.1443
39°	.6293	.7771	.8098	84°	.9945	.1045	9.5144
40°	.6428	.7660	.8391	85°	.9962	.0872	11.4301
41°	.6561	.7547	.8693	86°	.9976	.0698	14.3007
42°	.6691	.7431	.9004	87°	.9986	.0523	19.0811
43°	.6820	.7314	.9325	88°	.9994	.0349	28.6363
44°	.6947	.7193	.9657	89°	.9998	.0175	57.2900
45°	.7071	.7071	1.0000	90°	1.0000	.0000	

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TENTH YEAR MATHEMATICS
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Part I Score:
Rater's Initials:

ANSWER SHEET

Pupil.....Teacher.....

School.....

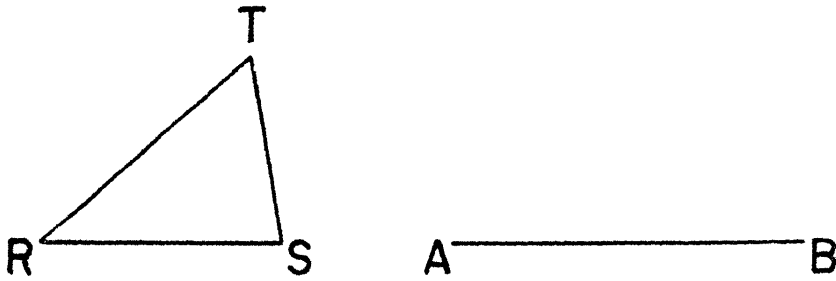
Name and author of textbook used.....

Your answers to Part I should be recorded on this answer sheet.

Part I

Answer all questions in this part.

- | | | |
|---------|---------|---|
| 1..... | 11..... | 21..... |
| 2..... | 12..... | 22..... |
| 3..... | 13..... | 23..... |
| 4..... | 14..... | 24..... |
| 5..... | 15..... | 25..... |
| 6..... | 16..... | 26..... |
| 7..... | 17..... | 27..... |
| 8..... | 18..... | 28..... |
| 9..... | 19..... | 29..... |
| 10..... | 20..... | 30 Answer question 30 on the other
side of this sheet. |



Your answers for Part II should be placed on paper provided by the school.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination, and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature

FOR TEACHERS ONLY

10

SCORING KEY TENTH YEAR MATHEMATICS

Friday, June 16, 1978 — 1:15 to 4:15 p.m., only

Use only *red* ink or *red* pencil in rating Regents papers. Do not attempt to *correct* the pupil's work by making insertions or changes of any kind. Use checkmarks to indicate pupil errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Part I

Allow 2 credits for each correct answer; allow no partial credit. For questions 16–29, allow credit if the pupil has written the correct answer instead of the numeral 1, 2, 3, or 4.

(1) 12	(11) 16	(21) 1
(2) \overline{BC} or a	(12) 2	(22) 1
(3) 9	(13) 24π	(23) 2
(4) 25	(14) 6	(24) 4
(5) 120	(15) 35	(25) 3
(6) $\sqrt{116}$ or $2\sqrt{29}$	(16) 2	(26) 4
(7) 4	(17) 2	(27) 1
(8) $(3,2)$ or $\begin{matrix} x = 3 \\ y = 2 \end{matrix}$	(18) 3	(28) 4
(9) 6	(19) 1	(29) 3
(10) 3	(20) 4	

[OVER]

Part II

Please refer to the Department's pamphlet *Suggestions on the Rating of Regents Examination Papers in Mathematics*. Care should be exercised in making deductions as to whether the error is purely a mechanical one or due to a violation of some principle. A mechanical error generally should receive a deduction of 10 percent, while an error due to a violation of some cardinal principle should receive a deduction ranging from 30 percent to 50 percent, depending on the relative importance of the principle in the solution of the problem.

$$(34) a \ 30 \quad [2]$$

$$b \ 120 \quad [3]$$

$$c \ 60 \quad [2]$$

$$d \ 90 \quad [3]$$

$$(36) b \ 9 \quad [4]$$

$$(37) a \ y - 2 = 2(x - 0)$$

or

$$y = 2x + 2 \quad [4]$$

$$b \ y - 1 = -\frac{1}{2}(x - 4)$$

or

$$x + 2y = 6 \quad [6]$$

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REGENTS HIGH SCHOOL EXAMINATION

B

TENTH YEAR MATHEMATICS

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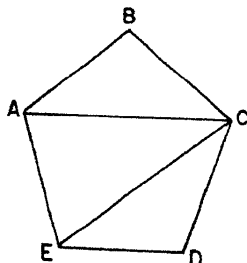
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- 1 In the accompanying diagram, $ABCDE$ is a regular pentagon and diagonals \overline{CE} and \overline{CA} are drawn. If $CE = 6$, what is the length of \overline{CA} ?



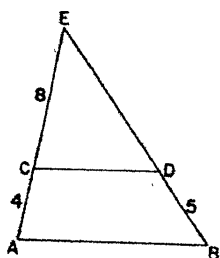
- 2 In $\triangle ABC$, D is the midpoint of \overline{AB} , E is the midpoint of \overline{BC} , and \overline{DE} is drawn. If $m\angle A = 75$, find $m\angle BDE$.

- 3 In triangle RST , $m\angle T = 60$ and $m\angle S > m\angle R$. Which is the longest side of the triangle?

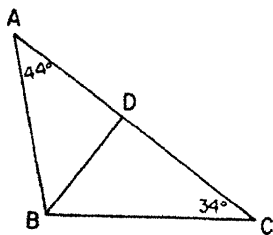
- 4 In triangle ABC , $\overline{AB} \cong \overline{AC}$ and $m\angle A = 70$. Find the number of degrees in the measure of an exterior angle at C .

- 5 The lengths of the diagonals of a rhombus are 10 and 15. Find the area of the rhombus.

- 6 In the accompanying diagram, \overline{CD} is parallel to \overline{AB} , $CA = 4$, $DB = 5$, and $EC = 8$. Find ED .



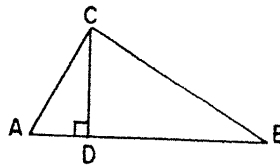
- 7 In the accompanying figure, \overrightarrow{BD} bisects $\angle ABC$. If $m\angle A = 44$ and $m\angle C = 34$, find $m\angle DBC$.



- 8 The length of a side of an equilateral triangle is 8. What is the length, in radical form, of an altitude of the triangle?

- 9 The length of a side of a square is 4. What is the length, in radical form, of a diagonal of the square?

- 10 In the accompanying diagram, $\triangle ABC$ is a right triangle with $m\angle ACB = 90$, $\overline{AD} \perp \overline{AB}$, and $\overline{CD} \perp \overline{AB}$. If $AB = 8$ and $AD = 2$, find the length of \overline{AC} .



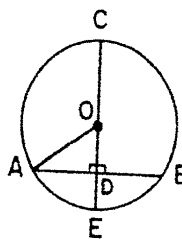
- 11 Find the distance from point $A(3, -1)$ to point $B(9, 7)$.

- 12 The area of a sector of a circle is 8 square inches and the measure of the central angle of the sector is 90° . Find the number of square inches in the area of the circle.

- 13 Quadrilateral $ABCD$ is inscribed in a circle. If $m\widehat{AB} = 70$, $m\widehat{BC} = 100$, and $m\widehat{CD} = 130$, find $m\angle ABC$.

- 14 The length of a side of a triangle is 12 and the length of the altitude drawn to that side is 11. Find the area of the triangle.

- 15 In the accompanying diagram, diameter \overline{CE} of circle O is perpendicular to chord \overline{AB} at D . If $AB = 8$ and $OD = 3$, find OA .



- 16 A line which passes through the points $(5, 3)$ and $(x, 6)$ has a slope of 1. What is the value of x ?

- 17 In triangle ABC , $AB =$

Direction: separate answer for each question that has a question.

- 18 Which diagonal?

A
B
C

- (1) A,
(2) A a

- 19 In the diagram, \overleftrightarrow{CD} are respectively $m\angle CH$

- (1) 35
(2) 70

- 20 If the length of the segment is

- (1) 7
(2) 2

- 21 The exterior angle is

- (1) 1
(2) 2

- 22 Two tangent lines intersect at point P. The measure of the angle formed by the tangents is

- (1) 20°
(2) 110°

- 23 Which type of triangle is formed?

- (1) To form an isosceles triangle
(2) To form a right triangle
(3) To form an equilateral triangle
(4) To form a scalene triangle

- 17 In triangle ABC , $m\angle C = 90$, $m\angle A = 30$, and $AB = 4$. Find BC .

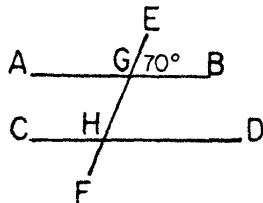
Directions (18–29): Write in the space provided on the separate answer sheet the *numeral* preceding the expression that best completes *each* statement or answers *each* question.

- 18 Which of the following must be true about the diagonals of a rectangle?

- A The diagonals are perpendicular.
 B The diagonals have the same length.
 C The diagonals bisect each other.

- (1) A, only (3) B and C, only
 (2) A and C, only (4) A, B, and C

- 19 In the accompanying diagram, parallel lines \overleftrightarrow{AB} and \overleftrightarrow{CD} are intersected by transversal \overleftrightarrow{EF} at G and H , respectively. If $m\angle BGE = 70$, then what is $m\angle CHG$?



- (1) 35 (3) 90
 (2) 70 (4) 110

- 20 If the lengths of two sides of a triangle are 7 and 10, the length of the third side may be

- (1) 7 (3) 3
 (2) 2 (4) 17

- 21 The exact number of points equidistant from the x - and y -axes and also two inches from the origin is

- (1) 1 (3) 3
 (2) 2 (4) 4

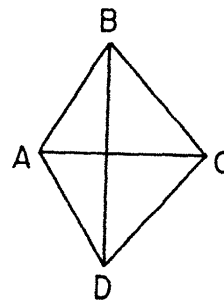
- 22 Two tangents are drawn to a circle from an exterior point. If the measure of the angle formed by the two tangents is 40° , then the measure of the *minor* intercepted arc is

- (1) 20° (3) 140°
 (2) 110° (4) 220°

- 23 Which is *not* a good example of indirect reasoning?

- (1) To prove a triangle is scalene, prove it is not isosceles and not equilateral.
 (2) To prove an angle is acute, prove it is not obtuse.
 (3) To prove two lines in a plane intersect, prove they are not parallel.
 (4) To prove AB is greater than BC , prove AB is not less than BC and AB is not equal to BC .

- 24 In the accompanying figure, $\overline{AB} \cong \overline{AD}$ and $\overline{BC} \cong \overline{CD}$. Which statement *must* be true?



- (1) $\overline{BD} \perp \overline{AC}$
 (2) $\overline{BD} \cong \overline{AC}$
 (3) $ABCD$ is a parallelogram.
 (4) $\angle BAD \cong \angle BCD$

- 25 If two circles have exactly three common tangents, then the circles

- (1) are internally tangent
 (2) are externally tangent
 (3) intersect in two distinct points
 (4) are nonintersecting

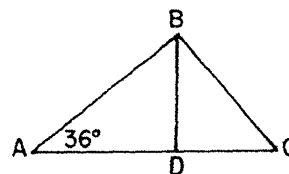
- 26 An isosceles trapezoid has two base angles whose measures are each 45 degrees. If the bases are 8 and 12, respectively, then the length of an altitude of the trapezoid must be

- (1) 6 (3) 10
 (2) 2 (4) 4

- 27 What is a converse of the statement, "If the altitude is drawn to the base of an isosceles triangle, then it bisects the base"?

- (1) If a triangle is isosceles, then the altitude does not bisect the base.
 (2) If a triangle is not isosceles, then the altitude does not bisect the base.
 (3) If the altitude bisects the base of a triangle, then the triangle is isosceles.
 (4) The altitude bisects the base of an isosceles triangle.

- 28 In the accompanying diagram, \overline{BD} is an altitude of $\triangle ABC$, $m\angle A = 36$, $AB = 6$, and $AC = 8$. What is the length of \overline{BD} to the *nearest tenth*?



- (1) 3.5 (3) 4.9
 (2) 4.7 (4) 6.5

29 If the area of a square is 64, then the length of its apothem is

- (1) 32 (3) 8
(2) 16 (4) 4

Directions (30): Leave all construction lines on the answer sheet

30 On the answer sheet, locate by construction a point on \overline{DC} that is equidistant from points A and B.

Answers to the following questions are to be written on paper provided by the school.

Part II

Answer four questions from this part. Show all work unless otherwise directed.

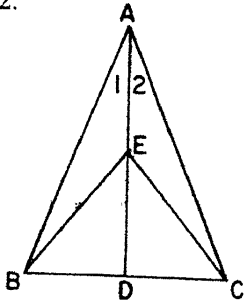
31 Prove either a or b, but not both:

a The square of the length of the hypotenuse of a right triangle is equal to the sum of the squares of the lengths of the legs. [10]

OR

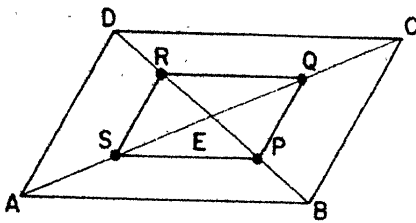
b If three angles of one triangle are congruent to the three angles of another triangle, the triangles are similar. [10]

32 Given: $\triangle ABC$ with $\overline{AB} \cong \overline{AC}$, \overline{BDC} , \overline{AED} , and $m\angle 1 = m\angle 2$.



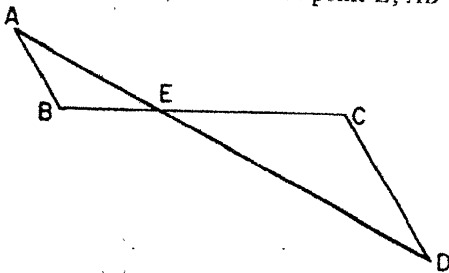
Prove: $\triangle BDE \cong \triangle CDE$ [10]

33 In the accompanying diagram, $ABCD$ is a parallelogram, and diagonals \overline{AC} and \overline{BD} intersect at E . The midpoints of \overline{AE} , \overline{BE} , \overline{CE} , and \overline{DE} are S , P , Q , and R , respectively.



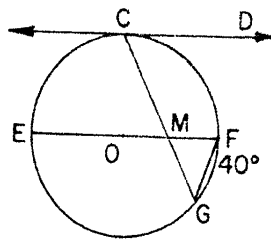
Prove: $PQRS$ is a parallelogram. [10]

34 Given: \overline{AD} and \overline{BC} intersect at point E , $\overline{AB} \parallel \overline{CD}$.



Prove: $AB \times DE = DC \times AE$ [10]

35 In the accompanying diagram, \overline{EOF} is a diameter of circle O , \overline{CD} is tangent to the circle at C , $\overline{CD} \parallel \overline{EF}$, and $m\widehat{FG} = 40$. Chords \overline{CG} and \overline{EF} intersect at M , and \overline{FG} is drawn.



- a Find $m\angle EFG$. [2]
b Find $m\widehat{CF}$. [2]
c Find $m\angle DCG$. [3]
d Find $m\angle EMG$. [3]

36 The vertices of parallelogram $ABCD$ are $A(4,6)$, $B(3,-7)$, $C(6,-8)$, and $D(r,t)$.

- a Find the coordinates of the midpoint of \overline{AC} . [2]
b Find the coordinates of the midpoint of \overline{BD} in terms of r and t . [4]
c Find the numerical value of r . [2]
d Find the numerical value of t . [2]

37 The vertices of triangle ABC are $A(-4,4)$, $B(6,4)$, and $C(5,1)$.

- a Using graph paper, draw $\triangle ABC$. [1]
b Using methods of coordinate geometry, show that triangle ABC is a right triangle, and state a reason for your conclusion. [5]
c Using methods of coordinate geometry, show that the median to the hypotenuse equals one-half the hypotenuse. [4]

THE UNIVERSITY OF THE STATE OF NEW YORK
THE STATE EDUCATION DEPARTMENT
 BUREAU OF ELEMENTARY AND SECONDARY EDUCATIONAL TESTING

Tables of Natural Trigonometric Functions
 (For use with 9th and 10th Year Mathematics Regents Examinations)

Angle	Sine	Cosine	Tangent	Angle	Sine	Cosine	Tangent
1°	.0175	.9998	.0175	46°	.7193	.6947	1.0355
2°	.0349	.9994	.0349	47°	.7314	.6820	1.0724
3°	.0523	.9986	.0524	48°	.7431	.6691	1.1106
4°	.0698	.9976	.0699	49°	.7547	.6561	1.1504
5°	.0872	.9962	.0875	50°	.7660	.6428	1.1918
6°	.1045	.9945	.1051	51°	.7771	.6293	1.2349
7°	.1219	.9925	.1228	52°	.7880	.6157	1.2799
8°	.1392	.9903	.1405	53°	.7986	.6018	1.3270
9°	.1564	.9877	.1584	54°	.8090	.5878	1.3764
10°	.1736	.9848	.1763	55°	.8192	.5736	1.4281
11°	.1908	.9816	.1944	56°	.8290	.5592	1.4826
12°	.2079	.9781	.2126	57°	.8387	.5446	1.5399
13°	.2250	.9744	.2309	58°	.8480	.5299	1.6003
14°	.2419	.9703	.2493	59°	.8572	.5150	1.6643
15°	.2588	.9659	.2679	60°	.8660	.5000	1.7321
16°	.2756	.9613	.2867	61°	.8746	.4848	1.8040
17°	.2924	.9563	.3057	62°	.8829	.4695	1.8807
18°	.3090	.9511	.3249	63°	.8910	.4540	1.9626
19°	.3256	.9455	.3443	64°	.8988	.4384	2.0503
20°	.3420	.9397	.3640	65°	.9063	.4226	2.1445
21°	.3584	.9336	.3839	66°	.9135	.4067	2.2460
22°	.3746	.9272	.4040	67°	.9205	.3907	2.3559
23°	.3907	.9205	.4245	68°	.9272	.3746	2.4751
24°	.4067	.9135	.4452	69°	.9336	.3584	2.6051
25°	.4226	.9063	.4663	70°	.9397	.3420	2.7475
26°	.4384	.8988	.4877	71°	.9455	.3256	2.9042
27°	.4540	.8910	.5095	72°	.9511	.3090	3.0777
28°	.4695	.8829	.5317	73°	.9563	.2924	3.2709
29°	.4848	.8746	.5543	74°	.9613	.2756	3.4874
30°	.5000	.8660	.5774	75°	.9659	.2588	3.7321
31°	.5150	.8572	.6009	76°	.9703	.2419	4.0108
32°	.5299	.8480	.6249	77°	.9744	.2250	4.3315
33°	.5446	.8387	.6494	78°	.9781	.2079	4.7046
34°	.5592	.8290	.6745	79°	.9816	.1908	5.1446
35°	.5736	.8192	.7002	80°	.9848	.1736	5.6713
36°	.5878	.8090	.7265	81°	.9877	.1564	6.3138
37°	.6018	.7986	.7536	82°	.9903	.1392	7.1154
38°	.6157	.7880	.7813	83°	.9925	.1219	8.1443
39°	.6293	.7771	.8098	84°	.9945	.1045	9.5144
40°	.6428	.7660	.8391	85°	.9962	.0872	11.4301
41°	.6561	.7547	.8693	86°	.9976	.0698	14.3007
42°	.6691	.7431	.9004	87°	.9986	.0523	19.0811
43°	.6820	.7314	.9325	88°	.9994	.0349	28.6363
44°	.6947	.7193	.9657	89°	.9998	.0175	57.2900
45°	.7071	.7071	1.0000	90°	1.0000	.0000	

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The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION
TENTH YEAR MATHEMATICS

Friday, June 23, 1978 — 1:15 to 4:15 p.m., only

B

Part I Score:

Rater's Initials:
.....

ANSWER SHEET

Pupil.....Teacher.....

School.....

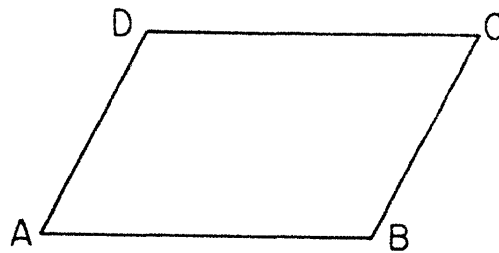
Name and author of textbook used.....

Your answers to Part I should be recorded on this answer sheet.

Part I

Answer all questions in this part.

- | | | |
|---------|---------|---|
| 1..... | 11..... | 21..... |
| 2..... | 12..... | 22..... |
| 3..... | 13..... | 23..... |
| 4..... | 14..... | 24..... |
| 5..... | 15..... | 25..... |
| 6..... | 16..... | 26..... |
| 7..... | 17..... | 27..... |
| 8..... | 18..... | 28..... |
| 9..... | 19..... | 29..... |
| 10..... | 20..... | 30 Answer question 30 on the other
side of this sheet. |



Your answers for Part II should be placed on paper provided by the school.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination, and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature

FOR TEACHERS ONLY

10

SCORING KEY
TENTH YEAR MATHEMATICS

B

Friday, June 23, 1978 — 1:15 to 4:15 p.m., only

Use only *red* ink or *red* pencil in rating Regents papers. Do not attempt to *correct* the pupil's work by making insertions or changes of any kind. Use checkmarks to indicate pupil errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Part I

Allow 2 credits for each correct answer; allow no partial credit. For questions 18–29, allow credit if the pupil has written the correct answer instead of the numeral 1, 2, 3, or 4.

(1) 6	(11) 10	(21) 4
(2) 75	(12) 32	(22) 3
(3) \overline{TR} or s	(13) 95	(23) 2
(4) 125	(14) 66	(24) 1
(5) 75	(15) 5	(25) 2
(6) 10	(16) 8	(26) 2
(7) 51	(17) 2	(27) 3
(8) $4\sqrt{3}$ or $\sqrt{48}$	(18) 3	(28) 1
(9) $4\sqrt{2}$ or $\sqrt{32}$	(19) 4	(29) 4
(10) 4	(20) 1	

[OVER]

TENTH YEAR MATHEMATICS — *concluded*

Part II

Please refer to the Department's pamphlet *Suggestions on the Rating of Regents Examination Papers in Mathematics*. Care should be exercised in making deductions as to whether the error is purely a mechanical one or due to a violation of some principle. A mechanical error generally should receive a deduction of 10 percent, while an error due to a violation of some cardinal principle should receive a deduction ranging from 30 percent to 50 percent, depending on the relative importance of the principle in the solution of the problem.

(35) a 70 [2]

b 90 [2]

c 65 [3]

d 115 [3]

(36) a (5, -1) or $x = 5, y = -1$ [2]

$$b \left(\frac{3+r}{2}, \frac{-7+t}{2} \right)$$

or

$$x = \frac{3+r}{2}, y = \frac{-7+t}{2} [4]$$

c 7 [2]

d 5 [2]

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fully, tea