

University of the State of New York

Examination Department

138TH EXAMINATION

PLANE TRIGONOMETRY

Thursday, June 18, 1896—9:15 a. m. to 12:15 p. m., only

100 credits, necessary to pass, 75

Answer 10 questions but no more. If more than 10 questions are answered only the first 10 of these answers will be considered. Division of groups is not allowed.  $A$ ,  $B$  and  $C$  represent the angles of a triangle,  $a$ ,  $b$  and  $c$  the opposite sides and  $S$  the area. In a right triangle  $C$  represents the right angle and  $c$  the hypotenuse. Each complete answer will receive 10 credits.

- 1 Define negative angle, tangent, cosecant, solution of a triangle, logarithm.
- 2 State and explain the rule for finding the characteristic of the logarithm of an integral number; of a decimal number.
- 3 Refer each of the following angles to its proper quadrant:  $289^\circ$ ,  $186^\circ$ ,  $168^\circ$ ,  $-80^\circ$ ,  $-188^\circ$ . Explain each answer.
- 4 Construct the negative functions of an arc in the second quadrant. Designate each negative function by name.
- 5 Express each function of  $A$  in terms of  $\tan A$ .
- 6 Prove that  $\cos A$  is equal to  $\sin A \operatorname{ctn} A$ ;  $\cos A$  is less than  $\operatorname{ctn} A$ ;  $\cos A$  is not greater than 1.
- 7 Deduce the values of all the functions of  $30^\circ$ .
- 8 Prove that  $\tan (180^\circ - A) = -\tan A$  and  $\tan (180^\circ + A) = +\tan A$ .
- 9-10 Compute the values of  $\sin B$ ,  $\cos B$ ,  $a$  and  $c$  of a right triangle, when  $\tan A = \frac{3}{4}$  and  $b = 50$ .
- 11 Prove that in any plane oblique triangle  $a + b : a - b = \tan \frac{1}{2} (A + B) : \tan \frac{1}{2} (A - B)$ .
- 12-13 Derive the formulas for computing  $C$ ,  $b$ ,  $c$  and  $S$  of an oblique triangle when  $A$ ,  $B$ , and  $a$  are given.
- 14-15 A tree stands on the side of a hill. Show what measurements must be made and what formulas are necessary to find  $h$ , the height of the tree;  $d$ , the distance from the observer to the top of the tree;  $d'$ , the distance from the observer to a point in the plane of the observer directly under the tree.