

University of the State of New York
Examinations Department

80th examination

PLANE TRIGONOMETRY

Thursday, March 17, 1892—9:15 a. m. to 12:15 p. m., only

40 credits, necessary to pass, 30

NOTE.—Draw carefully and neatly each figure, using letters instead of numerals. Arrange work logically.

1. Define (*a*) quadrant; (*b*) complement of an angle; (*c*) natural tangent; (*d*) logarithmic sine; (*e*) horizontal angle. 5
2. Name each function of an angle of a triangle which may be negative. State when the function would be negative and why. 4
3. Trace the changes in value and sign of $\sin A$ as A increases from 0° to 360° . 4
4. (*a*) Find the value of A when $\cot \frac{1}{2} A = \tan A$. 2
 (*b*) When $m = \tan A + \sin A$ and $n = \tan A - \sin A$, prove that $\frac{m-n}{m+n} = \cos A$. 3
5. Show how to find the value of $\cos 30^\circ$ and $\tan 15^\circ$ when $\sin 30^\circ = \frac{1}{2}$. 5
6. Let A , B and C represent the angles of an oblique triangle and a , b and c their opposite sides respectively; prove that
 (*a*) $\tan \frac{1}{2} (A + B) = \cot \frac{1}{2} C$. 2
 (*b*) $a + b : a - b = \tan \frac{1}{2} (A + B) : \tan \frac{1}{2} (A - B)$. 4
7. Given a and b the adjacent sides of a parallelogram and C the included angle, to find the formula for computing (*a*) the longer diagonal; (*b*) the area. 5
8. A tree stands on an inaccessible hill. From a point N of a plain the angles of elevation to the top and the bottom of the tree are A° and B° respectively. At a point M of the plain, d feet back from N and in-line with the tree, the angle of elevation to the top of the tree is C° . Show how to obtain the formula by which h , the height of the tree may be computed. 6