

Examination Department

142D EXAMINATION

PLANE TRIGONOMETRY

Thursday, January 28, 1897—9:15 a. m. to 12:15 p. m., only

100 credits, necessary to pass, 75

Answer 10 questions but no more. If more than 10 questions are answered only the first 10 of these answers will be considered. A , B and C represent the angles of a triangle, a , b and c the opposite sides, S the area. In a right triangle C represents the right angle and c the hypotenuse. Each complete answer will receive 10 credits.

1 Define cosine, logarithmic cosecant, angle of the third quadrant, negative angle, solution of a triangle.

2 How many degrees are there in an angle represented by $\frac{1}{2}\pi$, $\frac{3}{4}\pi$, 2π , $\frac{3}{16}\pi$, $n\pi$?

3 Construct the negative functions of a negative arc in the third quadrant, and write the name of each negative function.

4 Find the value of the other functions of A when $\text{ctn } A = \frac{8}{15}$

5 If A is an acute angle, show that $\tan A$ is greater than $\sin A$.

6 If $\sec A = n \tan A$, what is the value of each of the functions of A ?

7 Prove that any function of an angle is equal to the co-function of its complement.

8 If $2 \cos A + \sec A = 3$, what is the value of A ?

9 Prove that $\cos(A+B) = \cos A \cos B - \sin A \sin B$.

10 Given $\log 2 = .30$, $\log 3 = .48$, $\log 5 = .70$ and $\log 7 = .85$; find the logarithms of 42, .056, 3.75, $3^{\frac{4}{3}}$, $2^{\frac{7}{18}}$

11 Given $\log \cos 20^\circ = 9.97$ and $\log \text{ctn } 20^\circ = 10.44$; find each of the other logarithmic functions of 20°

12 Prove that in any plane triangle $b+c : b-c = \tan \frac{1}{2}(B+C) : \tan \frac{1}{2}(B-C) = \text{ctn } \frac{1}{2}A : \tan \frac{1}{2}(B-C)$.

13 In an oblique triangle, given a , b and c ; derive the formulas for computing A , B , C .

14 Prove that in an oblique triangle $2R = \frac{a}{\sin A} = \frac{b}{\sin B}$, R being the radius of the circumscribed circle.

15 A fort stands on a horizontal plain; the angle of depression measured from the top of the fort to a point P on the plain is A° , and to a point R , a feet beyond P , is B° . Derive the formulas for computing h , the height of the fort, and d , the distance from P to the bottom of the fort.