The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

MATHEMATICS A

Tuesday, January 23, 2001 — 1:15 to 4:15 p.m., only

Print Your Name:			
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Print Your School's	Name:		

Print your name and the name of your school in the boxes above. Then turn to the last page of this booklet, which is the answer sheet for Part I. Fold the last page along the perforations and, slowly and carefully, tear off the answer sheet. Then fill in the heading of your answer sheet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. Any work done on this sheet of scrap graph paper will *not* be scored. All work should be written in pen, except graphs and drawings, which should be done in pencil.

This examination has four parts, with a total of 35 questions. You must answer all questions in this examination. Write your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers for the questions in Parts II, III, and IV directly in this booklet. Clearly indicate the necessary steps you take, including appropriate formula substitutions, diagrams, graphs, charts, etc.

When you have completed the examination, you must sign the statement printed at the end of the answer paper, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer paper cannot be accepted if you fail to sign this declaration.

Notice...

A minimum of a scientific calculator, a straightedge (ruler), and a compass must be available for your use while taking this examination.

Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Record your answers in the spaces provided on the separate answer sheet. [40]

Use this space for

computations.

1 There are 461 students and 20 teachers taking buses on a trip to a museum. Each bus can seat a maximum of 52. What is the *least* number of buses needed for the trip?

- (1) 8 (3) 10
- (2) 9 (4) 11
- **2** In right triangle *ABC*, $m \angle C = 3y 10$, $m \angle B = y + 40$, and $m \angle A = 90$. What type of right triangle is triangle *ABC*?
 - (1) scalene (3) equilateral
 - (2) isosceles (4) obtuse
- **3** If x > 0, the expression $(\sqrt{x})(\sqrt{2x})$ is equivalent to

(1)	$\sqrt{2x}$	(3)	$x^2\sqrt{2}$
(2)	2x	(4)	$x\sqrt{2}$

- **4** Three times as many robins as cardinals visited a bird feeder. If a total of 20 robins and cardinals visited the feeder, how many were robins?
- **5** One of the factors of $4x^2 9$ is

(1)	(x + 3)	(3)	(4x - 3)
(2)	(2x + 3)	(4)	(x - 3)

6 At a school fair, the spinner represented in the accompanying diagram is spun twice.



What is the probability that it will land in section G the first time and then in section B the second time?

(1)	1	(3) $\frac{1}{2}$	
(-)	2	(3) 8	

(2) $\frac{1}{4}$ (4) $\frac{1}{16}$

7 If *a* and *b* are integers, which equation is always true?

Use this space for computations.

(1) $\frac{a}{b} = \frac{b}{a}$	(3) $a - b = b - a$
(2) $a + 2b = b + 2a$	(4) $a + b = b + a$

8 The sum of $3x^2 + 4x - 2$ and $x^2 - 5x + 3$ is

(1)	$4x^2 + x - 1$	(3) $4x^2 + x + 1$
(2)	$4x^2 - x + 1$	(4) $4x^2 - x - 1$

9 If $x \neq 0$, the expression $\frac{x^2 + 2x}{x}$ is equivalent to

10 Helen is using a capital H in an art design. The H has

- (1) only one line of symmetry
- (2) only two points of symmetry
- (3) two lines of symmetry and only one point of symmetry
- (4) two lines of symmetry and two points of symmetry
- 11 The distance from Earth to the Sun is approximately 93 million miles. A scientist would write that number as
- 12 Given the statement: "If two sides of a triangle are congruent, then the angles opposite these sides are congruent."

Given the converse of the statement: "If two angles of a triangle are congruent, then the sides opposite these angles are congruent."

What is true about this statement and its converse?

- (1) Both the statement and its converse are true.
- (2) Neither the statement nor its converse is true.
- (3) The statement is true but its converse is false.
- (4) The statement is false but its converse is true.
- **13** Which equation could represent the relationship between the x and y values shown in the accompanying table?

	x	y
	0	2
	1	3
	2	6
	3	11
	4	18
(3) (4)	y = y =	$\frac{x^2}{2^x}$

(1) y = x + 2(2) $y = x^2 + 2$ 14 A locker combination system uses three digits from 0 to 9. How many different three-digit combinations with no digit repeated are possible?

Use this space for computations.

- $(1) \ 30 \qquad \qquad (3) \ 720$
- (2) 504 (4) 1,000



15 What is the slope of line ℓ in the accompanying diagram?

16 If bx - 2 = K, then x equals

(1)	$\frac{K}{b} + 2$	(3)	$\frac{2-K}{b}$
(2)	$\frac{K-2}{b}$	(4)	$\frac{K+2}{b}$

17 In a molecule of water, there are two atoms of hydrogen and one atom of oxygen. How many atoms of hydrogen are in 28 molecules of water?

(1)	14	(3)	42
(2)	29	(4)	56

18 From January 3 to January 7, Buffalo recorded the following daily high temperatures: 5°, 7°, 6°, 5°, and 7°. Which statement about the temperatures is true?

(2) mean = mode (4) mean < median

19 In which of the accompanying figures are segments *XY* and *YZ* perpendicular?

Use this space for computations.



- (1) figure 1, only
- (2) figure 2, only
- (3) both figure 1 and figure 2
- (4) neither figure 1 nor figure 2
- **20** Let *x* and *y* be numbers such that 0 < x < y < 1, and let d = x y. Which graph could represent the location of *d* on the number line?



Part II

Answer all questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [10]



22 Sue bought a picnic table on sale for 50% off the original price. The store charged her 10% tax and her final cost was \$22.00. What was the original price of the picnic table?	
 23 A cardboard box has length x – 2, width x + 1, and height 2x. a Write an expression, in terms of x, to represent the volume of the box. 	
b If x = 8 centimeters, what is the number of cubic centimeters in the volume of the box?	

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25 Two trains leave the same station at the same time and travel in opposite directions. One train travels at 80 kilometers per hour and the other at 100 kilometers per hour. In how many hours will they be 900 kilometers apart?

Part III

Answer all questions in this part. Each correct answer will receive 3 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [15]

26 Sal has a small bag of candy containing three green candies and two red candies. While waiting for the bus, he ate two candies out of the bag, one after another, without looking. What is the probability that both candies were the same color?

27 Steve has a treasure map, represented in the accompanying diagram, that shows two trees 8 feet apart and a straight fence connecting them. The map states that treasure is buried 3 feet from the fence and equidistant from the two trees. 8 ft a Sketch a diagram to show all the places where the treasure could be buried. Clearly indicate in your diagram where the treasure could be buried. *b* What is the distance between the treasure and one of the trees?



29 Mark says, "The number I see is odd." Jan says, "That same number is prime." The teacher says, "Mark is correct or Jan is correct." Some integers would make the teacher's statement true while other integers would make it false. Give and explain *one* example of when the teacher's statement is true. Give and explain *one* example of when the teacher's statement is false.

30 Juan has a cellular phone that costs \$12.95 per month plus 25¢ per minute for each call. Tiffany has a cellular phone that costs \$14.95 per month plus 15¢ per minute for each call. For what number of minutes do the two plans cost the same?

Part IV

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [20]

31 Solve algebraically for *x*: $\frac{1}{x} = \frac{x+1}{6}$

32 On a science quiz, 20 students received the following scores: 100, 95, 95, 90, 85, 85, 85, 80, 80, 80, 75, 75, 75, 70, 70, 65, 65, 60, 55.

Construct a statistical graph, such as a histogram or a stem-and-leaf plot, to display this data. [*Be sure to title the graph and label all axes or parts used.*]

If your type of plot requires a grid, show your work here.

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If no grid is necessary, show your work here.



- **34** There were 100 more balcony tickets than main-floor tickets sold for a concert. The balcony tickets sold for \$4 and the main-floor tickets sold for \$12. The total amount of sales for both types of tickets was \$3,056.
 - *a* Write an equation or a system of equations that describes the given situation. Define the variables.

b Find the number of balcony tickets that were sold.

35 Find, to the *nearest tenth of a foot*, the height of the tree represented in the accompanying diagram.



15 ft (Not drawn to scale)



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Scrap Graph Paper — This sheet will *not* be scored.



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REGENTS HIGH SCHOOL EXAMINATION

MATHEMATICS A

Tuesday, January 23, 2001 — 1:15 to 4:15 p.m., only

ANSWER SHEET

Pupil	Sex: \Box Male \Box Female Grade
Teacher	School

Your answers to Part I should be recorded on this answer sheet.

Part I

Answer all 20 questions in this part.

1	6	11	16
2	7	12	17
3	8	13	18
4	9	14	19
5	10	15	20

Your answers for Parts II, III, and IV should be written in the test booklet.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature

MATHEMATICS A						
Questi	on	Maximum Credit	Credits Earned	Rater's/Scorer's Initials		
Part I 1	-20	40				
Part II	21	2				
	22	2				
	23	2				
	24	2				
	25	2				
Part III	26	3				
	27	3				
	28	3				
	29	3				
	30	3				
Part IV	31	4				
	32	4				
	33	4				
	34	4				
	35	4				
Maximum Total		85				
			Total Raw Score	Checked by		

Notes to raters. . .

- Each paper should be scored by a minimum of three raters.
- The table for converting the total raw score to the scaled score is provided in the scoring key for this examination.
- The scaled score is the student's final examination score.

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FOR TEACHERS ONLY

The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

MATHEMATICS A

Tuesday, January 23, 2001 — 1:15 to 4:15 p.m., only

SCORING KEY

Mechanics of Rating

The following procedures are to be followed for scoring student answer papers for the Mathematics A examination. More detailed information about scoring is provided in the publication *Information Booklet for Administering and Scoring the Regents Examination in Mathematics* A.

Use only *red* ink or *red* pencil in rating Regents papers. Do not attempt to *correct* the student's work by making insertions or changes of any kind. Use checkmarks to indicate student errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Each student's answer paper is to be scored by a minimum of three mathematics teachers. On the back of the student's detachable answer sheet, raters must enter their initials in the boxes next to the questions they have scored and also write their name in the box under the heading "Rater's/Scorer's Name."

Raters should record the student's scores for all questions and the total raw score on the student's detachable answer sheet. Then the student's total raw score should be converted to a scaled score by using the conversion chart printed at the end of this key. The student's scaled score should be entered in the box provided on the student's detachable answer sheet. The scaled score is the student's final examination score.

Part I

Allow a total of 40 credits, 2 credits for each of the following. Allow credit if the student has written the correct answer instead of the numeral 1, 2, 3, or 4.

(2) 1 (7) 4 (12) 1 (17) 4

(3) 4 (8) 2 (13) 2 (18) 1

(4) 3 (9) 1 (14) 3 (19) 3

(5) 2 (10) 3 (15) 2 (20) 4

[OVER]

Part II

For each question, use the specific criteria to award a maximum of two credits.

- (21) *a* [1] *B*, and an appropriate explanation is given.
 - *b* [1] 5 minutes

a and b

- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (22) **[2]** \$40, and appropriate work is shown.
 - [1] Appropriate work is shown, but one computational error is made.

or

- [1] \$40, but no work is shown.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(23) a [1] Either (x - 2)(x + 1)(2x) = V or the same expression without "= V" is shown.

or

- [1] $2x^3 2x^2 4x$ or an equivalent expression is shown.
- *b* **[1]** 864

- [1] The student substitutes appropriately into an incorrect part *a* equation.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (24) [2] A'(0,-2) and B'(4,-6) are stated, and an appropriate graph is drawn.
 - [1] Only one endpoint, A' or B', is graphed and stated correctly.

or

[1] Both endpoints are reflected in other than the *x*-axis, and the coordinates are graphed and stated correctly, such as:

y-axis A'(0,2) and B'(-4,6) y = x A'(2,0) and B'(6,4)Origin A'(0,-2) and B'(-4,-6)

or

[1] Both points A' and B' are stated correctly, but no graph is drawn.

or

- [1] An appropriate graph is drawn, but no coordinates or incorrect coordinates are labeled.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(25) [2] 5, and appropriate work is shown, such as solving the linear equation 80x + 100x = 900, using a diagram or proportion or trial and error.

[1] Appropriate work is shown, but one computational error is made.

- [1] 5, but no work is shown.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

Part III

For each question, use the specific criteria to award a maximum of three credits.

- (26) **[3]** $\frac{8}{20}$ or an equivalent answer, and appropriate work is shown, such as using a tree diagram or writing the equation $\frac{6}{20} + \frac{2}{20} = \frac{8}{20}$.
 - [2] One computational error is made in finding $\frac{6}{20}$ or $\frac{2}{20}$, but an appropriate sum is found.

or

- [2] $\frac{2}{20}$ and $\frac{6}{20}$ are found, but no sum is shown.
- [1] $\frac{6}{20}$ or $\frac{2}{20}$, and appropriate work is shown.

or

[1] An appropriate answer is found, using replacement with a tree diagram or an equation such as $\frac{3}{5} \cdot \frac{3}{5} + \frac{2}{5} \cdot \frac{2}{5} = \frac{13}{25}$.

or

- [1] $\frac{8}{20}$, but no work is shown.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (27) a [2] A correct sketch is drawn that shows two possible locations, such as parallel lines and a perpendicular bisector. Students can draw their own sketch or use the diagram given.
 - [1] A correct sketch is drawn, but with no indication of where the treasure is buried.

or

- [1] A partial sketch is drawn, showing either the distances from the fence or the distance from the trees.
- *b* **[1]** 5 feet

- [1] An appropriate answer is found for an incorrect part *a*.
- a and b
 - **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (28) **[3]** 120, and appropriate work is shown, such as 6t + 30 + 8t 60 = 180.
 - [2] The student finds correctly the unknown, t = 15, but does not find the measure of angle 4.

or

- [2] Appropriate work is shown, but one computational error is made.
- [1] The student forms an incorrect equation, such as setting the two angles equal, and arrives at t = 45 and an angle of 300.

or

- [1] 120, but no work is shown.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (29) [3] At least one example is shown that makes the statement true, such as 2, 3, 5, 7, 9, or a defined variable; and one example is shown that makes the statement false, such as any even number other than 2, with a correct explanation that shows that the student can recognize odd numbers and prime numbers. The explanation can be in words or as a Venn diagram.
 - [2] Two correct examples are shown, one that shows the statement is true and one that shows the statement is false, but no explanation or an inappropriate explanation is given.

- [2] Only one correct example is shown, but an appropriate explanation is given.
- [1] Only one correct example is shown, and no explanation or an incorrect explanation is given.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (30) **[3]** 20, and appropriate work is shown, such as an equation, trial and error, or a graph.
 - [2] Appropriate work is shown, such as 12.95 + 0.25x = 14.95 + 0.15x, but one computational error is made.

or

[2] Appropriate work is shown, but an answer of \$17.95 is found.

or

- [2] 20, and only a check is shown.
- [1] The student starts appropriate work to find when the prices are equal but does not complete it, such as starting to solve the correct equation, showing one incorrect trial, or drawing an incomplete graph.

- [1] 20, but no work is shown.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

Part IV

For each question, use the specific criteria to award a maximum of four credits.

- (31) [4] 2 and –3, and a correct quadratic equation is shown, such as x(x + 1) = 6, and solved algebraically.
 - [3] The student shows a correct quadratic equation but makes one algebraic error and carries it to solution or no solution for the equation generated.

or

- [3] Correct work is shown, but only one root is found as the answer.
- [2] A correct quadratic equation is used, but two or more errors are made.

or

- [2] An incorrect quadratic equation of equal difficulty is shown and solved appropriately.
- [1] The student cross multiplies but produces only a linear equation that is solved appropriately.

- [1] 2 and –3, but no algebraic work is shown.
- **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (32) [4] The student draws a histogram, a stem-and-leaf plot, or any other acceptable statistical graph, with proper labels and a title.
 - [3] The student makes one or two minor errors, such as a lack of label, title, or connected dots.
 - [2] The student makes several minor errors or one major error, such as not accounting for all 20 scores.
 - [1] The student draws just the beginning of a graph.
 - **[0]** A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (33) a [2] The student draws a circle with its center at (0,0) and a radius of 3.
 - [1] The student draws a circle, but it has an incorrect center or radius.
 - b [2] 28, and appropriate work or the expression 9π is shown, which rounds to 28.

or

- [2] An appropriate area is shown for the incorrect figure in part *a*.
- [1] The correct expression is shown, but the answer is left as 9π , not rounded, or not rounded correctly.

or

[1] An incorrect radius is used, but the area is rounded appropriately.

a and b

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(34) *a* **[2]** The student writes an appropriate system of equations, such as b = f + 100 and 4b + 12f = 3,056, and defines the variables.

or

- [2] The student writes an appropriate equation, such as 4(100 + x) + 12x = 3,056, and defines the variable.
- [1] A correct equation or correct equations are shown, but the variables are not defined.

or

- [1] One error is made in the setup, such as b + f = 100.
- **[0]** The student only defines the variables.
- *b* **[2]** 266, and appropriate work is shown, using an algebraic solution or a correct trialand-error method.

or

- [2] Appropriate work is shown for an incorrect part *a* equation or system of equations.
- [1] Work is shown, but the answer is inappropriate, such as \$1,064.

or

[1] 266, but no work is shown.

a and b

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(35) [4] 28.2, and an appropriate equation is shown, such as $\tan 62 = \frac{x}{15}$.

[3] Appropriate work is shown, but the answer is rounded incorrectly.

or

- [3] The student uses the correct tangent function and rounds the answer, but makes one computational error.
- [2] The student uses the correct tangent function, but makes several errors.

or

[2] An incorrect trigonometric function is used, but appropriate work is shown.

[1] The tangent function is indicated, but the ratio is set up incorrectly.

or

[1] 28.2, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

MATHEMATICS A

Map to	Learning	Stand	lards
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Key Ideas	Item Numbers
Mathematical Reasoning	12, 29
Number and Numeration	7, 22
Operations	2, 3, 5, 8, 9, 10, 11, 20
Modeling/Multiple Representation	1, 16, 19, 24, 27, 28
Measurement	15, 17, 18, 21, 23, 25, 32, 35
Uncertainty	6, 14, 26
Patterns/Functions	4, 13, 30, 31, 33, 34

Regents Examination in Mathematics A

January 2001

Chart for Converting Total Test Raw Scores to Final Examination Scores (Scaled Scores)

Raw	Scaled	Raw	Scaled	Raw	Scaled
Score	Score	Score	Score	Score	Score
85	100	56	75	27	45
84	99	55	74	26	44
83	99	54	73	25	43
82	98	53	72	24	42
81	98	52	71	23	41
80	97	51	70	22	40
79	96	50	69	21	39
78	95	49	68	20	38
77	94	48	67	19	37
76	94	47	66	18	36
75	93	46	65	17	35
74	92	45	64	16	34
73	91	44	63	15	33
72	90	43	62	14	32
71	89	42	61	13	31
70	88	41	60	12	30
69	87	40	59	11	29
68	86	39	58	10	28
67	86	38	57	9	27
66	85	37	56	8	26
65	84	36	55	7	25
64	83	35	53	6	24
63	82	34	52	5	22
62	81	33	51	4	19
61	80	32	50	3	15
60	79	31	49	2	10
59	78	30	48	1	5
58	77	29	47	0	0
57	76	28	46		

To determine the student's final examination score, find the student's total test raw score in the column labeled "Raw Score" and then locate the scaled score that corresponds to that raw score. The scaled score is the student's final examination score. Enter this score in the space labeled "Scaled Score" on the student's answer sheet.

All student answer papers that receive a scaled score of 60 through 64 **must** be scored a second time. For the second scoring, a different committee of teachers may score the student's paper or the original committee may score the paper, except that no teacher may score the same open-ended questions that he/she scored in the first rating of the paper. The school principal is responsible for assuring that the student's final examination score is based on a fair, accurate, and reliable scoring of the student's answer paper.

Because scaled scores corresponding to raw scores in the conversion chart may change from one examination to another, it is crucial that for each administration, the conversion chart provided in the scoring key for that administration be used to determine the student's final score. The chart above is usable only for this administration of the mathematics A examination.