

The University of the State of New York

EXAMINATION FOR QUALIFYING CERTIFICATES

INTERMEDIATE ALGEBRA

Tuesday, September 11, 1917—9.15 a. m. to 12.15 p. m., only

Answer question 1 and seven of the others. Each answer should be reduced to its simplest form. Papers entitled to less than 75 credits will not be accepted.

1 Without solving the equations, discuss the nature of the roots of

$$x^2 - 4x + 5 = 0$$

$$x + \frac{1}{x} = a + \frac{1}{a}$$

$$\frac{4}{x-1} - \frac{3}{x-2} = \frac{2}{x-3} - \frac{1}{x-4}$$

2 Simplify $(2 \pm \sqrt{(-2)^3}) - (-1 \pm \sqrt{(-2)^4})$

3 The floor of a room contains 320 square feet; one end wall is 152 square feet and one side wall is 190 square feet. Find the dimensions of the room.

4 Factor the following:

$$6x^4 + 2x^2y^2 - 8y^4$$

$$3x^2 + 6xy - 24y^2$$

$$6a^2 + 3ab + 2ac + bc$$

$$x^7 + x^4 - 16x^3 - 16$$

5 What two numbers whose sum is m are to each other as r is to s ?

6 If the second, fourth and eighth terms of an arithmetic series are in geometric progression, find the numeric relation between the first term and the common difference.

7 Solve $\begin{cases} x^2 - xy - 12y^2 = 8 \\ x^2 + xy - 10y^2 = 20 \end{cases}$

8 Find the square root of

$$a^{-2} + 9b^{\frac{2}{3}} + 16c^{-\frac{1}{2}} + 6a^{-1}b^{\frac{2}{3}} - 8a^{-1}c^{-\frac{1}{2}} - 24b^{\frac{2}{3}}c^{-\frac{1}{2}}$$

9 Find the values of the literal coefficients in the following equations:

$$ax^2 + 3x - 4 = 0 \text{ if one root is } 2$$

$$x^2 - 5x + c = 0 \text{ if the difference of the roots is } 3$$

10 For what value of k is one of the roots of the equation $(k-4)x^2 - (2k-1)x = 7-5k$ double the other?

11 Define polynomial, elimination, factor, coefficient.