

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

ELEVENTH YEAR MATHEMATICS

Thursday, January 25, 1979 — 1:15 to 4:15 p.m., only

The last page of the booklet is the answer sheet. Fold the last page along the perforations and, slowly and carefully, tear off the answer sheet. Then fill in the heading of your answer sheet.

The "Reference Tables for Mathematics" which you may need to answer some questions in this examination are stapled in the center of this booklet.

When you have completed the examination, you must sign the statement printed at the end of the answer paper, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer paper cannot be accepted if you fail to sign this declaration.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN

Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Unless otherwise specified, answers may be left in terms of π or in radical form. Write your answers in the spaces provided on the separate answer sheet.

- 1 If s varies directly as t and $s = 15$ when $t = 25$, find the value of s when $t = 10$.

- 2 Solve the following system of equations for $\sin A$:

$$\begin{aligned}4 \sin A + \cos B &= 2 \\2 \sin A + \cos B &= 1\end{aligned}$$

- 3 Factor: $12y^2 - 11y + 2$

$$\frac{1}{\sqrt{3}} - \frac{4}{\sqrt{3}}$$

- 4 Express in simplest form: $\frac{\sqrt{3}}{\sqrt{3}}$

- 5 Given: $A = \frac{2gr}{g + r}$

If $A = 4$, find the value of g when $r = 1$.

- 6 A straight line passes through the points $(1, 5)$, $(2, 3)$, and $(7, k)$. Find the numerical value of k .

- 7 Solve for x : $x^{\frac{1}{2}} = 3 - x^0$

- 8 Find $\sin 54^\circ 27'$.

- 9 Express, in radians, an angle of 280° .

- 10 In acute triangle ABC , $a = 4$, $b = 3$, and $\sin B = \frac{1}{2}$. Find the numerical value of $\sin A$.

- 11 If the number 0.000073 is written in the form 7.3×10^n , what is the value of n ?

Directions (12–30): Write in the space provided on the separate answer sheet the numeral preceding the expression that best completes each statement or answers each question.

- 12 The sum of $\sqrt{-4}$ and $\sqrt{-16}$ is

$$\begin{array}{ll}(1) -6 & (3) -20 \\(2) 6i & (4) 2i\sqrt{5}\end{array}$$

- 13 What is the amplitude of the graph of the function $y = \cos 2x$?

$$\begin{array}{ll}(1) 1 & (3) \frac{1}{2} \\(2) 2 & (4) 0\end{array}$$

- 14 The statement $\log_b x + \log_b y$ is equivalent to

$$\begin{array}{ll}(1) \log_b(x + y) & (3) \log_b\left(\frac{x}{y}\right) \\(2) \log_b(x - y) & (4) \log_b(xy)\end{array}$$

- 15 What is the solution set of the inequality $|x - 1| < 5$?

$$\begin{array}{ll}(1) \{x | -6 < x < 4\} & \\(2) \{x | -4 < x < 6\} & \\(3) \{x | x < -4 \text{ or } x > 6\} & \\(4) \{x | x < -6 \text{ or } x > 4\} &\end{array}$$

- 16 If $3 \sin x = 1$, then which is an expression for x in inverse trigonometric form?

$$\begin{array}{ll}(1) x = \text{Arc sin } 3 & (3) x = \text{Arc sin } \frac{1}{3} \\(2) x = \text{Arc sin } (-3) & (4) x = \text{Arc sin } (-\frac{1}{3})\end{array}$$

- 17 The fraction $\frac{3}{\sqrt{6} - 1}$ is equivalent to

$$\begin{array}{ll}(1) \frac{3\sqrt{6} - 3}{5} & (3) 3\sqrt{6} - 3 \\(2) \frac{3\sqrt{6} + 3}{5} & (4) 3\sqrt{6} + 3\end{array}$$

- 18 The graph of the equation $xy = 4$ is

$$\begin{array}{ll}(1) \text{a hyperbola} & (3) \text{an ellipse} \\(2) \text{a parabola} & (4) \text{a circle}\end{array}$$

- 19 The coordinates of one of the intersections of the graphs of $y = x^2$ and $y = x + 2$ are

$$\begin{array}{ll}(1) (1, 1) & (3) (1, -1) \\(2) (-1, -1) & (4) (-1, 1)\end{array}$$

- 20 The expression $1 - \cos 2x$ is equivalent to

$$\begin{array}{ll}(1) 1 & (3) 2 \sin^2 x \\(2) 0 & (4) -2 \sin^2 x\end{array}$$

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Answers to the following questions are to be placed on paper provided by the school.

Part II

Answer four questions from this part. Show all work unless otherwise directed.

- 31 a Find all the values of θ in the interval $0^\circ \leq \theta \leq 360^\circ$ that satisfy the equation $2 \sin^2 \theta + \sin \theta = 1$. [5]
- b Express the roots of $x^2 + 1 = 4(x - 3)$ in the form of $a + bi$. [5]
- 32 Given the function $\{x, y | y = 5 - 2x - x^2\}$ whose domain is $-4 \leq x \leq 2$.
- a Draw the graph of this function. [6]
- b What are the coordinates of the turning point of this graph? [2]
- c What is the range of the function over the given domain? [2]
- 33 The members of the Midville High School Math Club decided to go on a picnic and agreed to contribute equally to form a fund of \$240 to pay expenses. Three nonmembers asked to join the picnic and were accepted, with the result that each person going on the picnic would have to pay \$4 less than the amount originally agreed upon. How many students originally planned to go on the picnic? [Only an algebraic solution will be accepted.] [10]
- 34 Given: $N = \frac{(3.14)(\tan 70^\circ 40')^2}{\sqrt{49.6}}$

Using logarithms, find N to the nearest tenth. [10] _____

- 35 a Starting with the formula for $\sin(x + y)$, derive the formula for $\sin(x - y)$. [4]

- b For all values of θ for which the expression is defined, show that the following is an identity:

$$(\cos 2\theta)(1 + \tan^2 \theta) = 2 - \frac{1}{\cos^2 \theta} \quad [6]$$

- 36 Answer either a or b, but not both.

- a The area of triangular field ABC is 780 square meters. If the length of side \overline{AC} is 52 meters and $m\angle A = 68^\circ$, what is the length of side \overline{AB} to the nearest meter? [10]

OR

- b A body is acted upon by two forces of 8 and 9 pounds. If the resultant force is 11 pounds, find the angle between the two forces to the nearest degree. [10]

- *37 a On a single set of axes, graph the system of inequalities:

$$\begin{aligned} x^2 + y^2 &\leq 36 \\ x + y &> 4 \end{aligned} \quad [8]$$

- b Give the coordinates of one point in the solution set of the system. [2]

* This question is based on an optional topic in the syllabus.

Reference Tables for Mathematics

Ⓐ Common Logarithms of Numbers*

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| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|------|------|------|------|------|------|------|------|------|------|
| 10 | 0000 | 0043 | 0086 | 0128 | 0170 | 0212 | 0253 | 0294 | 0334 | 0374 |
| 11 | 0414 | 0453 | 0492 | 0531 | 0569 | 0607 | 0645 | 0682 | 0719 | 0755 |
| 12 | 0792 | 0828 | 0864 | 0899 | 0934 | 0969 | 1004 | 1038 | 1072 | 1106 |
| 13 | 1139 | 1173 | 1206 | 1239 | 1271 | 1303 | 1335 | 1367 | 1399 | 1430 |
| 14 | 1461 | 1492 | 1523 | 1553 | 1584 | 1614 | 1644 | 1673 | 1703 | 1732 |
| 15 | 1761 | 1790 | 1818 | 1847 | 1875 | 1903 | 1931 | 1959 | 1987 | 2014 |
| 16 | 2041 | 2068 | 2095 | 2122 | 2148 | 2175 | 2201 | 2227 | 2253 | 2279 |
| 17 | 2304 | 2330 | 2355 | 2380 | 2405 | 2430 | 2455 | 2480 | 2504 | 2529 |
| 18 | 2553 | 2577 | 2601 | 2625 | 2648 | 2672 | 2695 | 2718 | 2742 | 2765 |
| 19 | 2788 | 2810 | 2833 | 2856 | 2878 | 2900 | 2923 | 2945 | 2967 | 2989 |
| 20 | 3010 | 3032 | 3054 | 3075 | 3096 | 3118 | 3139 | 3160 | 3181 | 3201 |
| 21 | 3222 | 3243 | 3263 | 3284 | 3304 | 3324 | 3345 | 3365 | 3385 | 3404 |
| 22 | 3424 | 3444 | 3464 | 3483 | 3502 | 3522 | 3541 | 3560 | 3579 | 3598 |
| 23 | 3617 | 3636 | 3655 | 3674 | 3692 | 3711 | 3729 | 3747 | 3766 | 3784 |
| 24 | 3802 | 3820 | 3838 | 3856 | 3874 | 3892 | 3909 | 3927 | 3945 | 3962 |
| 25 | 3979 | 3997 | 4014 | 4031 | 4048 | 4065 | 4082 | 4099 | 4116 | 4133 |
| 26 | 4150 | 4166 | 4183 | 4200 | 4216 | 4232 | 4249 | 4265 | 4281 | 4298 |
| 27 | 4314 | 4330 | 4346 | 4362 | 4378 | 4393 | 4409 | 4425 | 4440 | 4456 |
| 28 | 4472 | 4487 | 4502 | 4518 | 4533 | 4548 | 4564 | 4579 | 4594 | 4609 |
| 29 | 4624 | 4639 | 4654 | 4669 | 4683 | 4698 | 4713 | 4728 | 4742 | 4757 |
| 30 | 4771 | 4786 | 4800 | 4814 | 4829 | 4843 | 4857 | 4871 | 4886 | 4900 |
| 31 | 4914 | 4928 | 4942 | 4955 | 4969 | 4983 | 4997 | 5011 | 5024 | 5038 |
| 32 | 5051 | 5065 | 5079 | 5092 | 5105 | 5119 | 5132 | 5145 | 5159 | 5172 |
| 33 | 5185 | 5198 | 5211 | 5224 | 5237 | 5250 | 5263 | 5276 | 5289 | 5302 |
| 34 | 5315 | 5328 | 5340 | 5353 | 5366 | 5378 | 5391 | 5403 | 5416 | 5428 |
| 35 | 5441 | 5453 | 5465 | 5478 | 5490 | 5502 | 5514 | 5527 | 5539 | 5551 |
| 36 | 5563 | 5575 | 5587 | 5599 | 5611 | 5623 | 5635 | 5647 | 5658 | 5670 |
| 37 | 5682 | 5694 | 5705 | 5717 | 5729 | 5740 | 5752 | 5763 | 5775 | 5786 |
| 38 | 5798 | 5809 | 5821 | 5832 | 5843 | 5855 | 5866 | 5877 | 5888 | 5899 |
| 39 | 5911 | 5922 | 5933 | 5944 | 5955 | 5966 | 5977 | 5988 | 5999 | 6010 |
| 40 | 6021 | 6031 | 6042 | 6053 | 6064 | 6075 | 6085 | 6096 | 6107 | 6117 |
| 41 | 6128 | 6138 | 6149 | 6160 | 6170 | 6180 | 6191 | 6201 | 6212 | 6222 |
| 42 | 6232 | 6243 | 6253 | 6263 | 6274 | 6284 | 6294 | 6304 | 6314 | 6325 |
| 43 | 6335 | 6345 | 6355 | 6365 | 6375 | 6385 | 6395 | 6405 | 6415 | 6425 |
| 44 | 6435 | 6444 | 6454 | 6464 | 6474 | 6484 | 6493 | 6503 | 6513 | 6522 |
| 45 | 6532 | 6542 | 6551 | 6561 | 6571 | 6580 | 6590 | 6599 | 6609 | 6618 |
| 46 | 6628 | 6637 | 6646 | 6656 | 6665 | 6675 | 6684 | 6693 | 6702 | 6712 |
| 47 | 6721 | 6730 | 6739 | 6749 | 6758 | 6767 | 6776 | 6785 | 6794 | 6803 |
| 48 | 6812 | 6821 | 6830 | 6839 | 6848 | 6857 | 6866 | 6875 | 6884 | 6893 |
| 49 | 6902 | 6911 | 6920 | 6928 | 6937 | 6946 | 6955 | 6964 | 6972 | 6981 |
| 50 | 6990 | 6998 | 7007 | 7016 | 7024 | 7033 | 7042 | 7050 | 7059 | 7067 |
| 51 | 7076 | 7084 | 7093 | 7101 | 7110 | 7118 | 7126 | 7135 | 7143 | 7152 |
| 52 | 7160 | 7168 | 7177 | 7185 | 7193 | 7202 | 7210 | 7218 | 7226 | 7235 |
| 53 | 7243 | 7251 | 7259 | 7267 | 7275 | 7284 | 7292 | 7300 | 7308 | 7316 |
| 54 | 7324 | 7332 | 7340 | 7348 | 7356 | 7364 | 7372 | 7380 | 7388 | 7396 |

N 0 1 2 3 4 5 6 7 8 9

* This table gives the mantissas of numbers with the decimal point omitted in each case. Characteristics are determined from the numbers by inspection.

Ⓐ Common Logarithms of Numbers*

| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|------|------|------|------|------|------|------|------|------|------|
| 55 | 7404 | 7412 | 7419 | 7427 | 7435 | 7443 | 7451 | 7459 | 7466 | 7474 |
| 56 | 7482 | 7490 | 7497 | 7505 | 7513 | 7520 | 7528 | 7536 | 7543 | 7551 |
| 57 | 7559 | 7566 | 7574 | 7582 | 7589 | 7597 | 7604 | 7612 | 7619 | 7627 |
| 58 | 7634 | 7642 | 7649 | 7657 | 7664 | 7672 | 7679 | 7686 | 7694 | 7701 |
| 59 | 7709 | 7716 | 7723 | 7731 | 7738 | 7745 | 7752 | 7760 | 7767 | 7774 |
| 60 | 7782 | 7789 | 7796 | 7803 | 7810 | 7818 | 7825 | 7832 | 7839 | 7846 |
| 61 | 7853 | 7860 | 7868 | 7875 | 7882 | 7889 | 7896 | 7903 | 7910 | 7917 |
| 62 | 7924 | 7931 | 7938 | 7945 | 7952 | 7959 | 7966 | 7973 | 7980 | 7987 |
| 63 | 7993 | 8000 | 8007 | 8014 | 8021 | 8028 | 8035 | 8041 | 8048 | 8055 |
| 64 | 8062 | 8069 | 8075 | 8082 | 8089 | 8096 | 8102 | 8109 | 8116 | 8122 |
| 65 | 8129 | 8136 | 8142 | 8149 | 8156 | 8162 | 8169 | 8176 | 8182 | 8189 |
| 66 | 8195 | 8202 | 8209 | 8215 | 8222 | 8228 | 8235 | 8241 | 8248 | 8254 |
| 67 | 8261 | 8267 | 8274 | 8280 | 8287 | 8293 | 8299 | 8306 | 8312 | 8319 |
| 68 | 8325 | 8331 | 8338 | 8344 | 8351 | 8357 | 8363 | 8370 | 8376 | 8382 |
| 69 | 8388 | 8395 | 8401 | 8407 | 8414 | 8420 | 8426 | 8432 | 8439 | 8445 |
| 70 | 8451 | 8457 | 8463 | 8470 | 8476 | 8482 | 8488 | 8494 | 8500 | 8506 |
| 71 | 8513 | 8519 | 8525 | 8531 | 8537 | 8543 | 8549 | 8555 | 8561 | 8567 |
| 72 | 8573 | 8579 | 8585 | 8591 | 8597 | 8603 | 8609 | 8615 | 8621 | 8627 |
| 73 | 8633 | 8639 | 8645 | 8651 | 8657 | 8663 | 8669 | 8675 | 8681 | 8686 |
| 74 | 8692 | 8698 | 8704 | 8710 | 8716 | 8722 | 8727 | 8733 | 8739 | 8745 |
| 75 | 8751 | 8756 | 8762 | 8768 | 8774 | 8779 | 8785 | 8791 | 8797 | 8802 |
| 76 | 8808 | 8814 | 8820 | 8825 | 8831 | 8837 | 8842 | 8848 | 8854 | 8859 |
| 77 | 8865 | 8871 | 8876 | 8882 | 8887 | 8893 | 8899 | 8904 | 8910 | 8915 |
| 78 | 8921 | 8927 | 8932 | 8938 | 8943 | 8949 | 8954 | 8960 | 8965 | 8971 |
| 79 | 8976 | 8982 | 8987 | 8993 | 8998 | 9004 | 9009 | 9015 | 9020 | 9025 |
| 80 | 9031 | 9036 | 9042 | 9047 | 9053 | 9058 | 9063 | 9069 | 9074 | 9079 |
| 81 | 9085 | 9090 | 9096 | 9101 | 9106 | 9112 | 9117 | 9122 | 9128 | 9133 |
| 82 | 9138 | 9143 | 9149 | 9154 | 9159 | 9165 | 9170 | 9175 | 9180 | 9186 |
| 83 | 9191 | 9196 | 9201 | 9206 | 9212 | 9217 | 9222 | 9227 | 9232 | 9238 |
| 84 | 9243 | 9248 | 9253 | 9258 | 9263 | 9269 | 9274 | 9279 | 9284 | 9289 |
| 85 | 9294 | 9299 | 9304 | 9309 | 9315 | 9320 | 9325 | 9330 | 9335 | 9340 |
| 86 | 9345 | 9350 | 9355 | 9360 | 9365 | 9370 | 9375 | 9380 | 9385 | 9390 |
| 87 | 9395 | 9400 | 9405 | 9410 | 9415 | 9420 | 9425 | 9430 | 9435 | 9440 |
| 88 | 9445 | 9450 | 9455 | 9460 | 9465 | 9469 | 9474 | 9479 | 9484 | 9489 |
| 89 | 9494 | 9499 | 9504 | 9509 | 9513 | 9518 | 9523 | 9528 | 9533 | 9538 |
| 90 | 9542 | 9547 | 9552 | 9557 | 9562 | 9566 | 9571 | 9576 | 9581 | 9586 |
| 91 | 9590 | 9595 | 9600 | 9605 | 9609 | 9614 | 9619 | 9624 | 9628 | 9633 |
| 92 | 9638 | 9643 | 9647 | 9652 | 9657 | 9661 | 9666 | 9671 | 9675 | 9680 |
| 93 | 9685 | 9689 | 9694 | 9699 | 9703 | 9708 | 9713 | 9717 | 9722 | 9727 |
| 94 | 9731 | 9736 | 9741 | 9745 | 9750 | 9754 | 9759 | 9763 | 9768 | 9773 |
| 95 | 9777 | 9782 | 9786 | 9791 | 9795 | 9800 | 9805 | 9809 | 9814 | 9818 |
| 96 | 9823 | 9827 | 9832 | 9836 | 9841 | 9845 | 9850 | 9854 | 9859 | 9863 |
| 97 | 9868 | 9872 | 9877 | 9881 | 9886 | 9890 | 9894 | 9899 | 9903 | 9908 |
| 98 | 9912 | 9917 | 9921 | 9926 | 9930 | 9934 | 9939 | 9943 | 9948 | 9952 |
| 99 | 9956 | 9961 | 9965 | 9969 | 9974 | 9978 | 9983 | 9987 | 9991 | 9996 |

N 0 1 2 3 4 5 6 7 8 9

(B) Values of Trigonometric Functions

(B) Values of Trigonometric Functions

| Angle | Sin | Cos | Tan | Cot | |
|--------|-------|--------|-------|--------|---------|
| 0° 00' | .0000 | 1.0000 | .0000 | — | 90° 00' |
| 10 | .0029 | 1.0000 | .0029 | 343.77 | 50 |
| 20 | .0058 | 1.0000 | .0058 | 171.89 | 40 |
| 30 | .0087 | 1.0000 | .0087 | 114.59 | 30 |
| 40 | .0116 | .9999 | .0116 | 85.940 | 20 |
| 50 | .0145 | .9999 | .0145 | 68.750 | 10 |
| 1° 00' | .0175 | .9998 | .0175 | 57.290 | 89° 00' |
| 10 | .0204 | .9998 | .0204 | 49.104 | 50 |
| 20 | .0233 | .9997 | .0233 | 42.964 | 40 |
| 30 | .0262 | .9997 | .0262 | 38.188 | 30 |
| 40 | .0291 | .9996 | .0291 | 34.368 | 20 |
| 50 | .0320 | .9995 | .0320 | 31.242 | 10 |
| 2° 00' | .0349 | .9994 | .0349 | 28.636 | 88° 00' |
| 10 | .0378 | .9993 | .0378 | 26.432 | 50 |
| 20 | .0407 | .9992 | .0407 | 24.542 | 40 |
| 30 | .0436 | .9990 | .0437 | 22.904 | 30 |
| 40 | .0465 | .9989 | .0466 | 21.470 | 20 |
| 50 | .0494 | .9988 | .0495 | 20.206 | 10 |
| 3° 00' | .0523 | .9986 | .0524 | 19.081 | 87° 00' |
| 10 | .0552 | .9985 | .0553 | 18.075 | 50 |
| 20 | .0581 | .9983 | .0582 | 17.169 | 40 |
| 30 | .0610 | .9981 | .0612 | 16.350 | 30 |
| 40 | .0640 | .9980 | .0641 | 15.605 | 20 |
| 50 | .0669 | .9978 | .0670 | 14.924 | 10 |
| 4° 00' | .0698 | .9976 | .0699 | 14.301 | 86° 00' |
| 10 | .0727 | .9974 | .0729 | 13.727 | 50 |
| 20 | .0756 | .9971 | .0758 | 13.197 | 40 |
| 30 | .0785 | .9969 | .0787 | 12.706 | 30 |
| 40 | .0814 | .9967 | .0816 | 12.251 | 20 |
| 50 | .0843 | .9964 | .0846 | 11.826 | 10 |
| 5° 00' | .0872 | .9962 | .0875 | 11.430 | 85° 00' |
| 10 | .0901 | .9959 | .0904 | 11.059 | 50 |
| 20 | .0929 | .9957 | .0934 | 10.712 | 40 |
| 30 | .0958 | .9954 | .0963 | 10.385 | 30 |
| 40 | .0987 | .9951 | .0992 | 10.078 | 20 |
| 50 | .1016 | .9948 | .1022 | 9.7882 | 10 |
| 6° 00' | .1045 | .9945 | .1051 | 9.5144 | 84° 00' |
| 10 | .1074 | .9942 | .1080 | 9.2553 | 50 |
| 20 | .1103 | .9939 | .1110 | 9.0098 | 40 |
| 30 | .1132 | .9936 | .1139 | 8.7769 | 30 |
| 40 | .1161 | .9932 | .1169 | 8.5555 | 20 |
| 50 | .1190 | .9929 | .1198 | 8.3450 | 10 |
| 7° 00' | .1219 | .9925 | .1228 | 8.1443 | 83° 00' |
| 10 | .1248 | .9922 | .1257 | 7.9530 | 50 |
| 20 | .1276 | .9918 | .1287 | 7.7704 | 40 |
| 30 | .1305 | .9914 | .1317 | 7.5958 | 30 |
| 40 | .1334 | .9911 | .1346 | 7.4287 | 20 |
| 50 | .1363 | .9907 | .1376 | 7.2687 | 10 |
| 8° 00' | .1392 | .9903 | .1405 | 7.1154 | 82° 00' |
| 10 | .1421 | .9899 | .1435 | 6.9682 | 50 |
| 20 | .1449 | .9894 | .1465 | 6.8269 | 40 |
| 30 | .1478 | .9890 | .1495 | 6.6912 | 30 |
| 40 | .1507 | .9886 | .1524 | 6.5606 | 20 |
| 50 | .1536 | .9881 | .1554 | 6.4348 | 10 |
| 9° 00' | .1564 | .9877 | .1584 | 6.3138 | 81° 00' |
| | Cos | Sin | Cot | Tan | Angle |

(B) Values of Trigonometric Functions

| Angle | Sin | Cos | Tan | Cot | |
|---------|-------|-------|-------|--------|---------|
| 9° 00' | .1564 | .9877 | .1584 | 6.3138 | 81° 00' |
| 10 | .1593 | .9872 | .1614 | 6.1970 | 50 |
| 20 | .1622 | .9868 | .1644 | 6.0844 | 40 |
| 30 | .1650 | .9863 | .1673 | 5.9758 | 30 |
| 40 | .1679 | .9858 | .1703 | 5.8708 | 20 |
| 50 | .1708 | .9853 | .1733 | 5.7694 | 10 |
| 10° 00' | .1736 | .9848 | .1763 | 5.6713 | 80° 00' |
| 10 | .1765 | .9843 | .1793 | 5.5764 | 50 |
| 20 | .1794 | .9838 | .1823 | 5.4845 | 40 |
| 30 | .1822 | .9833 | .1853 | 5.3955 | 30 |
| 40 | .1851 | .9827 | .1883 | 5.3093 | 20 |
| 50 | .1880 | .9822 | .1914 | 5.2257 | 10 |
| 11° 00' | .1908 | .9816 | .1944 | 5.1446 | 79° 00' |
| 10 | .1937 | .9811 | .1974 | 5.0658 | 50 |
| 20 | .1965 | .9805 | .2004 | 4.9894 | 40 |
| 30 | .1994 | .9799 | .2035 | 4.9152 | 30 |
| 40 | .2022 | .9793 | .2065 | 4.8430 | 20 |
| 50 | .2051 | .9787 | .2095 | 4.7729 | 10 |
| 12° 00' | .2079 | .9781 | .2126 | 4.7046 | 78° 00' |
| 10 | .2108 | .9775 | .2156 | 4.6382 | 50 |
| 20 | .2136 | .9769 | .2186 | 4.5736 | 40 |
| 30 | .2164 | .9763 | .2217 | 4.5107 | 30 |
| 40 | .2193 | .9757 | .2247 | 4.4494 | 20 |
| 50 | .2221 | .9750 | .2278 | 4.3897 | 10 |
| 13° 00' | .2250 | .9744 | .2309 | 4.3315 | 77° 00' |
| 10 | .2278 | .9737 | .2339 | 4.2747 | 50 |
| 20 | .2306 | .9730 | .2370 | 4.2193 | 40 |
| 30 | .2334 | .9724 | .2401 | 4.1653 | 30 |
| 40 | .2363 | .9717 | .2432 | 4.1126 | 20 |
| 50 | .2391 | .9710 | .2462 | 4.0611 | 10 |
| 14° 00' | .2419 | .9703 | .2493 | 4.0108 | 76° 00' |
| 10 | .2447 | .9696 | .2524 | 3.9617 | 50 |
| 20 | .2476 | .9689 | .2555 | 3.9136 | 40 |
| 30 | .2504 | .9681 | .2586 | 3.8667 | 30 |
| 40 | .2532 | .9674 | .2617 | 3.8208 | 20 |
| 50 | .2560 | .9667 | .2648 | 3.7760 | 10 |
| 15° 00' | .2588 | .9659 | .2679 | 3.7321 | 75° 00' |
| 10 | .2616 | .9652 | .2711 | 3.6891 | 50 |
| 20 | .2644 | .9644 | .2742 | 3.6470 | 40 |
| 30 | .2672 | .9636 | .2773 | 3.6059 | 30 |
| 40 | .2700 | .9628 | .2805 | 3.5656 | 20 |
| 50 | .2728 | .9621 | .2836 | 3.5261 | 10 |
| 16° 00' | .2756 | .9613 | .2867 | 3.4874 | 74° 00' |
| 10 | .2784 | .9605 | .2899 | 3.4495 | 50 |
| 20 | .2812 | .9596 | .2931 | 3.4124 | 40 |
| 30 | .2840 | .9588 | .2962 | 3.3759 | 30 |
| 40 | .2868 | .9580 | .2994 | 3.3402 | 20 |
| 50 | .2896 | .9572 | .3026 | 3.3052 | 10 |
| 17° 00' | .2924 | .9563 | .3057 | 3.2709 | 73° 00' |
| 10 | .2952 | .9555 | .3089 | 3.2371 | 50 |
| 20 | .2979 | .9546 | .3121 | 3.2041 | 40 |
| 30 | .3007 | .9537 | .3153 | 3.1716 | 30 |
| 40 | .3035 | .9528 | .3185 | 3.1397 | 20 |
| 50 | .3062 | .9520 | .3217 | 3.1084 | 10 |
| 18° 00' | .3090 | .9511 | .3249 | 3.0777 | 72° 00' |
| | Cos | Sin | Cot | Tan | Angle |

(B) Values of Trigonometric Functions

(B) Values of Trigonometric Functions

| Angle | Sin | Cos | Tan | Cot | |
|---------|-------|-------|-------|--------|---------|
| 18° 00' | .3090 | .9511 | .3239 | 3.0777 | 72° 00' |
| 10 | .3118 | .9502 | .3281 | 3.0475 | 50 |
| 20 | .3145 | .9492 | .3314 | 3.0178 | 40 |
| 30 | .3173 | .9483 | .3346 | 2.9887 | 30 |
| 40 | .3201 | .9474 | .3378 | 2.9600 | 20 |
| 50 | .3228 | .9465 | .3411 | 2.9319 | 10 |
| 19° 00' | .3256 | .9455 | .3443 | 2.9042 | 71° 00' |
| 10 | .3283 | .9446 | .3476 | 2.8770 | 50 |
| 20 | .3311 | .9436 | .3508 | 2.8502 | 40 |
| 30 | .3338 | .9426 | .3541 | 2.8239 | 30 |
| 40 | .3365 | .9417 | .3574 | 2.7980 | 20 |
| 50 | .3393 | .9407 | .3607 | 2.7725 | 10 |
| 20° 00' | .3420 | .9397 | .3640 | 2.7475 | 70° 00' |
| 10 | .3448 | .9387 | .3673 | 2.7228 | 50 |
| 20 | .3475 | .9377 | .3706 | 2.6985 | 40 |
| 30 | .3502 | .9367 | .3739 | 2.6746 | 30 |
| 40 | .3529 | .9356 | .3772 | 2.6511 | 20 |
| 50 | .3557 | .9346 | .3805 | 2.6279 | 10 |
| 21° 00' | .3584 | .9336 | .3839 | 2.6051 | 69° 00' |
| 10 | .3611 | .9325 | .3872 | 2.5826 | 50 |
| 20 | .3638 | .9315 | .3906 | 2.5605 | 40 |
| 30 | .3665 | .9304 | .3939 | 2.5386 | 30 |
| 40 | .3692 | .9293 | .3973 | 2.5172 | 20 |
| 50 | .3719 | .9283 | .4006 | 2.4960 | 10 |
| 22° 00' | .3746 | .9272 | .4040 | 2.4751 | 68° 00' |
| 10 | .3773 | .9261 | .4074 | 2.4545 | 50 |
| 20 | .3800 | .9250 | .4108 | 2.4342 | 40 |
| 30 | .3827 | .9239 | .4142 | 2.4142 | 30 |
| 40 | .3854 | .9228 | .4176 | 2.3945 | 20 |
| 50 | .3881 | .9216 | .4210 | 2.3750 | 10 |
| 23° 00' | .3907 | .9205 | .4245 | 2.3559 | 67° 00' |
| 10 | .3934 | .9194 | .4279 | 2.3369 | 50 |
| 20 | .3961 | .9182 | .4314 | 2.3183 | 40 |
| 30 | .3987 | .9171 | .4348 | 2.2998 | 30 |
| 40 | .4014 | .9159 | .4383 | 2.2817 | 20 |
| 50 | .4041 | .9147 | .4417 | 2.2637 | 10 |
| 24° 00' | .4067 | .9135 | .4452 | 2.2460 | 66° 00' |
| 10 | .4094 | .9124 | .4487 | 2.2286 | 50 |
| 20 | .4120 | .9112 | .4522 | 2.2113 | 40 |
| 30 | .4147 | .9100 | .4557 | 2.1943 | 30 |
| 40 | .4173 | .9088 | .4592 | 2.1775 | 20 |
| 50 | .4200 | .9075 | .4628 | 2.1609 | 10 |
| 25° 00' | .4226 | .9063 | .4663 | 2.1445 | 65° 00' |
| 10 | .4253 | .9051 | .4699 | 2.1283 | 50 |
| 20 | .4279 | .9038 | .4734 | 2.1123 | 40 |
| 30 | .4305 | .9026 | .4770 | 2.0965 | 30 |
| 40 | .4331 | .9013 | .4806 | 2.0809 | 20 |
| 50 | .4358 | .9001 | .4841 | 2.0655 | 10 |
| 26° 00' | .4384 | .8988 | .4877 | 2.0503 | 64° 00' |
| 10 | .4410 | .8975 | .4913 | 2.0353 | 50 |
| 20 | .4436 | .8962 | .4950 | 2.0204 | 40 |
| 30 | .4462 | .8949 | .4986 | 2.0057 | 30 |
| 40 | .4488 | .8936 | .5022 | 1.9912 | 20 |
| 50 | .4514 | .8923 | .5059 | 1.9768 | 10 |
| 27° 00' | .4540 | .8910 | .5095 | 1.9626 | 63° 00' |
| | Cos | Sin | Cot | Tan | Angle |

(B) Values of Trigonometric Functions

| Angle | Sin | Cos | Tan | Cot | |
|---------|-------|-------|-------|--------|---------|
| 27° 00' | .4540 | .8910 | .5095 | 1.9626 | 63° 00' |
| 10 | .4566 | .8897 | .5132 | 1.9486 | 50 |
| 20 | .4592 | .8884 | .5169 | 1.9347 | 40 |
| 30 | .4617 | .8870 | .5206 | 1.9210 | 30 |
| 40 | .4643 | .8857 | .5243 | 1.9074 | 20 |
| 50 | .4669 | .8843 | .5280 | 1.8940 | 10 |
| 28° 00' | .4695 | .8829 | .5317 | 1.8807 | 62° 00' |
| 10 | .4720 | .8816 | .5354 | 1.8676 | 50 |
| 20 | .4746 | .8802 | .5392 | 1.8546 | 40 |
| 30 | .4772 | .8788 | .5430 | 1.8418 | 30 |
| 40 | .4797 | .8774 | .5467 | 1.8291 | 20 |
| 50 | .4823 | .8760 | .5505 | 1.8165 | 10 |
| 29° 00' | .4848 | .8746 | .5543 | 1.8040 | 61° 00' |
| 10 | .4874 | .8732 | .5581 | 1.7917 | 50 |
| 20 | .4899 | .8718 | .5619 | 1.7796 | 40 |
| 30 | .4924 | .8704 | .5658 | 1.7675 | 30 |
| 40 | .4950 | .8689 | .5696 | 1.7556 | 20 |
| 50 | .4975 | .8675 | .5735 | 1.7437 | 10 |
| 30° 00' | .5000 | .8660 | .5774 | 1.7321 | 60° 00' |
| 10 | .5025 | .8646 | .5812 | 1.7205 | 50 |
| 20 | .5050 | .8631 | .5851 | 1.7090 | 40 |
| 30 | .5075 | .8616 | .5890 | 1.6977 | 30 |
| 40 | .5100 | .8601 | .5930 | 1.6864 | 20 |
| 50 | .5125 | .8587 | .5969 | 1.6753 | 10 |
| 31° 00' | .5150 | .8572 | .6009 | 1.6643 | 59° 00' |
| 10 | .5175 | .8557 | .6048 | 1.6534 | 50 |
| 20 | .5200 | .8542 | .6088 | 1.6426 | 40 |
| 30 | .5225 | .8526 | .6128 | 1.6319 | 30 |
| 40 | .5250 | .8511 | .6168 | 1.6212 | 20 |
| 50 | .5275 | .8496 | .6208 | 1.6107 | 10 |
| 32° 00' | .5299 | .8480 | .6249 | 1.6003 | 58° 00' |
| 10 | .5324 | .8465 | .6289 | 1.5900 | 50 |
| 20 | .5348 | .8450 | .6330 | 1.5798 | 40 |
| 30 | .5373 | .8434 | .6371 | 1.5697 | 30 |
| 40 | .5398 | .8418 | .6412 | 1.5597 | 20 |
| 50 | .5422 | .8403 | .6453 | 1.5497 | 10 |
| 33° 00' | .5446 | .8387 | .6494 | 1.5399 | 57° 00' |
| 10 | .5471 | .8371 | .6536 | 1.5301 | 50 |
| 20 | .5495 | .8355 | .6577 | 1.5204 | 40 |
| 30 | .5519 | .8339 | .6619 | 1.5108 | 30 |
| 40 | .5544 | .8323 | .6661 | 1.5013 | 20 |
| 50 | .5568 | .8307 | .6703 | 1.4919 | 10 |
| 34° 00' | .5592 | .8290 | .6745 | 1.4826 | 56° 00' |
| 10 | .5616 | .8274 | .6787 | 1.4733 | 50 |
| 20 | .5640 | .8258 | .6830 | 1.4641 | 40 |
| 30 | .5664 | .8241 | .6873 | 1.4550 | 30 |
| 40 | .5688 | .8225 | .6916 | 1.4460 | 20 |
| 50 | .5712 | .8208 | .6959 | 1.4370 | 10 |
| 35° 00' | .5736 | .8192 | .7002 | 1.4281 | 55° 00' |
| 10 | .5760 | .8175 | .7046 | 1.4193 | 50 |
| 20 | .5783 | .8158 | .7089 | 1.4106 | 40 |
| 30 | .5807 | .8141 | .7133 | 1.4019 | 30 |
| 40 | .5831 | .8124 | .7177 | 1.3934 | 20 |
| 50 | .5854 | .8107 | .7221 | 1.3848 | 10 |
| 36° 00' | .5878 | .8090 | .7265 | 1.3764 | 54° 00' |
| | Cos | Sin | Cot | Tan | Angle |

(B) Values of Trigonometric Functions

(C) Logarithms of Trigonometric Functions

(B) Values of Trigonometric Functions

| Angle | Sin | Cos | Tan | Cot | |
|---------|-------|-------|--------|--------|---------|
| 36° 00' | .5878 | .8090 | .7265 | 1.3764 | 54° 00' |
| 10 | .5901 | .8073 | .7310 | 1.3680 | 50 |
| 20 | .5925 | .8056 | .7355 | 1.3597 | 40 |
| 30 | .5948 | .8039 | .7400 | 1.3514 | 30 |
| 40 | .5972 | .8021 | .7445 | 1.3432 | 20 |
| 50 | .5995 | .8004 | .7490 | 1.3351 | 10 |
| 37° 00' | .6018 | .7986 | .7536 | 1.3270 | 53° 00' |
| 10 | .6041 | .7969 | .7581 | 1.3190 | 50 |
| 20 | .6065 | .7951 | .7627 | 1.3111 | 40 |
| 30 | .6088 | .7934 | .7673 | 1.3032 | 30 |
| 40 | .6111 | .7916 | .7720 | 1.2954 | 20 |
| 50 | .6134 | .7898 | .7766 | 1.2876 | 10 |
| 38° 00' | .6157 | .7880 | .7813 | 1.2799 | 52° 00' |
| 10 | .6180 | .7862 | .7860 | 1.2723 | 50 |
| 20 | .6202 | .7844 | .7907 | 1.2647 | 40 |
| 30 | .6225 | .7826 | .7954 | 1.2572 | 30 |
| 40 | .6248 | .7808 | .8002 | 1.2497 | 20 |
| 50 | .6271 | .7790 | .8050 | 1.2423 | 10 |
| 39° 00' | .6293 | .7771 | .8098 | 1.2349 | 51° 00' |
| 10 | .6316 | .7753 | .8146 | 1.2276 | 50 |
| 20 | .6338 | .7735 | .8195 | 1.2203 | 40 |
| 30 | .6361 | .7716 | .8243 | 1.2131 | 30 |
| 40 | .6383 | .7698 | .8292 | 1.2059 | 20 |
| 50 | .6406 | .7679 | .8342 | 1.1988 | 10 |
| 40° 00' | .6428 | .7660 | .8391 | 1.1918 | 50° 00' |
| 10 | .6450 | .7642 | .8441 | 1.1847 | 50 |
| 20 | .6472 | .7623 | .8491 | 1.1778 | 40 |
| 30 | .6494 | .7604 | .8541 | 1.1708 | 30 |
| 40 | .6517 | .7585 | .8591 | 1.1640 | 20 |
| 50 | .6539 | .7566 | .8642 | 1.1571 | 10 |
| 41° 00' | .6561 | .7547 | .8693 | 1.1504 | 49° 00' |
| 10 | .6583 | .7528 | .8744 | 1.1436 | 50 |
| 20 | .6604 | .7509 | .8796 | 1.1369 | 40 |
| 30 | .6626 | .7490 | .8847 | 1.1303 | 30 |
| 40 | .6648 | .7470 | .8899 | 1.1237 | 20 |
| 50 | .6670 | .7451 | .8952 | 1.1171 | 10 |
| 42° 00' | .6691 | .7431 | .9004 | 1.1106 | 48° 00' |
| 10 | .6713 | .7412 | .9057 | 1.1041 | 50 |
| 20 | .6734 | .7392 | .9110 | 1.0977 | 40 |
| 30 | .6756 | .7373 | .9163 | 1.0913 | 30 |
| 40 | .6777 | .7353 | .9217 | 1.0850 | 20 |
| 50 | .6799 | .7333 | .9271 | 1.0786 | 10 |
| 43° 00' | .6820 | .7314 | .9325 | 1.0724 | 47° 00' |
| 10 | .6841 | .7294 | .9380 | 1.0661 | 50 |
| 20 | .6862 | .7274 | .9435 | 1.0599 | 40 |
| 30 | .6884 | .7254 | .9490 | 1.0538 | 30 |
| 40 | .6905 | .7234 | .9545 | 1.0477 | 20 |
| 50 | .6926 | .7214 | .9601 | 1.0416 | 10 |
| 44° 00' | .6947 | .7193 | .9657 | 1.0355 | 46° 00' |
| 10 | .6967 | .7173 | .9713 | 1.0295 | 50 |
| 20 | .6988 | .7153 | .9770 | 1.0235 | 40 |
| 30 | .7009 | .7133 | .9827 | 1.0176 | 30 |
| 40 | .7030 | .7112 | .9884 | 1.0117 | 20 |
| 50 | .7050 | .7092 | .9942 | 1.0058 | 10 |
| 45° 00' | .7071 | .7071 | 1.0000 | 1.0000 | 45° 00' |
| | Cos | Sin | Cot | Tan | Angle |

(C) Logarithms of Trigonometric Functions*

| Angle | L Sin | L Cos | L Tan | L Cot | |
|--------|--------|---------|--------|---------|---------|
| 0° 00' | — | 10.0000 | — | — | 90° 00' |
| 10 | 7.4637 | 10.0000 | 7.4637 | 12.5363 | 50 |
| 20 | 7.7648 | 10.0000 | 7.7648 | 12.2352 | 40 |
| 30 | 7.9408 | 10.0000 | 7.9409 | 12.0591 | 30 |
| 40 | 8.0658 | 10.0000 | 8.0658 | 11.9342 | 20 |
| 50 | 8.1627 | 10.0000 | 8.1627 | 11.8373 | 10 |
| 1° 00' | 8.2419 | 9.9999 | 8.2419 | 11.7581 | 89° 00' |
| 10 | 8.3088 | 9.9999 | 8.3089 | 11.6911 | 50 |
| 20 | 8.3668 | 9.9999 | 8.3669 | 11.6331 | 40 |
| 30 | 8.4179 | 9.9999 | 8.4181 | 11.5819 | 30 |
| 40 | 8.4637 | 9.9998 | 8.4638 | 11.5362 | 20 |
| 50 | 8.5050 | 9.9998 | 8.5053 | 11.4947 | 10 |
| 2° 00' | 8.5428 | 9.9997 | 8.5431 | 11.4569 | 88° 00' |
| 10 | 8.5776 | 9.9997 | 8.5779 | 11.4221 | 50 |
| 20 | 8.6097 | 9.9996 | 8.6101 | 11.3899 | 40 |
| 30 | 8.6397 | 9.9996 | 8.6401 | 11.3599 | 30 |
| 40 | 8.6677 | 9.9995 | 8.6682 | 11.3318 | 20 |
| 50 | 8.6940 | 9.9995 | 8.6945 | 11.3055 | 10 |
| 3° 00' | 8.7188 | 9.9994 | 8.7194 | 11.2806 | 87° 00' |
| 10 | 8.7423 | 9.9993 | 8.7429 | 11.2571 | 50 |
| 20 | 8.7645 | 9.9993 | 8.7652 | 11.2348 | 40 |
| 30 | 8.7857 | 9.9992 | 8.7865 | 11.2135 | 30 |
| 40 | 8.8059 | 9.9991 | 8.8067 | 11.1933 | 20 |
| 50 | 8.8251 | 9.9990 | 8.8261 | 11.1739 | 10 |
| 4° 00' | 8.8436 | 9.9989 | 8.8446 | 11.1554 | 86° 00' |
| 10 | 8.8613 | 9.9989 | 8.8624 | 11.1376 | 50 |
| 20 | 8.8783 | 9.9988 | 8.8795 | 11.1205 | 40 |
| 30 | 8.8946 | 9.9987 | 8.8960 | 11.1040 | 30 |
| 40 | 8.9104 | 9.9986 | 8.9118 | 11.0882 | 20 |
| 50 | 8.9256 | 9.9985 | 8.9272 | 11.0728 | 10 |
| 5° 00' | 8.9403 | 9.9983 | 8.9420 | 11.0580 | 85° 00' |
| 10 | 8.9545 | 9.9982 | 8.9563 | 11.0437 | 50 |
| 20 | 8.9682 | 9.9981 | 8.9701 | 11.0299 | 40 |
| 30 | 8.9816 | 9.9980 | 8.9836 | 11.0164 | 30 |
| 40 | 8.9945 | 9.9979 | 8.9966 | 11.0034 | 20 |
| 50 | 9.0070 | 9.9977 | 9.0093 | 10.9907 | 10 |
| 6° 00' | 9.0192 | 9.9976 | 9.0216 | 10.9784 | 84° 00' |
| 10 | 9.0311 | 9.9975 | 9.0336 | 10.9664 | 50 |
| 20 | 9.0426 | 9.9973 | 9.0453 | 10.9547 | 40 |
| 30 | 9.0539 | 9.9972 | 9.0567 | 10.9433 | 30 |
| 40 | 9.0648 | 9.9971 | 9.0678 | 10.9322 | 20 |
| 50 | 9.0755 | 9.9969 | 9.0786 | 10.9214 | 10 |
| 7° 00' | 9.0859 | 9.9968 | 9.0891 | 10.9109 | 83° 00' |
| 10 | 9.0961 | 9.9966 | 9.0995 | 10.9005 | 50 |
| 20 | 9.1060 | 9.9964 | 9.1096 | 10.8904 | 40 |
| 30 | 9.1157 | 9.9963 | 9.1194 | 10.8806 | 30 |
| 40 | 9.1252 | 9.9961 | 9.1291 | 10.8709 | 20 |
| 50 | 9.1345 | 9.9959 | 9.1385 | 10.8615 | 10 |
| 8° 00' | 9.1436 | 9.9958 | 9.1478 | 10.8522 | 82° 00' |
| 10 | 9.1525 | 9.9956 | 9.1569 | 10.8431 | 50 |
| 20 | 9.1612 | 9.9954 | 9.1658 | 10.8342 | 40 |
| 30 | 9.1697 | 9.9952 | 9.1745 | 10.8255 | 30 |
| 40 | 9.1781 | 9.9950 | 9.1831 | 10.8169 | 20 |
| 50 | 9.1863 | 9.9948 | 9.1915 | 10.8085 | 10 |
| 9° 00' | 9.1943 | 9.9946 | 9.1997 | 10.8003 | 81° 00' |
| | L Cot | L Sin | L Tan | L Angle | |

* These tables give the logarithms increased by 10. Hence in each case 10 should be subtracted.

(C) Logarithms of Trigonometric Functions*

(C) Logarithms of Trigonometric Functions*

| Angle | L Sin | L Cos | L Tan | L Cot | |
|----------------|--------------|--------------|--------------|--------------|----------------|
| 9° 00' | 9.1943 | 9.9946 | 9.1997 | 10.8003 | 81° 00' |
| 10 | 9.2022 | 9.9944 | 9.2078 | 10.7922 | 50 |
| 20 | 9.2100 | 9.9942 | 9.2158 | 10.7842 | 40 |
| 30 | 9.2176 | 9.9940 | 9.2236 | 10.7764 | 30 |
| 40 | 9.2251 | 9.9938 | 9.2313 | 10.7687 | 20 |
| 50 | 9.2324 | 9.9936 | 9.2389 | 10.7611 | 10 |
| 10° 00' | 9.2397 | 9.9934 | 9.2463 | 10.7537 | 80° 00' |
| 10 | 9.2468 | 9.9931 | 9.2536 | 10.7464 | 50 |
| 20 | 9.2538 | 9.9929 | 9.2609 | 10.7391 | 40 |
| 30 | 9.2606 | 9.9927 | 9.2680 | 10.7320 | 30 |
| 40 | 9.2674 | 9.9924 | 9.2750 | 10.7250 | 20 |
| 50 | 9.2740 | 9.9922 | 9.2819 | 10.7181 | 10 |
| 11° 00' | 9.2806 | 9.9919 | 9.2887 | 10.7113 | 79° 00' |
| 10 | 9.2870 | 9.9917 | 9.2953 | 10.7047 | 50 |
| 20 | 9.2934 | 9.9914 | 9.3020 | 10.6980 | 40 |
| 30 | 9.2997 | 9.9912 | 9.3085 | 10.6915 | 30 |
| 40 | 9.3058 | 9.9909 | 9.3149 | 10.6851 | 20 |
| 50 | 9.3119 | 9.9907 | 9.3212 | 10.6788 | 10 |
| 12° 00' | 9.3179 | 9.9904 | 9.3275 | 10.6725 | 78° 00' |
| 10 | 9.3238 | 9.9901 | 9.3336 | 10.6664 | 50 |
| 20 | 9.3296 | 9.9899 | 9.3397 | 10.6603 | 40 |
| 30 | 9.3353 | 9.9896 | 9.3458 | 10.6542 | 30 |
| 40 | 9.3410 | 9.9893 | 9.3517 | 10.6483 | 20 |
| 50 | 9.3466 | 9.9890 | 9.3576 | 10.6424 | 10 |
| 13° 00' | 9.3521 | 9.9887 | 9.3634 | 10.6366 | 77° 00' |
| 10 | 9.3575 | 9.9884 | 9.3691 | 10.6309 | 50 |
| 20 | 9.3629 | 9.9881 | 9.3748 | 10.6252 | 40 |
| 30 | 9.3682 | 9.9878 | 9.3804 | 10.6196 | 30 |
| 40 | 9.3734 | 9.9875 | 9.3859 | 10.6141 | 20 |
| 50 | 9.3786 | 9.9872 | 9.3914 | 10.6086 | 10 |
| 14° 00' | 9.3837 | 9.9869 | 9.3968 | 10.6032 | 76° 00' |
| 10 | 9.3887 | 9.9866 | 9.4021 | 10.5979 | 50 |
| 20 | 9.3937 | 9.9863 | 9.4074 | 10.5926 | 40 |
| 30 | 9.3986 | 9.9859 | 9.4127 | 10.5873 | 30 |
| 40 | 9.4035 | 9.9856 | 9.4178 | 10.5822 | 20 |
| 50 | 9.4083 | 9.9853 | 9.4230 | 10.5770 | 10 |
| 15° 00' | 9.4130 | 9.9849 | 9.4281 | 10.5719 | 75° 00' |
| 10 | 9.4177 | 9.9846 | 9.4331 | 10.5669 | 50 |
| 20 | 9.4223 | 9.9843 | 9.4381 | 10.5619 | 40 |
| 30 | 9.4269 | 9.9839 | 9.4430 | 10.5570 | 30 |
| 40 | 9.4314 | 9.9836 | 9.4479 | 10.5521 | 20 |
| 50 | 9.4359 | 9.9832 | 9.4527 | 10.5473 | 10 |
| 16° 00' | 9.4403 | 9.9828 | 9.4575 | 10.5425 | 74° 00' |
| 10 | 9.4447 | 9.9825 | 9.4622 | 10.5378 | 50 |
| 20 | 9.4491 | 9.9821 | 9.4669 | 10.5331 | 40 |
| 30 | 9.4533 | 9.9817 | 9.4716 | 10.5284 | 30 |
| 40 | 9.4576 | 9.9814 | 9.4762 | 10.5238 | 20 |
| 50 | 9.4618 | 9.9810 | 9.4808 | 10.5192 | 10 |
| 17° 00' | 9.4659 | 9.9806 | 9.4853 | 10.5147 | 73° 00' |
| 10 | 9.4700 | 9.9802 | 9.4898 | 10.5102 | 50 |
| 20 | 9.4741 | 9.9798 | 9.4943 | 10.5057 | 40 |
| 30 | 9.4781 | 9.9794 | 9.4987 | 10.5013 | 30 |
| 40 | 9.4821 | 9.9790 | 9.5031 | 10.4969 | 20 |
| 50 | 9.4861 | 9.9786 | 9.5075 | 10.4925 | 10 |
| 18° 00' | 9.4900 | 9.9782 | 9.5118 | 10.4882 | 72° 00' |
| | L Cos | L Sin | L Cot | L Tan | Angle |

(C) Logarithms of Trigonometric Functions*

| Angle | L Sin | L Cos | L Tan | L Cot | |
|----------------|--------------|--------------|--------------|--------------|----------------|
| 18° 00' | 9.4900 | 9.9782 | 9.5118 | 10.4882 | 72° 00' |
| 10 | 9.4939 | 9.9778 | 9.5161 | 10.4839 | 50 |
| 20 | 9.4977 | 9.9774 | 9.5203 | 10.4797 | 40 |
| 30 | 9.5015 | 9.9770 | 9.5245 | 10.4755 | 30 |
| 40 | 9.5052 | 9.9765 | 9.5287 | 10.4713 | 20 |
| 50 | 9.5090 | 9.9761 | 9.5329 | 10.4671 | 10 |
| 19° 00' | 9.5126 | 9.9757 | 9.5370 | 10.4630 | 71° 00' |
| 10 | 9.5163 | 9.9752 | 9.5411 | 10.4589 | 50 |
| 20 | 9.5199 | 9.9748 | 9.5451 | 10.4549 | 40 |
| 30 | 9.5235 | 9.9743 | 9.5491 | 10.4509 | 30 |
| 40 | 9.5270 | 9.9739 | 9.5531 | 10.4469 | 20 |
| 50 | 9.5306 | 9.9734 | 9.5571 | 10.4429 | 10 |
| 20° 00' | 9.5341 | 9.9730 | 9.5611 | 10.4389 | 70° 00' |
| 10 | 9.5375 | 9.9725 | 9.5650 | 10.4350 | 50 |
| 20 | 9.5409 | 9.9721 | 9.5689 | 10.4311 | 40 |
| 30 | 9.5443 | 9.9716 | 9.5727 | 10.4273 | 30 |
| 40 | 9.5477 | 9.9711 | 9.5766 | 10.4234 | 20 |
| 50 | 9.5510 | 9.9706 | 9.5804 | 10.4196 | 10 |
| 21° 00' | 9.5543 | 9.9702 | 9.5842 | 10.4158 | 69° 00' |
| 10 | 9.5576 | 9.9697 | 9.5879 | 10.4121 | 50 |
| 20 | 9.5609 | 9.9692 | 9.5917 | 10.4083 | 40 |
| 30 | 9.5641 | 9.9687 | 9.5954 | 10.4046 | 30 |
| 40 | 9.5673 | 9.9682 | 9.5991 | 10.4009 | 20 |
| 50 | 9.5704 | 9.9677 | 9.6028 | 10.3972 | 10 |
| 22° 00' | 9.5736 | 9.9672 | 9.6064 | 10.3936 | 68° 00' |
| 10 | 9.5767 | 9.9667 | 9.6100 | 10.3900 | 50 |
| 20 | 9.5798 | 9.9661 | 9.6136 | 10.3864 | 40 |
| 30 | 9.5828 | 9.9656 | 9.6172 | 10.3828 | 30 |
| 40 | 9.5859 | 9.9651 | 9.6208 | 10.3792 | 20 |
| 50 | 9.5889 | 9.9646 | 9.6243 | 10.3757 | 10 |
| 23° 00' | 9.5919 | 9.9640 | 9.6279 | 10.3721 | 67° 00' |
| 10 | 9.5948 | 9.9635 | 9.6314 | 10.3686 | 50 |
| 20 | 9.5978 | 9.9629 | 9.6348 | 10.3652 | 40 |
| 30 | 9.6007 | 9.9624 | 9.6383 | 10.3617 | 30 |
| 40 | 9.6036 | 9.9618 | 9.6417 | 10.3583 | 20 |
| 50 | 9.6065 | 9.9613 | 9.6452 | 10.3548 | 10 |
| 24° 00' | 9.6093 | 9.9607 | 9.6486 | 10.3514 | 66° 00' |
| 10 | 9.6121 | 9.9602 | 9.6520 | 10.3480 | 50 |
| 20 | 9.6149 | 9.9596 | 9.6553 | 10.3447 | 40 |
| 30 | 9.6177 | 9.9590 | 9.6587 | 10.3413 | 30 |
| 40 | 9.6205 | 9.9584 | 9.6620 | 10.3380 | 20 |
| 50 | 9.6232 | 9.9579 | 9.6654 | 10.3346 | 10 |
| 25° 00' | 9.6259 | 9.9573 | 9.6687 | 10.3313 | 65° 00' |
| 10 | 9.6286 | 9.9567 | 9.6720 | 10.3280 | 50 |
| 20 | 9.6313 | 9.9561 | 9.6752 | 10.3248 | 40 |
| 30 | 9.6340 | 9.9555 | 9.6785 | 10.3215 | 30 |
| 40 | 9.6366 | 9.9549 | 9.6817 | 10.3183 | 20 |
| 50 | 9.6392 | 9.9543 | 9.6850 | 10.3150 | 10 |
| 26° 00' | 9.6418 | 9.9537 | 9.6882 | 10.3118 | 64° 00' |
| 10 | 9.6444 | 9.9530 | 9.6914 | 10.3086 | 50 |
| 20 | 9.6470 | 9.9524 | 9.6946 | 10.3054 | 40 |
| 30 | 9.6495 | 9.9518 | 9.6977 | 10.3023 | 30 |
| 40 | 9.6521 | 9.9512 | 9.7009 | 10.2991 | 20 |
| 50 | 9.6546 | 9.9505 | 9.7040 | 10.2960 | 10 |
| 27° 00' | 9.6570 | 9.9499 | 9.7072 | 10.2928 | 63° 00' |
| | L Cos | L Sin | L Cot | L Tan | Angle |

* These tables give the logarithms increased by 10. Hence in each case 10 should be subtracted.

(C) Logarithms of Trigonometric Functions *

(C) Logarithms of Trigonometric Functions*

| Angle | L Sin | L Cos | L Tan | L Cot | |
|---------|--------|--------|--------|---------|---------|
| 27° 00' | 9.6570 | 9.9499 | 9.7072 | 10.2928 | 63° 00' |
| 10 | 9.6595 | 9.9492 | 9.7103 | 10.2897 | 50 |
| 20 | 9.6620 | 9.9486 | 9.7134 | 10.2866 | 40 |
| 30 | 9.6644 | 9.9479 | 9.7165 | 10.2835 | 30 |
| 40 | 9.6668 | 9.9473 | 9.7196 | 10.2804 | 20 |
| 50 | 9.6692 | 9.9466 | 9.7226 | 10.2774 | 10 |
| 28° 00' | 9.6716 | 9.9459 | 9.7257 | 10.2743 | 62° 00' |
| 10 | 9.6740 | 9.9453 | 9.7287 | 10.2713 | 50 |
| 20 | 9.6763 | 9.9446 | 9.7317 | 10.2683 | 40 |
| 30 | 9.6787 | 9.9439 | 9.7348 | 10.2652 | 30 |
| 40 | 9.6810 | 9.9432 | 9.7378 | 10.2622 | 20 |
| 50 | 9.6833 | 9.9425 | 9.7408 | 10.2592 | 10 |
| 29° 00' | 9.6856 | 9.9418 | 9.7438 | 10.2562 | 61° 00' |
| 10 | 9.6878 | 9.9411 | 9.7467 | 10.2533 | 50 |
| 20 | 9.6901 | 9.9404 | 9.7497 | 10.2503 | 40 |
| 30 | 9.6923 | 9.9397 | 9.7526 | 10.2474 | 30 |
| 40 | 9.6946 | 9.9390 | 9.7556 | 10.2444 | 20 |
| 50 | 9.6968 | 9.9383 | 9.7585 | 10.2415 | 10 |
| 30° 00' | 9.6990 | 9.9375 | 9.7614 | 10.2386 | 60° 00' |
| 10 | 9.7012 | 9.9368 | 9.7644 | 10.2356 | 50 |
| 20 | 9.7033 | 9.9361 | 9.7673 | 10.2327 | 40 |
| 30 | 9.7055 | 9.9353 | 9.7701 | 10.2299 | 30 |
| 40 | 9.7076 | 9.9346 | 9.7730 | 10.2270 | 20 |
| 50 | 9.7097 | 9.9338 | 9.7759 | 10.2241 | 10 |
| 31° 00' | 9.7118 | 9.9331 | 9.7788 | 10.2212 | 59° 00' |
| 10 | 9.7139 | 9.9323 | 9.7816 | 10.2184 | 50 |
| 20 | 9.7160 | 9.9315 | 9.7845 | 10.2155 | 40 |
| 30 | 9.7181 | 9.9308 | 9.7873 | 10.2127 | 30 |
| 40 | 9.7201 | 9.9300 | 9.7902 | 10.2098 | 20 |
| 50 | 9.7222 | 9.9292 | 9.7930 | 10.2070 | 10 |
| 32° 00' | 9.7242 | 9.9284 | 9.7958 | 10.2042 | 58° 00' |
| 10 | 9.7262 | 9.9276 | 9.7986 | 10.2014 | 50 |
| 20 | 9.7282 | 9.9268 | 9.8014 | 10.1986 | 40 |
| 30 | 9.7302 | 9.9260 | 9.8042 | 10.1958 | 30 |
| 40 | 9.7322 | 9.9252 | 9.8070 | 10.1930 | 20 |
| 50 | 9.7342 | 9.9244 | 9.8097 | 10.1903 | 10 |
| 33° 00' | 9.7361 | 9.9236 | 9.8125 | 10.1875 | 57° 00' |
| 10 | 9.7380 | 9.9228 | 9.8153 | 10.1847 | 50 |
| 20 | 9.7400 | 9.9219 | 9.8180 | 10.1820 | 40 |
| 30 | 9.7419 | 9.9211 | 9.8208 | 10.1792 | 30 |
| 40 | 9.7438 | 9.9203 | 9.8235 | 10.1765 | 20 |
| 50 | 9.7457 | 9.9194 | 9.8263 | 10.1737 | 10 |
| 34° 00' | 9.7476 | 9.9186 | 9.8290 | 10.1710 | 56° 00' |
| 10 | 9.7494 | 9.9177 | 9.8317 | 10.1683 | 50 |
| 20 | 9.7513 | 9.9169 | 9.8344 | 10.1656 | 40 |
| 30 | 9.7531 | 9.9160 | 9.8371 | 10.1629 | 30 |
| 40 | 9.7550 | 9.9151 | 9.8398 | 10.1602 | 20 |
| 50 | 9.7568 | 9.9142 | 9.8425 | 10.1575 | 10 |
| 35° 00' | 9.7586 | 9.9134 | 9.8452 | 10.1548 | 55° 00' |
| 10 | 9.7604 | 9.9125 | 9.8479 | 10.1521 | 50 |
| 20 | 9.7622 | 9.9116 | 9.8506 | 10.1494 | 40 |
| 30 | 9.7640 | 9.9107 | 9.8533 | 10.1467 | 30 |
| 40 | 9.7657 | 9.9098 | 9.8559 | 10.1441 | 20 |
| 50 | 9.7675 | 9.9089 | 9.8586 | 10.1414 | 10 |
| 36° 00' | 9.7692 | 9.9080 | 9.8613 | 10.1387 | 54° 00' |
| | L Cos | L Sin | L Cot | L Tan | Angle |

(C) Logarithms of Trigonometric Functions*

| Angle | L Sin | L Cos | L Tan | L Cot | |
|---------|--------|--------|---------|---------|---------|
| 36° 00' | 9.7692 | 9.9080 | 9.8613 | 10.1387 | 54° 00' |
| 10 | 9.7710 | 9.9070 | 9.8639 | 10.1361 | 50 |
| 20 | 9.7727 | 9.9061 | 9.8666 | 10.1334 | 40 |
| 30 | 9.7744 | 9.9052 | 9.8692 | 10.1308 | 30 |
| 40 | 9.7761 | 9.9042 | 9.8718 | 10.1282 | 20 |
| 50 | 9.7778 | 9.9033 | 9.8745 | 10.1255 | 10 |
| 37° 00' | 9.7795 | 9.9023 | 9.8771 | 10.1229 | 53° 00' |
| 10 | 9.7811 | 9.9014 | 9.8797 | 10.1203 | 50 |
| 20 | 9.7828 | 9.9004 | 9.8824 | 10.1176 | 40 |
| 30 | 9.7844 | 9.8995 | 9.8850 | 10.1150 | 30 |
| 40 | 9.7861 | 9.8985 | 9.8876 | 10.1124 | 20 |
| 50 | 9.7877 | 9.8975 | 9.8902 | 10.1098 | 10 |
| 38° 00' | 9.7893 | 9.8965 | 9.8928 | 10.1072 | 52° 00' |
| 10 | 9.7910 | 9.8955 | 9.8954 | 10.1046 | 50 |
| 20 | 9.7926 | 9.8945 | 9.8980 | 10.1020 | 40 |
| 30 | 9.7941 | 9.8935 | 9.9006 | 10.0994 | 30 |
| 40 | 9.7957 | 9.8925 | 9.9032 | 10.0968 | 20 |
| 50 | 9.7973 | 9.8915 | 9.9058 | 10.0942 | 10 |
| 39° 00' | 9.7989 | 9.8905 | 9.9084 | 10.0916 | 51° 00' |
| 10 | 9.8004 | 9.8895 | 9.9110 | 10.0890 | 50 |
| 20 | 9.8020 | 9.8884 | 9.9135 | 10.0865 | 40 |
| 30 | 9.8035 | 9.8874 | 9.9161 | 10.0839 | 30 |
| 40 | 9.8050 | 9.8864 | 9.9187 | 10.0813 | 20 |
| 50 | 9.8066 | 9.8853 | 9.9212 | 10.0788 | 10 |
| 40° 00' | 9.8081 | 9.8843 | 9.9238 | 10.0762 | 50° 00' |
| 10 | 9.8096 | 9.8832 | 9.9264 | 10.0736 | 50 |
| 20 | 9.8111 | 9.8821 | 9.9289 | 10.0711 | 40 |
| 30 | 9.8125 | 9.8810 | 9.9315 | 10.0685 | 30 |
| 40 | 9.8140 | 9.8800 | 9.9341 | 10.0659 | 20 |
| 50 | 9.8155 | 9.8789 | 9.9366 | 10.0634 | 10 |
| 41° 00' | 9.8169 | 9.8778 | 9.9392 | 10.0608 | 49° 00' |
| 10 | 9.8184 | 9.8767 | 9.9417 | 10.0583 | 50 |
| 20 | 9.8198 | 9.8756 | 9.9443 | 10.0557 | 40 |
| 30 | 9.8213 | 9.8745 | 9.9468 | 10.0532 | 30 |
| 40 | 9.8227 | 9.8733 | 9.9494 | 10.0506 | 20 |
| 50 | 9.8241 | 9.8722 | 9.9519 | 10.0481 | 10 |
| 42° 00' | 9.8255 | 9.8711 | 9.9544 | 10.0456 | 48° 00' |
| 10 | 9.8269 | 9.8699 | 9.9570 | 10.0430 | 50 |
| 20 | 9.8283 | 9.8688 | 9.9595 | 10.0405 | 40 |
| 30 | 9.8297 | 9.8676 | 9.9621 | 10.0379 | 30 |
| 40 | 9.8311 | 9.8665 | 9.9646 | 10.0354 | 20 |
| 50 | 9.8324 | 9.8653 | 9.9671 | 10.0329 | 10 |
| 43° 00' | 9.8338 | 9.8641 | 9.9697 | 10.0303 | 47° 00' |
| 10 | 9.8351 | 9.8629 | 9.9722 | 10.0278 | 50 |
| 20 | 9.8365 | 9.8618 | 9.9747 | 10.0253 | 40 |
| 30 | 9.8378 | 9.8606 | 9.9772 | 10.0228 | 30 |
| 40 | 9.8391 | 9.8594 | 9.9798 | 10.0202 | 20 |
| 50 | 9.8405 | 9.8582 | 9.9823 | 10.0177 | 10 |
| 44° 00' | 9.8418 | 9.8569 | 9.9848 | 10.0152 | 46° 00' |
| 10 | 9.8431 | 9.8557 | 9.9874 | 10.0126 | 50 |
| 20 | 9.8444 | 9.8545 | 9.9899 | 10.0101 | 40 |
| 30 | 9.8457 | 9.8532 | 9.9924 | 10.0076 | 30 |
| 40 | 9.8469 | 9.8520 | 9.9949 | 10.0051 | 20 |
| 50 | 9.8482 | 9.8507 | 9.9975 | 10.0025 | 10 |
| 45° 00' | 9.8495 | 9.8495 | 10.0000 | 10.0000 | 45° 00' |
| | L Cos | L Sin | L Cot | L Tan | Angle |

* These tables give the logarithms increased by 10. Hence in each case 10 should be subtracted.

FOR TEACHERS ONLY

SCORING KEY

11

ELEVENTH YEAR MATHEMATICS

Thursday, January 25, 1979 — 1:15 to 4:15 p.m., only

Use only *red* ink or *red* pencil in rating Regents papers. Do not attempt to *correct* the pupil's work by making insertions or changes of any kind. Use checkmarks to indicate pupil errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. In problems involving logarithms, answers should be left correct to four significant digits unless directions say otherwise. Units need not be given when the wording of the questions allows such omissions.

Part I

Allow 2 credits for each correct answer; allow no partial credit. For questions 12–30, allow credit if the pupil has written the correct answer instead of the numeral 1, 2, 3, or 4.

(1) 6

(11) -5

(21) 3

(2) $\frac{1}{2}$

(12) 2

(22) 2

(3) $(4y - 1)(3y - 2)$

(13) 1

(23) 2

(4) -1

(14) 4

(24) 4

(5) -2

(15) 2

(25) 1

(6) -7

(16) 3

(26) 4

(7) 4

(17) 2

(27) 4

(8) 0.8136

(18) 1

(28) 3

(9) $\frac{14\pi}{9}$

(19) 4

(29) 1

(10) $\frac{2}{3}$

(20) 3

(30) 4

[OVER]

ELEVENTH YEAR MATHEMATICS — *concluded*

Part II

Please refer to the Department's pamphlet *Suggestions on the Rating of Regents Examination Papers in Mathematics*. Care should be exercised in making deductions as to whether the error is purely a mechanical one or due to a violation of some principle. A mechanical error generally should receive a deduction of 10 percent, while an error due to a violation of some cardinal principle should receive a deduction ranging from 30 percent to 50 percent, depending on the relative importance of the principle in the solution of the problem.

(31) *a* $30^\circ, 150^\circ, 270^\circ$ [5]

b $2 \pm 3i$ [5]

(32) *b* $(-1, 6)$ [2]

c $-3 \leq y \leq 6$ [2]

(33) 12 [10]

(34) 3.6 [10]

(36) *a* 32 [10]

OR

b 100 [10]