

0118AII Common Core State Standards

1 The operator of the local mall wants to find out how many of the mall's employees make purchases in the food court when they are working. She hopes to use these data to increase the rent and attract new food vendors. In total, there are 1023 employees who work at the mall. The best method to obtain a random sample of the employees would be to survey

- 1) all 170 employees at each of the larger stores
- 2) 50% of the 90 employees of the food court
- 3) every employee
- 4) every 30th employee entering each mall entrance for one week

2 What is the solution set for x in the equation below?

$$\sqrt{x+1} - 1 = x$$

- 1) $\{1\}$
- 2) $\{0\}$
- 3) $\{-1, 0\}$
- 4) $\{0, 1\}$

3 For the system shown below, what is the value of z ?

$$y = -2x + 14$$

$$3x - 4z = 2$$

$$3x - y = 16$$

- 1) 5
- 2) 2
- 3) 6
- 4) 4

4 The hours of daylight, y , in Utica in days, x , from January 1, 2013 can be modeled by the equation $y = 3.06 \sin(0.017x - 1.40) + 12.23$. How many hours of daylight, to the *nearest tenth*, does this model predict for February 14, 2013?

- 1) 9.4
- 2) 10.4
- 3) 12.1
- 4) 12.2

5 A certain pain reliever is taken in 220 mg dosages and has a half-life of 12 hours. The function

$$A = 220 \left(\frac{1}{2} \right)^{\frac{t}{12}}$$

can be used to model this situation,

where A is the amount of pain reliever in milligrams remaining in the body after t hours.

According to this function, which statement is true?

- 1) Every hour, the amount of pain reliever remaining is cut in half.
- 2) In 12 hours, there is no pain reliever remaining in the body.
- 3) In 24 hours, there is no pain reliever remaining in the body.
- 4) In 12 hours, 110 mg of pain reliever is remaining.

6 The expression $(x+a)(x+b)$ can *not* be written as

- 1) $a(x+b) + x(x+b)$
- 2) $x^2 + abx + ab$
- 3) $x^2 + (a+b)x + ab$
- 4) $x(x+a) + b(x+a)$

- 7 There are 440 students at Thomas Paine High School enrolled in U.S. History. On the April report card, the students' grades are approximately normally distributed with a mean of 79 and a standard deviation of 7. Students who earn a grade less than or equal to 64.9 must attend summer school. The number of students who must attend summer school for U.S. History is closest to
- 3
 - 5
 - 10
 - 22
- 8 For a given time, x , in seconds, an electric current, y , can be represented by $y = 2.5(1 - 2.7^{-10x})$. Which equation is *not* equivalent?
- $y = 2.5 - 2.5(2.7^{-10x})$
 - $y = 2.5 - 2.5\left((2.7^2)^{-0.5x}\right)$
 - $y = 2.5 - 2.5\left(\frac{1}{2.7^{10x}}\right)$
 - $y = 2.5 - 2.5(2.7^{-2})(2.7^{0.5x})$
- 9 What is the quotient when $10x^3 - 3x^2 - 7x + 3$ is divided by $2x - 1$?
- $5x^2 + x + 3$
 - $5x^2 - x + 3$
 - $5x^2 - x - 3$
 - $5x^2 + x - 3$
- 10 Judith puts \$5000 into an investment account with interest compounded continuously. Which approximate annual rate is needed for the account to grow to \$9110 after 30 years?
- 2%
 - 2.2%
 - 0.02%
 - 0.022%
- 11 If $n = \sqrt{a^5}$ and $m = a$, where $a > 0$, an expression for $\frac{n}{m}$ could be
- $a^{\frac{5}{2}}$
 - a^4
 - $\sqrt[3]{a^2}$
 - $\sqrt{a^3}$
- 12 The solutions to $x + 3 - \frac{4}{x-1} = 5$ are
- $\frac{3}{2} \pm \frac{\sqrt{17}}{2}$
 - $\frac{3}{2} \pm \frac{\sqrt{17}}{2}i$
 - $\frac{3}{2} \pm \frac{\sqrt{33}}{2}$
 - $\frac{3}{2} \pm \frac{\sqrt{33}}{2}i$
- 13 If $ae^{bt} = c$, where a , b , and c are positive, then t equals
- $\ln\left(\frac{c}{ab}\right)$
 - $\ln\left(\frac{cb}{a}\right)$
 - $\frac{\ln\left(\frac{c}{a}\right)}{b}$
 - $\frac{\ln\left(\frac{c}{a}\right)}{\ln b}$

- 14 For which values of x , rounded to the *nearest hundredth*, will $|x^2 - 9| - 3 = \log_3 x$?
- 1) 2.29 and 3.63
 - 2) 2.37 and 3.54
 - 3) 2.84 and 3.17
 - 4) 2.92 and 3.06
- 15 The terminal side of θ , an angle in standard position, intersects the unit circle at $P\left(-\frac{1}{3}, -\frac{\sqrt{8}}{3}\right)$.
- What is the value of $\sec \theta$?
- 1) -3
 - 2) $-\frac{3\sqrt{8}}{8}$
 - 3) $-\frac{1}{3}$
 - 4) $-\frac{\sqrt{8}}{3}$

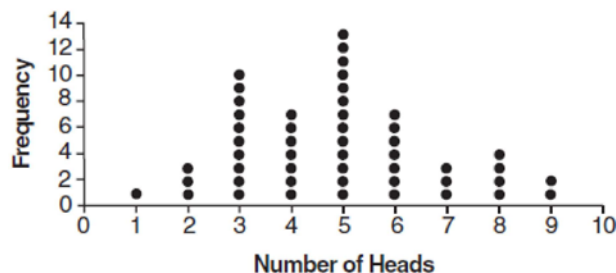
- 16 What is the equation of the directrix for the parabola $-8(y - 3) = (x + 4)^2$?
- 1) $y = 5$
 - 2) $y = 1$
 - 3) $y = -2$
 - 4) $y = -6$

- 17 The function below models the average price of gas in a small town since January 1st.
- $$G(t) = -0.0049t^4 + 0.0923t^3 - 0.56t^2 + 1.166t + 3.23,$$
- where $0 \leq t \leq 10$.
- If $G(t)$ is the average price of gas in dollars and t represents the number of months since January 1st, the absolute maximum $G(t)$ reaches over the given domain is about
- 1) \$1.60
 - 2) \$3.92
 - 3) \$4.01
 - 4) \$7.73

- 18 Written in simplest form, $\frac{c^2 - d^2}{d^2 + cd - 2c^2}$ where $c \neq d$, is equivalent to
- 1) $\frac{c + d}{d + 2c}$
 - 2) $\frac{c - d}{d + 2c}$
 - 3) $\frac{-c - d}{d + 2c}$
 - 4) $\frac{-c + d}{d + 2c}$

- 19 If $p(x) = 2x^3 - 3x + 5$, what is the remainder of $p(x) \div (x - 5)$?
- 1) -230
 - 2) 0
 - 3) 40
 - 4) 240

- 20 The results of simulating tossing a coin 10 times, recording the number of heads, and repeating this 50 times are shown in the graph below.



Based on the results of the simulation, which statement is *false*?

- 1) Five heads occurred most often, which is consistent with the theoretical probability of obtaining a heads.
- 2) Eight heads is unusual, as it falls outside the middle 95% of the data.
- 3) Obtaining three heads or fewer occurred 28% of the time.
- 4) Seven heads is not unusual, as it falls within the middle 95% of the data.

- 21 What is the inverse of $f(x) = -6(x - 2)$?
- 1) $f^{-1}(x) = -2 - \frac{x}{6}$
 - 2) $f^{-1}(x) = 2 - \frac{x}{6}$
 - 3) $f^{-1}(x) = \frac{1}{-6(x - 2)}$
 - 4) $f^{-1}(x) = 6(x + 2)$
- 22 Brian deposited 1 cent into an empty non-interest bearing bank account on the first day of the month. He then additionally deposited 3 cents on the second day, 9 cents on the third day, and 27 cents on the fourth day. What would be the total amount of money in the account at the end of the 20th day if the pattern continued?
- 1) \$11,622,614.67
 - 2) \$17,433,922.00
 - 3) \$116,226,146.80
 - 4) \$1,743,392,200.00
- 23 If the function $g(x) = ab^x$ represents exponential growth, which statement about $g(x)$ is *false*?
- 1) $a > 0$ and $b > 1$
 - 2) The y -intercept is $(0, a)$.
 - 3) The asymptote is $y = 0$.
 - 4) The x -intercept is $(b, 0)$.
- 24 At her job, Pat earns \$25,000 the first year and receives a raise of \$1000 each year. The explicit formula for the n th term of this sequence is $a_n = 25,000 + (n - 1)1000$. Which rule best represents the equivalent recursive formula?
- 1) $a_n = 24,000 + 1000n$
 - 2) $a_n = 25,000 + 1000n$
 - 3) $a_1 = 25,000, a_n = a_{n-1} + 1000$
 - 4) $a_1 = 25,000, a_n = a_{n+1} + 1000$
- 25 Elizabeth tried to find the product of $(2 + 4i)$ and $(3 - i)$, and her work is shown below.

$$\begin{aligned}
 &(2 + 4i)(3 - i) \\
 &= 6 - 2i + 12i - 4i^2 \\
 &= 6 + 10i - 4i^2 \\
 &= 6 + 10i - 4(1) \\
 &= 6 + 10i - 4 \\
 &= 2 + 10i
 \end{aligned}$$

Identify the error in the process shown and determine the correct product of $(2 + 4i)$ and $(3 - i)$.

- 26 A runner is using a nine-week training app to prepare for a "fun run." The table below represents the amount of the program completed, A , and the distance covered in a session, D , in miles.

A	$\frac{4}{9}$	$\frac{5}{9}$	$\frac{6}{9}$	$\frac{8}{9}$	1
D	2	2	2.25	3	3.25

Based on these data, write an exponential regression equation, rounded to the *nearest thousandth*, to model the distance the runner is able to complete in a session as she continues through the nine-week program.

- 27 A formula for work problems involving two people is shown below.

$$\frac{1}{t_1} + \frac{1}{t_2} = \frac{1}{t_b}$$

t_1 = the time taken by the first person to complete the job

t_2 = the time taken by the second person to complete the job

t_b = the time it takes for them working together to complete the job

Fred and Barney are carpenters who build the same model desk. It takes Fred eight hours to build the desk while it only takes Barney six hours. Write an equation that can be used to find the time it would take both carpenters working together to build a desk. Determine, to the *nearest tenth of an hour*, how long it would take Fred and Barney working together to build a desk.

- 28 Completely factor the following expression:

$$x^2 + 3xy + 3x^3 + y$$

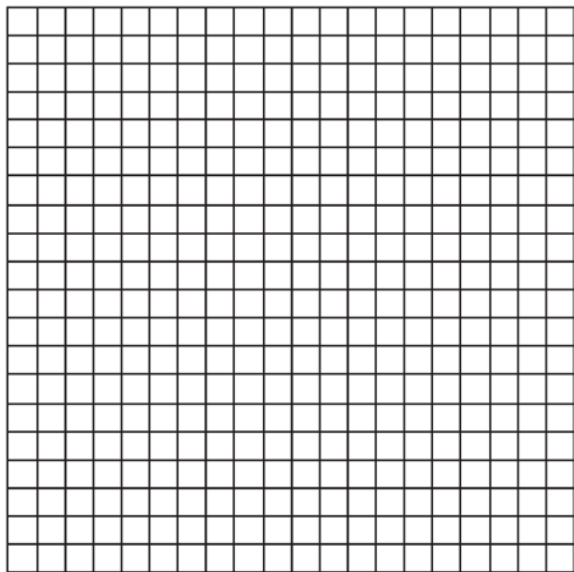
- 29 Researchers in a local area found that the population of rabbits with an initial population of 20 grew continuously at the rate of 5% per month. The fox population had an initial value of 30 and grew continuously at the rate of 3% per month. Find, to the *nearest tenth of a month*, how long it takes for these populations to be equal.

- 30 Consider the function $h(x) = 2 \sin(3x) + 1$ and the function q represented in the table below.

x	$q(x)$
-2	-8
-1	0
0	0
1	-2
2	0

Determine which function has the *smaller* minimum value for the domain $[-2, 2]$. Justify your answer.

- 31 The zeros of a quartic polynomial function h are $-1, \pm 2,$ and 3 . Sketch a graph of $y = h(x)$ on the grid below.

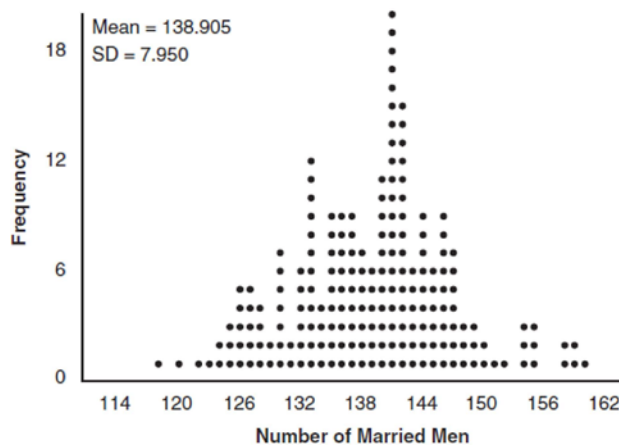


- 32 Explain why $81^{\frac{3}{4}}$ equals 27.

- 33 Given: $f(x) = 2x^2 + x - 3$ and $g(x) = x - 1$
Express $f(x) \cdot g(x) - [f(x) + g(x)]$ as a polynomial in standard form.

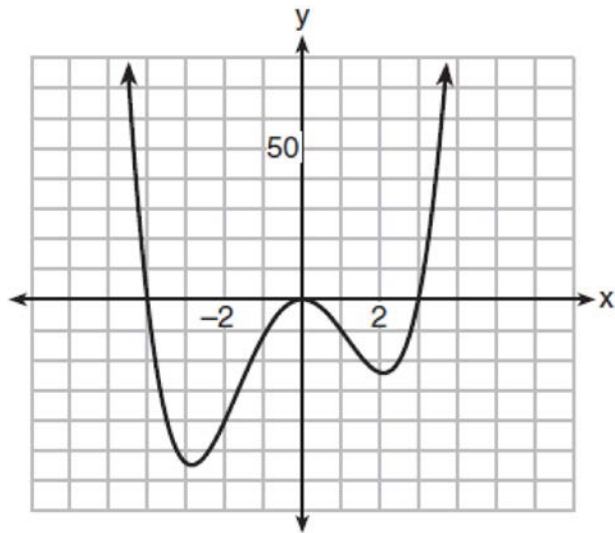
- 34 A student is chosen at random from the student body at a given high school. The probability that the student selects Math as the favorite subject is $\frac{1}{4}$. The probability that the student chosen is a junior is $\frac{116}{459}$. If the probability that the student selected is a junior or that the student chooses Math as the favorite subject is $\frac{47}{108}$, what is the exact probability that the student selected is a junior whose favorite subject is Math? Are the events "the student is a junior" and "the student's favorite subject is Math" independent of each other? Explain your answer.

- 35 In a random sample of 250 men in the United States, age 21 or older, 139 are married. The graph below simulated samples of 250 men, 200 times, assuming that 139 of the men are married.



- a) Based on the simulation, create an interval in which the middle 95% of the number of married men may fall. Round your answer to the *nearest integer*.
- b) A study claims "50 percent of men 21 and older in the United States are married." Do your results from part a contradict this claim? Explain.

- 36 The graph of $y = f(x)$ is shown below. The function has a leading coefficient of 1.

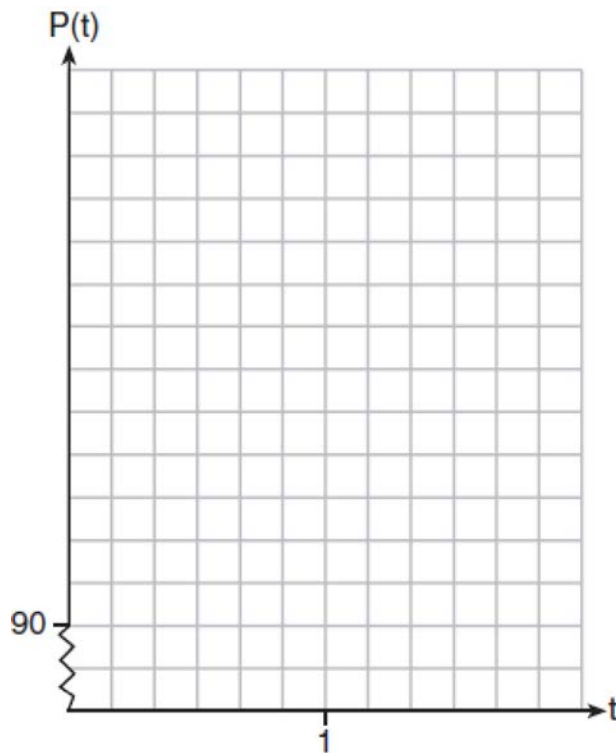


Write an equation for $f(x)$. The function g is formed by translating function f left 2 units. Write an equation for $g(x)$.

- 37 The resting blood pressure of an adult patient can be modeled by the function P below, where $P(t)$ is the pressure in millimeters of mercury after time t in seconds.

$$P(t) = 24 \cos(3\pi t) + 120$$

On the set of axes below, graph $y = P(t)$ over the domain $0 \leq t \leq 2$.



Determine the period of P . Explain what this value represents in the given context. Normal resting blood pressure for an adult is 120 over 80. This means that the blood pressure oscillates between a maximum of 120 and a minimum of 80. Adults with high blood pressure (above 140 over 90) and adults with low blood pressure (below 90 over 60) may be at risk for health disorders. Classify the given patient's blood pressure as low, normal, or high and explain your reasoning.

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Answer Section

1 ANS: 4 PTS: 2 REF: 011801aai NAT: S.IC.B.3
TOP: Analysis of Data KEY: bias

2 ANS: 3
 $\sqrt{x+1} = x+1$

$$x+1 = x^2 + 2x + 1$$

$$0 = x^2 + x$$

$$0 = x(x+1)$$

$$x = -1, 0$$

PTS: 2 REF: 011802aai NAT: A.REI.A.2 TOP: Solving Radicals
KEY: extraneous solutions

3 ANS: 4
 $3x - (-2x + 14) = 16$ $3(6) - 4z = 2$

$$5x = 30 \qquad -4z = -16$$

$$x = 6 \qquad z = 4$$

PTS: 2 REF: 011803aai NAT: A.REI.C.6 TOP: Solving Linear Systems
KEY: three variables

4 ANS: 2 PTS: 2 REF: 011804aai NAT: F.TF.A.2
TOP: Determining Trigonometric Functions KEY: radians

5 ANS: 4 PTS: 2 REF: 011805aai NAT: F.LE.B.5
TOP: Modeling Exponential Functions

6 ANS: 2 PTS: 2 REF: 011806aai NAT: A.APR.C.4
TOP: Polynomial Identities

7 ANS: 3
 $440 \times 2.3\% \approx 10$

PTS: 2 REF: 011807aai NAT: S.ID.A.4 TOP: Normal Distributions
KEY: predict

8 ANS: 4 PTS: 2 REF: 011808aai NAT: A.SSE.B.3
TOP: Modeling Exponential Functions KEY: All

9 ANS: 4

$$\begin{array}{r}
 \overline{) 10x^3 - 3x^2 - 7x + 3} \\
 \underline{10x^3 - 5x^2} \\
 2x^2 - 7x \\
 \underline{2x^2 - x} \\
 -6x + 3 \\
 \underline{-6x + 3} \\
 0
 \end{array}$$

PTS: 2 REF: 011809aai NAT: A.APR.D.6 TOP: Rational Expressions

10 ANS: 1

$$9110 = 5000e^{30r}$$

$$\ln \frac{911}{500} = \ln e^{30r}$$

$$\frac{\ln \frac{911}{500}}{30} = r$$

$$r \approx .02$$

PTS: 2 REF: 011810aai NAT: F.LE.A.4 TOP: Exponential Growth

11 ANS: 4

$$\frac{n}{m} = \frac{\sqrt{a^5}}{a} = \frac{a^{\frac{5}{2}}}{a^{\frac{2}{2}}} = a^{\frac{3}{2}} = \sqrt{a^3}$$

PTS: 2 REF: 011811aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

12 ANS: 1

$$x - \frac{4}{x-1} = 2 \quad x = \frac{3 \pm \sqrt{(-3)^2 - 4(1)(-2)}}{2(1)} = \frac{3 \pm \sqrt{17}}{2}$$

$$x(x-1) - 4 = 2(x-1)$$

$$x^2 - x - 4 = 2x - 2$$

$$x^2 - 3x - 2 = 0$$

PTS: 2 REF: 011812aai NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

13 ANS: 3

$$e^{bt} = \frac{c}{a}$$

$$\ln e^{bt} = \ln \frac{c}{a}$$

$$bt \ln e = \ln \frac{c}{a}$$

$$t = \frac{\ln \frac{c}{a}}{b}$$

PTS: 2 REF: 011813aai NAT: F.LE.A.4 TOP: Exponential Growth

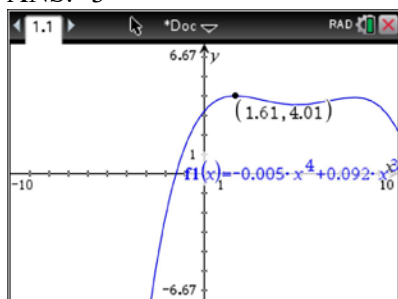
14 ANS: 1 PTS: 2 REF: 011814aai NAT: A.REI.D.11
TOP: Other Systems KEY: AII15 ANS: 1 PTS: 2 REF: 011815aai NAT: F.TF.A.2
TOP: Unit Circle

16 ANS: 1

In vertex form, the parabola is $y = -\frac{1}{4}(x+4)^2 + 3$. The vertex is $(-4, 3)$ and $p = 2$. $3 + 2 = 5$

PTS: 2 REF: 011816aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

17 ANS: 3



PTS: 2 REF: 011817aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

18 ANS: 3

$$\frac{c^2 - d^2}{d^2 + cd - 2c^2} = \frac{(c+d)(c-d)}{(d+2c)(d-c)} = \frac{-(c+d)}{d+2c} = \frac{-c-d}{d+2c}$$

PTS: 2 REF: 011818aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: $a > 0$

19 ANS: 4

$$p(5) = 2(5)^3 - 3(5) + 5 = 240$$

PTS: 2 REF: 011819aai NAT: A.APR.B.2 TOP: Remainder Theorem

20 ANS: 2 PTS: 2 REF: 011820aai NAT: S.IC.A.2
TOP: Analysis of Data

21 ANS: 2
 $x = -6(y - 2)$

$$-\frac{x}{6} = y - 2$$

$$-\frac{x}{6} + 2 = y$$

PTS: 2 REF: 011821aai NAT: F.BF.B.4 TOP: Inverse of Functions
 KEY: equations

22 ANS: 2

$$S_{20} = \frac{.01 - .01(3)^{20}}{1 - 3} = 17,433,922$$

PTS: 2 REF: 011822aai NAT: A.SSE.B.4 TOP: Series

23 ANS: 4

There is no x -intercept.

PTS: 2 REF: 011823aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions
 KEY: All

24 ANS: 3

PTS: 2

REF: 011824aai

NAT: F.BF.A.2

TOP: Sequences

25 ANS:

$$i^2 = -1, \text{ and not } 1; 10 + 10i$$

PTS: 2 REF: 011825aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

26 ANS:

$$D = 1.223(2.652)^4$$

PTS: 2 REF: 011826aai NAT: S.ID.B.6 TOP: Regression
 KEY: exponential All

27 ANS:

$$\frac{1}{8} + \frac{1}{6} = \frac{1}{t_b}; \frac{24t_b}{8} + \frac{24t_b}{6} = \frac{24t_b}{t_b}$$

$$3t_b + 4t_b = 24$$

$$t_b = \frac{24}{7} \approx 3.4$$

PTS: 2 REF: 011827aai NAT: A.CED.A.1 TOP: Modeling Rationals

28 ANS:

$$3x^3 + x^2 + 3xy + y = x^2(3x + 1) + y(3x + 1) = (x^2 + y)(3x + 1)$$

PTS: 2 REF: 011828aai NAT: A.SSE.A.2 TOP: Factoring Polynomials
 KEY: factoring by grouping

29 ANS:

$$20e^{.05t} = 30e^{.03t}$$

$$\frac{\frac{2}{3}e^{.05t}}{e^{.05t}} = \frac{e^{.03t}}{e^{.05t}}$$

$$\ln \frac{2}{3} = \ln e^{-.02t}$$

$$\ln \frac{2}{3} = -.02t \ln e$$

$$\frac{\ln \frac{2}{3}}{-.02} = t$$

$$20.3 \approx t$$

PTS: 2

REF: 011829aai

NAT: A.REI.D.11

TOP: Other Systems

KEY: AII

30 ANS:

q has the smaller minimum value for the domain $[-2,2]$. h 's minimum is $-1(2(-1)+1)$ and q 's minimum is -8 .

PTS: 2

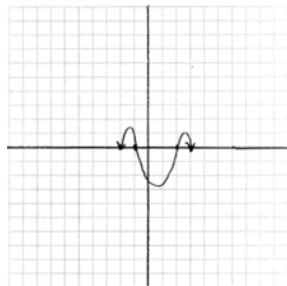
REF: 011830aai

NAT: F.IF.C.9

TOP: Comparing Functions

KEY: AII

31 ANS:



PTS: 2

REF: 011831aai

NAT: F.IF.C.7

TOP: Graphing Polynomial Functions

32 ANS:

The denominator of the rational exponent represents the index of a root, and the 4th root of 81 is 3 and 3^3 is 27.

PTS: 2

REF: 011832aai

NAT: N.RN.A.1

TOP: Radicals and Rational Exponents

33 ANS:

$$(2x^2 + x - 3) \cdot (x - 1) - \left[(2x^2 + x - 3) + (x - 1) \right]$$

$$(2x^3 - 2x^2 + x^2 - x - 3x + 3) - (2x^2 + 2x - 4)$$

$$2x^3 - 3x^2 - 6x + 7$$

PTS: 4

REF: 011833aai

NAT: F.BF.A.1

TOP: Operations with Functions

34 ANS:

$$\frac{47}{108} = \frac{1}{4} + \frac{116}{459} - P(M \text{ and } J); \text{ No, because } \frac{31}{459} \neq \frac{1}{4} \cdot \frac{116}{459}$$

$$P(M \text{ and } J) = \frac{31}{459}$$

PTS: 4 REF: 011834aai NAT: S.CP.A.3 TOP: Conditional Probability

35 ANS:

$138.905 \pm 2 \cdot 7.95 = 123 - 155$. No, since 125 (50% of 250) falls within the 95% interval.

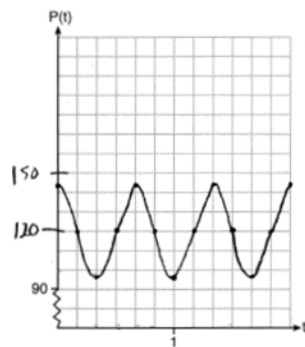
PTS: 4 REF: 011835aai NAT: S.IC.A.2 TOP: Analysis of Data

36 ANS:

$$f(x) = x^2(x+4)(x-3); \quad g(x) = (x+2)^2(x+6)(x-1)$$

PTS: 4 REF: 011836aai NAT: A.APR.B.3 TOP: Zeros of Polynomials

37 ANS:



The period of P is $\frac{2}{3}$, which means the patient's blood pressure reaches a high every $\frac{2}{3}$ second and a low every $\frac{2}{3}$ second. The patient's blood pressure is high because 144 over 96 is greater than 120 over 80.

PTS: 6 REF: 011837aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions
KEY: graph