

**0624AI**

- 1 A ball was launched into the air, and its height above the ground was recorded each second, as shown in the table below.

<b>Time (sec)</b>	0	1	2	3	4
<b>Height (ft)</b>	11	59	75	59	11

Based on these data, which statement is a valid conclusion?

- 1) The ball lands on the ground at 4 seconds.
- 2) The ball reaches a maximum height of 11 feet.
- 3) The ball was launched from a height of 0 feet.
- 4) The ball reaches its maximum height at 2 seconds.
- 2 A tour bus can seat, at most, 48 passengers. An adult ticket costs \$18 and a child ticket costs \$12. The bus company must collect at least \$650 to make a profit. If  $a$  represents the number of adult tickets sold and  $c$  represents the number of child tickets sold, which system of inequalities models this situation if they make a profit?
- 1)  $a + c < 48$   
 $18a + 12c > 650$
- 2)  $a + c \leq 48$   
 $18a + 12c \geq 650$
- 3)  $a + c < 48$   
 $18a + 12c < 650$
- 4)  $a + c \leq 48$   
 $18a + 12c \leq 650$
- 3 Which equation is always true?
- 1)  $x^2 \cdot x^3 = x^5$
- 2)  $3^x \cdot 3^2 = 9^{2x}$
- 3)  $-z^2 = z^2$
- 4)  $7^a \cdot 7^b = 7^{ab}$
- 4 The expression  $-2(x^2 - 2x + 1) + (3x^2 + 3x - 5)$  is equivalent to
- 1)  $x^2 + x - 4$
- 2)  $x^2 - x - 7$
- 3)  $x^2 + 7x - 4$
- 4)  $x^2 + 7x - 7$
- 5 Which sum is irrational?
- 1)  $-2\sqrt{12} + \sqrt{100}$
- 2)  $-\sqrt{4} + \frac{1}{3}\sqrt{900}$
- 3)  $\frac{1}{2}\sqrt{25} + \sqrt{64}$
- 4)  $\sqrt{49} + 3\sqrt{121}$
- 6 The solution to  $\frac{4(x-5)}{3} + 2 = 14$  is
- 1) 15
- 2) 14
- 3) 6
- 4) 4
- 7 On an island, a rare breed of rabbit doubled its population each month for two years. Which type of function best models the increase in population at the end of two years?
- 1) linear growth
- 2) linear decay
- 3) exponential growth
- 4) exponential decay



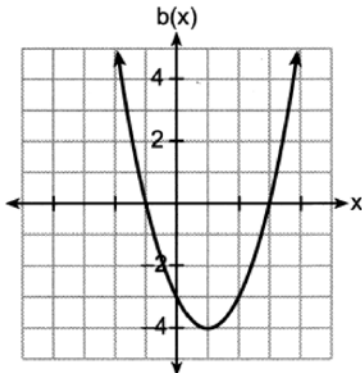
14 Four quadratic functions are represented below.

$$a(x) = (x - 3)^2 - 7$$

I

$$c(x) = x^2 + 6x + 3$$

III



II

x	d(x)
-4	-1
-3	-4
-2	-5
-1	-4
0	-1

IV

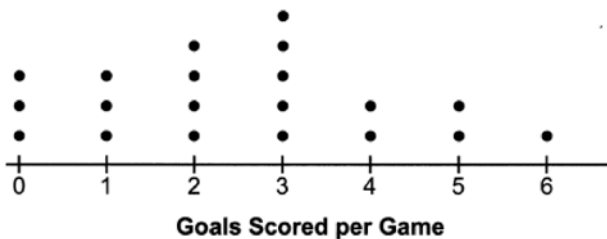
Which function has the *smallest* minimum value?

- 1) I
- 2) II
- 3) III
- 4) IV

15 The equation that represents the sequence  $-2, -5, -8, -11, -14, \dots$  is

- 1)  $a_n = -3 + (-2)(n - 1)$
- 2)  $a_n = -2 + (-3)(n - 1)$
- 3)  $a_n = 3 + (-2)(n - 1)$
- 4)  $a_n = -2 + (3)(n - 1)$

16 The dot plot below shows the number of goals Jessica scored in each lacrosse game last season.



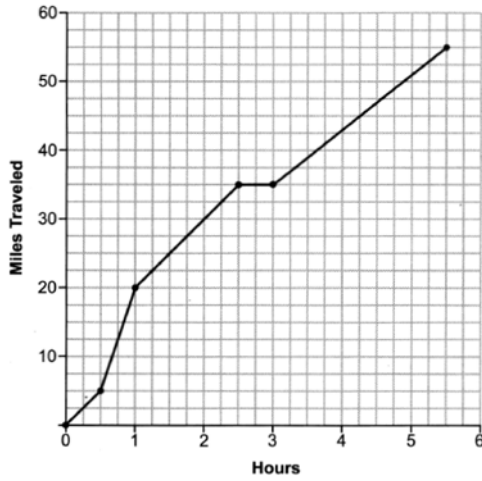
Which statement about the dot plot is correct?

- 1) mean > mode
- 2) mean = median
- 3) mode = median
- 4) median > mean

17 The students in Mrs. Smith's algebra class were asked to describe the graph of  $g(x) = 2(x - 3)^2$  compared to the graph of  $f(x) = x^2$ . Which student response is correct?

- 1) Ashley said that the graph of  $g(x)$  is wider and shifted left 3 units.
- 2) Beth said that the graph of  $g(x)$  is narrower and shifted left 3 units.
- 3) Carl said that the graph of  $g(x)$  is wider and shifted right 3 units.
- 4) Don said that the graph of  $g(x)$  is narrower and shifted right 3 units.

18 One Saturday, Dave took a long bike ride. The graph below models his trip.



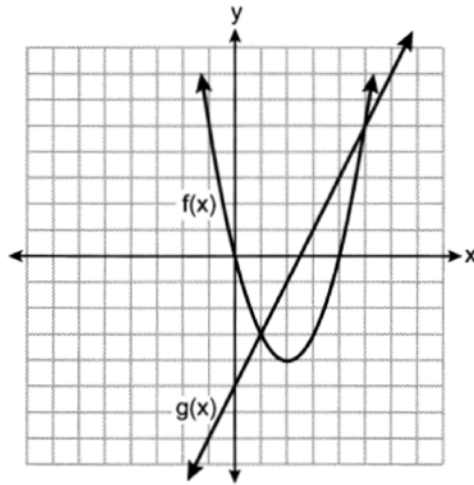
What was Dave's average rate of change, in miles per hour, on this trip?

- 1) 10
- 2) 11
- 3) 11.6
- 4) 14.5

19 Which expression is equivalent to  $(x - 5)(2x + 7) - (x + 5)$ ?

- 1)  $2x^2 - 2x - 30$
- 2)  $2x^2 - 2x - 40$
- 3)  $2x^2 - 4x - 30$
- 4)  $2x^2 - 4x - 40$

20 The functions  $f(x)$  and  $g(x)$  are graphed on the set of axes below.



What is the solution to the equation  $f(x) = g(x)$ ?

- 1) 1 and 5
- 2) -5 and 0
- 3) -3 and 5
- 4) 0 and 4

- 21 When babysitting, Nicole charges an hourly rate and an additional charge for gas. She uses the function  $C(h) = 6h + 5$  to determine how much to charge for babysitting. The constant term of this function represents
- 1) the additional charge for gas
  - 2) the hourly rate Nicole charges
  - 3) the number of hours Nicole babysits
  - 4) the total Nicole earns from babysitting
- 22 When solved for  $x$  in terms of  $a$ , the solution to the equation  $3x - 7 = ax + 5$  is
- 1)  $\frac{12}{3a}$
  - 2)  $\frac{12}{3-a}$
  - 3)  $\frac{3a}{12}$
  - 4)  $\frac{3-a}{12}$
- 23 Wayne van Niekerk, a runner from South Africa, ran 400 meters in 43.03 seconds to set a world record. Which calculation would determine his average speed, in miles per hour?
- 1)  $\frac{400 \text{ m}}{43.03 \text{ sec}} \cdot \frac{1000 \text{ m}}{0.62 \text{ mi}} \cdot \frac{1 \text{ hr}}{3600 \text{ sec}}$
  - 2)  $\frac{400 \text{ m}}{43.03 \text{ sec}} \cdot \frac{0.62 \text{ mi}}{1000 \text{ m}} \cdot \frac{1 \text{ hr}}{3600 \text{ sec}}$
  - 3)  $\frac{400 \text{ m}}{43.03 \text{ sec}} \cdot \frac{0.62 \text{ mi}}{1000 \text{ m}} \cdot \frac{3600 \text{ sec}}{1 \text{ hr}}$
  - 4)  $\frac{400 \text{ m}}{43.03 \text{ sec}} \cdot \frac{1000 \text{ m}}{0.62 \text{ mi}} \cdot \frac{3600 \text{ sec}}{1 \text{ hr}}$
- 24 Which function has a domain of all real numbers and a range greater than or equal to three?
- 1)  $f(x) = -x + 3$
  - 2)  $g(x) = x^2 + 3$
  - 3)  $h(x) = 3^x$
  - 4)  $m(x) = |x + 3|$
- 25 Solve  $5(x - 2) \leq 3x + 20$  algebraically.
- 26 Given  $g(x) = x^3 + 2x^2 - x$ , evaluate  $g(-3)$ .
- 27 Given the relation  $R = \{(-1, 1), (0, 3), (-2, -4), (x, 5)\}$ . State a value for  $x$  that will make this relation a function. Explain why your answer makes this a function.
- 28 A survey of 150 students was taken. It was determined that  $\frac{2}{3}$  of the students play video games. Of the students that play video games, 85 also use social media. Of the students that do not play video games, 20% do not use social media. Complete the two-way frequency table.

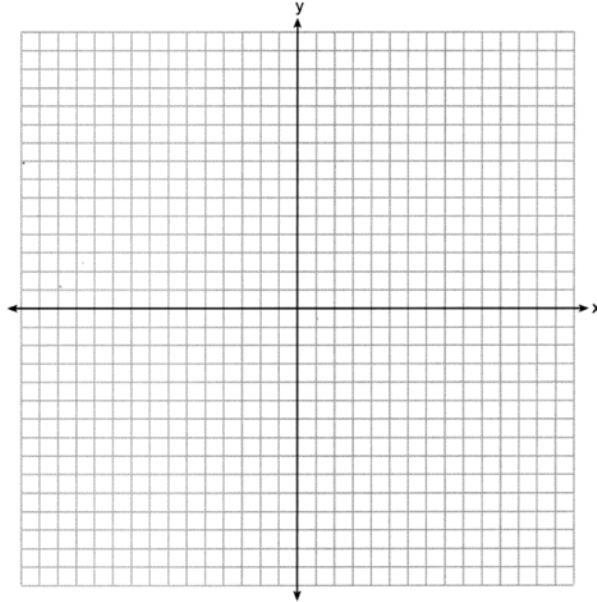
	Play Video Games	Do Not Play Video Games	Total
Social Media			
No Social Media			
Total			

- 29 Use the method of completing the square to determine the exact values of  $x$  for the equation  $x^2 + 10x - 30 = 0$ .
- 30 Factor  $20x^3 - 45x$  completely.

- 31 Graph the following system of equations on the set of axes below.

$$y = x^2 - 3x - 6$$

$$y = x - 1$$



State the coordinates of all solutions.

- 32 The table below shows the amount of money a popular movie earned, in millions of dollars, during its first six weeks in theaters.

<b>Week (x)</b>	1	2	3	4	5	6
<b>Dollars Earned, in Millions (y)</b>	185	150	90	50	25	5

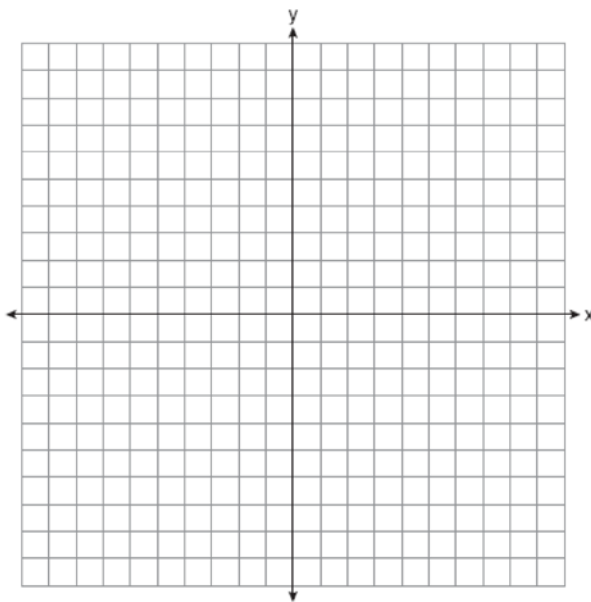
Write the linear regression equation for this data set, rounding all values to the *nearest hundredth*. State the correlation coefficient to the *nearest hundredth*. State what this correlation coefficient indicates about the linear fit of the data.

- 33 Use the quadratic formula to solve the equation  $3x^2 - 10x + 5 = 0$ . Express the answer in simplest radical form.

- 34 Graph the system of inequalities on the set of axes below.

$$3y + 2x \leq 15$$

$$y - x > 1$$



State the coordinates of a point in the solution to this system. Justify your answer.

- 35 Courtney went to a coffee shop to purchase lattes and donuts for her friends. One day she spent a total of \$15.50 on four lattes and two donuts. The next day she spent a total of \$18.10 on three lattes and five donuts. All prices included tax. If  $x$  represents the cost of one latte and  $y$  represents the cost of one donut, write a system of equations that can be used to model this situation. Courtney thinks that one latte costs \$2.75 and one donut costs \$2.25. Is Courtney correct? Justify your answer. Use your equations to determine algebraically the exact cost of one latte and the exact cost of one donut.

## 0624AI

## Answer Section

- 1 ANS: 4                      PTS: 2                      REF: 062401ai                      NAT: F.IF.B.4  
TOP: Graphing Quadratic Functions                      KEY: key features
- 2 ANS: 2                      PTS: 2                      REF: 062402ai                      NAT: A.CED.A.3  
TOP: Modeling Systems of Linear Inequalities
- 3 ANS: 1                      PTS: 2                      REF: 062403ai                      NAT: A.APR.A.1  
TOP: Multiplication of Powers
- 4 ANS: 4  
 $-2x^2 + 4x - 2 + 3x^2 + 3x - 5 = x^2 + 7x - 7$
- PTS: 2                      REF: 062404ai                      NAT: A.APR.A.1                      TOP: Operations with Polynomials  
KEY: addition
- 5 ANS: 1                      PTS: 2                      REF: 062405ai                      NAT: N.RN.B.3  
TOP: Operations with Radicals                      KEY: classify
- 6 ANS: 2  
 $\frac{4(x-5)}{3} = 12$   
 $4x - 20 = 36$   
 $4x = 56$   
 $x = 14$
- PTS: 2                      REF: 062406ai                      NAT: A.REI.B.3                      TOP: Solving Linear Equations
- 7 ANS: 3                      PTS: 2                      REF: 062407ai                      NAT: F.LE.A.1  
TOP: Families of Functions
- 8 ANS: 3                      PTS: 2                      REF: 062408ai                      NAT: A.SSE.A.1  
TOP: Modeling Expressions
- 9 ANS: 2                      PTS: 2                      REF: 062409ai                      NAT: A.APR.B.3  
TOP: Zeros of Polynomials
- 10 ANS: 3  
 $\frac{5 - -1}{-1 - 2} = \frac{6}{-3} = -2$   $5 = -2(-1) + b$   
 $3 = b$
- PTS: 2                      REF: 062410ai                      NAT: F.IF.B.4                      TOP: Graphing Linear Functions
- 11 ANS: 1  
 $a(8) = 2^8 + 25 = 281$   $b(8) = 10(8) + 75 = 155$   $c(8) = \sqrt{400(8)} + 80 \approx 137$   $d(8) = 2(8 + 1)^2 - 10(8) + 50 = 132$
- PTS: 2                      REF: 062411ai                      NAT: F.LE.A.3                      TOP: Families of Functions



12 ANS: 2  
 $25r^2 = 625$

$$r^2 = 25$$

$$r = \pm 5$$

PTS: 2 REF: 062412ai NAT: F.IF.A.3 TOP: Sequences  
 KEY: difference or ratio

13 ANS: 2  
 $110 - 60 = 50$

PTS: 2 REF: 062413ai NAT: S.ID.A.1 TOP: Box Plots  
 KEY: interpret

14 ANS: 1

1)  $-7$ ; 2)  $-4$ ; 3)  $x = \frac{-6}{2(1)} = -3$ ,  $c(-3) = (-3)^2 + 6(-3) + 3 = -6$ ; 4)  $-5$

PTS: 2 REF: 062414ai NAT: F.IF.C.9 TOP: Comparing Quadratic Functions  
 15 ANS: 2 PTS: 2 REF: 062415ai NAT: F.BF.A.1  
 TOP: Sequences KEY: explicit

16 ANS: 2

mean:  $\frac{3(0) + 3(1) + 4(2) + 5(3) + 2(4) + 2(5) + 1(6)}{3 + 3 + 4 + 5 + 2 + 2 + 1} = \frac{50}{20} = 2.5$ , mode: 3, median:  $\frac{2+3}{2} = 2.5$

PTS: 2 REF: 062416ai NAT: S.ID.A.1 TOP: Dot Plots  
 17 ANS: 4 PTS: 2 REF: 062417ai NAT: F.BF.B.3  
 TOP: Transformations with Functions

18 ANS: 1

$$\frac{55 - 0}{5.5 - 0} = 10$$

PTS: 2 REF: 062418ai NAT: F.IF.B.6 TOP: Rate of Change  
 19 ANS: 4

$$2x^2 + 7x - 10x - 35 - x - 5 = 2x^2 - 4x - 40$$

PTS: 2 REF: 062419ai NAT: A.APR.A.1 TOP: Operations with Polynomials  
 KEY: multiplication

20 ANS: 1 PTS: 2 REF: 062420ai NAT: A.REI.D.11  
 TOP: Quadratic-Linear Systems

21 ANS: 1 PTS: 2 REF: 062421ai NAT: F.LE.B.5  
 TOP: Modeling Linear Functions

22 ANS: 2

$$3x - ax = 12$$

$$x(3 - a) = 12$$

$$x = \frac{12}{3 - a}$$

PTS: 2 REF: 062422ai NAT: A.CED.A.4 TOP: Transforming Formulas

23 ANS: 3 PTS: 2 REF: 062423ai NAT: N.Q.A.1

TOP: Conversions

24 ANS: 2

All four functions have a real domain.  $f$  has a real range.  $h$  has a positive real range.  $m$  has a nonnegative real range.

PTS: 2 REF: 062424ai NAT: F.IF.A.2 TOP: Domain and Range

25 ANS:

$$5x - 10 \leq 3x + 20$$

$$2x \leq 30$$

$$x \leq 15$$

PTS: 2 REF: 062425ai NAT: A.REI.B.3 TOP: Solving Linear Inequalities

26 ANS:

$$g(-3) = (-3)^3 + 2(-3)^2 - (-3) = -27 + 18 + 3 = -6$$

PTS: 2 REF: 062426ai NAT: F.IF.A.2 TOP: Functional Notation

27 ANS:

$x$  may be any value other than  $-2, -1, 0$ , so that for any value of  $x$ , there is a unique  $y$ .

PTS: 2 REF: 062427ai NAT: F.IF.A.1 TOP: Defining Functions

28 ANS:

	Play Video Games	Do Not Play Video Games	Total
Social Media	85	40	125
No Social Media	15	10	25
Total	100	50	150

PTS: 2 REF: 062428ai NAT: S.ID.B.5 TOP: Frequency Tables

KEY: two-way

29 ANS:

$$x^2 + 10x = 30$$

$$x^2 + 10x + 25 = 30 + 25$$

$$(x + 5)^2 = 55$$

$$x + 5 = \pm\sqrt{55}$$

$$x = -5 \pm \sqrt{55}$$

PTS: 2 REF: 062429ai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: completing the square

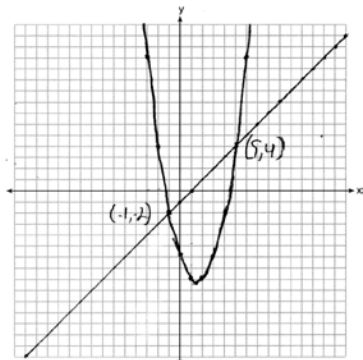
30 ANS:

$$20x^3 - 45x = 5x(4x^2 - 9) = 5x(2x + 3)(2x - 3)$$

PTS: 2 REF: 062430ai NAT: A.SSE.A.2

TOP: Factoring the Difference of Perfect Squares

31 ANS:



PTS: 4 REF: 062431ai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

32 ANS:

$$y = -37.57x + 215.67, -0.98, \text{strong}$$

PTS: 4 REF: 062432ai NAT: S.ID.B.6 TOP: Regression

KEY: linear with correlation coefficient

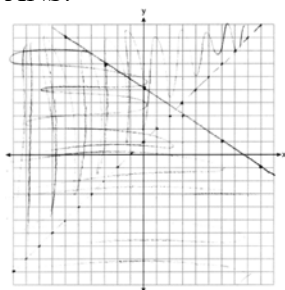
33 ANS:

$$x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(3)(5)}}{2(3)} = \frac{10 \pm \sqrt{40}}{6} = \frac{10 \pm 2\sqrt{10}}{6} = \frac{5 \pm \sqrt{10}}{3}$$

PTS: 4 REF: 062433ai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: quadratic formula

34 ANS:



$(-1, 1)$  is a solution as it is in the overlap area.

PTS: 4

REF: 062434ai

NAT: A.REI.D.12

TOP: Graphing Systems of Linear Inequalities

35 ANS:

$4x + 2y = 15.5$   $5(4x + 2y = 15.5)$  Courtney is incorrect because of the following calculations:  $20x + 10y = 77.5$

$3x + 5y = 18.1$   $2(3x + 5y = 18.1)$

$6x + 10y = 36.2$

$14x = 41.3$

$x = 2.95$

$4(2.95) + 2y = 15.5$

$11.8 + 2y = 15.5$

$2y = 3.7$

$y = 1.85$

PTS: 6

REF: 062435ai

NAT: A.CED.A.3

TOP: Modeling Linear Systems