

**22***University of the State of New York***Examination Department**

124th examination

**ALGEBRA****August 1894 — Three hours, only**

100 credits, necessary to pass, 75

*Answer to questions but no more. Division of groups is not allowed. If more than 10 questions are answered only the first 10 of these answers will be considered. Give each step of solution. Reduce fractions to lowest terms. Express final result in its simplest form and mark it Ans. Each complete answer will receive 10 credits.*

1 Define power, root, degree of a term, surd, affected quadratic equation.

2 Remove parentheses and simplify  $a[(a+b)(2a-3b) - (-a+b)(3b+a) - a(1+3b)]$

3-4 Simplify  $\frac{3}{x+y} + \frac{1}{x-y} - \frac{x-y}{x^2+y^2} - \frac{x+y}{x^2-y^2}$

5-6 Find the greatest common divisor of  $a^3 x^2 + 2a^2 x^3 + 2a^2 b x^2 + 4ab x^3$  and  $a^2 b x + 2aby + 2ab^2 x + 4b^2 y$

7-8 Solve  $\frac{x}{2a} + \frac{y}{3b} = 3a + 1$ ,  $ax + 2by = 6(a^3 + b^2)$

9-10 Solve  $x^4 + 4x^2 = 32$ . Find four roots.

11-12 Solve  $x^3 - y^3 = 2b (3a^2 + b^2)$ ,  $x - y = 2b$

13 Simplify  $\sqrt{50}$ ,  $\frac{1}{2}\sqrt{\frac{1}{2}}$ ,  $\sqrt[3]{16a^4b^3}$ ,  $\sqrt{a} \times \sqrt[3]{b}$ ,  $\sqrt{12} + \sqrt{27}$

14 Form an equation whose roots are  $a$  and  $-\frac{b}{2}$

15 Expand by the binomial formula  $\left(\frac{a}{2} - 3b\right)^5$ , giving all the work of finding the coefficients.