The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

TWELFTH YEAR MATHEMATICS

12A (Advanced Algebra)

Thursday, June 20, 1963 - 9:15 a.m. to 12:15 p.m., only

The last page of the booklet is the answer sheet, which is perforated. Fold the last page along the perforation and then, slowly and carefully, tear off the answer sheet. Now fill in the heading of your answer sheet. When you have finished the heading, you may begin the examination immediately.

Part I

Answer all questions in this part. Each correct answer will receive 21/2 credits. No partial credit will be allowed. Write your answers in the spaces provided on the separate answer sheet.

- 1 What is the remainder when $2x^2 3x^2 5x + 4$ is divided by x + 2?
- 2 Find the nonintegral rational root of $5x^2 8x^2 2x + 3 = 0$.
- 3 Find the radius of the circle whose equation is $x^2 4x + y^2 + 6y 36 = 0$.
- 4 Find the value of $3x^{0} 54x^{3} + 64^{x}$ when $x = -\frac{1}{3}$.
- 5 When the number $\frac{2-i}{3+i}$ is expressed in a+bi form, what is the value of b?
- 6 Find all values of x for which 4x 3 > x + 5.
- 7 Find the area of the triangle bounded by the coordinate axes and the line $\frac{x}{5} + \frac{y}{12} = 1$.
- 8 Write in simplest form the fourth term *only* of the expansion of $\left(\frac{1}{x} \frac{x}{2}\right)^9$.
- 9 Express the repeating decimal 0.272727... in the form $\frac{a}{b}$ where a and b are integers.
- 10 The graph of $y = x^2 6x + k$ is tangent to the x-axis. Find the value of k.
- 11 Between what two consecutive positive integers does the real root of $4x^8 10x^2 + 8x 3 = 0$ lie?

- 12 A bag contains buttons that are identical except that some are red and all the rest are white. There are 6 times as many white buttons as red. If one button is taken out at random, what is the probability that it is white?
- 13 In how many different ways may the seven letters of the word MINIMUM be arranged if all of the letters are used each time?
- 14 Write an equation of the straight line which is tangent to the graph of $y = x^2 2x + 9$ at the point (2, 9).
- 15 Find an amplitude of the complex number which is the product of 2(cos 10° + i sin 10°) and 3(cos 128° + i sin 128°).
- 16 In the equation $x^4 + p_1x^3 + p_2x^2 + p_3x + p_4 = 0$, the coefficients are rational numbers. If two roots are $3 + \sqrt{2}$ and 5 i, find the value of p_4 .
- 17 If x varies directly as y^2 and inversely as z and if x = 4 when y = 0.2 and z = 0.7, find the value of the constant of variation.
- Write an equation of the axis of symmetry of the graph of $y = 3x^2 5x + 9$.
- 19 Solve for n (a positive integer) ${}_{n}C_{n-2} = 36$.
- 20 The sum of the first four terms of a geometric progression is 65. If the common ratio is 3, find the first term
- 21 Write an equation of the straight line which is perpendicular to the line 2x 3y = 5 at the point (4, 1).

to cars of the following by writing the number 1, 2, 3 or 4 in the space provided on the separate answer sheet,

22 The graph of y = 2 + lies in quadrants

(2) II and III

(1) I and II (3) III and IV

(4) IV and I

23 If $s = 5t^3 + t - 3$, the average rate of change of s with respect to t for the interval from t = 0 to t = 4 is

(2) 21 (3) 101

(4) 41

If n is divided by d, the quotient is q and the remaind is r. This may be expressed by

Part II

Answer sixteen questions from this part, 25-48. Each correct answer will receive 21/2 credits. No partial credit will be allowed. Questions marked are based upon optional topics in the syllabus. Write your answers on the separate answer sheet.

- 25 Eleven different points lie on a circle. With these points as vertices, how many different triangles can
- 26 Solve for $x: 8^{r+3} = 2^{4r}$
- 27 If $f(x) = x^2 + x 2$, find 4f(-a).
- 28 Express in simplest form: $\frac{\frac{x-2}{3}+1}{\frac{x+3}{2}-1}$
- 29 One root of $x^5 + 32 = 0$ lies in quadrant IV. Write this root in the form $r(\cos \theta + i \sin \theta)$.
- 30 A point moves along a line so that its distance from the starting point at the time t is given by the equation $s = 13t^3 - 4t^2$. Find the acceleration of the point when t = 1.
- 31 How many quarts of water must be added to 9 quarts of a 30% solution of antifreeze to obtain a 15% solution?
- 32 The solution of the inequality $x^2 + 2x 15 > 0$ has the form x > a or x < b. What is the value of b?
- 33 The sum of an infinite geometric series is 6. The first term is a and the common ratio is r. Express r in terms of a.
- 34 Find to the nearest tenth: log 27
- 35 Solve for x: $\log (3x + 2) \log x = 1$

- *36 Solve for y: $\begin{vmatrix} 2 & 1 & 1 \\ 5 & -1 & 1 \\ 4 & y & 1 \end{vmatrix} = 16$
- 37 Find the value of k in $x^3 3x^2 49x + k = 0$ if the sum of two of the roots is zero.
- 38 The arithmetic mean between two numbers is 7 and their positive geometric mean is 3\sqrt{5}. Find both numbers.
- 39 A root of $x^8 2x^2 + 3x 4 = 0$ lies between 1 and 2. Find this root to the nearest integer.
- *40 Transform the equation $r = 5 \sin \theta$ from polar to rectangular coordinates.
- 41 Write a general equation of the family of lines parallel to 4x - 2y + 5 = 0.
- 42 Find the abscissa of the point of inflection of the graph of $y = x^3 - 5x^2 + 3x - 7$.

Directions (43-48): For each of those chosen, write in the space provided on the separate answer sheet the number preceding the expression that best completes the statement or answers the question.

43 Which of the following defines a rational integral function of x?

(1) $y = \sqrt{x-1}$ (3) $y = x^{-2} + 4$

- (2) $y = \frac{1}{x^2}$ (4) $y = x^{11} \sqrt{3}$
- 44 If $y = (x + 3)^2$ and $(x + 3)^2 + y^2 = 4$ are graphed on the same axes, the total number of points of intersection is
 - (1) 1
- (2) 2 (3) 3 (4) 0

the form $(x + k)^s = k^s - \frac{c}{a}$ by completing the square. The value of k in terms of a and b is

 $(1) \frac{b}{a}$

 $(3) \ \frac{b^a}{a^a}$

 $(2) \ \frac{b}{2a}$

 $(4) \frac{b^a}{4a^a}$

46 The equation $3x - \sqrt{x} - 10 = 0$ has

- (1) the two roots 4 and $-\frac{25}{9}$
- (2) the two roots 4 and $\frac{25}{9}$
- (3) the single root $\frac{25}{9}$
- (4) the single root 4

48 The complex numbers a + bi, c + di, e + fi may be considered graphically or algebraically. Which statement is not true for all real values of a, b, c, d, e and f?

$$(1) (a + bi) + (c + di) + (e + fi) = 0$$

$$(2) (a+bi) + (c+di) = (c+di) + (a+bi)$$

(3)
$$3(a + bi) = 3a + 3bi$$

(4)
$$(a + bi) + [(c + di) + (e + fi)] = [(a + bi) + (c + di)] + (e + fi)$$

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ANSWER SHEET

Teacher...

16,		
All of your a	nswers should be recorded on this ans	wer sheet.
	Part I Answer all questions in this part.	
1	9	17
2	10	18
3,	11	19
4	12	20
5	13	21
6	14	22
7	15	23
8	16	24
Your answers for part II	should be placed in the proper spaces	on the back of this sheet



Answer only sixteen questions from this part. Be sure to write in the properly numbered spaces the snewers to the questions you do not choose to answer. 27..... 28...... 32.....

I have regularly studied twelfth year mathematics 12A (advanced algebra) for weeks and have had recitations per week.

I do so declare.....(Signature)

FOR TEACHERS ONLY

12A

SCORING KEY TWELFTH YEAR MATHEMATICS 12A (Advanced Algebra)

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Use only red ink or pencil in rating Regents papers. Do not attempt to correct the pupil's work by making insertions or changes of any kind. Use checkmarks to indicate pupil errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. In problems involving logarithms, answers should be left correct to four significant digits unless directions say otherwise. Units need not be given when the wording of the questions allows such omissions.

Part I

Allow $2\frac{1}{2}$ credits for each correct answer; allow no partial credit. For questions 22-24, allow credit if the pupil has written the correct answer instead of the number 1, 2, 3 or 4.

$$(1)$$
 -14

$$(9) \frac{3}{11}$$

(18)
$$x = \frac{5}{6}$$

$$(4)$$
 $5\frac{1}{4}$

$$(12) \frac{6}{7}$$

(5)
$$\frac{1}{2}$$
 [Do not accept $\frac{1}{2} - \frac{1}{2}i$ or $\frac{1-i}{2}$.]

$$(21) \ 3x + 2y = 14$$

$$(14) \ y - 2x - 5 = 0$$

(6)
$$x > \frac{8}{3}$$

(8)
$$-\frac{21}{2x^3}$$

Part II

Allow 2½ credits for each of not more than 16 correct answers; allow no partial credit. If more than sixteen questions have been answered, only the first sixteen of these should be considered. For questions 43-48, allow credit if the pupil has written the correct answer instead of the number 1, 2, 3 or 4.

(33)
$$1 - \frac{a}{6}$$

(41)
$$y = 2x + b$$

$$(42) \frac{5}{3}$$

$$(27)$$
 $4a^2 - 4a - 8$

(29)
$$2(\cos 324^{\circ} + i \sin 324^{\circ})$$

$$(32) -5$$

$$(40) x^2 + y^2 = 5y$$

