

# JMAP REGENTS BY TYPE

The NY Algebra II Regents Exams Questions  
from Spring 2015 to January 2023 Sorted by Type

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## Algebra II Multiple Choice Regents Exam Questions

- 1 Given the polynomial identity  $x^6 + y^6 = (x^2 + y^2)(x^4 - x^2y^2 + y^4)$ , which equation must also be true for all values of  $x$  and  $y$ ?

- 1)  $x^6 + y^6 = x^2(x^4 - x^2y^2 + y^4) + y^2(x^4 - x^2y^2 + y^4)$
- 2)  $x^6 + y^6 = (x^2 + y^2)(x^2 - y^2)(x^2 - y^2)$
- 3)  $(x^3 + y^3)^2 = (x^2 + y^2)(x^4 - x^2y^2 + y^4)$
- 4)  $(x^6 + y^6) - (x^2 + y^2) = x^4 - x^2y^2 + y^4$

- 2 The formula below can be used to model which scenario?

$$a_1 = 3000$$

$$a_n = 0.80a_{n-1}$$

- 1) The first row of a stadium has 3000 seats, and each row thereafter has 80 more seats than the row in front of it.
- 2) The last row of a stadium has 3000 seats, and each row before it has 80 fewer seats than the row behind it.
- 3) A bank account starts with a deposit of \$3000, and each year it grows by 80%.
- 4) The initial value of a specialty toy is \$3000, and its value each of the following years is 20% less.

- 3 The population of Jamesburg for the years 2010-2013, respectively, was reported as follows:  
250,000 250,937 251,878 252,822  
How can this sequence be recursively modeled?

- 1)  $j_n = 250,000(1.00375)^{n-1}$
- 2)  $j_n = 250,000 + 937^{(n-1)}$
- 3)  $j_1 = 250,000$

$$j_n = 1.00375j_{n-1}$$

- 4)  $j_1 = 250,000$

$$j_n = j_{n-1} + 937$$

- 4 Pedro and Bobby each own an ant farm. Pedro starts with 100 ants and says his farm is growing exponentially at a rate of 15% per month. Bobby starts with 350 ants and says his farm is steadily decreasing by 5 ants per month. Assuming both boys are accurate in describing the population of their ant farms, after how many months will they both have approximately the same number of ants?

- 1) 7
- 2) 8
- 3) 13
- 4) 36

- 5 Which expression is equivalent to  $\frac{x^3 - 2}{x - 2}$ ?

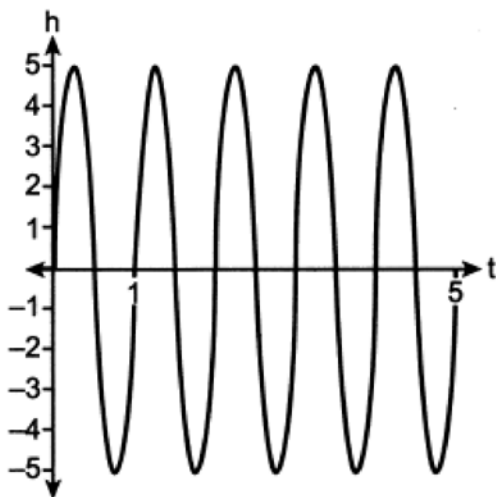
- 1)  $x^2$
- 2)  $x^2 + 2x + 4 + \frac{6}{x-2}$
- 3)  $x^2 - 2$
- 4)  $x^2 - 2x + 4 - \frac{10}{x-2}$

- 6 If  $f(x) = \frac{1}{2}x + 2$ , then the inverse function is

- 1)  $f^{-1}(x) = -\frac{1}{2}x - 2$
- 2)  $f^{-1}(x) = \frac{1}{2}x - 1$
- 3)  $f^{-1}(x) = 2x - 4$
- 4)  $f^{-1}(x) = 2x + 2$

- 7 Given that  $i$  is the imaginary unit, the expression  $(x - 2i)^2$  is equivalent to
- 1)  $x^2 + 4$
  - 2)  $x^2 - 4$
  - 3)  $x^2 - 2xi - 4$
  - 4)  $x^2 - 4xi - 4$

- 8 A cyclist pedals a bike at a rate of 60 revolutions per minute. The height,  $h$ , of a pedal at time  $t$ , in seconds, is plotted below.



The graph can be modeled by the function  $h(t) = 5 \sin(kt)$ , where  $k$  is equal to

- 1) 1
  - 2)  $2\pi$
  - 3) 60
  - 4)  $\frac{\pi}{30}$
- 9 The roots of the equation  $x^2 + 2x + 5 = 0$  are
- 1)  $-3$  and  $1$
  - 2)  $-1$ , only
  - 3)  $-1 + 2i$  and  $-1 - 2i$
  - 4)  $-1 + 4i$  and  $-1 - 4i$

- 10 The sum of the first 20 terms of the series  $-2 + 6 - 18 + 54 - \dots$  is

- 1)  $-610$
- 2)  $-59$
- 3)  $1,743,392,200$
- 4)  $2,324,522,934$

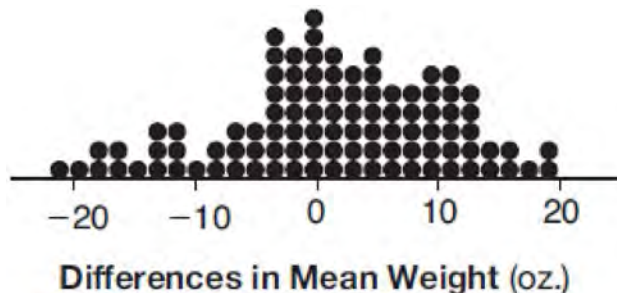
- 11 Kristin wants to increase her running endurance. According to experts, a gradual mileage increase of 10% per week can reduce the risk of injury. If Kristin runs 8 miles in week one, which expression can help her find the total number of miles she will have run over the course of her 6-week training program?

- 1)  $\sum_{n=1}^6 8(1.10)^{n-1}$
- 2)  $\sum_{n=1}^6 8(1.10)^n$
- 3)  $\frac{8 - 8(1.10)^6}{0.90}$
- 4)  $\frac{8 - 8(0.10)^n}{1.10}$

- 12 The Hot and Tasty Coffee chain conducts a survey of its customers at its location at the Staten Island ferry terminal. After the survey is completed, the statistical consultant states that 70% of customers who took the survey said the most important factor in choosing where to get their coffee is how fast they are served. Based on this result, Hot and Tasty Coffee can infer that

- 1) most of its customers in New York State care most about being served quickly
- 2) coffee drinkers care less about taste and more about being served quickly
- 3) most of its customers at the Staten Island ferry terminal care most about being served quickly
- 4) most of its customers at transportation terminals and stations care most about being served quickly

- 13 Gabriel performed an experiment to see if planting 13 tomato plants in black plastic mulch leads to larger tomatoes than if 13 plants are planted without mulch. He observed that the average weight of the tomatoes from tomato plants grown in black plastic mulch was 5 ounces greater than those from the plants planted without mulch. To determine if the observed difference is statistically significant, he rerandomized the tomato groups 100 times to study these random differences in the mean weights. The output of his simulation is summarized in the dotplot below.



Given these results, what is an appropriate inference that can be drawn?

- |   |   |
|---|---|
| <p>1) There was no effect observed between the two groups.</p> <p>2) There was an effect observed that could be due to the random assignment of plants to the groups.</p> | <p>3) There is strong evidence to support the hypothesis that tomatoes from plants planted in black plastic mulch are larger than those planted without mulch.</p> <p>4) There is strong evidence to support the hypothesis that tomatoes from plants planted without mulch are larger than those planted in black plastic mulch.</p> |
|---|---|
- 
- 14 Iridium-192 is an isotope of iridium and has a half-life of 73.83 days. If a laboratory experiment begins with 100 grams of Iridium-192, the number of grams,  $A$ , of Iridium-192 present after  $t$  days would be  $A = 100\left(\frac{1}{2}\right)^{\frac{t}{73.83}}$ . Which equation approximates the amount of Iridium-192 present after  $t$  days?
- 1)  $A = 100\left(\frac{73.83}{2}\right)^t$
  - 2)  $A = 100\left(\frac{1}{147.66}\right)^t$
  - 3)  $A = 100(0.990656)^t$
  - 4)  $A = 100(0.116381)^t$
- 
- 15 In 2010, the population of New York State was approximately 19,378,000 with an annual growth rate of 1.5%. Assuming the growth rate is maintained for a large number of years, which equation can be used to predict the population of New York State  $t$  years after 2010?
- 1)  $P_t = 19,378,000(1.5)^t$
  - 2)  $P_0 = 19,378,000$   
 $P_t = 19,378,000 + 1.015P_{t-1}$
  - 3)  $P_t = 19,378,000(1.015)^{t-1}$
  - 4)  $P_0 = 19,378,000$   
 $P_t = 1.015P_{t-1}$

- 16 The solution set for the equation  $\sqrt{56-x} = x$  is
- 1)  $\{-8, 7\}$
  - 2)  $\{-7, 8\}$
  - 3)  $\{7\}$
  - 4)  $\{ \}$
- 17 What is the solution set of the equation  $\frac{x+2}{x} + \frac{x}{3} = \frac{2x^2+6}{3x}$ ?
- 1)  $\{-3\}$
  - 2)  $\{-3, 0\}$
  - 3)  $\{3\}$
  - 4)  $\{0, 3\}$
- 18 The expression  $\frac{x^4 - 5x^2 + 4x + 14}{x + 2}$  is equivalent to
- 1)  $x^3 - 2x^2 - x + 6 + \frac{2}{x+2}$
  - 2)  $x^3 - 5x + 4 - \frac{14}{x+2}$
  - 3)  $x^3 + 2x^2 - x + 2 + \frac{18}{x+2}$
  - 4)  $x^3 + 2x^2 - 9x + 22 - \frac{30}{x+2}$
- 19 The voltage used by most households can be modeled by a sine function. The maximum voltage is 120 volts, and there are 60 cycles *every second*. Which equation best represents the value of the voltage as it flows through the electric wires, where  $t$  is time in seconds?
- 1)  $V = 120 \sin(t)$
  - 2)  $V = 120 \sin(60t)$
  - 3)  $V = 120 \sin(60\pi t)$
  - 4)  $V = 120 \sin(120\pi t)$
- 20 When factored completely,  $m^5 + m^3 - 6m$  is equivalent to
- 1)  $(m+3)(m-2)$
  - 2)  $(m^2+3m)(m^2-2)$
  - 3)  $m(m^4+m^2-6)$
  - 4)  $m(m^2+3)(m^2-2)$
- 21 Sean's team has a baseball game tomorrow. He pitches 50% of the games. There is a 40% chance of rain during the game tomorrow. If the probability that it rains given that Sean pitches is 40%, it can be concluded that these two events are
- 1) independent
  - 2) dependent
  - 3) mutually exclusive
  - 4) complements
- 22 A payday loan company makes loans between \$100 and \$1000 available to customers. Every 14 days, customers are charged 30% interest with compounding. In 2013, Remi took out a \$300 payday loan. Which expression can be used to calculate the amount she would owe, in dollars, after one year if she did not make payments?
- 1)  $300(.30)^{\frac{14}{365}}$
  - 2)  $300(1.30)^{\frac{14}{365}}$
  - 3)  $300(.30)^{\frac{365}{14}}$
  - 4)  $300(1.30)^{\frac{365}{14}}$

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- 23 Julie averaged 85 on the first three tests of the semester in her mathematics class. If she scores 93 on each of the remaining tests, her average will be 90. Which equation could be used to determine how many tests,  $T$ , are left in the semester?

- 1)  $\frac{255 + 93T}{3T} = 90$
- 2)  $\frac{255 + 90T}{3T} = 93$
- 3)  $\frac{255 + 93T}{T + 3} = 90$
- 4)  $\frac{255 + 90T}{T + 3} = 93$

- 24 A rabbit population doubles every 4 weeks. There are currently five rabbits in a restricted area. If  $t$  represents the time, in weeks, and  $P(t)$  is the population of rabbits with respect to time, about how many rabbits will there be in 98 days?

- 1) 56
- 2) 152
- 3) 3688
- 4) 81,920

- 25 Monthly mortgage payments can be found using the formula below, where  $M$  is the monthly payment,  $P$  is the amount borrowed,  $r$  is the annual interest rate, and  $n$  is the total number of monthly payments.

$$M = \frac{P\left(\frac{r}{12}\right)\left(1 + \frac{r}{12}\right)^n}{\left(1 + \frac{r}{12}\right)^n - 1}$$

If Adam takes out a 15-year mortgage, borrowing \$240,000 at an annual interest rate of 4.5%, his monthly payment will be

- 1) \$1379.09
- 2) \$1604.80
- 3) \$1835.98
- 4) \$9011.94

- 26 Consider the system below.

$$x + y + z = 9$$

$$x - y - z = -1$$

$$x - y + z = 21$$

Which value is *not* in the solution,  $(x, y, z)$ , of the system?

- 1) -8
- 2) -6
- 3) 11
- 4) 4

- 27 The amount of a substance,  $A(t)$ , that remains after  $t$  days can be given by the equation

$A(t) = A_0(0.5)^{\frac{t}{0.0803}}$ , where  $A_0$  represents the initial amount of the substance. An equivalent form of this equation is

- 1)  $A(t) = A_0(0.000178)^t$
- 2)  $A(t) = A_0(0.945861)^t$
- 3)  $A(t) = A_0(0.04015)^t$
- 4)  $A(t) = A_0(1.08361)^t$

- 28 Which expression is *not* a solution to the equation

$$2^t = \sqrt{10}?$$

- 1)  $\frac{1}{2} \log_2 10$
- 2)  $\log_2 \sqrt{10}$
- 3)  $\log_4 10$
- 4)  $\log_{10} 4$

- 29 The expression  $\left(a\sqrt[3]{2b^2}\right)\left(\sqrt[3]{4a^2b}\right)$  is equivalent

to

- 1)  $2ab\sqrt[3]{a^2}$
- 2)  $2ab$
- 3)  $2ab\sqrt[3]{2a^2}$
- 4)  $2a^2b\sqrt[3]{2b}$

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30 What are the zeros of  $P(m) = (m^2 - 4)(m^2 + 1)$ ?

- 1) 2 and -2, only
- 2) 2, -2, and -4
- 3) -4,  $i$ , and  $-i$
- 4) 2, -2,  $i$ , and  $-i$

31 Consider a cubic polynomial with the characteristics below.

- exactly one real root
- as  $x \rightarrow \infty, f(x) \rightarrow -\infty$

Given  $a > 0$  and  $b > 0$ , which equation represents a cubic polynomial with these characteristics?

- 1)  $f(x) = (x - a)(x^2 + b)$
- 2)  $f(x) = (a - x)(x^2 + b)$
- 3)  $f(x) = (a - x^2)(x^2 + b)$
- 4)  $f(x) = (x - a)(b - x^2)$

32 The expression  $6xi^3(-4xi + 5)$  is equivalent to

- 1)  $2x - 5i$
- 2)  $-24x^2 - 30xi$
- 3)  $-24x^2 + 30x - i$
- 4)  $26x - 24x^2i - 5i$

33 A recursive formula for the sequence 40, 30, 22.5, ... is

- 1)  $g_n = 40\left(\frac{3}{4}\right)^n$
- 2)  $g_1 = 40$   
 $g_n = g_{n-1} - 10$
- 3)  $g_n = 40\left(\frac{3}{4}\right)^{n-1}$
- 4)  $g_1 = 40$   
 $g_n = \frac{3}{4}g_{n-1}$

34 Which statement(s) about statistical studies is true?

- I. A survey of all English classes in a high school would be a good sample to determine the number of hours students throughout the school spend studying.
  - II. A survey of all ninth graders in a high school would be a good sample to determine the number of student parking spaces needed at that high school.
  - III. A survey of all students in one lunch period in a high school would be a good sample to determine the number of hours adults spend on social media websites.
  - IV. A survey of all Calculus students in a high school would be a good sample to determine the number of students throughout the school who don't like math.
- 1) I, only
  - 2) II, only
  - 3) I and III
  - 4) III and IV

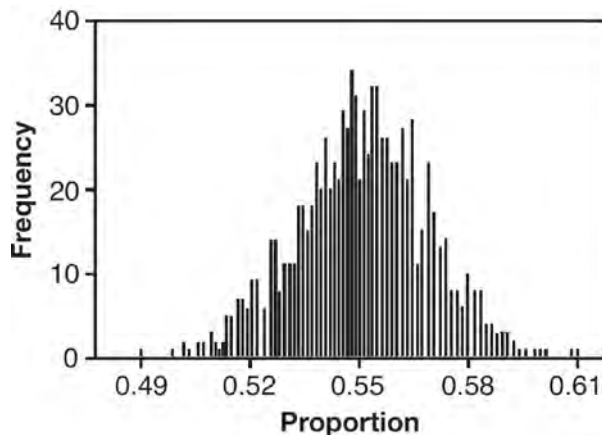
35 A tree farm initially has 150 trees. Each year, 20% of the trees are cut down and 80 seedlings are planted. Which recursive formula models the number of trees,  $a_n$ , after  $n$  years?

- 1)  $a_1 = 150$   
 $a_n = a_{n-1}(0.2) + 80$
- 2)  $a_1 = 150$   
 $a_n = a_{n-1}(0.8) + 80$
- 3)  $a_n = 150(0.2)^n + 80$
- 4)  $a_n = 150(0.8)^n + 80$

36 Expressed in simplest  $a + bi$  form,  $(7 - 3i) + (x - 2i)^2 - (4i + 2x^2)$  is

- 1)  $(3 - x^2) - (4x + 7)i$
- 2)  $(3 + 3x^2) - (4x + 7)i$
- 3)  $(3 - x^2) - 7i$
- 4)  $(3 + 3x^2) - 7i$

- 37 A candidate for political office commissioned a poll. His staff received responses from 900 likely voters and 55% of them said they would vote for the candidate. The staff then conducted a simulation of 1000 more polls of 900 voters, assuming that 55% of voters would vote for their candidate. The output of the simulation is shown in the diagram below.



Given this output, and assuming a 95% confidence level, the margin of error for the poll is closest to

- 1) 0.01
  - 2) 0.03
  - 3) 0.06
  - 4) 0.12
- 38 What is the solution to  $8(2^{x+3}) = 48$ ?
- 1)  $x = \frac{\ln 6}{\ln 2} - 3$
  - 2)  $x = 0$
  - 3)  $x = \frac{\ln 48}{\ln 16} - 3$
  - 4)  $x = \ln 4 - 3$

- 39 The eighth and tenth terms of a sequence are 64 and 100. If the sequence is either arithmetic or geometric, the ninth term can *not* be
- 1) -82
  - 2) -80
  - 3) 80
  - 4) 82

- 40 Which value is *not* contained in the solution of the system shown below?

$$a + 5b - c = -20$$

$$4a - 5b + 4c = 19$$

$$-a - 5b - 5c = 2$$

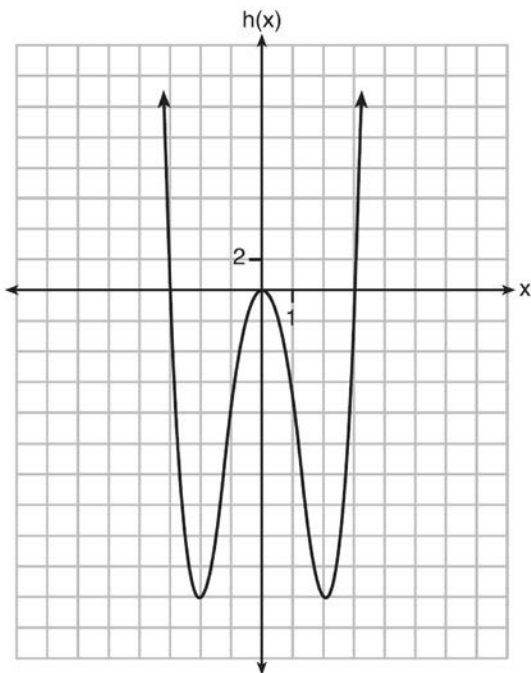
- 1) -2
  - 2) 2
  - 3) 3
  - 4) -3
- 41 For all values of  $x$  for which the expression is defined,  $\frac{x^2 + 3x}{x^2 + 5x + 6}$  is equivalent to
- 1)  $1 - \frac{x}{x+2}$
  - 2)  $\frac{x}{x+2}$
  - 3)  $\frac{3x}{5x+6}$
  - 4)  $1 + \frac{1}{2x+6}$
- 42 The distribution of the diameters of ball bearings made under a given manufacturing process is normally distributed with a mean of 4 cm and a standard deviation of 0.2 cm. What proportion of the ball bearings will have a diameter less than 3.7 cm?
- 1) 0.0668
  - 2) 0.4332
  - 3) 0.8664
  - 4) 0.9500



43 Functions  $f$ ,  $g$ , and  $h$  are given below.

$$f(x) = \sin(2x)$$

$$g(x) = f(x) + 1$$



Which statement is true about functions  $f$ ,  $g$ , and  $h$ ?

- 1)  $f(x)$  and  $g(x)$  are odd,  $h(x)$  is even.
- 2)  $f(x)$  and  $g(x)$  are even,  $h(x)$  is odd.
- 3)  $f(x)$  is odd,  $g(x)$  is neither,  $h(x)$  is even.
- 4)  $f(x)$  is even,  $g(x)$  is neither,  $h(x)$  is odd.

44 The inverse of the function  $f(x) = \frac{x+1}{x-2}$  is

- 1)  $f^{-1}(x) = \frac{x+1}{x+2}$
- 2)  $f^{-1}(x) = \frac{2x+1}{x-1}$
- 3)  $f^{-1}(x) = \frac{x+1}{x-2}$
- 4)  $f^{-1}(x) = \frac{x-1}{x+1}$

45 The expression  $\sqrt[4]{81x^8y^6}$  is equivalent to

- 1)  $3x^2y^{\frac{3}{2}}$
- 2)  $3x^4y^2$
- 3)  $9x^2y^{\frac{3}{2}}$
- 4)  $9x^4y^2$

46 The solutions to the equation  $-\frac{1}{2}x^2 = -6x + 20$  are

- 1)  $-6 \pm 2i$
- 2)  $-6 \pm 2\sqrt{19}$
- 3)  $6 \pm 2i$
- 4)  $6 \pm 2\sqrt{19}$

47 To the *nearest tenth*, the solution to the equation  $4300e^{0.07x} - 123 = 5000$  is

- 1) 1.1
- 2) 2.5
- 3) 6.3
- 4) 68.5

48 Emmeline is working on one side of a polynomial identity proof used to form Pythagorean triples. Her work is shown below:

$$(5x)^2 + (5x^2 - 5)^2$$

Step 1:  $25x^2 + (5x^2 - 5)^2$

Step 2:  $25x^2 + 25x^2 + 25$

Step 3:  $50x^2 + 25$

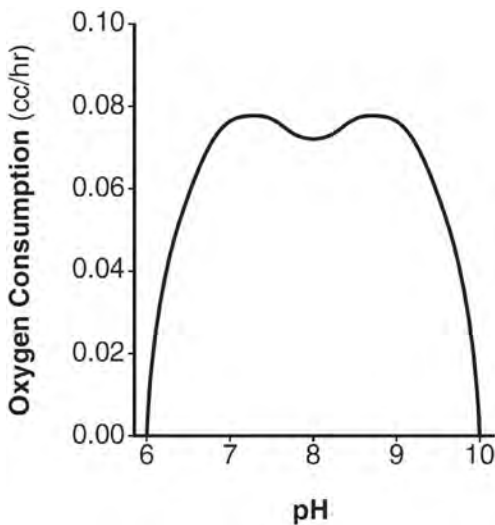
Step 4:  $75x^2$

What statement is true regarding Emmeline's work?

- 1) Emmeline's work is entirely correct.
- 2) There is a mistake in step 2, only.
- 3) There are mistakes in step 2 and step 4.
- 4) There is a mistake in step 4, only.

- 49 According to a study, 45% of Americans have type O blood. If a random number generator produces three-digit values from 000 to 999, which values would represent those having type O blood?
- 1) between 000 and 045, inclusive
  - 2) between 000 and 444, inclusive
  - 3) between 000 and 449, inclusive
  - 4) between 000 and 450, inclusive

- 50 There was a study done on oxygen consumption of snails as a function of pH, and the result was a degree 4 polynomial function whose graph is shown below.



Which statement about this function is *incorrect*?

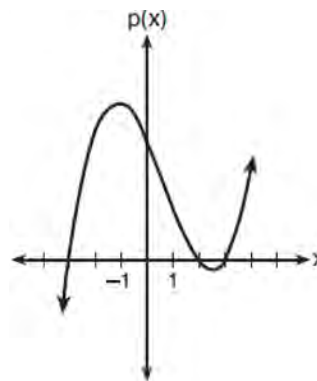
- 1) The degree of the polynomial is even.
- 2) There is a positive leading coefficient.
- 3) At two pH values, there is a relative maximum value.
- 4) There are two intervals where the function is decreasing.

- 51 For the polynomial  $p(x)$ , if  $p(3) = 0$ , it can be concluded that
- 1)  $x + 3$  is a factor of  $p(x)$
  - 2)  $x - 3$  is a factor of  $p(x)$
  - 3) when  $p(x)$  is divided by 3, the remainder is zero
  - 4) when  $p(x)$  is divided by  $-3$ , the remainder is zero

- 52 Chet has \$1200 invested in a bank account modeled by the function  $P(n) = 1200(1.002)^n$ , where  $P(n)$  is the value of his account, in dollars, after  $n$  months. Chet's debt is modeled by the function  $Q(n) = 100n$ , where  $Q(n)$  is the value of debt, in dollars, after  $n$  months. After  $n$  months, which function represents Chet's net worth,  $R(n)$ ?

- 1)  $R(n) = 1200(1.002)^n + 100n$
- 2)  $R(n) = 1200(1.002)^{12n} + 100n$
- 3)  $R(n) = 1200(1.002)^n - 100n$
- 4)  $R(n) = 1200(1.002)^{12n} - 100n$

- 53 The graph of the function  $p(x)$  is sketched below.



Which equation could represent  $p(x)$ ?

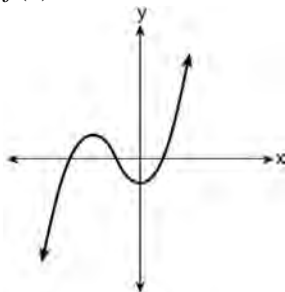
- 1)  $p(x) = (x^2 - 9)(x - 2)$
- 2)  $p(x) = x^3 - 2x^2 + 9x + 18$
- 3)  $p(x) = (x^2 + 9)(x - 2)$
- 4)  $p(x) = x^3 + 2x^2 - 9x - 18$

- 54 Which situation best describes conditional probability?
- 1) finding the probability of an event occurring two or more times
  - 2) finding the probability of an event occurring only once
  - 3) finding the probability of two independent events occurring at the same time
  - 4) finding the probability of an event occurring given another event had already occurred

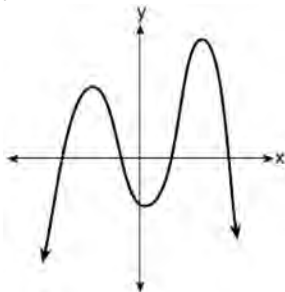
- 55 Which factorization is *incorrect*?
- 1)  $4k^2 - 49 = (2k + 7)(2k - 7)$
  - 2)  $a^3 - 8b^3 = (a - 2b)(a^2 + 2ab + 4b^2)$
  - 3)  $m^3 + 3m^2 - 4m + 12 = (m - 2)^2(m + 3)$
  - 4)  $t^3 + 5t^2 + 6t + t^2 + 5t + 6 = (t + 1)(t + 2)(t + 3)$

- 56 Consider the end behavior description below.
- as  $x \rightarrow -\infty, f(x) \rightarrow \infty$
  - as  $x \rightarrow \infty, f(x) \rightarrow -\infty$
- Which function satisfies the given conditions?

1)  $f(x) = x^4 + 2x^2 + 1$



2)  $f(x) = -x^3 + 2x - 6$



4)

- 57 Mallory wants to buy a new window air conditioning unit. The cost for the unit is \$329.99. If she plans to run the unit three months out of the year for an annual operating cost of \$108.78, which function models the cost per year over the lifetime of the unit,  $C(n)$ , in terms of the number of years,  $n$ , that she owns the air conditioner.
- 1)  $C(n) = 329.99 + 108.78n$
  - 2)  $C(n) = 329.99 + 326.34n$
  - 3)  $C(n) = \frac{329.99 + 108.78n}{n}$
  - 4)  $C(n) = \frac{329.99 + 326.34n}{n}$

- 58 The equation below can be used to model the height of a tide in feet,  $H(t)$ , on a beach at  $t$  hours.

$$H(t) = 4.8 \sin\left(\frac{\pi}{6}(t + 3)\right) + 5.1$$

Using this function, the amplitude of the tide is

- 1)  $\frac{\pi}{6}$
- 2) 4.8
- 3) 3
- 4) 5.1

- 59 A polynomial equation of degree three,  $p(x)$ , is used to model the volume of a rectangular box. The graph of  $p(x)$  has  $x$  intercepts at  $-2$ ,  $10$ , and  $14$ . Which statements regarding  $p(x)$  could be true?
- A. The equation of  $p(x) = (x - 2)(x + 10)(x + 14)$ .
  - B. The equation of  $p(x) = -(x + 2)(x - 10)(x - 14)$ .
  - C. The maximum volume occurs when  $x = 10$ .
  - D. The maximum volume of the box is approximately 56.
- 1) A and C
  - 2) A and D
  - 3) B and C
  - 4) B and D

Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 60 When  $g(x)$  is divided by  $x + 4$ , the remainder is 0. Given  $g(x) = x^4 + 3x^3 - 6x^2 - 6x + 8$ , which conclusion about  $g(x)$  is true?
- 1)  $g(4) = 0$
  - 2)  $g(-4) = 0$
  - 3)  $x - 4$  is a factor of  $g(x)$ .
  - 4) No conclusion can be made regarding  $g(x)$ .
- 61 A study of the annual population of the red-winged blackbird in Ft. Mill, South Carolina, shows the population,  $B(t)$ , can be represented by the function  $B(t) = 750(1.16)^t$ , where the  $t$  represents the number of years since the study began. In terms of the monthly rate of growth, the population of red-winged blackbirds can be best approximated by the function
- 1)  $B(t) = 750(1.012)^t$
  - 2)  $B(t) = 750(1.012)^{12t}$
  - 3)  $B(t) = 750(1.16)^{12t}$
  - 4)  $B(t) = 750(1.16)^{\frac{t}{12}}$
- 62 The probability that Gary and Jane have a child with blue eyes is 0.25, and the probability that they have a child with blond hair is 0.5. The probability that they have a child with both blue eyes and blond hair is 0.125. Given this information, the events blue eyes and blond hair are
- I: dependent
  - II: independent
  - III: mutually exclusive
- 1) I, only
  - 2) II, only
  - 3) I and III
  - 4) II and III
- 63 What is the completely factored form of  $k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$ ?
- 1)  $(k - 2)(k - 2)(k + 3)(k + 4)$
  - 2)  $(k - 2)(k - 2)(k + 6)(k + 2)$
  - 3)  $(k + 2)(k - 2)(k + 3)(k + 4)$
  - 4)  $(k + 2)(k - 2)(k + 6)(k + 2)$
- 64 Which equation represents an odd function?
- 1)  $y = \sin x$
  - 2)  $y = \cos x$
  - 3)  $y = (x + 1)^3$
  - 4)  $y = e^{5x}$
- 65 What is the solution set of the equation  $\frac{4}{k^2 - 8k + 12} = \frac{k}{k - 2} + \frac{1}{k - 6}$ ?
- 1)  $\{-1, 6\}$
  - 2)  $\{1, -6\}$
  - 3)  $\{-1\}$
  - 4)  $\{1\}$
- 66 If  $\sin^2(32^\circ) + \cos^2(M) = 1$ , then  $M$  equals
- 1)  $32^\circ$
  - 2)  $58^\circ$
  - 3)  $68^\circ$
  - 4)  $72^\circ$
- 67 The expression  $\frac{-3x^2 - 5x + 2}{x^3 + 2x^2}$  can be rewritten as
- 1)  $\frac{-3x - 3}{x^2 + 2x}$
  - 2)  $\frac{-3x - 1}{x^2}$
  - 3)  $-3x^{-1} + 1$
  - 4)  $-3x^{-1} + x^{-2}$

Algebra II Multiple Choice Regents Exam Questions

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- 68 The expression  $\frac{6x^3 + 17x^2 + 10x + 2}{2x + 3}$  equals
- 1)  $3x^2 + 4x - 1 + \frac{5}{2x + 3}$
  - 2)  $6x^2 + 8x - 2 + \frac{5}{2x + 3}$
  - 3)  $6x^2 - x + 13 - \frac{37}{2x + 3}$
  - 4)  $3x^2 + 13x + \frac{49}{2} + \frac{151}{2x + 3}$
- 69 Which investigation technique is most often used to determine if a single variable has an impact on a given population?
- 1) observational study
  - 2) random survey
  - 3) controlled experiment
  - 4) formal interview
- 70 In a group of 40 people, 20 have brown hair, 22 have blue eyes, and 15 have both brown hair and blue eyes. How many people have neither brown hair nor blue eyes?
- 1) 0
  - 2) 13
  - 3) 27
  - 4) 32
- 71 The depth of the water,  $d(t)$ , in feet, on a given day at Thunder Bay,  $t$  hours after midnight is modeled by  $d(t) = 5 \sin\left(\frac{\pi}{6}(t - 5)\right) + 7$ . Which statement about the Thunder Bay tide is *false*?
- 1) A low tide occurred at 2 a.m.
  - 2) The maximum depth of the water was 12 feet.
  - 3) The water depth at 9 a.m. was approximately 11 feet.
  - 4) The difference in water depth between high tide and low tide is 14 feet.
- 72 Given  $i$  is the imaginary unit,  $(2 - yi)^2$  in simplest form is
- 1)  $y^2 - 4yi + 4$
  - 2)  $-y^2 - 4yi + 4$
  - 3)  $-y^2 + 4$
  - 4)  $y^2 + 4$
- 73 Given  $p(\theta) = 3 \sin\left(\frac{1}{2}\theta\right)$  on the interval  $-\pi < \theta < \pi$ , the function  $p$
- 1) decreases, then increases
  - 2) increases, then decreases
  - 3) decreases throughout the interval
  - 4) increases throughout the interval
- 74 The function  $f(x) = 2^{-0.25x} \cdot \sin\left(\frac{\pi}{2}x\right)$  represents a damped sound wave function. What is the average rate of change for this function on the interval  $[-7, 7]$ , to the *nearest hundredth*?
- 1) -3.66
  - 2) -0.30
  - 3) -0.26
  - 4) 3.36
- 75 For  $x \neq 0$ , which expressions are equivalent to one divided by the sixth root of  $x$ ?
- I.  $\frac{\sqrt[6]{x}}{\sqrt[3]{x}}$     II.  $\frac{x^{\frac{1}{6}}}{x^{\frac{1}{3}}}$     III.  $x^{\frac{-1}{6}}$
- 1) I and II, only
  - 2) I and III, only
  - 3) II and III, only
  - 4) I, II, and III

Algebra II Multiple Choice Regents Exam Questions

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- 76 The loudness of sound is measured in units called decibels (dB). These units are measured by first assigning an intensity  $I_0$  to a very soft sound that is called the threshold sound. The sound to be measured is assigned an intensity,  $I$ , and the decibel rating,  $d$ , of this sound is found using  $d = 10 \log \frac{I}{I_0}$ . The threshold sound audible to the average person is  $1.0 \times 10^{-12}$  W/m<sup>2</sup> (watts per square meter). Consider the following sound level classifications:

Moderate	45-69 dB
Loud	70-89 dB
Very loud	90-109 dB
Deafening	>110 dB

How would a sound with intensity  $6.3 \times 10^{-3}$  W/m<sup>2</sup> be classified?

- 1) moderate  
2) loud  
3) very loud  
4) deafening
- 77 The inverse of  $f(x) = -6x + \frac{1}{2}$  is
- 1)  $f^{-1}(x) = 6x - \frac{1}{2}$   
2)  $f^{-1}(x) = \frac{1}{-6x + \frac{1}{2}}$   
3)  $f^{-1}(x) = -\frac{1}{6}x + \frac{1}{12}$   
4)  $f^{-1}(x) = -\frac{1}{6}x + 2$
- 78 The solution to the equation  $18x^2 - 24x + 87 = 0$  is
- 1)  $-\frac{2}{3} \pm 6i\sqrt{158}$   
2)  $-\frac{2}{3} \pm \frac{1}{6}i\sqrt{158}$   
3)  $\frac{2}{3} \pm 6i\sqrt{158}$   
4)  $\frac{2}{3} \pm \frac{1}{6}i\sqrt{158}$
- 79 A local university has a current enrollment of 12,000 students. The enrollment is increasing continuously at a rate of 2.5% each year. Which logarithm is equal to the number of years it will take for the population to increase to 15,000 students?
- 1)  $\frac{\ln 1.25}{0.25}$   
2)  $\frac{\ln 3000}{0.025}$   
3)  $\frac{\ln 1.25}{2.5}$   
4)  $\frac{\ln 1.25}{0.025}$
- 80 For which approximate value(s) of  $x$  will  $\log(x + 5) = |x - 1| - 3$ ?
- 1) 5, 1  
2) -2.41, 0.41  
3) -2.41, 5  
4) 5, only

- 81 A recursive formula for the sequence 64, 48, 36, ... is

1)  $a_n = 64(0.75)^{n-1}$

2)  $a_1 = 64$

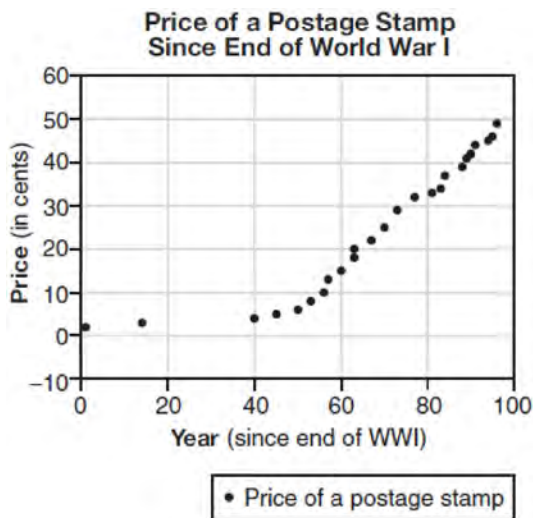
$a_n = a_{n-1} - 16$

3)  $a_n = 64 + (n-1)(-16)$

4)  $a_1 = 64$

$a_n = 0.75a_{n-1}$

- 82 The price of a postage stamp in the years since the end of World War I is shown in the scatterplot below.



The equation that best models the price, in cents, of a postage stamp based on these data is

1)  $y = 0.59x - 14.82$

2)  $y = 1.04(1.43)^x$

3)  $y = 1.43(1.04)^x$

4)  $y = 24 \sin(14x) + 25$

- 83 Which binomial is a factor of  $x^4 - 4x^2 - 4x + 8$ ?

1)  $x - 2$

2)  $x + 2$

3)  $x - 4$

4)  $x + 4$

- 84 Given  $f(x) = 3^{x-1} + 2$ , as  $x \rightarrow -\infty$

1)  $f(x) \rightarrow -1$

2)  $f(x) \rightarrow 0$

3)  $f(x) \rightarrow 2$

4)  $f(x) \rightarrow -\infty$

- 85 If  $f(t) = 50(.5)^{\frac{t}{5715}}$  represents a mass, in grams, of carbon-14 remaining after  $t$  years, which statement(s) must be true?

I. The mass of the carbon-14 is decreasing by half each year.

II. The mass of the original sample is 50 g.

1) I, only

2) II, only

3) I and II

4) neither I nor II

- 86 According to a pricing website, Indroid phones lose 58% of their cash value over 1.5 years. Which expression can be used to estimate the value of a \$300 Indroid phone in 1.5 years?

1)  $300e^{-0.87}$

2)  $300e^{-0.63}$

3)  $300e^{-0.58}$

4)  $300e^{-0.42}$

- 87 Which function represents exponential decay?

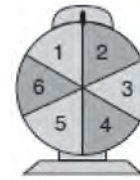
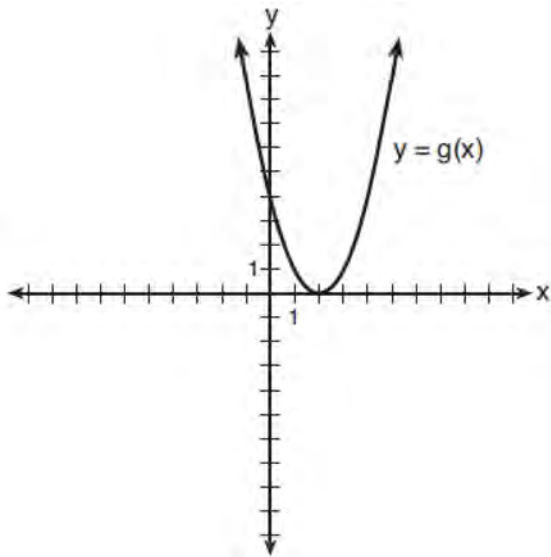
1)  $p(x) = \left(\frac{1}{4}\right)^{-x}$

2)  $q(x) = 1.8^{-x}$

3)  $r(x) = 2.3^{2x}$

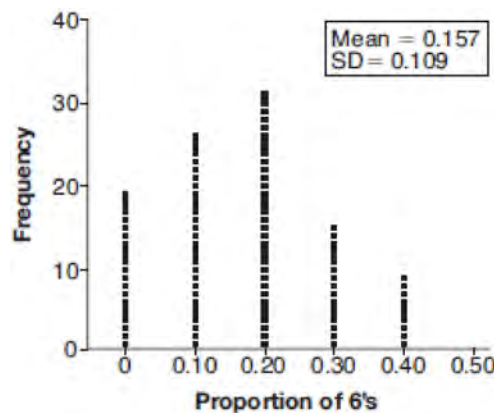
4)  $s(x) = 4^{\frac{x}{2}}$

- 88 What is the solution to the system of equations  $y = 3x - 2$  and  $y = g(x)$  where  $g(x)$  is defined by the function below?



For Miles to win, the spinner must land on the number 6. After spinning the spinner 10 times, and losing all 10 times, Miles complained that the spinner is unfair. At home, his dad ran 100 simulations of spinning the spinner 10 times, assuming the probability of winning each spin is  $\frac{1}{6}$ .

The output of the simulation is shown in the diagram below.



- 1)  $\{(0, -2)\}$
- 2)  $\{(0, -2), (1, 6)\}$
- 3)  $\{(1, 6)\}$
- 4)  $\{(1, 1), (6, 16)\}$

- 89 Last year, the total revenue for Home Style, a national restaurant chain, increased 5.25% over the previous year. If this trend were to continue, which expression could the company's chief financial officer use to approximate their monthly percent increase in revenue? [Let  $m$  represent months.]

- 1)  $(1.0525)^m$
- 2)  $(1.0525)^{\frac{12}{m}}$
- 3)  $(1.00427)^m$
- 4)  $(1.00427)^{\frac{m}{12}}$

- 90 A game spinner is divided into 6 equally sized regions, as shown in the diagram below.

Which explanation is appropriate for Miles and his dad to make?

- 1) The spinner was likely unfair, since the number 6 failed to occur in about 20% of the simulations.
- 2) The spinner was likely unfair, since the spinner should have landed on the number 6 by the sixth spin.
- 3) The spinner was likely not unfair, since the number 6 failed to occur in about 20% of the simulations.
- 4) The spinner was likely not unfair, since in the output the player wins once or twice in the majority of the simulations.



Algebra II Multiple Choice Regents Exam Questions

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91 Consider the function  $f(x) = 2x^3 + x^2 - 18x - 9$ .

Which statement is true?

- 1)  $2x - 1$  is a factor of  $f(x)$ .
- 2)  $x - 3$  is a factor of  $f(x)$ .
- 3)  $f(3) \neq f\left(-\frac{1}{2}\right)$
- 4)  $f\left(\frac{1}{2}\right) = 0$

92 Which expression has been rewritten correctly to form a true statement?

- 1)  $(x + 2)^2 + 2(x + 2) - 8 = (x + 6)x$
- 2)  $x^4 + 4x^2 + 9x^2y^2 - 36y^2 = (x + 3y)^2(x - 2)^2$
- 3)  $x^3 + 3x^2 - 4xy^2 - 12y^2 = (x - 2y)(x + 3)^2$
- 4)  $(x^2 - 4)^2 - 5(x^2 - 4) - 6 = (x^2 - 7)(x^2 - 6)$

93 Consider the system of equations below?

$$\begin{aligned} x + 2y - z &= 1 \\ -x - 3y + 2z &= 0 \\ 2x - 4y + z &= 10 \end{aligned}$$

What is the solution to the given system of equations?

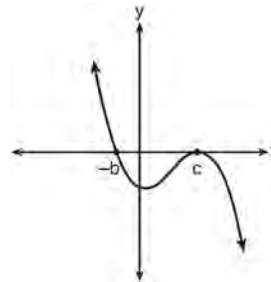
- 1)  $(1, 1, 2)$
- 2)  $(3, -1, 0)$
- 3)  $(5, -1, 2)$
- 4)  $(3, 5, 8)$

94 Which equation represents a parabola with a focus of  $(0, 4)$  and a directrix of  $y = 2$ ?

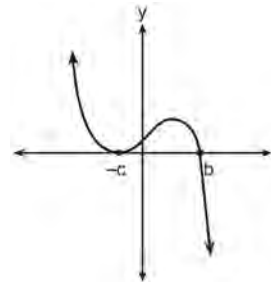
- 1)  $y = x^2 + 3$
- 2)  $y = -x^2 + 1$
- 3)  $y = \frac{x^2}{2} + 3$
- 4)  $y = \frac{x^2}{4} + 3$

95 If  $a$ ,  $b$ , and  $c$  are all positive real numbers, which graph could represent the sketch of the graph of

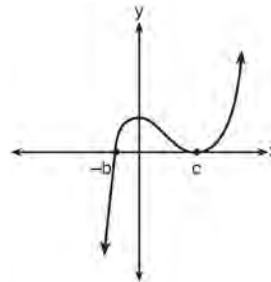
$$p(x) = -a(x + b)(x^2 - 2cx + c^2)?$$



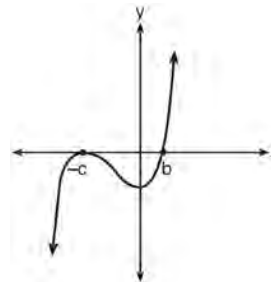
1)



2)



3)



4)

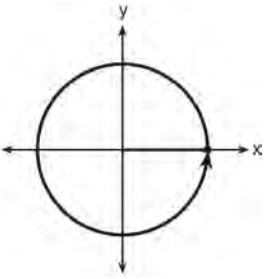
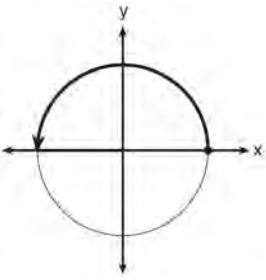
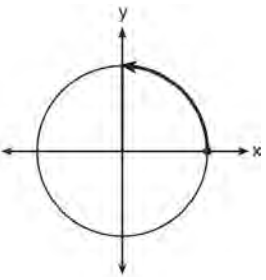
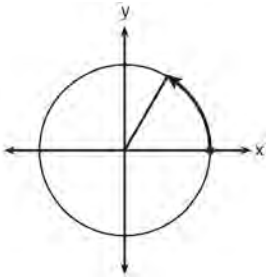
96 Which equation represents a parabola with a focus of  $(4, -3)$  and directrix of  $y = 1$ ?

- 1)  $(x - 1)^2 = 4(y + 3)$
- 2)  $(x - 1)^2 = -8(y - 3)$
- 3)  $(x + 4)^2 = 4(y - 3)$
- 4)  $(x - 4)^2 = -8(y + 1)$

Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 97 Which diagram shows an angle rotation of 1 radian on the unit circle?

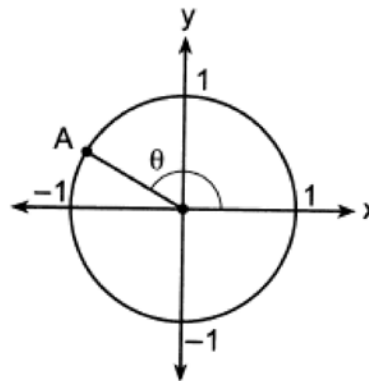


- 98 The function  $N(x) = 90(0.86)^x + 69$  can be used to predict the temperature of a cup of hot chocolate in degrees Fahrenheit after  $x$  minutes. What is the approximate average rate of change of the temperature of the hot chocolate, in degrees per minute, over the interval  $[0, 6]$ ?
- 1)  $-8.93$
  - 2)  $-0.11$
  - 3)  $0.11$
  - 4)  $8.93$

- 99 A student studying public policy created a model for the population of Detroit, where the population decreased 25% over a decade. He used the model  $P = 714(0.75)^d$ , where  $P$  is the population, in thousands,  $d$  decades after 2010. Another student, Suzanne, wants to use a model that would predict the population after  $y$  years. Suzanne's model is best represented by

- 1)  $P = 714(0.6500)^y$
- 2)  $P = 714(0.8500)^y$
- 3)  $P = 714(0.9716)^y$
- 4)  $P = 714(0.9750)^y$

- 100 In the diagram of a unit circle below, point A,  $\left(-\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$ , represents the point where the terminal side of  $\theta$  intersects the unit circle.



What is  $m\angle\theta$ ?

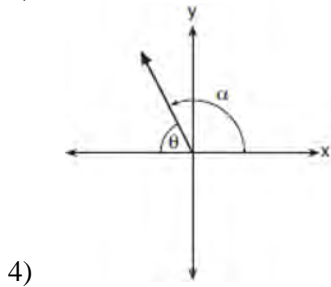
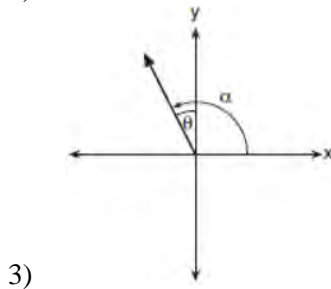
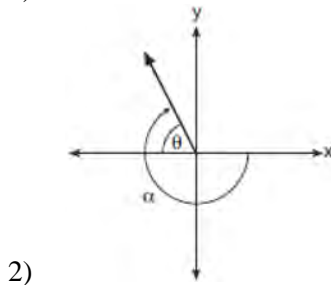
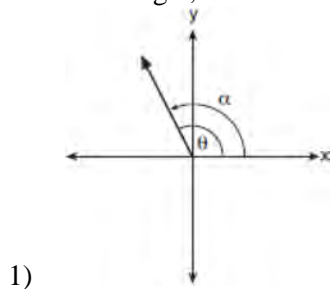
- 1)  $30^\circ$
- 2)  $120^\circ$
- 3)  $135^\circ$
- 4)  $150^\circ$

Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 101 The expression  $(x + a)^2 + 5(x + a) + 4$  is equivalent to
- 1)  $(a + 1)(a + 4)$
  - 2)  $(x + 1)(x + 4)$
  - 3)  $(x + a + 1)(x + a + 4)$
  - 4)  $x^2 + a^2 + 5x + 5a + 4$

- 102 Which diagram represents an angle,  $\alpha$ , measuring  $\frac{13\pi}{20}$  radians drawn in standard position, and its reference angle,  $\theta$ ?



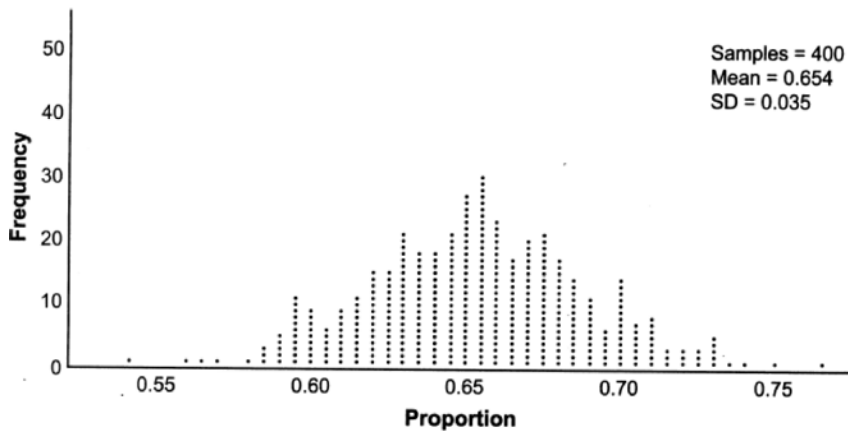
- 103 The solution to the equation  $5e^{x+2} = 7$  is
- 1)  $-2 + \ln\left(\frac{7}{5}\right)$
  - 2)  $\left(\frac{\ln 7}{\ln 5}\right) - 2$
  - 3)  $\frac{-3}{5}$
  - 4)  $-2 + \ln(2)$

- 104 Which statement regarding polynomials and their zeros is true?
- 1)  $f(x) = (x^2 - 1)(x + a)$  has zeros of 1 and  $-a$ , only.
  - 2)  $f(x) = x^3 - ax^2 + 16x - 16a$  has zeros of 4 and  $a$ , only.
  - 3)  $f(x) = (x^2 + 25)(x + a)$  has zeros of  $\pm 5$  and  $-a$ .
  - 4)  $f(x) = x^3 - ax^2 - 9x + 9a$  has zeros of  $\pm 3$  and  $a$ .

- 105 A circle centered at the origin has a radius of 10 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant II at point  $C$ . The  $y$ -coordinate of point  $C$  is 8. What is the value of  $\cos \theta$ ?
- 1)  $-\frac{3}{5}$
  - 2)  $-\frac{3}{4}$
  - 3)  $\frac{3}{5}$
  - 4)  $\frac{4}{5}$

- 106 Which value, to the nearest tenth, is not a solution of  $p(x) = q(x)$  if  $p(x) = x^3 + 3x^2 - 3x - 1$  and  $q(x) = 3x + 8$ ?
- 1)  $-3.9$
  - 2)  $-1.1$
  - 3)  $2.1$
  - 4)  $4.7$

- 107 Betty conducted a survey of her class to see if they like pizza. She gathered 200 responses and 65% of the voters said they did like pizza. Betty then ran a simulation of 400 more surveys, each with 200 responses, assuming that 65% of the voters would like pizza. The output of the simulation is shown below.



Considering the middle 95% of the data, what is the margin of error for the simulation?

- |         |         |
|---------|---------|
| 1) 0.01 | 3) 0.05 |
| 2) 0.02 | 4) 0.07 |
- 108 A company fired several employees in order to save money. The amount of money the company saved per year over five years following the loss of employees is shown in the table below.

Year	Amount Saved (in dollars)
1	59,000
2	64,900
3	71,390
4	78,529
5	86,381.9

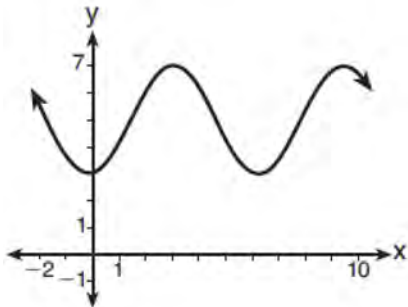
Which expression determines the total amount of money saved by the company over 5 years?

- |   |                                     |
|---|-------------------------------------|
| 1) $\frac{59,000 - 59,000(1.1)^5}{1 - 1.1}$ | 3) $\sum_{n=1}^5 59,000(1.1)^n$     |
| 2) $\frac{59,000 - 59,000(0.1)^5}{1 - 0.1}$ | 4) $\sum_{n=1}^5 59,000(0.1)^{n-1}$ |

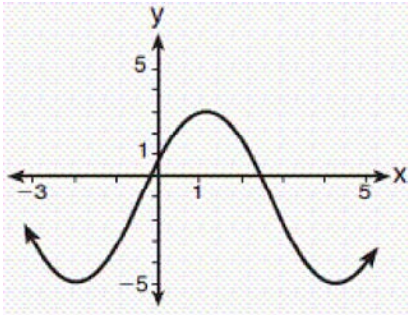
109 An equation to represent the value of a car after  $t$  months of ownership is  $v = 32,000(0.81)^{\frac{t}{12}}$ . Which statement is *not* correct?

- 1) The car lost approximately 19% of its value each month.
- 2) The car maintained approximately 98% of its value each month.
- 3) The value of the car when it was purchased was \$32,000.
- 4) The value of the car 1 year after it was purchased was \$25,920.

110 Which sinusoid has the greatest amplitude?

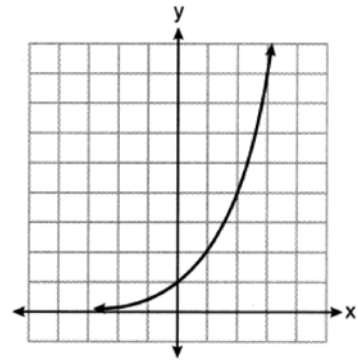


- 1)
- 2)  $y = 3 \sin(\theta - 3) + 5$

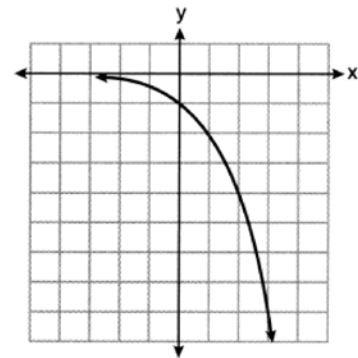


- 3)
- 4)  $y = -5 \sin(\theta - 1) - 3$

111 Consider the function  $y = h(x)$ , defined by the graph below.



Which equation could be used to represent the graph shown below?



- 1)  $y = h(x) - 2$
- 2)  $y = h(x - 2)$
- 3)  $y = -h(x)$
- 4)  $y = h(-x)$

112 Jasmine decides to put \$100 in a savings account each month. The account pays 3% annual interest, compounded monthly. How much money,  $S$ , will Jasmine have after one year?

- 1)  $S = 100(1.03)^{12}$
- 2)  $S = \frac{100 - 100(1.0025)^{12}}{1 - 1.0025}$
- 3)  $S = 100(1.0025)^{12}$
- 4)  $S = \frac{100 - 100(1.03)^{12}}{1 - 1.03}$

113 Which statement regarding the graphs of the functions below is *untrue*?

$$f(x) = 3 \sin 2x, \text{ from } -\pi < x < \pi$$

$$g(x) = (x - 0.5)(x + 4)(x - 2)$$

$$h(x) = \log_2 x$$

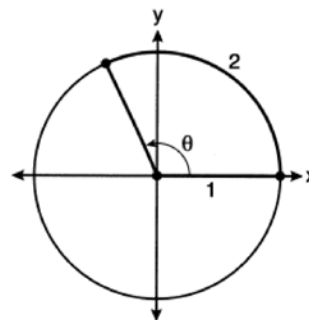
$$j(x) = -|4x - 2| + 3$$

- 1)  $f(x)$  and  $j(x)$  have a maximum  $y$ -value of 3.
- 2)  $f(x)$ ,  $h(x)$ , and  $j(x)$  have one  $y$ -intercept.
- 3)  $g(x)$  and  $j(x)$  have the same end behavior as  $x \rightarrow -\infty$ .
- 4)  $g(x)$ ,  $h(x)$ , and  $j(x)$  have rational zeros.

114 A public opinion poll was conducted on behalf of Mayor Ortega's reelection campaign shortly before the election. 264 out of 550 likely voters said they would vote for Mayor Ortega; the rest said they would vote for his opponent. Which statement is *least* appropriate to make, according to the results of the poll?

- 1) There is a 48% chance that Mayor Ortega will win the election.
- 2) The point estimate ( $\hat{p}$ ) of voters who will vote for Mayor Ortega is 48%.
- 3) It is most likely that between 44% and 52% of voters will vote for Mayor Ortega.
- 4) Due to the margin of error, an inference cannot be made regarding whether Mayor Ortega or his opponent is most likely to win the election.

115 An angle,  $\theta$ , is rotated counterclockwise on the unit circle, with its terminal side in the second quadrant, as shown in the diagram below.



Which value represents the radian measure of angle  $\theta$ ?

- 1) 1
- 2) 2
- 3) 65.4
- 4) 114.6

116 Mr. Farison gave his class the three mathematical rules shown below to either prove or disprove. Which rules can be proved for all real numbers?

I  $(m + p)^2 = m^2 + 2mp + p^2$

II  $(x + y)^3 = x^3 + 3xy + y^3$

III  $(a^2 + b^2)^2 = (a^2 - b^2)^2 + (2ab)^2$

- 1) I, only
- 2) I and II
- 3) II and III
- 4) I and III

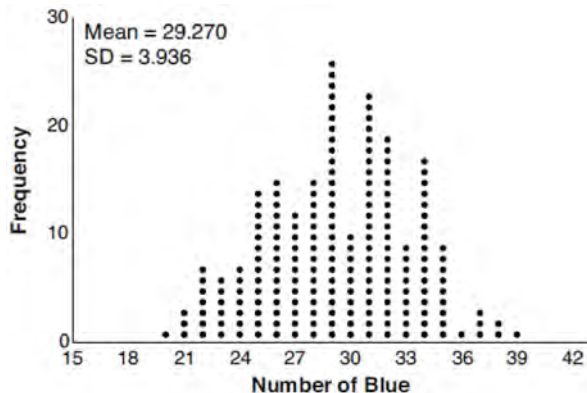
117 Which equation has  $1 - i$  as a solution?

- 1)  $x^2 + 2x - 2 = 0$
- 2)  $x^2 + 2x + 2 = 0$
- 3)  $x^2 - 2x - 2 = 0$
- 4)  $x^2 - 2x + 2 = 0$

Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 118 The J& B candy company claims that 45% of the candies it produces are blue, 30% are brown, and 25% are yellow. Each bag holds 65 candies. A simulation was run 200 times, each of sample size 65, based on the premise that 45% of the candies are blue. The results of the simulation are shown below.



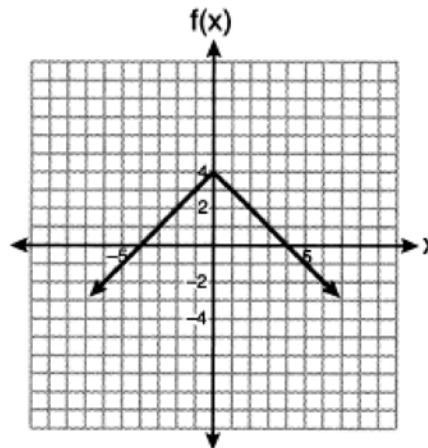
Bonnie purchased a bag of J& B's candy and counted 24 blue candies. What inference can be made regarding a bag of J& B's with only 24 blue candies?

- 1) The company is not meeting their production standard.
  - 2) Bonnie's bag was a rarity and the company should not be concerned.
  - 3) The company should change their claim to 37% blue candies are produced.
  - 4) Bonnie's bag is within the middle 95% of the simulated data supporting the company's claim.
- 119 A function is defined as  $a_n = a_{n-1} + \log_{n+1}(n-1)$ , where  $a_1 = 8$ . What is the value of  $a_3$ ?

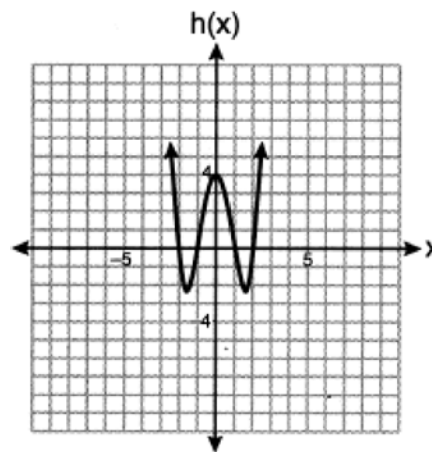
- 1) 8
- 2) 8.5
- 3) 9.2
- 4) 10

- 120 What is the solution set of  $x = \sqrt{3x + 40}$ ?
- 1)  $\{-5, 8\}$
  - 2)  $\{8\}$
  - 3)  $\{-4, 10\}$
  - 4)  $\{ \}$

- 121 Which function has a maximum y-value of 4 and a midline of  $y = 1$ ?



- 1)
- 2)  $g(x) = -3 \cos(x) + 1$



- 3)
- 4)  $j(x) = 4 \sin(x) + 1$

Algebra II Multiple Choice Regents Exam Questions

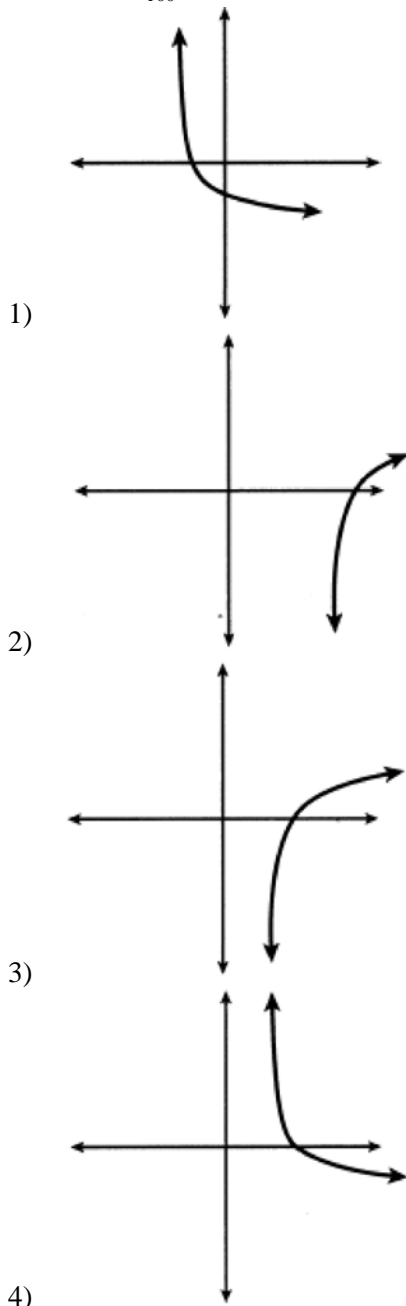
[www.jmap.org](http://www.jmap.org)

- 122 Which scenario is best described as an observational study?
- 1) For a class project, students in Health class ask every tenth student entering the school if they eat breakfast in the morning.
  - 2) A social researcher wants to learn whether or not there is a link between attendance and grades. She gathers data from 15 school districts.
  - 3) A researcher wants to learn whether or not there is a link between children's daily amount of physical activity and their overall energy level. During lunch at the local high school, she distributed a short questionnaire to students in the cafeteria.
  - 4) Sixty seniors taking a course in Advanced Algebra Concepts are randomly divided into two classes. One class uses a graphing calculator all the time, and the other class never uses graphing calculators. A guidance counselor wants to determine whether there is a link between graphing calculator use and students' final exam grades.

- 123 A sine function increasing through the origin can be used to model light waves. Violet light has a wavelength of 400 nanometers. Over which interval is the height of the wave *decreasing*, only?
- 1)  $(0, 200)$
  - 2)  $(100, 300)$
  - 3)  $(200, 400)$
  - 4)  $(300, 400)$

- 124 Given  $f(x) = x^4 - x^3 - 6x^2$ , for what values of  $x$  will  $f(x) > 0$ ?
- 1)  $x < -2$ , only
  - 2)  $x < -2$  or  $x > 3$
  - 3)  $x < -2$  or  $0 \leq x \leq 3$
  - 4)  $x > 3$ , only

- 125 Which sketch could represent the function  $m(x) = -\log_{100}(x - 2)$ ?

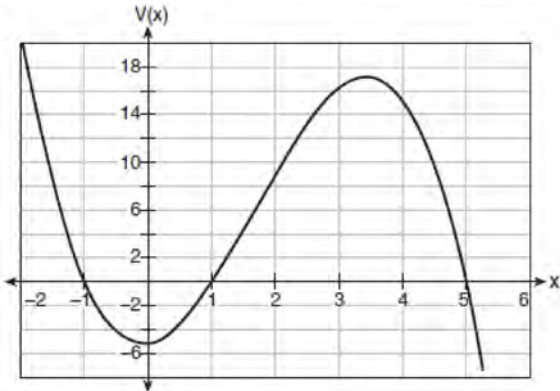




Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 126 A cardboard box manufacturing company is building boxes with length represented by  $x + 1$ , width by  $5 - x$ , and height by  $x - 1$ . The volume of the box is modeled by the function below.



Over which interval is the volume of the box changing at the fastest average rate?

- 1)  $[1, 2]$
  - 2)  $[1, 3.5]$
  - 3)  $[1, 5]$
  - 4)  $[0, 3.5]$
- 127 Consider the system shown below.
- $$2x - y = 4$$
- $$(x + 3)^2 + y^2 = 8$$
- The two solutions of the system can be described as
- 1) both imaginary
  - 2) both irrational
  - 3) both rational
  - 4) one rational and one irrational
- 128 If  $p(x) = ab^x$  and  $r(x) = cd^x$ , then  $p(x) \bullet r(x)$  equals

- 1)  $ac(b + d)^x$
- 2)  $ac(b + d)^{2x}$
- 3)  $ac(bd)^x$
- 4)  $ac(bd)^{x^2}$

- 129 Given  $f^{-1}(x) = -\frac{3}{4}x + 2$ , which equation represents  $f(x)$ ?

- 1)  $f(x) = \frac{4}{3}x - \frac{8}{3}$
- 2)  $f(x) = -\frac{4}{3}x + \frac{8}{3}$
- 3)  $f(x) = \frac{3}{4}x - 2$
- 4)  $f(x) = -\frac{3}{4}x + 2$

- 130 The zeros for  $f(x) = x^4 - 4x^3 - 9x^2 + 36x$  are

- 1)  $\{0, \pm 3, 4\}$
- 2)  $\{0, 3, 4\}$
- 3)  $\{0, \pm 3, -4\}$
- 4)  $\{0, 3, -4\}$

- 131 If a solution of  $2(2x - 1) = 5x^2$  is expressed in simplest  $a + bi$  form, the value of  $b$  is

- 1)  $\frac{\sqrt{6}}{5}i$
- 2)  $\frac{\sqrt{6}}{5}$
- 3)  $\frac{1}{5}i$
- 4)  $\frac{1}{5}$

- 132 The value of an automobile  $t$  years after it was purchased is given by the function

$V = 38,000(0.84)^t$ . Which statement is true?

- 1) The value of the car increases 84% each year.
- 2) The value of the car decreases 84% each year.
- 3) The value of the car increases 16% each year.
- 4) The value of the car decreases 16% each year.

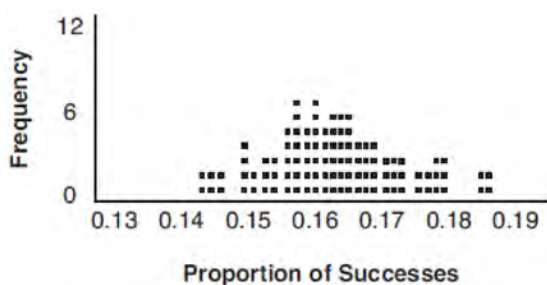
133 If  $\cos A = \frac{\sqrt{5}}{3}$  and  $\tan A < 0$ , what is the value of  $\sin A$ ?

- 1)  $\frac{2}{3}$
- 2)  $-\frac{\sqrt{5}}{3}$
- 3)  $-\frac{2}{3}$
- 4)  $\frac{3}{\sqrt{5}}$

134 Given  $f(9) = -2$ , which function can be used to generate the sequence  $-8, -7.25, -6.5, -5.75, \dots$ ?

- 1)  $f(n) = -8 + 0.75n$
- 2)  $f(n) = -8 - 0.75(n - 1)$
- 3)  $f(n) = -8.75 + 0.75n$
- 4)  $f(n) = -0.75 + 8(n - 1)$

135 A study conducted in 2004 in New York City found that 212 out of 1334 participants had hypertension. Kim ran a simulation of 100 studies based on these data. The output of the simulation is shown in the diagram below.



At a 95% confidence level, the proportion of New York City residents with hypertension and the margin of error are closest to

- 1) proportion  $\approx .16$ ; margin of error  $\approx .01$
- 2) proportion  $\approx .16$ ; margin of error  $\approx .02$
- 3) proportion  $\approx .01$ ; margin of error  $\approx .16$
- 4) proportion  $\approx .02$ ; margin of error  $\approx .16$

136 Cheap and Fast gas station is conducting a consumer satisfaction survey. Which method of collecting data would most likely lead to a biased sample?

- 1) interviewing every 5th customer to come into the station
- 2) interviewing customers chosen at random by a computer at the checkout
- 3) interviewing customers who call an 800 number posted on the customers' receipts
- 4) interviewing every customer who comes into the station on a day of the week chosen at random out of a hat

137 For all positive values of  $x$ , which expression is equivalent to  $x^{\frac{3}{4}}$ ?

- 1)  $\sqrt[4]{x^3}$
- 2)  $\sqrt[3]{x^4}$
- 3)  $(x^3)^4$
- 4)  $3(x^4)$

138 Which binomial is *not* a factor of the expression  $x^3 - 11x^2 + 16x + 84$ ?

- 1)  $x + 2$
- 2)  $x + 4$
- 3)  $x - 6$
- 4)  $x - 7$

139 Which statement below about the graph of  $f(x) = -\log(x + 4) + 2$  is true?

- 1)  $f(x)$  has a y-intercept at  $(0, 2)$ .
- 2)  $-f(x)$  has a y-intercept at  $(0, 2)$ .
- 3) As  $x \rightarrow \infty, f(x) \rightarrow \infty$ .
- 4)  $x \rightarrow -4, f(x) \rightarrow \infty$ .

140 Consider the data in the table below.

	Right Handed	Left Handed
Male	87	13
Female	89	11

What is the probability that a randomly selected person is male given the person is left handed?

- 1)  $\frac{13}{200}$                       3)  $\frac{13}{50}$   
2)  $\frac{13}{100}$                       4)  $\frac{13}{24}$

141 The focal length,  $F$ , of a camera's lens is related to the distance of the object from the lens,  $J$ , and the distance to the image area in the camera,  $W$ , by the formula below.

$$\frac{1}{J} + \frac{1}{W} = \frac{1}{F}$$

When this equation is solved for  $J$  in terms of  $F$  and  $W$ ,  $J$  equals

- 1)  $F - W$   
2)  $\frac{FW}{F - W}$   
3)  $\frac{FW}{W - F}$   
4)  $\frac{1}{F} - \frac{1}{W}$
- 142 Which statement about the graph of  $c(x) = \log_6 x$  is *false*?
- 1) The asymptote has equation  $y = 0$ .  
2) The graph has no  $y$ -intercept.  
3) The domain is the set of positive reals.  
4) The range is the set of all real numbers.

143 Written in simplest form, the fraction  $\frac{x^3 - 9x}{9 - x^2}$ ,

where  $x \neq \pm 3$ , is equivalent to

- 1)  $-x$   
2)  $x$   
3)  $\frac{-x(x+3)}{(3+x)}$   
4)  $\frac{x(x-3)}{(3-x)}$

144 Relative to the graph of  $y = 3 \sin x$ , what is the shift of the graph of  $y = 3 \sin\left(x + \frac{\pi}{3}\right)$ ?

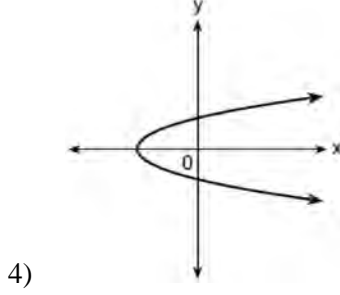
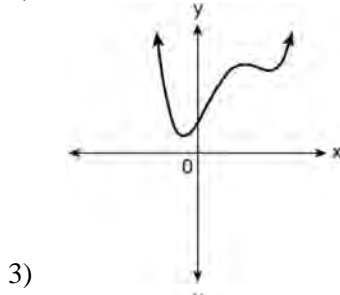
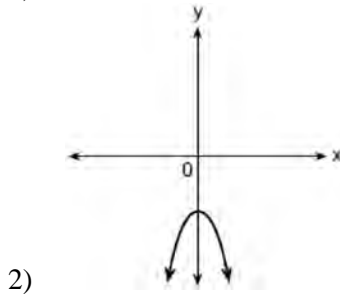
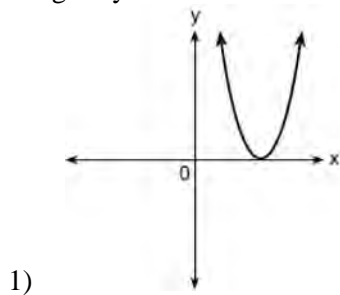
- 1)  $\frac{\pi}{3}$  right  
2)  $\frac{\pi}{3}$  left  
3)  $\frac{\pi}{3}$  up  
4)  $\frac{\pi}{3}$  down

Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 145 For all real values of  $x$ , if  $f(x) = (x - 3)^2$  and  $g(x) = (x + 3)^2$ , what is  $f(x) - g(x)$ ?
- 1)  $-18$
  - 2)  $0$
  - 3)  $-12x$
  - 4)  $2x^2 - 12x - 18$
- 146 The equation  $4x^2 - 24x + 4y^2 + 72y = 76$  is equivalent to
- 1)  $4(x - 3)^2 + 4(y + 9)^2 = 76$
  - 2)  $4(x - 3)^2 + 4(y + 9)^2 = 121$
  - 3)  $4(x - 3)^2 + 4(y + 9)^2 = 166$
  - 4)  $4(x - 3)^2 + 4(y + 9)^2 = 436$
- 147 A rush-hour commuter train has arrived on time 64 of its first 80 days. As arrivals continue, which equation can be used to find  $x$ , the number of consecutive days that the train must arrive on schedule to raise its on-time performance rate to 90%?
- 1)  $\frac{64}{80+x} = \frac{90}{100}$
  - 2)  $\frac{64+x}{80+x} = \frac{90}{100}$
  - 3)  $\frac{64+x}{80} = \frac{90}{100}$
  - 4)  $\frac{x}{80+x} = \frac{90}{100}$
- 148 In 2013, approximately 1.6 million students took the Critical Reading portion of the SAT exam. The mean score, the modal score, and the standard deviation were calculated to be 496, 430, and 115, respectively. Which interval reflects 95% of the Critical Reading scores?
- 1)  $430 \pm 115$
  - 2)  $430 \pm 230$
  - 3)  $496 \pm 115$
  - 4)  $496 \pm 230$
- 149 Which statement about statistical analysis is *false*?
- 1) Experiments can suggest patterns and relationships in data.
  - 2) Experiments can determine cause and effect relationships.
  - 3) Observational studies can determine cause and effect relationships.
  - 4) Observational studies can suggest patterns and relationships in data.
- 150 Given  $f(x) = -\frac{2}{5}x + 4$ , which statement is true of the inverse function  $f^{-1}(x)$ ?
- 1)  $f^{-1}(x)$  is a line with slope  $\frac{5}{2}$ .
  - 2)  $f^{-1}(x)$  is a line with slope  $\frac{2}{5}$ .
  - 3)  $f^{-1}(x)$  passes through the point  $(6, -5)$ .
  - 4)  $f^{-1}(x)$  has a y-intercept at  $(0, -4)$ .
- 151 To solve  $\frac{2x}{x-2} - \frac{11}{x} = \frac{8}{x^2 - 2x}$ , Ren multiplied both sides by the least common denominator. Which statement is true?
- 1) 2 is an extraneous solution.
  - 2)  $\frac{7}{2}$  is an extraneous solution.
  - 3) 0 and 2 are extraneous solutions.
  - 4) This equation does not contain any extraneous solutions.
- 152 If  $f(x) = 2x^4 - x^3 - 16x + 8$ , then  $f\left(\frac{1}{2}\right)$
- 1) equals 0 and  $2x + 1$  is a factor of  $f(x)$
  - 2) equals 0 and  $2x - 1$  is a factor of  $f(x)$
  - 3) does not equal 0 and  $2x + 1$  is not a factor of  $f(x)$
  - 4) does not equal 0 and  $2x - 1$  is a factor of  $f(x)$

- 153 Which graph shows a quadratic function with two imaginary zeros?



- 154 Which equation has roots of  $3 + i$  and  $3 - i$ ?

- 1)  $x^2 - 6x + 10 = 0$
- 2)  $x^2 + 6x - 10 = 0$
- 3)  $x^2 - 10x + 6 = 0$
- 4)  $x^2 + 10x - 6 = 0$

- 155 The lifespan of a 60-watt lightbulb produced by a company is normally distributed with a mean of 1450 hours and a standard deviation of 8.5 hours. If a 60-watt lightbulb produced by this company is selected at random, what is the probability that its lifespan will be between 1440 and 1465 hours?

- 1) 0.3803
- 2) 0.4612
- 3) 0.8415
- 4) 0.9612

- 156 The expression  $\frac{4x^3 + 5x + 10}{2x + 3}$  is equivalent to

- 1)  $2x^2 + 3x - 7 + \frac{31}{2x + 3}$
- 2)  $2x^2 - 3x + 7 - \frac{11}{2x + 3}$
- 3)  $2x^2 + 2.5x + 5 + \frac{15}{2x + 3}$
- 4)  $2x^2 - 2.5x - 5 - \frac{20}{2x + 3}$

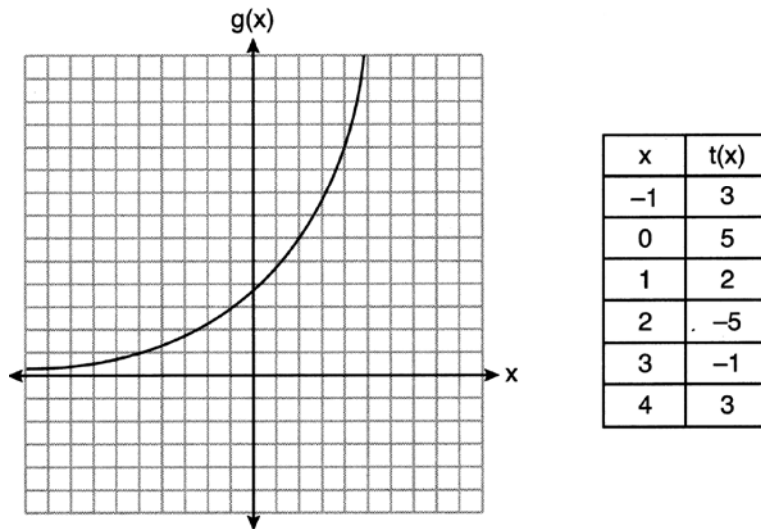
- 157 Given  $x \neq -3$ , the expression  $\frac{2x^3 + 7x^2 - 3x - 25}{x + 3}$  is equivalent to

- 1)  $2x^2 + x - 6 - \frac{7}{x + 3}$
- 2)  $2x^2 + 13x - 36 + \frac{83}{x + 3}$
- 3)  $2x^2 + x - 13$
- 4)  $x^2 + 4x - 15 + \frac{20}{x + 3}$

- 158 To the nearest tenth, the value of  $x$  that satisfies  $2^x = -2x + 11$  is

- 1) 2.5
- 2) 2.6
- 3) 5.8
- 4) 5.9

159 Consider the graph of  $g$  and the table representing  $t$  below.



Over the interval  $[2,4]$ , which statement regarding the average rate of change for  $g$  and  $t$  is true?

- 1)  $g$  has a greater average rate of change.
- 2) The average rates of change are equal.
- 3) The average rate of change for  $g$  is twice the average rate of change for  $t$ .
- 4) The average rate of change for  $g$  is half the average rate of change for  $t$ .

160 Which statement about data collection is most accurate?

- 1) A survey about parenting styles given to every tenth student entering the library will provide unbiased results.
- 2) An observational study allows a researcher to determine the cause of an outcome.
- 3) Margin of error increases as sample size increases.
- 4) A survey collected from a random sample of students in a school can be used to represent the opinions of the school population.

161 The growth of a \$500 investment can be modeled by the function  $P(t) = 500(1.03)^t$ , where  $t$  represents time in years. In terms of the monthly rate of growth, the value of the investment can be best approximated by

- 1)  $P(t) = 500(1.00247)^{12t}$
- 2)  $P(t) = 500(1.00247)^t$
- 3)  $P(t) = 500(1.03)^{12t}$
- 4)  $P(t) = 500(1.03)^{\frac{t}{12}}$

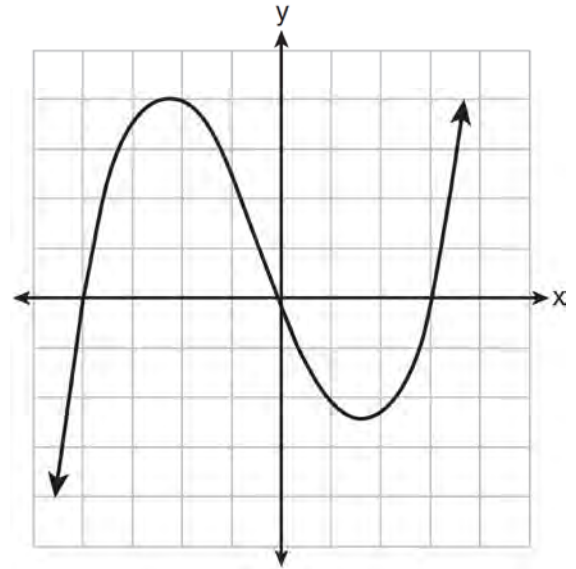
- 162 A parabola has a directrix of  $y = 3$  and a vertex at  $(2, 1)$ . Which ordered pair is the focus of the parabola?
- 1)  $(2, -1)$
  - 2)  $(2, 0)$
  - 3)  $(2, 2)$
  - 4)  $(2, 5)$

- 163 The function  $p(t) = 110e^{0.03922t}$  models the population of a city, in millions,  $t$  years after 2010. As of today, consider the following two statements:
- I. The current population is 110 million.
  - II. The population increases continuously by approximately 3.9% per year.
- This model supports
- 1) I, only
  - 2) II, only
  - 3) both I and II
  - 4) neither I nor II

- 164 As  $x$  increases from 0 to  $\frac{\pi}{2}$ , the graph of the equation  $y = 2 \tan x$  will
- 1) increase from 0 to 2
  - 2) decrease from 0 to  $-2$
  - 3) increase without limit
  - 4) decrease without limit

- 165 What is the solution, if any, of the equation  $\frac{2}{x+3} - \frac{3}{4-x} = \frac{2x-2}{x^2-x-12}$ ?
- 1)  $-1$
  - 2)  $-5$
  - 3) all real numbers
  - 4) no real solution

- 166 The graph of  $p(x)$  is shown below.



What is the remainder when  $p(x)$  is divided by  $x + 4$ ?

- 1)  $x - 4$
  - 2)  $-4$
  - 3)  $0$
  - 4)  $4$
- 167 Mia has a student loan that is in deferment, meaning that she does not need to make payments right now. The balance of her loan account during her deferment can be represented by the function  $f(x) = 35,000(1.0325)^x$ , where  $x$  is the number of years since the deferment began. If the bank decides to calculate her balance showing a monthly growth rate, an approximately equivalent function would be
- 1)  $f(x) = 35,000(1.0027)^{12x}$
  - 2)  $f(x) = 35,000(1.0027)^{\frac{x}{12}}$
  - 3)  $f(x) = 35,000(1.0325)^{12x}$
  - 4)  $f(x) = 35,000(1.0325)^{\frac{x}{12}}$



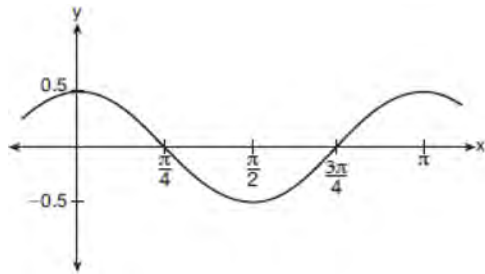


Algebra II Multiple Choice Regents Exam Questions

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- 172 The sequence  $a_1 = 6$ ,  $a_n = 3a_{n-1}$  can also be written as
- 1)  $a_n = 6 \cdot 3^n$
  - 2)  $a_n = 6 \cdot 3^{n+1}$
  - 3)  $a_n = 2 \cdot 3^n$
  - 4)  $a_n = 2 \cdot 3^{n+1}$
- 173 When  $b > 0$  and  $d$  is a positive integer, the expression  $(3b)^{\frac{2}{d}}$  is equivalent to
- 1)  $\frac{1}{\left(\sqrt[d]{3b}\right)^2}$
  - 2)  $\left(\sqrt{3b}\right)^d$
  - 3)  $\frac{1}{\sqrt{3b^d}}$
  - 4)  $\left(\sqrt[d]{3b}\right)^2$
- 174 In watching auditions for lead singer in a band, Liem became curious as to whether there is an association between how animated the leadsinger is and the amount of applause from the audience. He decided to watch each singer and rate the singer on a scale of 1 to 5, where 1 is the least animated and 5 is the most animated. He did this for all 5 nights of auditions and found that the more animated singers did receive louder applause. The study Liem conducted would be best described as
- 1) experimental
  - 2) observational
  - 3) a sample survey
  - 4) a random assignment
- 175 The heights of women in the United States are normally distributed with a mean of 64 inches and a standard deviation of 2.75 inches. The percent of women whose heights are between 64 and 69.5 inches, to the *nearest whole percent*, is
- 1) 6
  - 2) 48
  - 3) 68
  - 4) 95
- 176 Given the parent function  $p(x) = \cos x$ , which phrase best describes the transformation used to obtain the graph of  $g(x) = \cos(x + a) - b$ , if  $a$  and  $b$  are positive constants?
- 1) right  $a$  units, up  $b$  units
  - 2) right  $a$  units, down  $b$  units
  - 3) left  $a$  units, up  $b$  units
  - 4) left  $a$  units, down  $b$  units
- 177 A parabola that has a vertex at  $(2, 1)$  and a focus of  $(2, -3)$  has an equation of
- 1)  $y = \frac{1}{16}(x - 2)^2 + 1$
  - 2)  $y = -\frac{1}{16}(x + 2)^2 - 1$
  - 3)  $y = -\frac{1}{16}(x - 2)^2 + 1$
  - 4)  $y = -\frac{1}{16}(x - 2)^2 - 3$
- 178 How many real solutions exist for the system of equations below?
- $$y = \frac{1}{4}x - 8$$
- $$y = \frac{1}{2}x^2 + 2x$$
- 1) 1
  - 2) 2
  - 3) 3
  - 4) 0

- 179 Which equation is represented by the graph shown below?



- 1)  $y = \frac{1}{2} \cos 2x$
  - 2)  $y = \cos x$
  - 3)  $y = \frac{1}{2} \cos x$
  - 4)  $y = 2 \cos \frac{1}{2}x$
- 180 The amount of a substance,  $A(t)$ , in grams, remaining after  $t$  days is modeled by  $A(t) = 50(0.5)^{\frac{t}{3}}$ . Which statement is false?
- 1) In 20 days, there is no substance remaining.
  - 2) After two half-lives, there is 25% of the substance remaining.
  - 3) The amount of the substance remaining can also be modeled by  $A(t) = 50(2)^{\frac{-t}{3}}$ .
  - 4) After one week, there is less than 10g of the substance remaining.
- 181 If  $(6 - ki)^2 = 27 - 36i$ , the value of  $k$  is
- 1)  $-36$
  - 2)  $-3$
  - 3)  $3$
  - 4)  $6$

- 182 The completely factored form of  $2d^4 + 6d^3 - 18d^2 - 54d$  is

- 1)  $2d(d^2 - 9)(d + 3)$
- 2)  $2d(d^2 + 9)(d + 3)$
- 3)  $2d(d + 3)^2(d - 3)$
- 4)  $2d(d - 3)^2(d + 3)$

- 183 What is the inverse of the function  $y = \log_3 x$ ?

- 1)  $y = x^3$
- 2)  $y = \log_x 3$
- 3)  $y = 3^x$
- 4)  $x = 3^y$

- 184 Given  $x \neq -2$ , the expression  $\frac{2x^2 + 5x + 8}{x + 2}$  is equivalent to

- 1)  $2x^2 + \frac{9}{x + 2}$
- 2)  $2x + \frac{7}{x + 2}$
- 3)  $2x + 1 + \frac{6}{x + 2}$
- 4)  $2x + 9 - \frac{10}{x + 2}$

- 185 The Ferris wheel at the landmark Navy Pier in Chicago takes 7 minutes to make one full rotation. The height,  $H$ , in feet, above the ground of one of the six-person cars can be modeled by

$$H(t) = 70 \sin\left(\frac{2\pi}{7}(t - 1.75)\right) + 80, \text{ where } t \text{ is time,}$$

in minutes. Using  $H(t)$  for one full rotation, this car's minimum height, in feet, is

- 1) 150
- 2) 70
- 3) 10
- 4) 0

Algebra II Multiple Choice Regents Exam Questions

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- 186 As  $\theta$  increases from  $-\frac{\pi}{2}$  to 0 radians, the value of  $\cos \theta$  will
- 1) decrease from 1 to 0
  - 2) decrease from 0 to  $-1$
  - 3) increase from  $-1$  to 0
  - 4) increase from 0 to 1
- 187 If the terminal side of angle  $\theta$ , in standard position, passes through point  $(-4,3)$ , what is the numerical value of  $\sin \theta$ ?
- 1)  $\frac{3}{5}$
  - 2)  $\frac{4}{5}$
  - 3)  $-\frac{3}{5}$
  - 4)  $-\frac{4}{5}$
- 188 A manufacturing company has developed a cost model,  $C(x) = 0.15x^3 + 0.01x^2 + 2x + 120$ , where  $x$  is the number of items sold, in thousands. The sales price can be modeled by  $S(x) = 30 - 0.01x$ . Therefore, revenue is modeled by  $R(x) = x \cdot S(x)$ . The company's profit,  $P(x) = R(x) - C(x)$ , could be modeled by
- 1)  $0.15x^3 + 0.02x^2 - 28x + 120$
  - 2)  $-0.15x^3 - 0.02x^2 + 28x - 120$
  - 3)  $-0.15x^3 + 0.01x^2 - 2.01x - 120$
  - 4)  $-0.15x^3 + 32x + 120$
- 189 The solution set for the equation  $\sqrt{x+14} - \sqrt{2x+5} = 1$  is
- 1)  $\{-6\}$
  - 2)  $\{2\}$
  - 3)  $\{18\}$
  - 4)  $\{2,22\}$
- 190 Which expression is equivalent to  $(x + yi)(x^2 - xyi - y^2)$ , where  $i$  is the imaginary unit?
- 1)  $x^3 + y^3i$
  - 2)  $x^3 - xy^2 - (xy^2 + y^3)i$
  - 3)  $x^3 - 2xy^2 - y^3i$
  - 4)  $x^3 - y^3i$
- 191 Mrs. Favata's statistics class wants to conduct a survey to see how students feel about changing the school mascot's name. Which plan is the best process for gathering an appropriate sample?
- 1) Survey students in a random sample of senior homerooms.
  - 2) Survey every tenth student entering art classes in the school.
  - 3) Survey every fourth student entering the cafeteria during each lunch period.
  - 4) Survey all members of the school's varsity sports teams.
- 192 When  $g(x) = \frac{2}{x+2}$  and  $h(x) = \log(x+1) + 3$  are graphed on the same set of axes, which coordinates best approximate their point of intersection?
- 1)  $(-0.9, 1.8)$
  - 2)  $(-0.9, 1.9)$
  - 3)  $(1.4, 3.3)$
  - 4)  $(1.4, 3.4)$
- 193 A parabola has its focus at  $(1,2)$  and its directrix is  $y = -2$ . The equation of this parabola could be
- 1)  $y = 8(x+1)^2$
  - 2)  $y = \frac{1}{8}(x+1)^2$
  - 3)  $y = 8(x-1)^2$
  - 4)  $y = \frac{1}{8}(x-1)^2$

194 The expression  $\frac{x^2 + 12}{x^2 + 3}$  can be rewritten as

- 1)  $\frac{10}{x^2 + 3}$
- 2)  $1 + \frac{9}{x^2 + 3}$
- 3)  $x + 9$
- 4) 4

195 The expression  $\frac{x^3 + 2x^2 + x + 6}{x + 2}$  is equivalent to

- 1)  $x^2 + 3$
- 2)  $x^2 + 1 + \frac{4}{x + 2}$
- 3)  $2x^2 + x + 6$
- 4)  $2x^2 + 1 + \frac{4}{x + 2}$

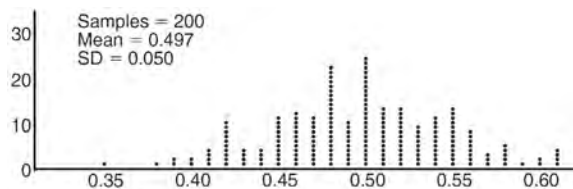
196 Given that  $\sin^2 \theta + \cos^2 \theta = 1$  and  $\sin \theta = -\frac{\sqrt{2}}{5}$ , what is a possible value of  $\cos \theta$ ?

- 1)  $\frac{5 + \sqrt{2}}{5}$
- 2)  $\frac{\sqrt{23}}{5}$
- 3)  $\frac{3\sqrt{3}}{5}$
- 4)  $\frac{\sqrt{35}}{5}$

197 Which equation represents a parabola with the focus at  $(0, -1)$  and the directrix of  $y = 1$ ?

- 1)  $x^2 = -8y$
- 2)  $x^2 = -4y$
- 3)  $x^2 = 8y$
- 4)  $x^2 = 4y$

198 Anne has a coin. She does not know if it is a fair coin. She flipped the coin 100 times and obtained 73 heads and 27 tails. She ran a computer simulation of 200 samples of 100 fair coin flips. The output of the proportion of heads is shown below.



Given the results of her coin flips and of her computer simulation, which statement is most accurate?

- 1) 73 of the computer's next 100 coin flips will be heads.
- 2) 50 of her next 100 coin flips will be heads.
- 3) Her coin is not fair.
- 4) Her coin is fair.

199 Which expression is equivalent to  $(x + 2)^2 - 5(x + 2) + 6$ ?

- 1)  $x(x - 1)$
- 2)  $(x - 3)(x - 2)$
- 3)  $(x - 4)(x + 3)$
- 4)  $(x - 6)(x + 1)$

200 A researcher wants to determine if room-darkening shades cause people to sleep longer. Which method of data collection is most appropriate?

- 1) census
- 2) survey
- 3) observation study
- 4) controlled experiment

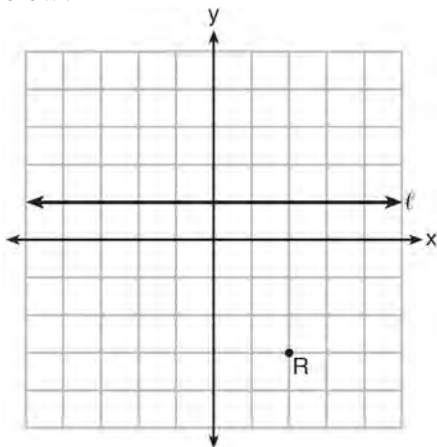
Algebra II Multiple Choice Regents Exam Questions

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201 Which statement is *incorrect* for the graph of the function  $y = -3 \cos \left[ \frac{\pi}{3} (x - 4) \right] + 7$ ?

- 1) The period is 6.
- 2) The amplitude is 3.
- 3) The range is  $[4, 10]$ .
- 4) The midline is  $y = -4$ .

202 Which equation represents the set of points equidistant from line  $\ell$  and point  $R$  shown on the graph below?



- 1)  $y = -\frac{1}{8}(x + 2)^2 + 1$
- 2)  $y = -\frac{1}{8}(x + 2)^2 - 1$
- 3)  $y = -\frac{1}{8}(x - 2)^2 + 1$
- 4)  $y = -\frac{1}{8}(x - 2)^2 - 1$

203 The function  $f(x) = \frac{x - 3}{x^2 + 2x - 8}$  is undefined when

- $x$  equals
- 1) 2 or  $-4$
  - 2) 4 or  $-2$
  - 3) 3, only
  - 4) 2, only

204 Which function represents exponential decay?

- 1)  $y = 2^{0.3t}$
- 2)  $y = 1.2^{3t}$
- 3)  $y = \left(\frac{1}{2}\right)^{-t}$
- 4)  $y = 5^{-t}$

205 A solution of the equation  $2x^2 + 3x + 2 = 0$  is

- 1)  $-\frac{3}{4} + \frac{1}{4}i\sqrt{7}$
- 2)  $-\frac{3}{4} + \frac{1}{4}i$
- 3)  $-\frac{3}{4} + \frac{1}{4}\sqrt{7}$
- 4)  $\frac{1}{2}$

206 Given  $x > 0$ , the expression  $\frac{x^{\frac{1}{5}}}{x^{\frac{1}{2}}}$  can be rewritten as

- 1)  $\sqrt[3]{x}$
- 2)  $-\sqrt[10]{x^3}$
- 3)  $\frac{1}{\sqrt[10]{x^3}}$
- 4)  $\sqrt[3]{x^{10}}$

207 A ball is dropped from a height of 32 feet. It bounces and rebounds 80% of the height from which it was falling. What is the total downward distance, in feet, the ball traveled up to the 12th bounce?

- 1) 29
- 2) 58
- 3) 120
- 4) 149

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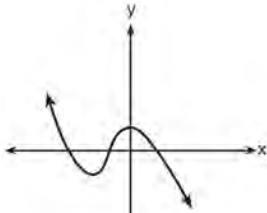
- 208 A recursive formula for the sequence 18,9,4.5,... is
- 1)  $g_1 = 18$   
 $g_n = \frac{1}{2}g_{n-1}$
  - 2)  $g_n = 18\left(\frac{1}{2}\right)^{n-1}$
  - 3)  $g_1 = 18$   
 $g_n = 2g_{n-1}$
  - 4)  $g_n = 18(2)^{n-1}$
- 209 The Rickerts decided to set up an account for their daughter to pay for her college education. The day their daughter was born, they deposited \$1000 in an account that pays 1.8% compounded annually. Beginning with her first birthday, they deposit an additional \$750 into the account on each of her birthdays. Which expression correctly represents the amount of money in the account  $n$  years after their daughter was born?
- 1)  $a_n = 1000(1.018)^n + 750$
  - 2)  $a_n = 1000(1.018)^n + 750n$
  - 3)  $a_0 = 1000$   
 $a_n = a_{n-1}(1.018) + 750$
  - 4)  $a_0 = 1000$   
 $a_n = a_{n-1}(1.018) + 750n$
- 210 Consider the following patterns:
- I. 16, -12, 9, -6.75, ...
  - II. 1, 4, 9, 16, ...
  - III. 6, 18, 30, 42, ...
  - IV.  $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \dots$
- Which pattern is geometric?
- 1) I
  - 2) II
  - 3) III
  - 4) IV
- 211 Sally's high school is planning their spring musical. The revenue,  $R$ , generated can be determined by the function  $R(t) = -33t^2 + 360t$ , where  $t$  represents the price of a ticket. The production cost,  $C$ , of the musical is represented by the function  $C(t) = 700 + 5t$ . What is the highest ticket price, to the nearest dollar, they can charge in order to *not* lose money on the event?
- 1)  $t = 3$
  - 2)  $t = 5$
  - 3)  $t = 8$
  - 4)  $t = 11$
- 212 The heights of the 3300 students at Oceanview High School are approximately normally distributed with a mean of 65.5 inches and a standard deviation of 2.9 inches. The number of students at Oceanview who are between 64 and 68 inches tall is closest to
- 1) 1660
  - 2) 1070
  - 3) 2244
  - 4) 1640
- 213 If  $f(x) = 3|x| - 1$  and  $g(x) = 0.03x^3 - x + 1$ , an approximate solution for the equation  $f(x) = g(x)$  is
- 1) 1.96
  - 2) 11.29
  - 3) (-0.99, 1.96)
  - 4) (11.29, 32.87)
- 214 Which expression is equivalent to  $(3k - 2i)^2$ , where  $i$  is the imaginary unit?
- 1)  $9k^2 - 4$
  - 2)  $9k^2 + 4$
  - 3)  $9k^2 - 12ki - 4$
  - 4)  $9k^2 - 12ki + 4$

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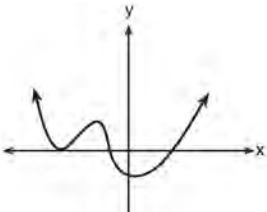
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215 Which graph has the following characteristics?

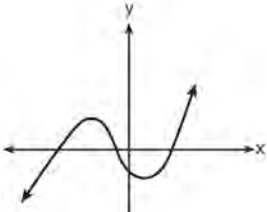
- three real zeros
- as  $x \rightarrow -\infty$ ,  $f(x) \rightarrow -\infty$
- as  $x \rightarrow \infty$ ,  $f(x) \rightarrow \infty$



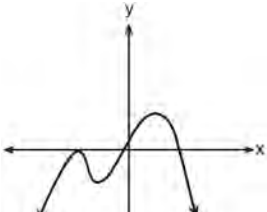
1)



2)



3)



4)

216 The solution to the equation  $4x^2 + 98 = 0$  is

- 1)  $\pm 7$
- 2)  $\pm 7i$
- 3)  $\pm \frac{7\sqrt{2}}{2}$
- 4)  $\pm \frac{7i\sqrt{2}}{2}$

217 What is the solution set of the equation

$$\frac{3x+25}{x+7} - 5 = \frac{3}{x}?$$

- 1)  $\left\{\frac{3}{2}, 7\right\}$
- 2)  $\left\{\frac{7}{2}, -3\right\}$
- 3)  $\left\{-\frac{3}{2}, 7\right\}$
- 4)  $\left\{-\frac{7}{2}, -3\right\}$

218 What is the total number of points of intersection of the graphs of the equations  $y = e^x$  and  $xy = 20$ ?

- 1) 1
- 2) 2
- 3) 3
- 4) 0

219 What does  $\left(\frac{-54x^9}{y^4}\right)^{\frac{2}{3}}$  equal?

- 1)  $\frac{9ix^6\sqrt[3]{4}}{y^2\sqrt[3]{y^2}}$
- 2)  $\frac{9ix^6\sqrt[3]{4}}{y^2\sqrt[3]{y^2}}$
- 3)  $\frac{9x^6\sqrt[3]{4}}{y^2\sqrt[3]{y}}$
- 4)  $\frac{9x^6\sqrt[3]{4}}{y^2\sqrt[3]{y^2}}$

Algebra II Multiple Choice Regents Exam Questions

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- 220 Joelle has a credit card that has a 19.2% annual interest rate compounded monthly. She owes a total balance of  $B$  dollars after  $m$  months. Assuming she makes no payments on her account, the table below illustrates the balance she owes after  $m$  months.

<b>m</b>	<b>B</b>
0	100.00
10	1172.00
19	1352.00
36	1770.80
60	2591.90
69	2990.00
72	3135.80
73	3186.00

Over which interval of time is her average rate of change for the balance on her credit card account the greatest?

- 1) month 10 to month 60  
 2) month 19 to month 69  
 3) month 36 to month 72  
 4) month 60 to month 73
- 221 Which value, to the *nearest tenth*, is the *smallest* solution of  $f(x) = g(x)$  if  $f(x) = 3 \sin\left(\frac{1}{2}x\right) - 1$  and  $g(x) = x^3 - 2x + 1$ ?
- 1) -3.6  
 2) -2.1  
 3) -1.8  
 4) 1.4
- 222 The value of a new car depreciates over time. Greg purchased a new car in June 2011. The value,  $V$ , of his car after  $t$  years can be modeled by the equation  $\log_{0.8}\left(\frac{V}{17000}\right) = t$ . What is the average decreasing rate of change per year of the value of the car from June 2012 to June 2014, to the *nearest ten dollars per year*?
- 1) 1960  
 2) 2180  
 3) 2450  
 4) 2770
- 223 The expression  $\left(\frac{m^2}{m^{\frac{1}{3}}}\right)^{\frac{1}{2}}$  is equivalent to
- 1)  $-\sqrt[6]{m^5}$   
 2)  $\frac{1}{\sqrt[6]{m^5}}$   
 3)  $-m^5\sqrt{m}$   
 4)  $\frac{1}{m^5\sqrt{m}}$
- 224 If  $g(c) = 1 - c^2$  and  $m(c) = c + 1$ , then which statement is *not* true?
- 1)  $g(c) \cdot m(c) = 1 + c - c^2 - c^3$   
 2)  $g(c) + m(c) = 2 + c - c^2$   
 3)  $m(c) - g(c) = c + c^2$   
 4)  $\frac{m(c)}{g(c)} = \frac{-1}{1 - c}$



**Algebra II Multiple Choice Regents Exam Questions**

- 225 Jake wants to buy a car and hopes to save at least \$5000 for a down payment. The table below summarizes the amount of money he plans to save each week.

<b>Week</b>	1	2	3	4	5
<b>Money Saved, in Dollars</b>	2	5	12.5	31.25	...

Based on this plan, which expression should he use to determine how much he has saved in  $n$  weeks?

- 1)  $\frac{2 - 2(2.5^n)}{1 - 2.5}$
- 2)  $\frac{2 - 2(2.5^{n-1})}{1 - 2.5}$
- 3)  $\frac{1 - 2.5^n}{1 - 2.5}$
- 4)  $\frac{1 - 2.5^{n-1}}{1 - 2.5}$
- 226 Given  $f(x) = \frac{1}{2}x + 8$ , which equation represents the inverse,  $g(x)$ ?
- 1)  $g(x) = 2x - 8$
- 2)  $g(x) = 2x - 16$
- 3)  $g(x) = -\frac{1}{2}x + 8$
- 4)  $g(x) = -\frac{1}{2}x - 16$
- 227 A manufacturing plant produces two different-sized containers of peanuts. One container weighs  $x$  ounces and the other weighs  $y$  pounds. If a gift set can hold one of each size container, which expression represents the number of gift sets needed to hold 124 ounces?
- 1)  $\frac{124}{16x + y}$
- 2)  $\frac{x + 16y}{124}$
- 3)  $\frac{124}{x + 16y}$
- 4)  $\frac{16x + y}{124}$
- 228 At her job, Pat earns \$25,000 the first year and receives a raise of \$1000 each year. The explicit formula for the  $n$ th term of this sequence is  $a_n = 25,000 + (n - 1)1000$ . Which rule best represents the equivalent recursive formula?
- 1)  $a_n = 24,000 + 1000n$
- 2)  $a_n = 25,000 + 1000n$
- 3)  $a_1 = 25,000, a_n = a_{n-1} + 1000$
- 4)  $a_1 = 25,000, a_n = a_{n+1} + 1000$
- 229 A researcher randomly divides 50 bean plants into two groups. He puts one group by a window to receive natural light and the second group under artificial light. He records the growth of the plants weekly. Which data collection method is described in this situation?
- 1) observational study
- 2) controlled experiment
- 3) survey
- 4) systematic sample

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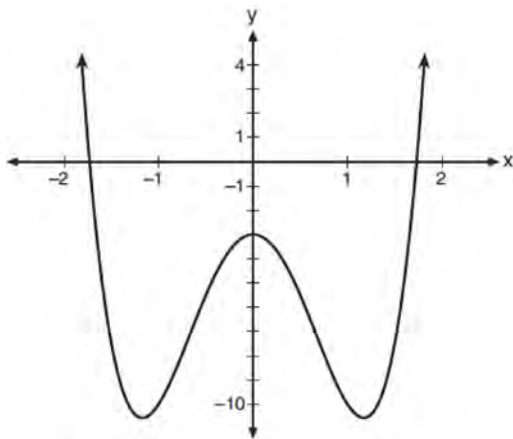
- 230 The operator of the local mall wants to find out how many of the mall's employees make purchases in the food court when they are working. She hopes to use these data to increase the rent and attract new food vendors. In total, there are 1023 employees who work at the mall. The best method to obtain a random sample of the employees would be to survey
- 1) all 170 employees at each of the larger stores
  - 2) 50% of the 90 employees of the food court
  - 3) every employee
  - 4) every 30th employee entering each mall entrance for one week
- 231 Tides are a periodic rise and fall of ocean water. On a typical day at a seaport, to predict the time of the next high tide, the most important value to have would be the
- 1) time between consecutive low tides
  - 2) time when the tide height is 20 feet
  - 3) average depth of water over a 24-hour period
  - 4) difference between the water heights at low and high tide
- 232 The profit function,  $p(x)$ , for a company is the cost function,  $c(x)$ , subtracted from the revenue function,  $r(x)$ . The profit function for the Acme Corporation is  $p(x) = -0.5x^2 + 250x - 300$  and the revenue function is  $r(x) = -0.3x^2 + 150x$ . The cost function for the Acme Corporation is
- 1)  $c(x) = 0.2x^2 - 100x + 300$
  - 2)  $c(x) = 0.2x^2 + 100x + 300$
  - 3)  $c(x) = -0.2x^2 + 100x - 300$
  - 4)  $c(x) = -0.8x^2 + 400x - 300$
- 233 If  $\cos \theta = -\frac{3}{4}$  and  $\theta$  is in Quadrant III, then  $\sin \theta$  is equivalent to
- 1)  $-\frac{\sqrt{7}}{4}$
  - 2)  $\frac{\sqrt{7}}{4}$
  - 3)  $-\frac{5}{4}$
  - 4)  $\frac{5}{4}$
- 234 For  $x > 0$ , which expression is equivalent to  $\frac{\sqrt[3]{x^2} \cdot \sqrt{x^5}}{\sqrt[6]{x}}$ ?
- 1)  $x$
  - 2)  $x^{\frac{3}{2}}$
  - 3)  $x^3$
  - 4)  $x^{10}$
- 235 The first term of a geometric sequence is 8 and the fourth term is 216. What is the sum of the first 12 terms of the corresponding series?
- 1) 236,192
  - 2) 708,584
  - 3) 2,125,760
  - 4) 6,377,288
- 236 The parabola described by the equation  $y = \frac{1}{12}(x - 2)^2 + 2$  has the directrix at  $y = -1$ . The focus of the parabola is
- 1) (2, -1)
  - 2) (2, 2)
  - 3) (2, 3)
  - 4) (2, 5)

Algebra II Multiple Choice Regents Exam Questions

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- 237 If  $(a^3 + 27) = (a + 3)(a^2 + ma + 9)$ , then  $m$  equals
- 1) -9
  - 2) -3
  - 3) 3
  - 4) 6
- 238 The equation  $t = \frac{1}{0.0105} \ln\left(\frac{A}{5000}\right)$  relates time,  $t$ , in years, to the amount of money,  $A$ , earned by a \$5000 investment. Which statement accurately describes the relationship between the average rates of change of  $t$  on the intervals [6000, 8000] and [9000, 12,000]?
- 1) A comparison cannot be made because the intervals are different sizes.
  - 2) The average rate of change is equal for both intervals.
  - 3) The average rate of change is larger for the interval [6000, 8000].
  - 4) The average rate of change is larger for the interval [9000, 12,000].
- 239 Consider the probability statements regarding events  $A$  and  $B$  below.
- $$P(A \text{ or } B) = 0.3;$$
- $$P(A \text{ and } B) = 0.2; \text{ and}$$
- $$P(A|B) = 0.8$$
- What is  $P(B)$ ?
- 1) 0.1
  - 2) 0.25
  - 3) 0.375
  - 4) 0.667
- 240 If  $x - 1$  is a factor of  $x^3 - kx^2 + 2x$ , what is the value of  $k$ ?
- 1) 0
  - 2) 2
  - 3) 3
  - 4) -3
- 241 Suppose two sets of test scores have the same mean, but different standard deviations,  $\sigma_1$  and  $\sigma_2$ , with  $\sigma_2 > \sigma_1$ . Which statement best describes the variability of these data sets?
- 1) Data set one has the greater variability.
  - 2) Data set two has the greater variability.
  - 3) The variability will be the same for each data set.
  - 4) No conclusion can be made regarding the variability of either set.
- 242 What is the solution set of the equation  $\frac{2}{3x+1} = \frac{1}{x} - \frac{6x}{3x+1}$ ?
- 1)  $\left\{-\frac{1}{3}, \frac{1}{2}\right\}$
  - 2)  $\left\{-\frac{1}{3}\right\}$
  - 3)  $\left\{\frac{1}{2}\right\}$
  - 4)  $\left\{\frac{1}{3}, -2\right\}$
- 243 Which equation represents a parabola with a focus of  $(-2, 5)$  and a directrix of  $y = 9$ ?
- 1)  $(y - 7)^2 = 8(x + 2)$
  - 2)  $(y - 7)^2 = -8(x + 2)$
  - 3)  $(x + 2)^2 = 8(y - 7)$
  - 4)  $(x + 2)^2 = -8(y - 7)$
- 244 If the function  $g(x) = ab^x$  represents exponential growth, which statement about  $g(x)$  is *false*?
- 1)  $a > 0$  and  $b > 1$
  - 2) The  $y$ -intercept is  $(0, a)$ .
  - 3) The asymptote is  $y = 0$ .
  - 4) The  $x$ -intercept is  $(b, 0)$ .

- 245 Consider the function  $p(x) = 3x^3 + x^2 - 5x$  and the graph of  $y = m(x)$  below.



Which statement is true?

- 1)  $p(x)$  has three real roots and  $m(x)$  has two real roots.
  - 2)  $p(x)$  has one real root and  $m(x)$  has two real roots.
  - 3)  $p(x)$  has two real roots and  $m(x)$  has three real roots.
  - 4)  $p(x)$  has three real roots and  $m(x)$  has four real roots.
- 246 Given the following polynomials

$$x = (a + b + c)^2$$

$$y = a^2 + b^2 + c^2$$

$$z = ab + bc + ac$$

Which identity is true?

- 1)  $x = y - z$
- 2)  $x = y + z$
- 3)  $x = y - 2z$
- 4)  $x = y + 2z$

- 247 If  $f(x) = \log_3 x$  and  $g(x)$  is the image of  $f(x)$  after a translation five units to the left, which equation represents  $g(x)$ ?

- 1)  $g(x) = \log_3(x + 5)$
- 2)  $g(x) = \log_3 x + 5$
- 3)  $g(x) = \log_3(x - 5)$
- 4)  $g(x) = \log_3 x - 5$

- 248 A random sample of 100 people that would best estimate the proportion of all registered voters in a district who support improvements to the high school football field should be drawn from registered voters in the district at a

- 1) football game
- 2) supermarket
- 3) school fund-raiser
- 4) high school band concert

- 249 Savannah just got contact lenses. Her doctor said she can wear them 2 hours the first day, and can then increase the length of time by 30 minutes each day. If this pattern continues, which formula would *not* be appropriate to determine the length of time, in either minutes or hours, she could wear her contact lenses on the  $n$ th day?

- 1)  $a_1 = 120$   
 $a_n = a_{n-1} + 30$
- 2)  $a_n = 90 + 30n$
- 3)  $a_1 = 2$   
 $a_n = a_{n-1} + 0.5$
- 4)  $a_n = 2.5 + 0.5n$

- 250 The expression  $6 - (3x - 2i)^2$  is equivalent to

- 1)  $-9x^2 + 12xi + 10$
- 2)  $9x^2 - 12xi + 2$
- 3)  $-9x^2 + 10$
- 4)  $-9x^2 + 12xi - 4i + 6$

Algebra II Multiple Choice Regents Exam Questions

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251 Which table best represents an exponential relationship?

1) 

x	y
1	8
2	4
3	2
4	1
5	$\frac{1}{2}$

2) 

x	y
8	0
4	1
0	2
-4	3
-8	4

3) 

x	y
0	0
1	1
2	4
3	9
4	16

4) 

x	y
1	1
2	8
3	27
4	64
5	125

252 There are 400 students in the senior class at Oak Creek High School. All of these students took the SAT. The distribution of their SAT scores is approximately normal. The number of students who scored within 2 standard deviations of the mean is approximately

- 1) 75
- 2) 95
- 3) 300
- 4) 380

253 If  $n = \sqrt{a^5}$  and  $m = a$ , where  $a > 0$ , an expression for  $\frac{n}{m}$  could be

- 1)  $a^{\frac{5}{2}}$
- 2)  $a^4$
- 3)  $\sqrt[3]{a^2}$
- 4)  $\sqrt{a^3}$

254 A savings account,  $S$ , has an initial value of \$50. The account grows at a 2% interest rate compounded  $n$  times per year,  $t$ , according to the function below.

$$S(t) = 50 \left( 1 + \frac{.02}{n} \right)^{nt}$$

Which statement about the account is correct?

- 1) As the value of  $n$  increases, the amount of interest per year decreases.
- 2) As the value of  $n$  increases, the value of the account approaches the function  $S(t) = 50e^{0.02t}$ .
- 3) As the value of  $n$  decreases to one, the amount of interest per year increases.
- 4) As the value of  $n$  decreases to one, the value of the account approaches the function  $S(t) = 50(1 - 0.02)^t$ .

255 A study of black bears in the Adirondacks reveals that their population can be represented by the function  $P(t) = 3500(1.025)^t$ , where  $t$  is the number of years since the study began. Which function is correctly rewritten to reveal the monthly growth rate of the black bear population?

- 1)  $P(t) = 3500(1.00206)^{12t}$
- 2)  $P(t) = 3500(1.00206)^{\frac{t}{12}}$
- 3)  $P(t) = 3500(1.34489)^{12t}$
- 4)  $P(t) = 3500(1.34489)^{\frac{t}{12}}$

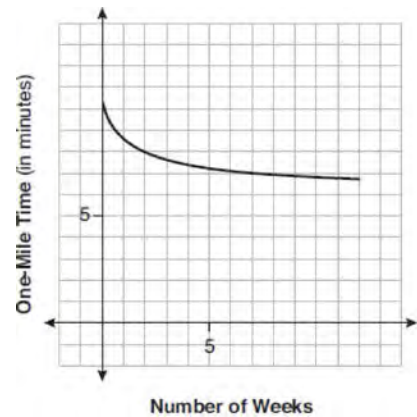
256 Susan won \$2,000 and invested it into an account with an annual interest rate of 3.2%. If her investment were compounded monthly, which expression best represents the value of her investment after  $t$  years?

- 1)  $2000(1.003)^{12t}$
- 2)  $2000(1.032)^{\frac{t}{12}}$
- 3)  $2064^{\frac{t}{12}}$
- 4)  $\frac{2000(1.032)^t}{12}$

257 Stephanie found that the number of white-winged cross bills in an area can be represented by the formula  $C = 550(1.08)^t$ , where  $t$  represents the number of years since 2010. Which equation correctly represents the number of white-winged cross bills in terms of the monthly rate of population growth?

- 1)  $C = 550(1.00643)^t$
- 2)  $C = 550(1.00643)^{12t}$
- 3)  $C = 550(1.00643)^{\frac{t}{12}}$
- 4)  $C = 550(1.00643)^{t+12}$

258 Irma initially ran one mile in over ten minutes. She then began a training program to reduce her one-mile time. She recorded her one-mile time once a week for twelve consecutive weeks, as modeled in the graph below.



Which statement regarding Irma's one-mile training program is correct?

- 1) Her one-mile speed increased as the number of weeks increased.
- 2) Her one-mile speed decreased as the number of weeks increased.
- 3) If the trend continues, she will run under a six-minute mile by week thirteen.
- 4) She reduced her one-mile time the most between weeks ten and twelve.

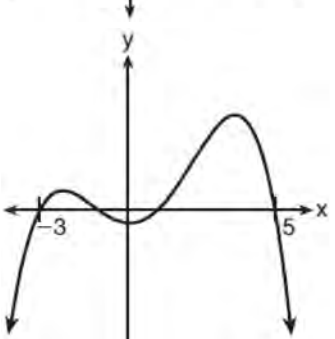
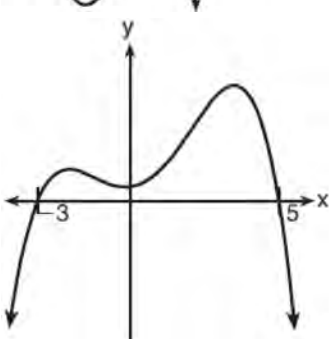
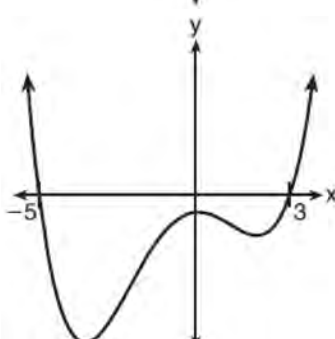
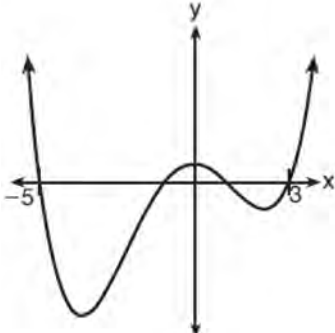
259 Brian deposited 1 cent into an empty non-interest bearing bank account on the first day of the month. He then additionally deposited 3 cents on the second day, 9 cents on the third day, and 27 cents on the fourth day. What would be the total amount of money in the account at the end of the 20th day if the pattern continued?

- 1) \$11,622,614.67
- 2) \$17,433,922.00
- 3) \$116,226,146.80
- 4) \$1,743,392,200.00

Algebra II Multiple Choice Regents Exam Questions

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- 260 A 4th degree polynomial has zeros  $-5$ ,  $3$ ,  $i$ , and  $-i$ . Which graph could represent the function defined by this polynomial?



- 261 The expression  $2 - \frac{x-1}{x+2}$  is equivalent to

- 1)  $1 - \frac{3}{x+2}$
- 2)  $1 + \frac{3}{x+2}$
- 3)  $1 - \frac{1}{x+2}$
- 4)  $1 + \frac{1}{x+2}$

- 262 Kelly-Ann has \$20,000 to invest. She puts half of the money into an account that grows at an annual rate of 0.9% compounded monthly. At the same time, she puts the other half of the money into an account that grows continuously at an annual rate of 0.8%. Which function represents the value of Kelly-Ann's investments after  $t$  years?

- 1)  $f(t) = 10,000(1.9)^t + 10,000e^{0.8t}$
- 2)  $f(t) = 10,000(1.009)^t + 10,000e^{0.008t}$
- 3)  $f(t) = 10,000(1.075)^{12t} + 10,000e^{0.8t}$
- 4)  $f(t) = 10,000(1.00075)^{12t} + 10,000e^{0.008t}$

- 263 Which expression(s) are equivalent to  $\frac{x^2 - 4x}{2x}$ , where  $x \neq 0$ ?

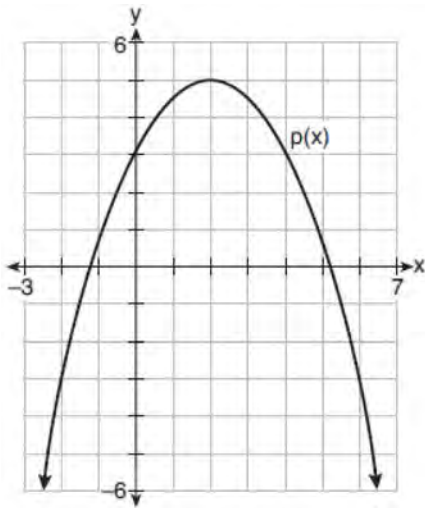
I.  $\frac{x}{2} - 2$     II.  $\frac{x-4}{2}$     III.  $\frac{x-1}{2} - \frac{3}{2}$

- 1) II, only
- 2) I and II
- 3) II and III
- 4) I, II, and III

- 264 What is the inverse of  $f(x) = x^3 - 2$ ?

- 1)  $f^{-1}(x) = \sqrt[3]{x} + 2$
- 2)  $f^{-1}(x) = \pm \sqrt[3]{x} + 2$
- 3)  $f^{-1}(x) = \sqrt[3]{x+2}$
- 4)  $f^{-1}(x) = \pm \sqrt[3]{x+2}$

- 265 Consider  $f(x) = 4x^2 + 6x - 3$ , and  $p(x)$  defined by the graph below.



The difference between the values of the maximum of  $p$  and minimum of  $f$  is

- 1) 0.25
  - 2) 1.25
  - 3) 3.25
  - 4) 10.25
- 266 A sociologist reviews randomly selected surveillance videos from a public park over a period of several years and records the amount of time people spent on a smartphone. The statistical procedure the sociologist used is called
- 1) a census
  - 2) an experiment
  - 3) an observational study
  - 4) a sample survey
- 267 The function  $N(t) = 100e^{-0.023t}$  models the number of grams in a sample of cesium-137 that remain after  $t$  years. On which interval is the sample's average rate of decay the fastest?
- 1)  $[1, 10]$
  - 2)  $[10, 20]$
  - 3)  $[15, 25]$
  - 4)  $[1, 30]$

- 268 How many solutions exist for

$$\frac{1}{1-x^2} = -|3x-2| + 5?$$

- 1) 1
  - 2) 2
  - 3) 3
  - 4) 4
- 269 The graphs of the equations  $y = x^2 + 4x - 1$  and  $y + 3 = x$  are drawn on the same set of axes. One solution of this system is
- 1)  $(-5, -2)$
  - 2)  $(-1, -4)$
  - 3)  $(1, 4)$
  - 4)  $(-2, -1)$

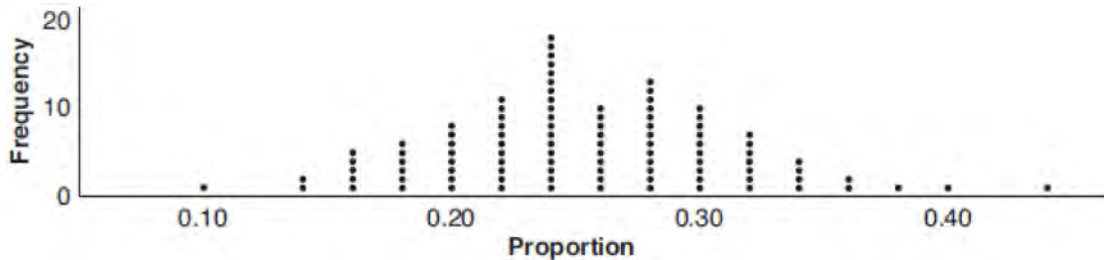
- 270 The value(s) of  $x$  that satisfy

$$\sqrt{x^2 - 4x - 5} = 2x - 10$$

- 1)  $\{5\}$
  - 2)  $\{7\}$
  - 3)  $\{5, 7\}$
  - 4)  $\{3, 5, 7\}$
- 271 A certain pain reliever is taken in 220 mg dosages and has a half-life of 12 hours. The function
- $$A = 220\left(\frac{1}{2}\right)^{\frac{t}{12}}$$
- can be used to model this situation, where  $A$  is the amount of pain reliever in milligrams remaining in the body after  $t$  hours. According to this function, which statement is true?
- 1) Every hour, the amount of pain reliever remaining is cut in half.
  - 2) In 12 hours, there is no pain reliever remaining in the body.
  - 3) In 24 hours, there is no pain reliever remaining in the body.
  - 4) In 12 hours, 110 mg of pain reliever is remaining.



- 272 A group of students was trying to determine the proportion of candies in a bag that are blue. The company claims that 24% of candies in bags are blue. A simulation was run 100 times with a sample size of 50, based on the premise that 24% of the candies are blue. The approximately normal results of the simulation are shown in the dot plot below.



The simulation results in a mean of 0.254 and a standard deviation of 0.060. Based on this simulation, what is a plausible interval containing the middle 95% of the data?

- |   |  |
|---|--|
| <p>1) (0.194,0.314)</p> <p>2) (0.134,0.374)</p> | <p>3) (-0.448,0.568)</p> <p>4) (0.254,0.374)</p> |
|---|--|
- 
- |   |   |
|---|---|
| <p>273 The weights of bags of Graseck's Chocolate Candies are normally distributed with a mean of 4.3 ounces and a standard deviation of 0.05 ounces. What is the probability that a bag of these chocolate candies weighs less than 4.27 ounces?</p> <p>1) 0.2257</p> <p>2) 0.2743</p> <p>3) 0.7257</p> <p>4) 0.7757</p> | <p>275 A number, minus twenty times its reciprocal, equals eight. The number is</p> <p>1) 10 or -2</p> <p>2) 10 or 2</p> <p>3) -10 or -2</p> <p>4) -10 or 2</p> |
|---|---|
- 
- |   |  |
|---|--|
| <p>274 Given <math>\cos \theta = \frac{7}{25}</math>, where <math>\theta</math> is an angle in standard position terminating in quadrant IV, and <math>\sin^2 \theta + \cos^2 \theta = 1</math>, what is the value of <math>\tan \theta</math>?</p> <p>1) <math>-\frac{24}{25}</math></p> <p>2) <math>-\frac{24}{7}</math></p> <p>3) <math>\frac{24}{25}</math></p> <p>4) <math>\frac{24}{7}</math></p> | <p>276 The solutions to the equation <math>5x^2 - 2x + 13 = 9</math> are</p> <p>1) <math>\frac{1}{5} \pm \frac{\sqrt{21}}{5}</math></p> <p>2) <math>\frac{1}{5} \pm \frac{\sqrt{19}}{5} i</math></p> <p>3) <math>\frac{1}{5} \pm \frac{\sqrt{66}}{5} i</math></p> <p>4) <math>\frac{1}{5} \pm \frac{\sqrt{66}}{5}</math></p> |
|---|--|

Algebra II Multiple Choice Regents Exam Questions

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- 277 The expression  $(x + a)(x + b)$  can *not* be written as
- 1)  $a(x + b) + x(x + b)$
  - 2)  $x^2 + abx + ab$
  - 3)  $x^2 + (a + b)x + ab$
  - 4)  $x(x + a) + b(x + a)$

- 278 Evan graphed a cubic function,  $f(x) = ax^3 + bx^2 + cx + d$ , and determined the roots of  $f(x)$  to be  $\pm 1$  and 2. What is the value of  $b$ , if  $a = 1$ ?
- 1) 1
  - 2) 2
  - 3) -1
  - 4) -2

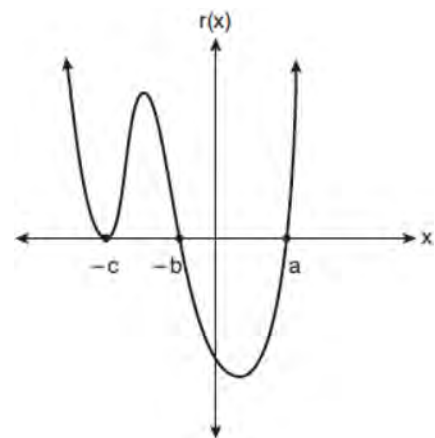
- 279 The average monthly temperature of a city can be modeled by a cosine graph. Melissa has been living in Phoenix, Arizona, where the average annual temperature is  $75^\circ\text{F}$ . She would like to move, and live in a location where the average annual temperature is  $62^\circ\text{F}$ . When examining the graphs of the average monthly temperatures for various locations, Melissa should focus on the
- 1) amplitude
  - 2) horizontal shift
  - 3) period
  - 4) midline

- 280 Perry invested in property that cost him \$1500. Five years later it was worth \$3000, and 10 years from his original purchase, it was worth \$6000. Assuming the growth rate remains the same, which type of function could he create to find the value of his investment 30 years from his original purchase?
- 1) exponential function
  - 2) linear function
  - 3) quadratic function
  - 4) trigonometric function

- 281 Which expression is equivalent to  $x^6y^4(x^4 - 16) - 9(x^4 - 16)$ ?
- 1)  $x^{10}y^4 - 16x^6y^4 - 9x^4 - 144$
  - 2)  $(x^6y^4 - 9)(x + 2)^3(x - 2)$
  - 3)  $(x^3y^2 + 3)(x^3y^2 - 3)(x + 2)^2(x - 2)^2$
  - 4)  $(x^3y^2 + 3)(x^3y^2 - 3)(x^2 + 4)(x^2 - 4)$

- 282 When the expression  $(x + 2)^2 + 4(x + 2) + 3$  is rewritten as the product of two binomials, the result is
- 1)  $(x + 3)(x + 1)$
  - 2)  $(x + 5)(x + 3)$
  - 3)  $(x + 2)(x + 2)$
  - 4)  $(x + 6)(x + 1)$

- 283 A sketch of  $r(x)$  is shown below.



An equation for  $r(x)$  could be

- 1)  $r(x) = (x - a)(x + b)(x + c)$
- 2)  $r(x) = (x + a)(x - b)(x - c)^2$
- 3)  $r(x) = (x + a)(x - b)(x - c)$
- 4)  $r(x) = (x - a)(x + b)(x + c)^2$

Algebra II Multiple Choice Regents Exam Questions

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- 284 What is the equation of the directrix for the parabola  $-8(y - 3) = (x + 4)^2$ ?
- 1)  $y = 5$
  - 2)  $y = 1$
  - 3)  $y = -2$
  - 4)  $y = -6$
- 285 Which expression is equivalent to  $(2x - i)^2 - (2x - i)(2x + 3i)$  where  $i$  is the imaginary unit and  $x$  is a real number?
- 1)  $-4 - 8xi$
  - 2)  $-4 - 4xi$
  - 3)  $2$
  - 4)  $8x - 4i$
- 286 What is the solution set for  $x$  in the equation below?
- $$\sqrt{x + 1} - 1 = x$$
- 1)  $\{1\}$
  - 2)  $\{0\}$
  - 3)  $\{-1, 0\}$
  - 4)  $\{0, 1\}$
- 287 The function below models the average price of gas in a small town since January 1st.
- $$G(t) = -0.0049t^4 + 0.0923t^3 - 0.56t^2 + 1.166t + 3.23,$$
- where  $0 \leq t \leq 10$ .
- If  $G(t)$  is the average price of gas in dollars and  $t$  represents the number of months since January 1st, the absolute maximum  $G(t)$  reaches over the given domain is about
- 1) \$1.60
  - 2) \$3.92
  - 3) \$4.01
  - 4) \$7.73
- 288 The roots of the equation  $3x^2 + 2x = -7$  are
- 1)  $-2, -\frac{1}{3}$
  - 2)  $-\frac{7}{3}, 1$
  - 3)  $-\frac{1}{3} \pm \frac{2i\sqrt{5}}{3}$
  - 4)  $-\frac{1}{3} \pm \frac{\sqrt{11}}{3}$
- 289 Which expression can be rewritten as  $(x + 7)(x - 1)$ ?
- 1)  $(x + 3)^2 - 16$
  - 2)  $(x + 3)^2 - 10(x + 3) - 2(x + 3) + 20$
  - 3)  $\frac{(x - 1)(x^2 - 6x - 7)}{(x + 1)}$
  - 4)  $\frac{(x + 7)(x^2 + 4x + 3)}{(x + 3)}$
- 290 Which function is even?
- 1)  $f(x) = \sin x$
  - 2)  $f(x) = x^2 - 4$
  - 3)  $f(x) = |x - 2| + 5$
  - 4)  $f(x) = x^4 + 3x^3 + 4$
- 291 Given  $c(m) = m^3 - 2m^2 + 4m - 8$ , the solution of  $c(m) = 0$  is
- 1)  $\pm 2$
  - 2)  $2, \text{ only}$
  - 3)  $2i, 2$
  - 4)  $\pm 2i, 2$

292 The graph of  $y = \log_2 x$  is translated to the right 1 unit and down 1 unit. The coordinates of the  $x$ -intercept of the translated graph are

- 1) (0,0)
- 2) (1,0)
- 3) (2,0)
- 4) (3,0)

293 On average, college seniors graduating in 2012 could compute their growing student loan debt using the function  $D(t) = 29,400(1.068)^t$ , where  $t$  is time in years. Which expression is equivalent to  $29,400(1.068)^t$  and could be used by students to identify an approximate daily interest rate on their loans?

- 1)  $29,400 \left( 1.068^{\frac{1}{365}} \right)^t$
- 2)  $29,400 \left( \frac{1.068}{365} \right)^{365t}$
- 3)  $29,400 \left( 1 + \frac{0.068}{365} \right)^t$
- 4)  $29,400 \left( 1.068^{\frac{1}{365}} \right)^{365t}$

294 What is the inverse of  $f(x) = \frac{x}{x+2}$ , where  $x \neq -2$ ?

- 1)  $f^{-1}(x) = \frac{2x}{x-1}$
- 2)  $f^{-1}(x) = \frac{-2x}{x-1}$
- 3)  $f^{-1}(x) = \frac{x}{x-2}$
- 4)  $f^{-1}(x) = \frac{-x}{x-2}$

295 A fast-food restaurant analyzes data to better serve its customers. After its analysis, it discovers that the events  $D$ , that a customer uses the drive-thru, and  $F$ , that a customer orders French fries, are independent. The following data are given in a report:

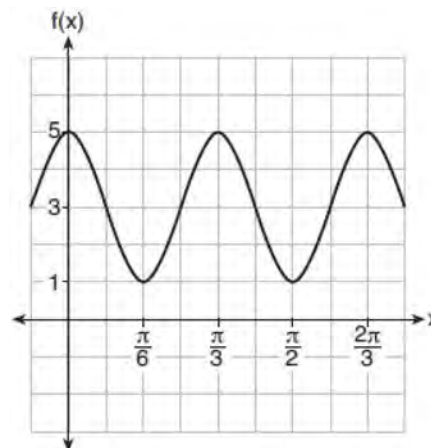
$$P(F) = 0.8$$

$$P(F \cap D) = 0.456$$

Given this information,  $P(F|D)$  is

- 1) 0.344
- 2) 0.3648
- 3) 0.57
- 4) 0.8

296 The function  $f(x) = a \cos bx + c$  is plotted on the graph shown below.



What are the values of  $a$ ,  $b$ , and  $c$ ?

- 1)  $a = 2, b = 6, c = 3$
- 2)  $a = 2, b = 3, c = 1$
- 3)  $a = 4, b = 6, c = 5$
- 4)  $a = 4, b = \frac{\pi}{3}, c = 3$

297 Selected values for the functions  $f$  and  $g$  are shown in the tables below.

$x$	$f(x)$		$x$	$g(x)$
-3.12	-4.88		-2.01	-1.01
0	-6		0	0.58
1.23	-4.77		8.52	2.53
8.52	2.53		13.11	3.01
9.01	3.01		16.52	3.29

A solution to the equation  $f(x) = g(x)$  is

- 1) 0  
 2) 2.53  
 3) 3.01  
 4) 8.52

298 What are the solution(s) to the system of equations shown below?

$$x^2 + y^2 = 5$$

$$y = 2x$$

- 1)  $x = 1$  and  $x = -1$   
 2)  $x = 1$   
 3) (1,2) and (-1,-2)  
 4) (1,2), only

299 Which situation could be modeled using a geometric sequence?

- 1) A cell phone company charges \$30.00 per month for 2 gigabytes of data and \$12.50 for each additional gigabyte of data.  
 2) The temperature in your car is  $79^\circ$ . You lower the temperature of your air conditioning by  $2^\circ$  every 3 minutes in order to find a comfortable temperature.  
 3) David's parents have set a limit of 50 minutes per week that he may play online games during the school year. However, they will increase his time by 5% per week for the next ten weeks.  
 4) Sarah has \$100.00 in her piggy bank and saves an additional \$15.00 each week.

300 Suppose events  $A$  and  $B$  are independent and  $P(A \text{ and } B)$  is 0.2. Which statement could be true?

- 1)  $P(A) = 0.4, P(B) = 0.3, P(A \text{ or } B) = 0.5$   
 2)  $P(A) = 0.8, P(B) = 0.25$   
 3)  $P(A|B) = 0.2, P(B) = 0.2$   
 4)  $P(A) = 0.15, P(B) = 0.05$

301 The average depreciation rate of a new boat is approximately 8% per year. If a new boat is purchased at a price of \$75,000, which model is a recursive formula representing the value of the boat  $n$  years after it was purchased?

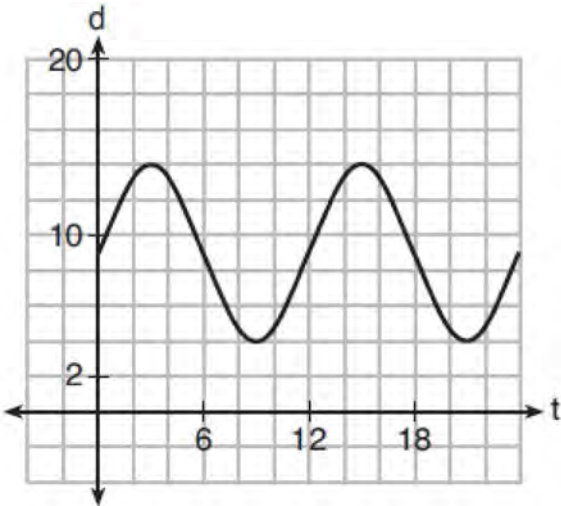
- 1)  $a_n = 75,000(0.08)^n$   
 2)  $a_0 = 75,000$   
 $a_n = (0.92)^n$   
 3)  $a_n = 75,000(1.08)^n$   
 4)  $a_0 = 75,000$   
 $a_n = 0.92(a_{n-1})$

Algebra II Multiple Choice Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 302 The temperature, in degrees Fahrenheit, in Times Square during a day in August can be predicted by the function  $T(x) = 8 \sin(0.3x - 3) + 74$ , where  $x$  is the number of hours after midnight. According to this model, the predicted temperature, to the nearest degree Fahrenheit, at 7 P.M. is
- 1) 68
  - 2) 74
  - 3) 77
  - 4) 81
- 303 The solutions to  $x + 3 - \frac{4}{x-1} = 5$  are
- 1)  $\frac{3}{2} \pm \frac{\sqrt{17}}{2}$
  - 2)  $\frac{3}{2} \pm \frac{\sqrt{17}}{2} i$
  - 3)  $\frac{3}{2} \pm \frac{\sqrt{33}}{2}$
  - 4)  $\frac{3}{2} \pm \frac{\sqrt{33}}{2} i$
- 304 For a given time,  $x$ , in seconds, an electric current,  $y$ , can be represented by  $y = 2.5(1 - 2.7^{-10x})$ . Which equation is *not* equivalent?
- 1)  $y = 2.5 - 2.5(2.7^{-10x})$
  - 2)  $y = 2.5 - 2.5\left((2.7^2)^{-0.5x}\right)$
  - 3)  $y = 2.5 - 2.5\left(\frac{1}{2.7^{10x}}\right)$
  - 4)  $y = 2.5 - 2.5(2.7^{-2})(2.7^{0.5x})$
- 305 Camryn puts \$400 into a savings account that earns 6% annually. The amount in her account can be modeled by  $C(t) = 400(1.06)^t$  where  $t$  is the time in years. Which expression best approximates the amount of money in her account using a weekly growth rate?
- 1)  $400(1.001153846)^t$
  - 2)  $400(1.001121184)^t$
  - 3)  $400(1.001153846)^{52t}$
  - 4)  $400(1.001121184)^{52t}$
- 306 When factoring to reveal the roots of the equation  $x^3 + 2x^2 - 9x - 18 = 0$ , which equations can be used?
- I.  $x^2(x + 2) - 9(x + 2) = 0$
  - II.  $x(x^2 - 9) + 2(x^2 - 9) = 0$
  - III.  $(x - 2)(x^2 - 9) = 0$
- 1) I and II, only
  - 2) I and III, only
  - 3) II and III, only
  - 4) I, II, and III
- 307 Given  $y > 0$ , the expression  $\sqrt{3x^2y} \cdot \sqrt[3]{27x^3y^2}$  is equivalent to
- 1)  $81x^5y^3$
  - 2)  $3^{1.5}x^2y$
  - 3)  $3^{\frac{5}{2}}x^2y^{\frac{5}{3}}$
  - 4)  $3^{\frac{3}{2}}x^2y^{\frac{7}{6}}$

- 308 The depth of the water at a marker 20 feet from the shore in a bay is depicted in the graph below.



If the depth,  $d$ , is measured in feet and time,  $t$ , is measured in hours since midnight, what is an equation for the depth of the water at the marker?

- 1)  $d = 5 \cos\left(\frac{\pi}{6} t\right) + 9$
  - 2)  $d = 9 \cos\left(\frac{\pi}{6} t\right) + 5$
  - 3)  $d = 9 \sin\left(\frac{\pi}{6} t\right) + 5$
  - 4)  $d = 5 \sin\left(\frac{\pi}{6} t\right) + 9$
- 309 If \$5000 is put into a savings account that pays 3.5% interest compounded monthly, how much money, to the nearest ten cents, would be in that account after 6 years, assuming no money was added or withdrawn?
- 1) \$5177.80
  - 2) \$5941.30
  - 3) \$6146.30
  - 4) \$6166.50

- 310 The height above ground for a person riding a Ferris wheel after  $t$  seconds is modeled by

$$h(t) = 150 \sin\left(\frac{\pi}{45} t + 67.5\right) + 160 \text{ feet.}$$

How many seconds does it take to go from the bottom of the wheel to the top of the wheel?

- 1) 10
  - 2) 45
  - 3) 90
  - 4) 150
- 311 If  $p(x) = 2x^3 - 3x + 5$ , what is the remainder of  $p(x) \div (x - 5)$ ?
- 1) -230
  - 2) 0
  - 3) 40
  - 4) 240

- 312 Written in simplest form,  $\frac{c^2 - d^2}{d^2 + cd - 2c^2}$  where

$c \neq d$ , is equivalent to

- 1)  $\frac{c + d}{d + 2c}$
  - 2)  $\frac{c - d}{d + 2c}$
  - 3)  $\frac{-c - d}{d + 2c}$
  - 4)  $\frac{-c + d}{d + 2c}$
- 313 For the system shown below, what is the value of  $z$ ?
- $$y = -2x + 14$$
- $$3x - 4z = 2$$
- $$3x - y = 16$$
- 1) 5
  - 2) 2
  - 3) 6
  - 4) 4

314 For positive values of  $x$ , which expression is

equivalent to  $\sqrt{16x^2} \cdot x^{\frac{2}{3}} + \sqrt[3]{8x^5}$

- 1)  $6\sqrt{x^3}$
- 2)  $6\sqrt[3]{x^5}$
- 3)  $4\sqrt[3]{x^2} + 2\sqrt[3]{x^5}$
- 4)  $4\sqrt{x^3} + 2\sqrt[5]{x^3}$

315 When a ball bounces, the heights of consecutive bounces form a geometric sequence. The height of the first bounce is 121 centimeters and the height of the third bounce is 64 centimeters. To the *nearest centimeter*, what is the height of the fifth bounce?

- 1) 25
- 2) 34
- 3) 36
- 4) 42

316 The completely factored form of  $n^4 - 9n^2 + 4n^3 - 36n - 12n^2 + 108$  is

- 1)  $(n^2 - 9)(n + 6)(n - 2)$
- 2)  $(n + 3)(n - 3)(n + 6)(n - 2)$
- 3)  $(n - 3)(n - 3)(n + 6)(n - 2)$
- 4)  $(n + 3)(n - 3)(n - 6)(n + 2)$

317 What is the solution when the equation  $wx^2 + w = 0$  is solved for  $x$ , where  $w$  is a positive integer?

- 1)  $-1$
- 2)  $0$
- 3)  $6$
- 4)  $\pm i$

318 If  $f(x) = a^x$  where  $a > 1$ , then the inverse of the function is

- 1)  $f^{-1}(x) = \log_x a$
- 2)  $f^{-1}(x) = a \log x$
- 3)  $f^{-1}(x) = \log_a x$
- 4)  $f^{-1}(x) = x \log a$

319 Which statement(s) are true for all real numbers?

I  $(x - y)^2 = x^2 + y^2$

II  $(x + y)^3 = x^3 + 3xy + y^3$

- 1) I, only
- 2) II, only
- 3) I and II
- 4) neither I nor II

320 Which function's graph has a period of 8 and reaches a maximum height of 1 if at least one full period is graphed?

- 1)  $y = -4 \cos\left(\frac{\pi}{4}x\right) - 3$
- 2)  $y = -4 \cos\left(\frac{\pi}{4}x\right) + 5$
- 3)  $y = -4 \cos(8x) - 3$
- 4)  $y = -4 \cos(8x) + 5$

321 Which description could represent the graph of  $f(x) = 4x^2(x + a) - x - a$ , if  $a$  is an integer?

- 1) As  $x \rightarrow -\infty, f(x) \rightarrow \infty$ , as  $x \rightarrow \infty, f(x) \rightarrow \infty$ , and the graph has 3  $x$ -intercepts.
- 2) As  $x \rightarrow -\infty, f(x) \rightarrow -\infty$ , as  $x \rightarrow \infty, f(x) \rightarrow \infty$ , and the graph has 3  $x$ -intercepts.
- 3) As  $x \rightarrow -\infty, f(x) \rightarrow \infty$ , as  $x \rightarrow \infty, f(x) \rightarrow -\infty$ , and the graph has 4  $x$ -intercepts.
- 4) As  $x \rightarrow -\infty, f(x) \rightarrow -\infty$ , as  $x \rightarrow \infty, f(x) \rightarrow \infty$ , and the graph has 4  $x$ -intercepts.



Algebra II Multiple Choice Regents Exam Questions

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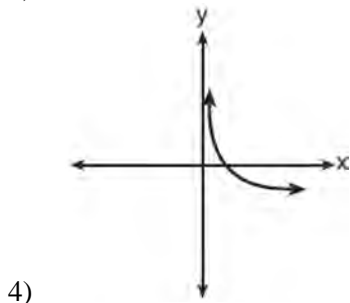
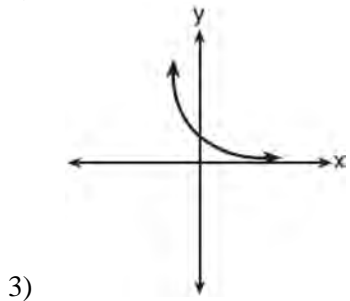
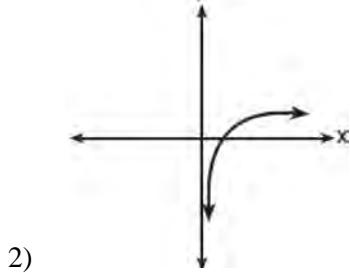
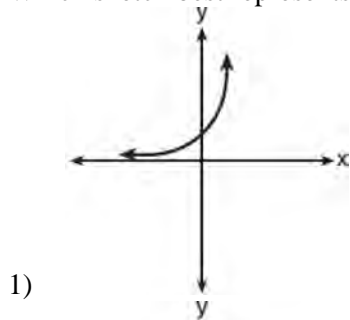
- 322 The populations of two small towns at the beginning of 2018 and their annual population growth rate are shown in the table below.

Town	Population	Annual Population Growth Rate
Jonesville	1240	6% increase
Williamstown	890	11% increase

Assuming the trend continues, approximately how many years after the beginning of 2018 will it take for the populations to be equal?

- 1) 7  
2) 20  
3) 68  
4) 125
- 323 Consider the system of equations below:
- $$x + y - z = 6$$
- $$2x - 3y + 2z = -19$$
- $$-x + 4y - z = 17$$
- Which number is *not* the value of any variable in the solution of the system?
- 1) -1  
2) 2  
3) 3  
4) -4
- 324 For  $x \geq 0$ , which equation is *false*?
- 1)  $(x^{\frac{3}{2}})^2 = \sqrt[4]{x^3}$   
2)  $(x^3)^{\frac{1}{4}} = \sqrt[4]{x^3}$   
3)  $(x^{\frac{3}{2}})^{\frac{1}{2}} = \sqrt[4]{x^3}$   
4)  $(x^{\frac{2}{3}})^2 = \sqrt[3]{x^4}$
- 325 What is the inverse of  $f(x) = -6(x - 2)$ ?
- 1)  $f^{-1}(x) = -2 - \frac{x}{6}$   
2)  $f^{-1}(x) = 2 - \frac{x}{6}$   
3)  $f^{-1}(x) = \frac{1}{-6(x - 2)}$   
4)  $f^{-1}(x) = 6(x + 2)$
- 326 A 7-year lease for office space states that the annual rent is \$85,000 for the first year and will increase by 6% each additional year of the lease. What will the total rent expense be for the entire 7-year lease?
- 1) \$42,809.63  
2) \$90,425.53  
3) \$595,000.00  
4) \$713,476.20

327 Which sketch best represents the graph of  $x = 3^y$ ?



328 What is the inverse of the function  $y = 4x + 5$ ?

- 1)  $x = \frac{1}{4}y - \frac{5}{4}$
- 2)  $y = \frac{1}{4}x - \frac{5}{4}$
- 3)  $y = 4x - 5$
- 4)  $y = \frac{1}{4x + 5}$

329 Which expression is equivalent to  $\frac{2x^4 + 8x^3 - 25x^2 - 6x + 14}{x + 6}$ ?

- 1)  $2x^3 + 4x^2 + x - 12 + \frac{86}{x + 6}$
- 2)  $2x^3 - 4x^2 - x + 14$
- 3)  $2x^3 - 4x^2 - x + \frac{14}{x + 6}$
- 4)  $2x^3 - 4x^2 - x$

330 Which expression is equivalent to  $\frac{4x^3 + 9x - 5}{2x - 1}$ , where  $x \neq \frac{1}{2}$ ?

- 1)  $2x^2 + x + 5$
- 2)  $2x^2 + \frac{11}{2} + \frac{1}{2(2x - 1)}$
- 3)  $2x^2 - x + 5$
- 4)  $2x^2 - x + 4 + \frac{1}{2x - 1}$

331 The scores on a mathematics college-entry exam are normally distributed with a mean of 68 and standard deviation 7.2. Students scoring higher than one standard deviation above the mean will not be enrolled in the mathematics tutoring program. How many of the 750 incoming students can be expected to be enrolled in the tutoring program?

- 1) 631
- 2) 512
- 3) 238
- 4) 119

332 The solution of  $87e^{0.3x} = 5918$ , to the nearest thousandth, is

- 1) 0.583
- 2) 1.945
- 3) 4.220
- 4) 14.066

333 Julia deposits \$2000 into a savings account that earns 4% interest per year. The exponential function that models this savings account is  $y = 2000(1.04)^t$ , where  $t$  is the time in years. Which equation correctly represents the amount of money in her savings account in terms of the monthly growth rate?

- 1)  $y = 166.67(1.04)^{0.12t}$
- 2)  $y = 2000(1.01)^t$
- 3)  $y = 2000(1.0032737)^{12t}$
- 4)  $y = 166.67(1.0032737)^t$

334 Where  $i$  is the imaginary unit, the expression  $(x + 3i)^2 - (2x - 3i)^2$  is equivalent to

- 1)  $-3x^2$
- 2)  $-3x^2 - 18$
- 3)  $-3x^2 + 18xi$
- 4)  $-3x^2 - 6xi - 18$

335 If  $f(x) = x^2 + 9$  and  $g(x) = x + 3$ , which operation would not result in a polynomial expression?

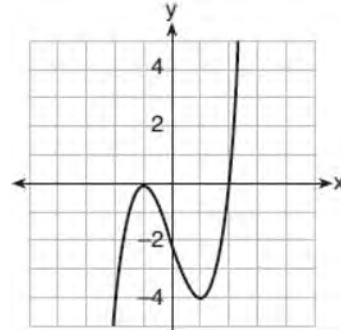
- 1)  $f(x) + g(x)$
- 2)  $f(x) - g(x)$
- 3)  $f(x) \cdot g(x)$
- 4)  $f(x) \div g(x)$

336 The terminal side of  $\theta$ , an angle in standard position, intersects the unit circle at  $P\left(-\frac{1}{3}, -\frac{\sqrt{8}}{3}\right)$ .

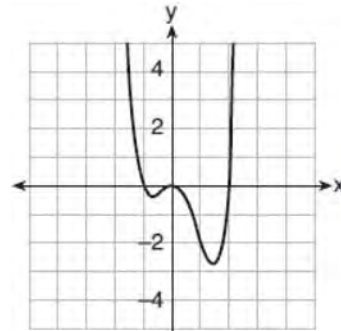
What is the value of  $\sec \theta$ ?

- 1)  $-3$
- 2)  $-\frac{3\sqrt{8}}{8}$
- 3)  $-\frac{1}{3}$
- 4)  $-\frac{\sqrt{8}}{3}$

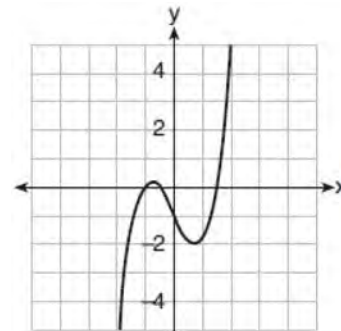
337 Which graph represents a polynomial function that contains  $x^2 + 2x + 1$  as a factor?



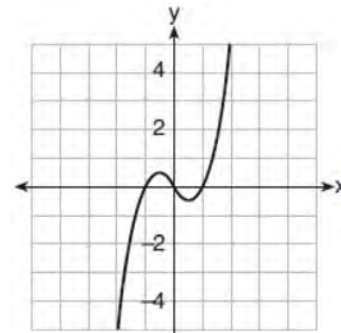
1)



2)



3)



4)

338 Sodium iodide-131, used to treat certain medical conditions, has a half-life of 1.8 hours. The data table below shows the amount of sodium iodide-131, rounded to the nearest thousandth, as the dose fades over time.

Number of Half Lives	1	2	3	4	5
Amount of Sodium Iodide-131	139.000	69.500	34.750	17.375	8.688

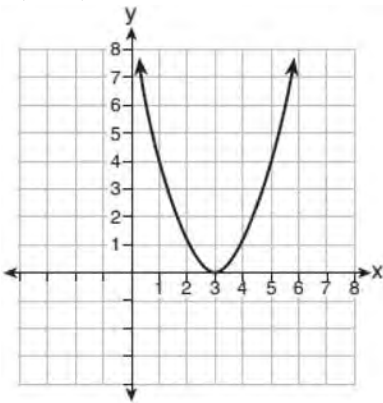
What approximate amount of sodium iodide-131 will remain in the body after 18 hours?

- 1) 0.001  
 2) 0.136  
 3) 0.271  
 4) 0.543

339 Which representation of a quadratic has imaginary roots?

x	y
-2.5	2
-2.0	0
-1.5	-1
-1.0	-1
-0.5	0
0.0	2

- 1)  
 2)  $2(x + 3)^2 = 64$



- 3)  
 4)  $2x^2 + 32 = 0$

340 What is the solution set of the following system of equations?

$$y = 3x + 6$$

$$y = (x + 4)^2 - 10$$

- 1)  $\{-5, -9\}$   
 2)  $\{(5, 21)\}$   
 3)  $\{(0, 6), (-5, -9)\}$   
 4)  $\{(0, 6), (5, 21)\}$

341 The Fahrenheit temperature,  $F(t)$ , of a heated object at time  $t$ , in minutes, can be modeled by the function below.  $F_s$  is the surrounding temperature,  $F_0$  is the initial temperature of the object, and  $k$  is a constant.

$$F(t) = F_s + (F_0 - F_s)e^{-kt}$$

Coffee at a temperature of 195°F is poured into a container. The room temperature is kept at a constant 68°F and  $k = 0.05$ . Coffee is safe to drink when its temperature is, at most, 120°F. To the nearest minute, how long will it take until the coffee is safe to drink?

- 1) 7  
 2) 10  
 3) 11  
 4) 18

342 What is the solution set of the equation

$$\frac{2}{x} - \frac{3x}{x+3} = \frac{x}{x+3}?$$

- 1)  $\{3\}$
- 2)  $\left\{\frac{3}{2}\right\}$
- 3)  $\{-2, 3\}$
- 4)  $\left\{-1, \frac{3}{2}\right\}$

343 For which values of  $x$ , rounded to the *nearest*

*hundredth*, will  $|x^2 - 9| - 3 = \log_3 x$ ?

- 1) 2.29 and 3.63
- 2) 2.37 and 3.54
- 3) 2.84 and 3.17
- 4) 2.92 and 3.06

344 The half-life of iodine-131 is 8 days. The percent of the isotope left in the body  $d$  days after being

introduced is  $I = 100\left(\frac{1}{2}\right)^{\frac{d}{8}}$ . When this equation is

written in terms of the number  $e$ , the base of the natural logarithm, it is equivalent to  $I = 100e^{kd}$ .

What is the approximate value of the constant,  $k$ ?

- 1)  $-0.087$
- 2)  $0.087$
- 3)  $-11.542$
- 4)  $11.542$

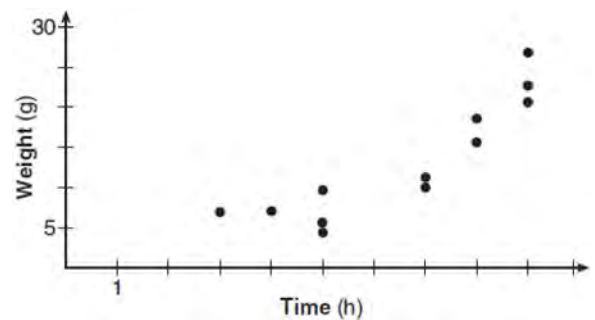
345 If  $p(x) = 2\ln(x) - 1$  and  $m(x) = \ln(x + 6)$ , then what is the solution for  $p(x) = m(x)$ ?

- 1) 1.65
- 2) 3.14
- 3) 5.62
- 4) no solution

346 On a given school day, the probability that Nick oversleeps is 48% and the probability he has a pop quiz is 25%. Assuming these two events are independent, what is the probability that Nick oversleeps and has a pop quiz on the same day?

- 1) 73%
- 2) 36%
- 3) 23%
- 4) 12%

347 A scatterplot showing the weight,  $w$ , in grams, of each crystal after growing  $t$  hours is shown below.



The relationship between weight,  $w$ , and time,  $t$ , is best modeled by

- 1)  $w = 4^t + 5$
- 2)  $w = (1.4)^t + 2$
- 3)  $w = 5(2.1)^t$
- 4)  $w = 8(.75)^t$

348 What is the quotient when  $10x^3 - 3x^2 - 7x + 3$  is divided by  $2x - 1$ ?

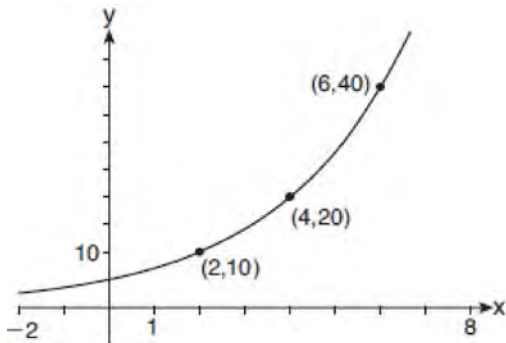
- 1)  $5x^2 + x + 3$
- 2)  $5x^2 - x + 3$
- 3)  $5x^2 - x - 3$
- 4)  $5x^2 + x - 3$

Algebra II Multiple Choice Regents Exam Questions

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- 349 The solution set for the equation  $b = \sqrt{2b^2 - 64}$  is
- 1)  $\{-8\}$
  - 2)  $\{8\}$
  - 3)  $\{\pm 8\}$
  - 4)  $\{\}$

- 350 The graph of  $y = f(x)$  is shown below.



Which expression defines  $f(x)$ ?

- 1)  $2x$
  - 2)  $5(2^x)$
  - 3)  $5(2^{\frac{x}{2}})$
  - 4)  $5(2^{2x})$
- 351 An estimate of the number of milligrams of a medication in the bloodstream  $t$  hours after 400 mg has been taken can be modeled by the function below.

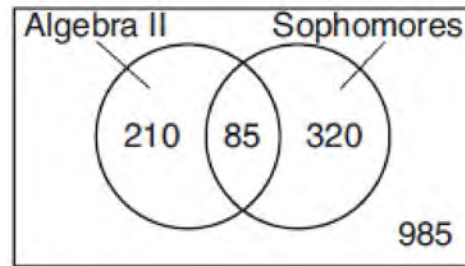
$$I(t) = 0.5t^4 + 3.45t^3 - 96.65t^2 + 347.7t,$$

where  $0 \leq t \leq 6$

Over what time interval does the amount of medication in the bloodstream strictly increase?

- 1) 0 to 2 hours
- 2) 0 to 3 hours
- 3) 2 to 6 hours
- 4) 3 to 6 hours

- 352 Data for the students enrolled in a local high school are shown in the Venn diagram below.

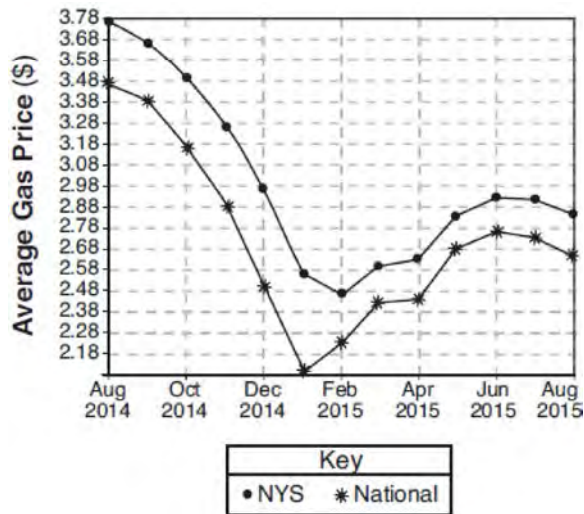


If a student from the high school is selected at random, what is the probability that the student is a sophomore given that the student is enrolled in Algebra II?

- 1)  $\frac{85}{210}$
  - 2)  $\frac{85}{295}$
  - 3)  $\frac{85}{405}$
  - 4)  $\frac{85}{1600}$
- 353 Given  $P(x) = x^3 - 3x^2 - 2x + 4$ , which statement is true?
- 1)  $(x - 1)$  is a factor because  $P(-1) = 2$ .
  - 2)  $(x + 1)$  is a factor because  $P(-1) = 2$ .
  - 3)  $(x + 1)$  is a factor because  $P(1) = 0$ .
  - 4)  $(x - 1)$  is a factor because  $P(1) = 0$ .

- 354 A veterinary pharmaceutical company plans to test a new drug to treat a common intestinal infection among puppies. The puppies are randomly assigned to two equal groups. Half of the puppies will receive the drug, and the other half will receive a placebo. The veterinarians monitor the puppies. This is an example of which study method?
- 1) census
  - 2) observational study
  - 3) survey
  - 4) controlled experiment

- 355 The graph below represents national and New York State average gas prices.



If New York State's gas prices are modeled by  $G(x)$  and  $C > 0$ , which expression best approximates the national average  $x$  months from August 2014?

- 1)  $G(x + C)$
  - 2)  $G(x) + C$
  - 3)  $G(x - C)$
  - 4)  $G(x) - C$
- 356 The expression  $\frac{9x^2 - 2}{3x + 1}$  is equivalent to
- 1)  $3x - 1 - \frac{1}{3x + 1}$
  - 2)  $3x - 1 + \frac{1}{3x + 1}$
  - 3)  $3x + 1 - \frac{1}{3x + 1}$
  - 4)  $3x + 1 + \frac{1}{3x + 1}$
- 357 After examining the functions  $f(x) = \ln(x + 2)$  and  $g(x) = e^{x-1}$  over the interval  $(-2, 3]$ , Lexi determined that the correct number of solutions to the equation  $f(x) = g(x)$  is
- 1) 1
  - 2) 2
  - 3) 3
  - 4) 0
- 358 The mean intelligence quotient (IQ) score is 100, with a standard deviation of 15, and the scores are normally distributed. Given this information, the approximate percentage of the population with an IQ greater than 130 is closest to
- 1) 2%
  - 2) 31%
  - 3) 48%
  - 4) 95%
- 359 If  $f(x)$  is an even function, which function must also be even?
- 1)  $f(x - 2)$
  - 2)  $f(x) + 3$
  - 3)  $f(x + 1)$
  - 4)  $f(x + 1) + 3$
- 360 Judith puts \$5000 into an investment account with interest compounded continuously. Which approximate annual rate is needed for the account to grow to \$9110 after 30 years?
- 1) 2%
  - 2) 2.2%
  - 3) 0.02%
  - 4) 0.022%

Algebra II Multiple Choice Regents Exam Questions

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- 361 After Roger’s surgery, his doctor administered pain medication in the following amounts in milligrams over four days.

Day (n)	1	2	3	4
Dosage (m)	2000	1680	1411.2	1185.4

How can this sequence best be modeled recursively?

- 1)  $m_1 = 2000$   
 $m_n = m_{n-1} - 320$
- 2)  $m_n = 2000(0.84)^{n-1}$
- 3)  $m_1 = 2000$   
 $m_n = (0.84)m_{n-1}$
- 4)  $m_n = 2000(0.84)^{n+1}$
- 362 Which statement is true about the graph of  $f(x) = \left(\frac{1}{8}\right)^x$ ?
- 1) The graph is always increasing.  
 2) The graph is always decreasing.  
 3) The graph passes through (1,0).  
 4) The graph has an asymptote,  $x = 0$ .
- 363 The hours of daylight,  $y$ , in Utica in days,  $x$ , from January 1, 2013 can be modeled by the equation  $y = 3.06\sin(0.017x - 1.40) + 12.23$ . How many hours of daylight, to the *nearest tenth*, does this model predict for February 14, 2013?
- 1) 9.4  
 2) 10.4  
 3) 12.1  
 4) 12.2
- 364 What is the solution set of the equation  $\frac{10}{x^2 - 2x} + \frac{4}{x} = \frac{5}{x - 2}$ ?
- 1)  $\{0, 2\}$   
 2)  $\{0\}$   
 3)  $\{2\}$   
 4)  $\{ \}$
- 365 There are 440 students at Thomas Paine High School enrolled in U.S. History. On the April report card, the students' grades are approximately normally distributed with a mean of 79 and a standard deviation of 7. Students who earn a grade less than or equal to 64.9 must attend summer school. The number of students who must attend summer school for U.S. History is closest to
- 1) 3  
 2) 5  
 3) 10  
 4) 22
- 366 If  $ae^{bt} = c$ , where  $a$ ,  $b$ , and  $c$  are positive, then  $t$  equals
- 1)  $\ln\left(\frac{c}{ab}\right)$   
 2)  $\ln\left(\frac{cb}{a}\right)$   
 3)  $\frac{\ln\left(\frac{c}{a}\right)}{b}$   
 4)  $\frac{\ln\left(\frac{c}{a}\right)}{\ln b}$

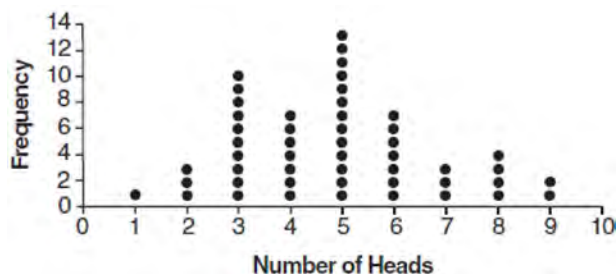


367 For all values of  $x$  for which the expression is defined,  $\frac{x^3 + 2x^2 - 9x - 18}{x^3 - x^2 - 6x}$ , in simplest form, is

equivalent to

- 1) 3
- 2)  $-\frac{17}{2}$
- 3)  $\frac{x+3}{x}$
- 4)  $\frac{x^2-9}{x(x-3)}$

368 The results of simulating tossing a coin 10 times, recording the number of heads, and repeating this 50 times are shown in the graph below.



Based on the results of the simulation, which statement is *false*?

- 1) Five heads occurred most often, which is consistent with the theoretical probability of obtaining a heads.
- 2) Eight heads is unusual, as it falls outside the middle 95% of the data.
- 3) Obtaining three heads or fewer occurred 28% of the time.
- 4) Seven heads is not unusual, as it falls within the middle 95% of the data.

369 If  $A = -3 + 5i$ ,  $B = 4 - 2i$ , and  $C = 1 + 6i$ , where  $i$  is the imaginary unit, then  $A - BC$  equals

- 1)  $5 - 17i$
- 2)  $5 + 27i$
- 3)  $-19 - 17i$
- 4)  $-19 + 27i$

370 Which equation represents the equation of the parabola with focus  $(-3, 3)$  and directrix  $y = 7$ ?

- 1)  $y = \frac{1}{8}(x+3)^2 - 5$
- 2)  $y = \frac{1}{8}(x-3)^2 + 5$
- 3)  $y = -\frac{1}{8}(x+3)^2 + 5$
- 4)  $y = -\frac{1}{8}(x-3)^2 + 5$

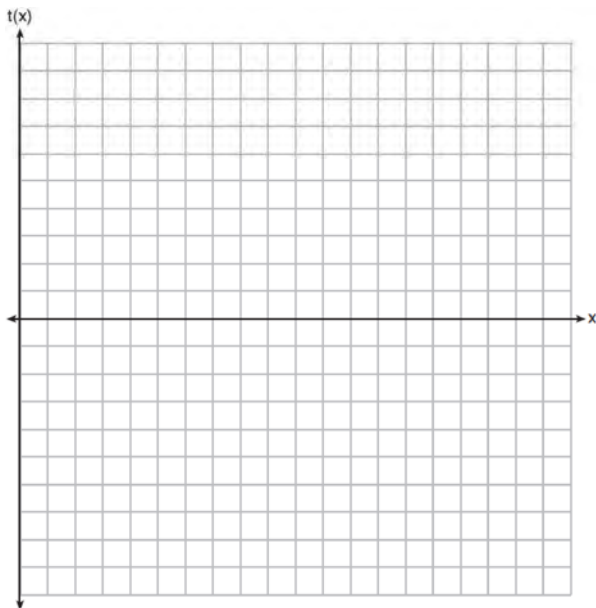
**Algebra II 2 Point Regents Exam Questions**

371 Data collected about jogging from students with two older siblings are shown in the table below.

	<b>Neither Sibling Jogs</b>	<b>One Sibling Jogs</b>	<b>Both Siblings Jog</b>
<b>Student Does Not Jog</b>	1168	1823	1380
<b>Student Jogs</b>	188	416	400

Using these data, determine whether a student with two older siblings is more likely to jog if one sibling jogs or if both siblings jog. Justify your answer.

372 Graph  $t(x) = 3\sin(2x) + 2$  over the domain  $[0, 2\pi]$  on the set of axes below.



373 Completely factor the following expression:

$$x^2 + 3xy + 3x^3 + y$$

374 Describe how a controlled experiment can be created to examine the effect of ingredient  $X$  in a toothpaste.

375 The world population was 2560 million people in 1950 and 3040 million in 1960 and can be modeled by the function  $p(t) = 2560e^{0.017185t}$ , where  $t$  is time in years after 1950 and  $p(t)$  is the population in millions. Determine the average rate of change of  $p(t)$  in millions of people per year, from  $4 \leq t \leq 8$ . Round your answer to the *nearest hundredth*.

376 A person's lung capacity can be modeled by the function  $C(t) = 250 \sin\left(\frac{2\pi}{5}t\right) + 2450$ , where  $C(t)$  represents the volume in mL present in the lungs after  $t$  seconds. State the maximum value of this function over one full cycle, and explain what this value represents.

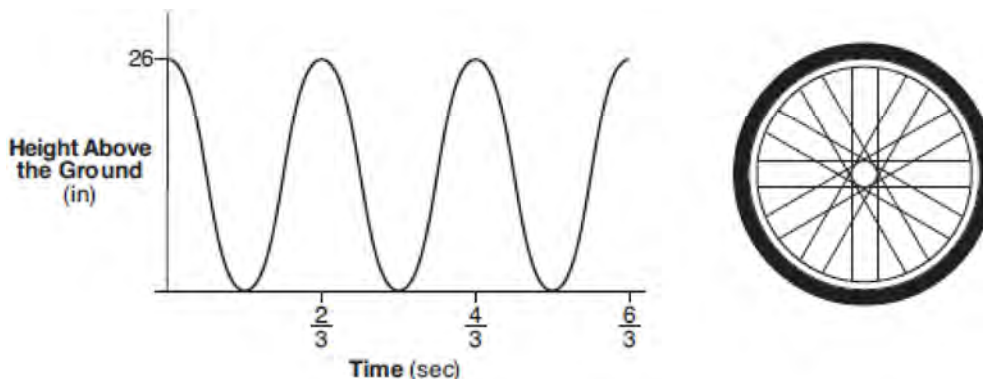
377 Given  $f(x) = 3x^2 + 7x - 20$  and  $g(x) = x - 2$ , state the quotient and remainder of  $\frac{f(x)}{g(x)}$ , in the form

$$q(x) + \frac{r(x)}{g(x)}.$$

Algebra II 2 Point Regents Exam Questions

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- 378 The graph below represents the height above the ground,  $h$ , in inches, of a point on a triathlete's bike wheel during a training ride in terms of time,  $t$ , in seconds.



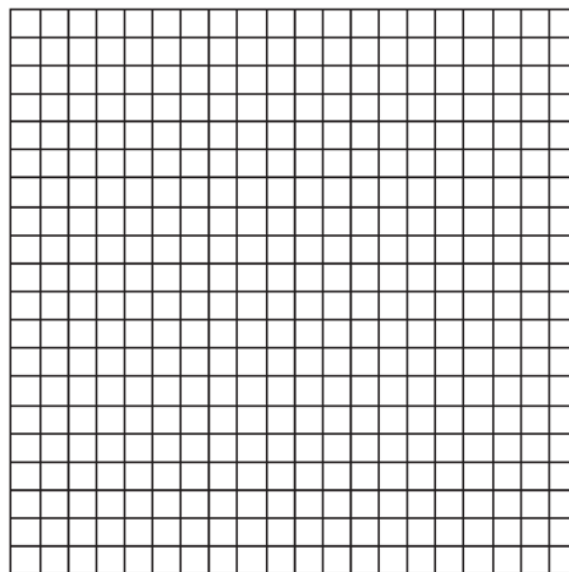
Identify the period of the graph and describe what the period represents in this context.

- 379 Algebraically determine the values of  $x$  that satisfy the system of equations below.

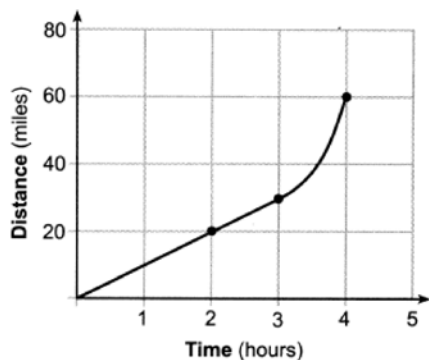
$$y = -2x + 1$$

$$y = -2x^2 + 3x + 1$$

- 382 The parabola  $y = -\frac{1}{20}(x - 3)^2 + 6$  has its focus at  $(3, 1)$ . Determine and state the equation of the directrix. (The use of the grid below is optional.)

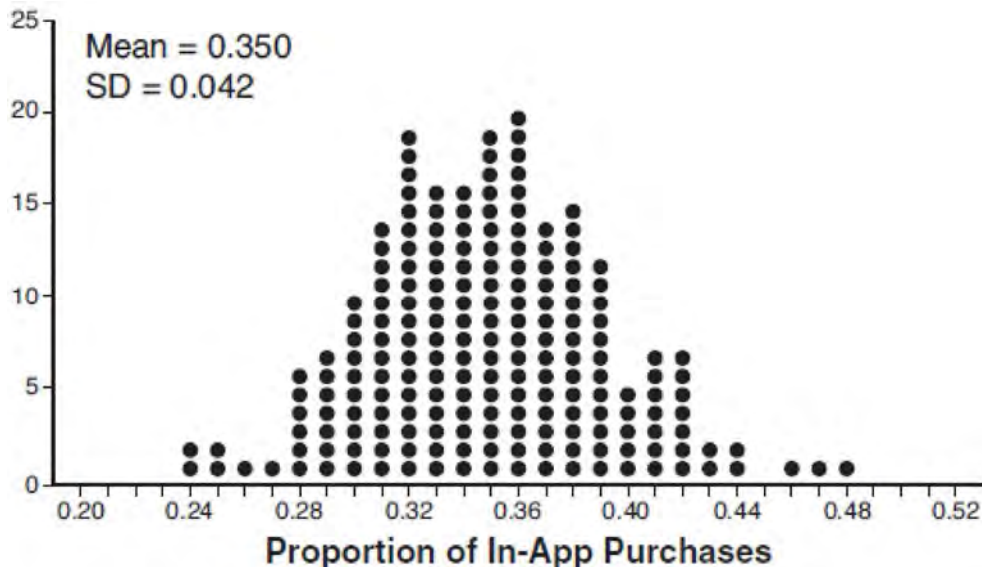


- 380 Determine the average rate of change, in mph, from 2 to 4 hours on the graph shown below.



- 381 Describe the transformation applied to the graph of  $p(x) = 2^x$  that forms the new function  $q(x) = 2^{x-3} + 4$ .

- 383 Some smart-phone applications contain "in-app" purchases, which allow users to purchase special content within the application. A random sample of 140 users found that 35 percent made in-app purchases. A simulation was conducted with 200 samples of 140 users assuming 35 percent of the samples make in-app purchases. The approximately normal results are shown below.



Considering the middle 95% of the data, determine the margin of error, to the *nearest hundredth*, for the simulated results. In the given context, explain what this value represents.

- 384 According to a study done at a hospital, the average weight of a newborn baby is 3.39 kg, with a standard deviation of 0.55 kg. The weights of all the newborns in this hospital closely follow a normal distribution. Last year, 9256 babies were born at this hospital. Determine, to the *nearest integer*, approximately how many babies weighed more than 4 kg.

- 386 Given  $P(A) = \frac{1}{3}$  and  $P(B) = \frac{5}{12}$ , where  $A$  and  $B$  are independent events, determine  $P(A \cap B)$ .

- 385 For  $n$  and  $p > 0$ , is the expression

$$\left( p^2 n^{\frac{1}{2}} \right)^8 \sqrt{p^5 n^4} \text{ equivalent to } p^{18} n^6 \sqrt{p}?$$

Justify your answer.

- 387 Mrs. Jones had hundreds of jelly beans in a bag that contained equal numbers of six different flavors. Her student randomly selected four jelly beans and they were all black licorice. Her student complained and said "What are the odds I got all of that kind?" Mrs. Jones replied, "simulate rolling a die 250 times and tell me if four black licorice jelly beans is unusual." Explain how this simulation could be used to solve the problem.

Algebra II 2 Point Regents Exam Questions

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388 Write  $(5 + 2yi)(4 - 3i) - (5 - 2yi)(4 - 3i)$  in  $a + bi$  form, where  $y$  is a real number.

389 The Wells family is looking to purchase a home in a suburb of Rochester with a 30-year mortgage that has an annual interest rate of 3.6%. The house the family wants to purchase is \$152,500 and they will make a \$15,250 down payment and borrow the remainder. Use the formula below to determine their monthly payment, to the *nearest dollar*.

$$M = \frac{P \left( \frac{r}{12} \right) \left( 1 + \frac{r}{12} \right)^n}{\left( 1 + \frac{r}{12} \right)^n - 1}$$

$M$  = monthly payment

$P$  = amount borrowed

$r$  = annual interest rate

$n$  = total number of monthly payments

390 A suburban high school has a population of 1376 students. The number of students who participate in sports is 649. The number of students who participate in music is 433. If the probability that a student participates in either sports or music is  $\frac{974}{1376}$ , what is the probability that a student participates in both sports and music?

391 The function  $M(t)$  represents the mass of radium over time,  $t$ , in years.

$$M(t) = 100e^{\frac{\left( \ln \frac{1}{2} \right) t}{1590}}$$

Determine if the function  $M(t)$  represents growth or decay. Explain your reasoning.

392 Point  $M \left( t, \frac{4}{7} \right)$  is located in the second quadrant on the unit circle. Determine the exact value of  $t$ .

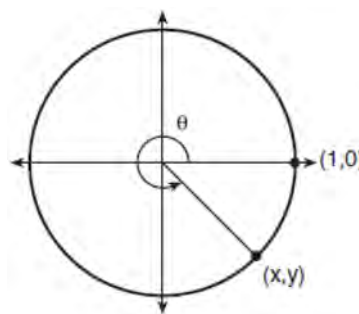
393 Explain why  $81^{\frac{3}{4}}$  equals 27.

394 Chuck's Trucking Company has decided to initiate an Employee of the Month program. To determine the recipient, they put the following sign on the back of each truck.



The driver who receives the highest number of positive comments will win the recognition. Explain *one* statistical bias in this data collection method.

395 Using the unit circle below, explain why  $\csc \theta = \frac{1}{y}$ .



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396 The  $x$ -value of which function's  $x$ -intercept is larger,  $f$  or  $h$ ? Justify your answer.

$$f(x) = \log(x - 4)$$

$x$	$h(x)$
-1	6
0	4
1	2
2	0
3	-2

397 Given:  $h(x) = \frac{2}{9}x^3 + \frac{8}{9}x^2 - \frac{16}{13}x + 2$

$$k(x) = -|0.7x| + 5$$

State the solutions to the equation  $h(x) = k(x)$ , rounded to the *nearest hundredth*.

398 Solve for  $x$ :  $\frac{1}{x} - \frac{1}{3} = -\frac{1}{3x}$

399 Simplify  $xi(i - 7i)^2$ , where  $i$  is the imaginary unit.

400 Use the properties of rational exponents to determine the value of  $y$  for the equation:

$$\frac{\sqrt[3]{x^8}}{(x^4)^{\frac{1}{3}}} = x^y, \quad x > 1$$

401 The weight of a bag of pears at the local market averages 8 pounds with a standard deviation of 0.5 pound. The weights of all the bags of pears at the market closely follow a normal distribution. Determine what percentage of bags, to the *nearest integer*, weighed *less* than 8.25 pounds.

402 Use an appropriate procedure to show that  $x - 4$  is a factor of the function  $f(x) = 2x^3 - 5x^2 - 11x - 4$ . Explain your answer.

403 Given the geometric series  $300 + 360 + 432 + 518.4 + \dots$ , write a geometric series formula,  $S_n$ , for the sum of the first  $n$  terms. Use the formula to find the sum of the first 10 terms, to the *nearest tenth*.

404 Erin and Christa were working on cubing binomials for math homework. Erin believed they could save time with a shortcut. She wrote down the rule below for Christa to follow.

$$(a + b)^3 = a^3 + b^3$$

Does Erin's shortcut always work? Justify your result algebraically.

405 Determine the quotient and remainder when  $(6a^3 + 11a^2 - 4a - 9)$  is divided by  $(3a - 2)$ . Express your answer in the form  $q(a) + \frac{r(a)}{d(a)}$ .

Algebra II 2 Point Regents Exam Questions

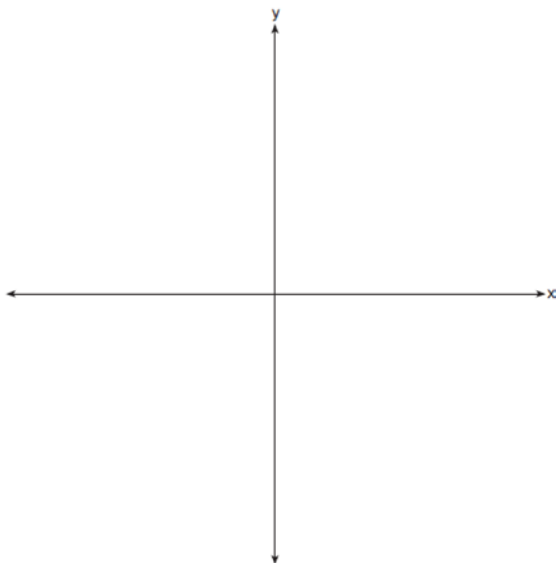
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406 Given  $\cos A = \frac{3}{\sqrt{10}}$  and  $\cot A = -3$ , determine the value of  $\sin A$  in radical form.

407 On July 21, 2016, the water level in Puget Sound, WA reached a high of 10.1 ft at 6 a.m. and a low of -2 ft at 12:30 p.m. Across the country in Long Island, NY, Shinnecock Bay's water level reached a high of 2.5 ft at 10:42 p.m. and a low of -0.1 ft at 5:31 a.m. The water levels of both locations are affected by the tides and can be modeled by sinusoidal functions. Determine the difference in amplitudes, in feet, for these two locations.

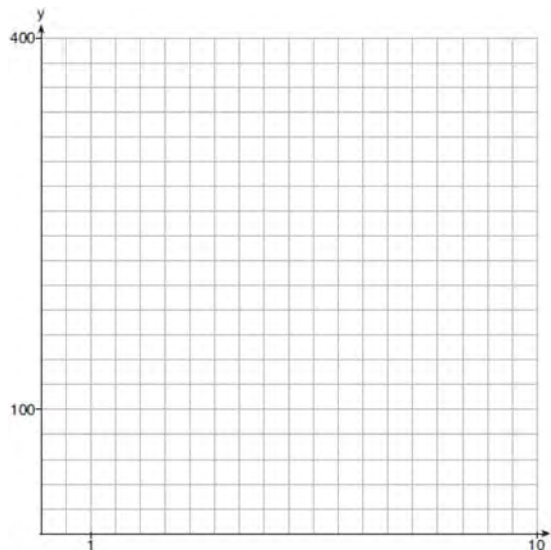
408 Algebraically solve for  $x$ :  $\frac{-3}{x+3} + \frac{1}{2} = \frac{x}{6} - \frac{1}{2}$

409 Sketch the graphs of  $r(x) = \frac{1}{x}$  and  $a(x) = |x| - 3$  on the set of axes below. Determine, to the *nearest tenth*, the positive solution of  $r(x) = a(x)$ .



410 Factor completely over the set of integers:  $-2x^4 + x^3 + 18x^2 - 9x$

411 Graph  $y = 400(.85)^{2x} - 6$  on the set of axes below.



412 The scores of a recent test taken by 1200 students had an approximately normal distribution with a mean of 225 and a standard deviation of 18. Determine the number of students who scored between 200 and 245.

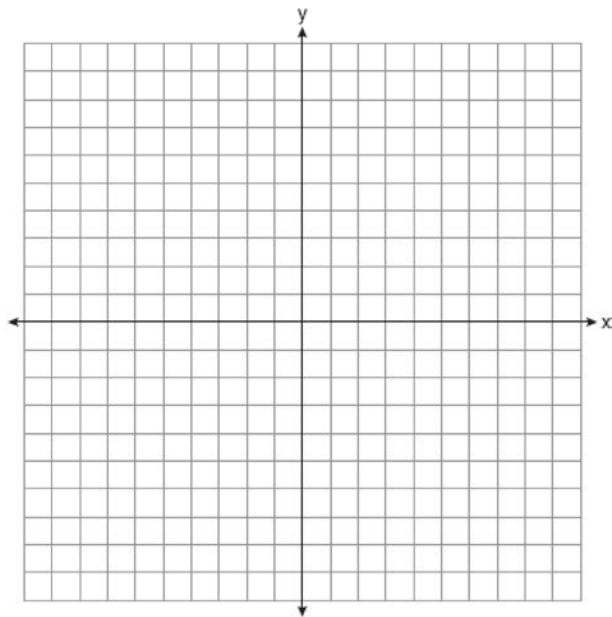
413 A house purchased 5 years ago for \$100,000 was just sold for \$135,000. Assuming exponential growth, approximate the annual growth rate, to the *nearest percent*.

414 Algebraically solve for  $x$ :  $\frac{7}{2x} - \frac{2}{x+1} = \frac{1}{4}$

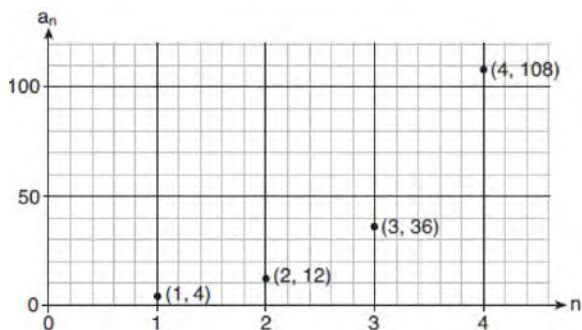
Algebra II 2 Point Regents Exam Questions

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- 415 On the axes below, graph *one* cycle of a cosine function with amplitude 3, period  $\frac{\pi}{2}$ , midline  $y = -1$ , and passing through the point  $(0, 2)$ .



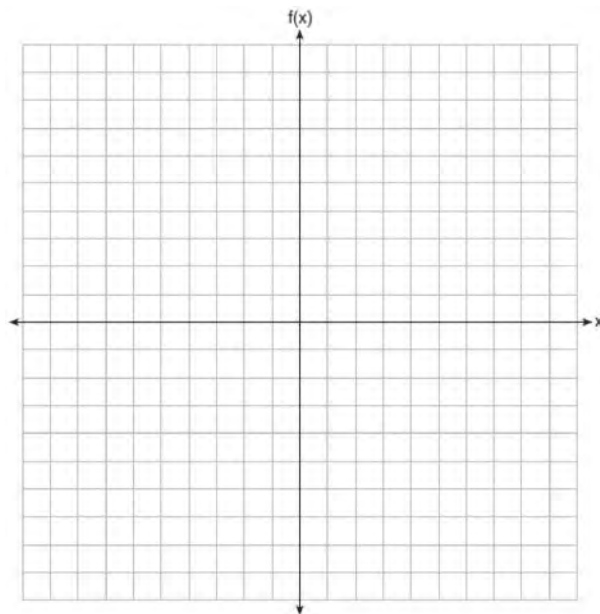
- 416 Write a recursive formula,  $a_n$ , to describe the sequence graphed below.



- 417 Solve algebraically for all values of  $x$ :

$$\sqrt{4x + 1} = 11 - x$$

- 418 Graph  $f(x) = \log_2(x + 6)$  on the set of axes below.



- 419 When the function  $p(x)$  is divided by  $x - 1$  the quotient is  $x^2 + 7 + \frac{5}{x - 1}$ . State  $p(x)$  in standard form.

- 420 Determine for which polynomial(s)  $(x + 2)$  is a factor. Explain your answer.

$$P(x) = x^4 - 3x^3 - 16x - 12$$

$$Q(x) = x^3 - 3x^2 - 16x - 12$$

- 421 The scores on a collegiate mathematics readiness assessment are approximately normally distributed with a mean of 680 and a standard deviation of 120. Determine the percentage of scores between 690 and 900, to the *nearest percent*.



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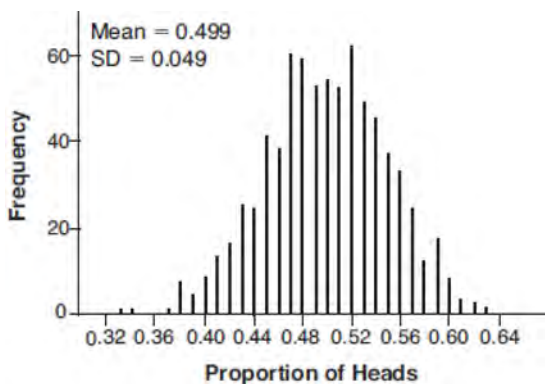
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- 422 The results of a survey of the student body at Central High School about television viewing preferences are shown below.

	Comedy Series	Drama Series	Reality Series	Total
Males	95	65	70	230
Females	80	70	110	260
Total	175	135	180	490

Are the events “student is a male” and “student prefers reality series” independent of each other? Justify your answer.

- 423 Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.



Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.

- 424 Justify why  $\frac{\sqrt[3]{x^2y^5}}{\sqrt[4]{x^3y^4}}$  is equivalent to  $x^{-\frac{1}{12}}y^{\frac{2}{3}}$  using

properties of rational exponents, where  $x \neq 0$  and  $y \neq 0$ .

- 425 The initial push of a child on a swing causes the swing to travel a total of 6 feet. Each successive swing travels 80% of the distance of the previous swing. Determine the total distance, to the *nearest hundredth of a foot*, a child travels in the first five swings.

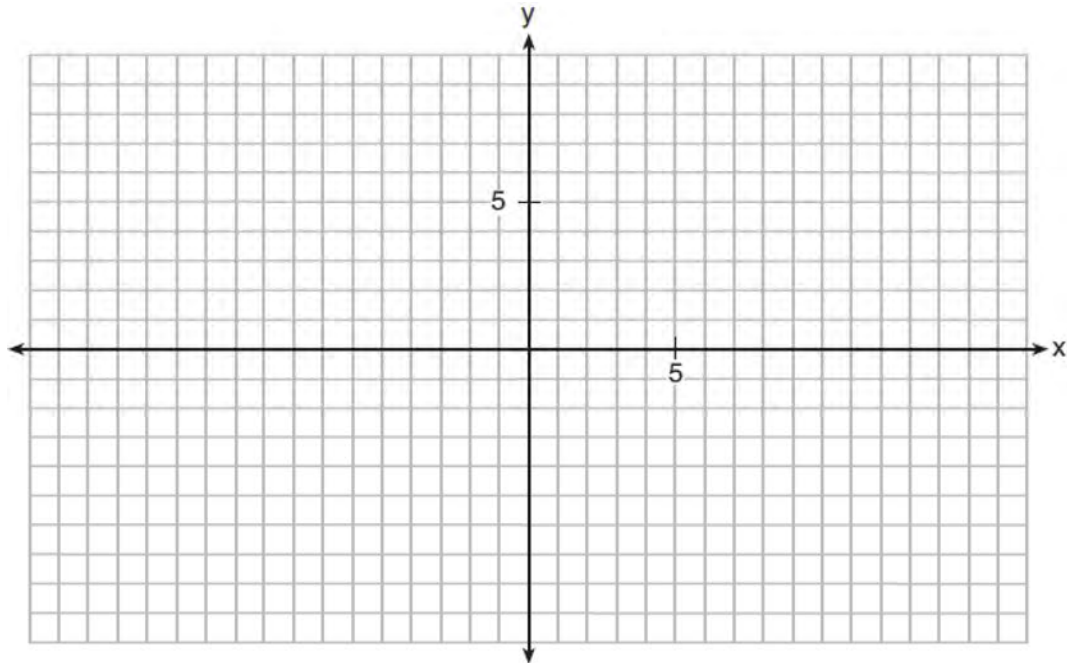
- 426 Express the fraction  $\frac{2x^{\frac{3}{2}}}{(16x^4)^{\frac{1}{4}}}$  in simplest radical form.

- 427 An orange-juice processing plant receives a truckload of oranges. The quality control team randomly chooses three pails of oranges, each containing 50 oranges, from the truckload. Identify the sample and the population in the given scenario. State *one* conclusion that the quality control team could make about the population if 5% of the sample was found to be unsatisfactory.

Algebra II 2 Point Regents Exam Questions

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428 On the grid below, graph the function  $y = \log_2(x - 3) + 1$



429 The relative frequency table shows the proportion of a population who have a given eye color and the proportion of the same population who wear glasses.

	<b>Wear Glasses</b>	<b>Don't Wear Glasses</b>
<b>Blue Eyes</b>	0.14	0.26
<b>Brown Eyes</b>	0.11	0.24
<b>Green Eyes</b>	0.10	0.15

Given the data, are the events of having blue eyes and wearing glasses independent? Justify your answer.

430 For  $x \neq 0$  and  $y \neq 0$ ,  $\sqrt[3]{81x^{15}y^9} = 3^a x^5 y^3$ .  
Determine the value of  $a$ .

432 Algebraically determine the solution set for the system of equations below.

$$y = 2x^2 - 7x + 4$$

$$y = 11 - 2x$$

431 Algebraically prove that the difference of the squares of any two consecutive integers is an odd integer.

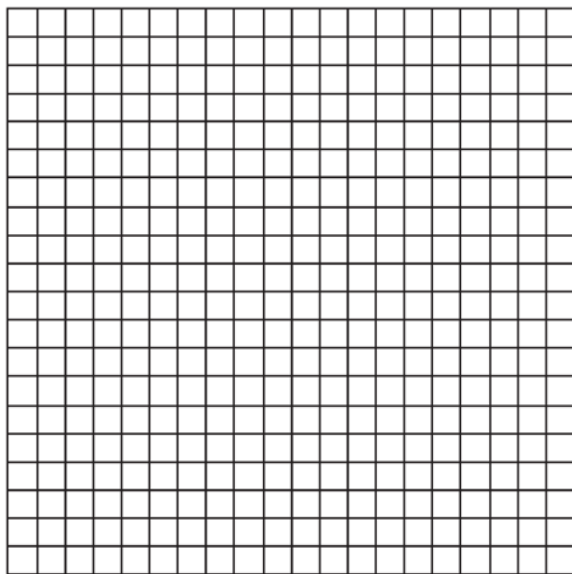
Algebra II 2 Point Regents Exam Questions

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- 433 Solve algebraically for all values of  $x$ :

$$\sqrt{x-4} + x = 6$$

- 434 The zeros of a quartic polynomial function  $h$  are  $-1, \pm 2$ , and  $3$ . Sketch a graph of  $y = h(x)$  on the grid below.



- 435 Explain what a rational exponent, such as  $\frac{5}{2}$  means.

Use this explanation to evaluate  $9^{\frac{5}{2}}$ .

- 436 Given that  $\left(\frac{\frac{17}{8}}{y^{\frac{5}{4}}}\right)^{-4} = y^n$ , where  $y > 0$ , determine

the value of  $n$ .

- 437 An angle,  $\theta$ , is in standard position and its terminal side passes through the point  $(2, -1)$ . Find the *exact* value of  $\sin \theta$ .

- 438 Using the identity  $\sin^2 \theta + \cos^2 \theta = 1$ , find the value of  $\tan \theta$ , to the *nearest hundredth*, if  $\cos \theta$  is  $-0.7$  and  $\theta$  is in Quadrant II.

- 439 A formula for work problems involving two people is shown below.

$$\frac{1}{t_1} + \frac{1}{t_2} = \frac{1}{t_b}$$

$t_1$  = the time taken by the first person to complete the job

$t_2$  = the time taken by the second person to complete the job

$t_b$  = the time it takes for them working together to complete the job

Fred and Barney are carpenters who build the same model desk. It takes Fred eight hours to build the desk while it only takes Barney six hours. Write an equation that can be used to find the time it would take both carpenters working together to build a desk. Determine, to the *nearest tenth of an hour*, how long it would take Fred and Barney working together to build a desk.

- 440 For the function  $f(x) = (x - 3)^3 + 1$ , find  $f^{-1}(x)$ .

- 441 Given  $a > 0$ , solve the equation  $a^{x+1} = \sqrt[3]{a^2}$  for  $x$  algebraically.

- 442 While experimenting with her calculator, Candy creates the sequence  $4, 9, 19, 39, 79, \dots$ . Write a recursive formula for Candy's sequence. Determine the eighth term in Candy's sequence.

Algebra II 2 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

443 Consider the data in the table below.

<b>x</b>	1	2	3	4	5	6
<b>y</b>	3.9	6	11	18.1	28	40.3

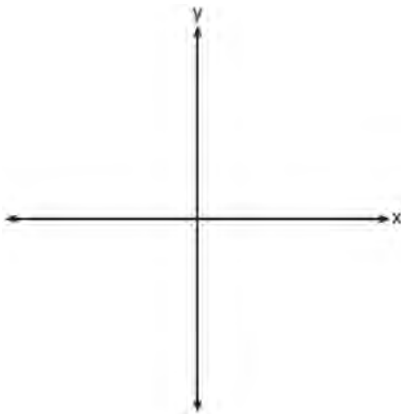
State an exponential regression equation to model these data, rounding all values to the *nearest thousandth*.

444 A survey about television-viewing preferences was given to randomly selected freshmen and seniors at Fairport High School. The results are shown in the table below.

Favorite Type of Program			
	Sports	Reality Show	Comedy Series
Senior	83	110	67
Freshmen	119	103	54

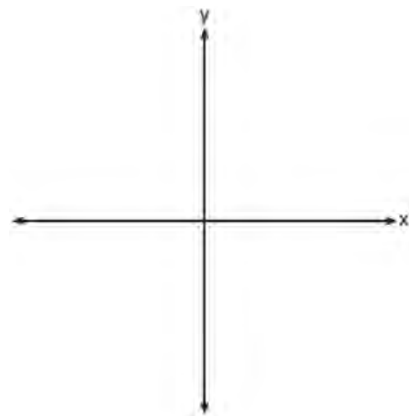
A student response is selected at random from the results. State the *exact* probability the student response is from a freshman, given the student prefers to watch reality shows on television.

445 On the axes below, sketch a possible function  $p(x) = (x - a)(x - b)(x + c)$ , where  $a$ ,  $b$ , and  $c$  are positive,  $a > b$ , and  $p(x)$  has a positive  $y$ -intercept of  $d$ . Label all intercepts.



447 In New York State, the minimum wage has grown exponentially. In 1966, the minimum wage was \$1.25 an hour and in 2015, it was \$8.75. Algebraically determine the rate of growth to the *nearest percent*.

448 The zeros of a quartic polynomial function are 2,  $-2$ , 4, and  $-4$ . Use the zeros to construct a possible sketch of the function, on the set of axes below.



446 Factor the expression  $x^3 - 2x^2 - 9x + 18$  completely.

Algebra II 2 Point Regents Exam Questions

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449 Rowan is training to run in a race. He runs 15 miles in the first week, and each week following, he runs 3% more than the week before. Using a geometric series formula, find the total number of miles Rowan runs over the first ten weeks of training, rounded to the *nearest thousandth*.

450 Given the equal terms  $\sqrt[3]{x^5}$  and  $y^{\frac{5}{6}}$ , determine and state  $y$ , in terms of  $x$ .

451 Over the set of integers, factor the expression  $4x^3 - x^2 + 16x - 4$  completely.

452 Algebraically determine whether the function  $j(x) = x^4 - 3x^2 - 4$  is odd, even, or neither.

453 Algebraically determine the zeros of the function below.

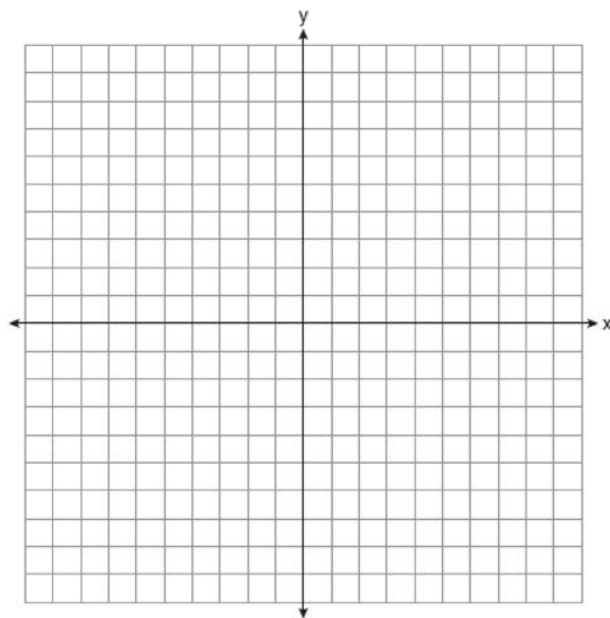
$$r(x) = 3x^3 + 12x^2 - 3x - 12$$

454 Given  $\tan \theta = \frac{7}{24}$ , and  $\theta$  terminates in Quadrant III, determine the value of  $\cos \theta$ .

455 Express  $(1 - i)^3$  in  $a + bi$  form.

456 Over the set of integers, completely factor  $x^4 - 5x^2 + 4$ .

457 Graph  $y = x^3 - 4x^2 + 2x + 7$  on the set of axes below.



458 Write  $\sqrt[3]{x} \cdot \sqrt{x}$  as a single term with a rational exponent.

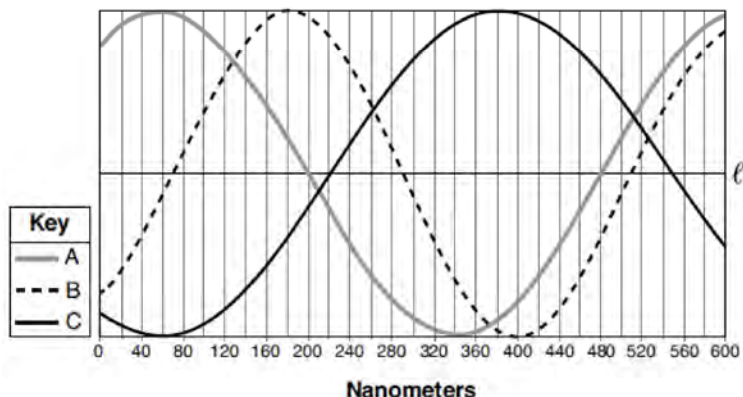
459 The table below shows the results of gender and music preference. Based on these data, determine if the events "the person is female" and "the person prefers classic rock" are independent of each other. Justify your answer.

	Rap	Techno	Classic Rock	Classical
Male	39	17	42	12
Female	17	37	36	15

Algebra II 2 Point Regents Exam Questions

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- 460 Visible light can be represented by sinusoidal waves. Three visible light waves are shown in the graph below. The midline of each wave is labeled  $\ell$ .



Based on the graph, which light wave has the longest period? Justify your answer.

- 461 Consider the function  $h(x) = 2\sin(3x) + 1$  and the function  $q$  represented in the table below.

$x$	$q(x)$
-2	-8
-1	0
0	0
1	-2
2	0

Determine which function has the *smaller* minimum value for the domain  $[-2, 2]$ . Justify your answer.

- 462 Determine if  $x - 5$  is a factor of  $2x^3 - 4x^2 - 7x - 10$ . Explain your answer.
- 463 The directrix of the parabola  $12(y + 3) = (x - 4)^2$  has the equation  $y = -6$ . Find the coordinates of the focus of the parabola.
- 464 Show why  $x - 3$  is a factor of  $m(x) = x^3 - x^2 - 5x - 3$ . Justify your answer.
- 465 Given  $r(x) = x^3 - 4x^2 + 4x - 6$ , find the value of  $r(2)$ . What does your answer tell you about  $x - 2$  as a factor of  $r(x)$ ? Explain.
- 466 The recursive formula to describe a sequence is shown below.
- $$a_1 = 3$$
- $$a_n = 1 + 2a_{n-1}$$
- State the first four terms of this sequence. Can this sequence be represented using an explicit geometric formula? Justify your answer.

Algebra II 2 Point Regents Exam Questions

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- 467 The distance needed to stop a car after applying the brakes varies directly with the square of the car's speed. The table below shows stopping distances for various speeds.

<b>Speed (mph)</b>	10	20	30	40	50	60	70
<b>Distance (ft)</b>	6.25	25	56.25	100	156.25	225	306.25

Determine the average rate of change in braking distance, in ft/mph, between one car traveling at 50 mph and one traveling at 70 mph. Explain what this rate of change means as it relates to braking distance.

- 468 Write the expression  $A(x) \cdot B(x) - 3C(x)$  as a polynomial in standard form.

$$A(x) = x^3 + 2x - 1$$

$$B(x) = x^2 + 7$$

$$C(x) = x^4 - 5x$$

- 469 Over the set of integers, factor the expression  $x^4 - 4x^2 - 12$ .

- 470 A study was designed to test the effectiveness of a new drug. Half of the volunteers received the drug. The other half received a sugar pill. The probability of a volunteer receiving the drug and getting well was 40%. What is the probability of a volunteer getting well, given that the volunteer received the drug?

- 471 Biologists are studying a new bacterium. They create a culture with 100 of the bacteria and anticipate that the number of bacteria will double every 30 hours. Write an equation for the number of bacteria,  $B$ , in terms of the number of hours,  $t$ , since the experiment began.

- 472 The volume of air in a person's lungs, as the person breathes in and out, can be modeled by a sine graph. A scientist is studying the differences in this volume for people at rest compared to people told to take a deep breath. When examining the graphs, should the scientist focus on the amplitude, period, or midline? Explain your choice.

- 473 Explain how  $\left(3^{\frac{1}{5}}\right)^2$  can be written as the equivalent radical expression  $\sqrt[5]{9}$ .

- 474 Researchers in a local area found that the population of rabbits with an initial population of 20 grew continuously at the rate of 5% per month. The fox population had an initial value of 30 and grew continuously at the rate of 3% per month. Find, to the *nearest tenth of a month*, how long it takes for these populations to be equal.

- 475 Kenzie believes that for  $x \geq 0$ , the expression  $\left(\sqrt[7]{x^2}\right)\left(\sqrt[5]{x^3}\right)$  is equivalent to  $\sqrt[35]{x^6}$ . Is she correct? Justify your response algebraically.

Algebra II 2 Point Regents Exam Questions

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476 The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

Month	Hours of Daylight
Jan.	9.4
Feb.	10.6
March	11.9
April	13.9
May	14.7
June	15.4
July	15.1
Aug.	13.9
Sept.	12.5
Oct.	11.1
Nov.	9.7
Dec.	9.0

Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st? Interpret what this means in the context of the problem.

477 A runner is using a nine-week training app to prepare for a "fun run." The table below represents the amount of the program completed,  $A$ , and the distance covered in a session,  $D$ , in miles.

<b>A</b>	$\frac{4}{9}$	$\frac{5}{9}$	$\frac{6}{9}$	$\frac{8}{9}$	1
<b>D</b>	2	2	2.25	3	3.25

Based on these data, write an exponential regression equation, rounded to the *nearest thousandth*, to model the distance the runner is able to complete in a session as she continues through the nine-week program.

478 Explain how  $(-8)^{\frac{4}{3}}$  can be evaluated using properties of rational exponents to result in an integer answer.

479 Solve the equation  $2x^2 + 5x + 8 = 0$ . Express the answer in  $a + bi$  form.

480 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, ...

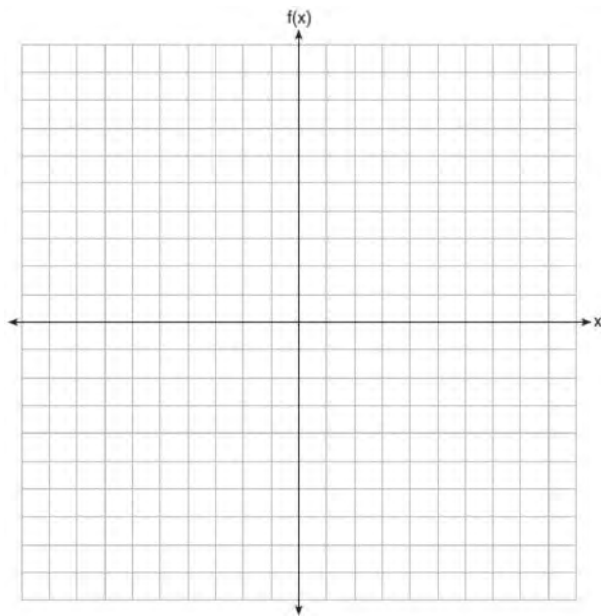
481 At Andrew Jackson High School, students are only allowed to enroll in AP U.S. History if they have already taken AP World History or AP European History. Out of 825 incoming seniors, 165 took AP World History, 66 took AP European History, and 33 took both. Given this information, determine the probability a randomly selected incoming senior is allowed to enroll in AP U.S. History.



Algebra II 2 Point Regents Exam Questions

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- 482 On the grid below, graph the function  $f(x) = x^3 - 6x^2 + 9x + 6$  on the domain  $-1 \leq x \leq 4$ .



- 483 Elizabeth waited for 6 minutes at the drive thru at her favorite fast-food restaurant the last time she visited. She was upset about having to wait that long and notified the manager. The manager assured her that her experience was very unusual and that it would not happen again. A study of customers commissioned by this restaurant found an approximately normal distribution of results. The mean wait time was 226 seconds and the standard deviation was 38 seconds. Given these data, and using a 95% level of confidence, was Elizabeth's wait time unusual? Justify your answer.

- 484 Solve algebraically for all values of  $x$ :  
 $\sqrt{x-5} + x = 7$

- 485 Solve algebraically for  $n$ :  $\frac{2}{n^2} + \frac{3}{n} = \frac{4}{n^2}$

- 486 Elizabeth tried to find the product of  $(2 + 4i)$  and  $(3 - i)$ , and her work is shown below.

$$\begin{aligned} &(2 + 4i)(3 - i) \\ &= 6 - 2i + 12i - 4i^2 \\ &= 6 + 10i - 4i^2 \\ &= 6 + 10i - 4(1) \\ &= 6 + 10i - 4 \\ &= 2 + 10i \end{aligned}$$

Identify the error in the process shown and determine the correct product of  $(2 + 4i)$  and  $(3 - i)$ .

- 487 Natalia's teacher has given her the following information about angle  $\theta$ .

- $\pi < \theta < 2\pi$
- $\cos \theta = \frac{\sqrt{3}}{4}$

Explain how Natalia can determine if the value of  $\tan \theta$  is positive or negative.

- 488 The average monthly high temperature in Buffalo, in degrees Fahrenheit, can be modeled by the function  $B(t) = 25.29 \sin(0.4895t - 1.9752) + 55.2877$ , where  $t$  is the month number (January = 1). State, to the nearest tenth, the average monthly rate of temperature change between August and November. Explain its meaning in the given context.

- 489 Write  $-\frac{1}{2}i^3(\sqrt{-9} - 4) - 3i^2$  in simplest  $a + bi$  form.

Algebra II 2 Point Regents Exam Questions

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490 The results of a poll of 200 students are shown in the table below:

	Preferred Music Style		
	Techno	Rap	Country
Female	54	25	27
Male	36	40	18

For this group of students, do these data suggest that gender and preferred music styles are independent of each other? Justify your answer.

491 A cup of coffee is left out on a countertop to cool. The table below represents the temperature,  $F(t)$ , in degrees Fahrenheit, of the coffee after it is left out for  $t$  minutes.

$t$	0	5	10	15	20	25
$F(t)$	180	144	120	104	93.3	86.2

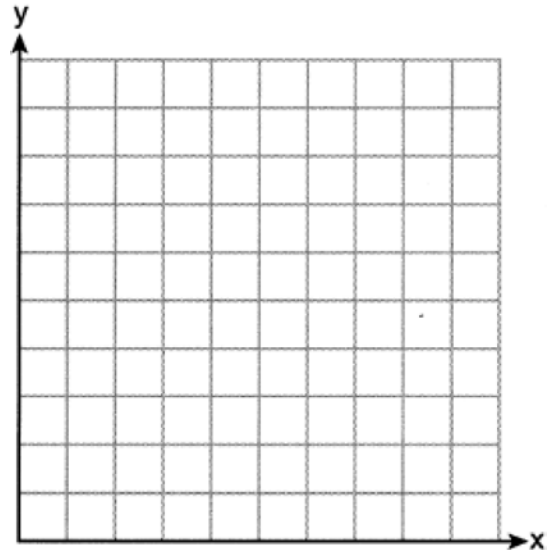
Based on these data, write an exponential regression equation,  $F(t)$ , to model the temperature of the coffee. Round all values to the *nearest thousandth*.

492 Given events  $A$  and  $B$ , such that  $P(A) = 0.6$ ,  $P(B) = 0.5$ , and  $P(A \cup B) = 0.8$ , determine whether  $A$  and  $B$  are independent or dependent.

495 Graph  $y = 2 \cos\left(\frac{1}{2}x\right) + 5$  on the interval  $[0, 2\pi]$ , using the axes below.

493 Does the equation  $x^2 - 4x + 13 = 0$  have imaginary solutions? Justify your answer.

494 The probability that a resident of a housing community opposes spending money for community improvement on plumbing issues is 0.8. The probability that a resident favors spending money on improving walkways given that the resident opposes spending money on plumbing issues is 0.85. Determine the probability that a randomly selected resident opposes spending money on plumbing issues and favors spending money on walkways.



Algebra II 2 Point Regents Exam Questions

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- 496 Verify the following Pythagorean identity for all values of  $x$  and  $y$ :

$$(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$$

- 497 On the grid below, sketch a cubic polynomial whose zeros are 1, 3, and -2.



- 498 Solve the following system of equations algebraically.  $x^2 + y^2 = 400$

$$y = x - 28$$

- 499 Algebraically prove that  $\frac{x^3 + 9}{x^3 + 8} = 1 + \frac{1}{x^3 + 8}$ , where  $x \neq -2$ .

- 500 Rewrite the expression

$(4x^2 + 5x)^2 - 5(4x^2 + 5x) - 6$  as a product of four linear factors.

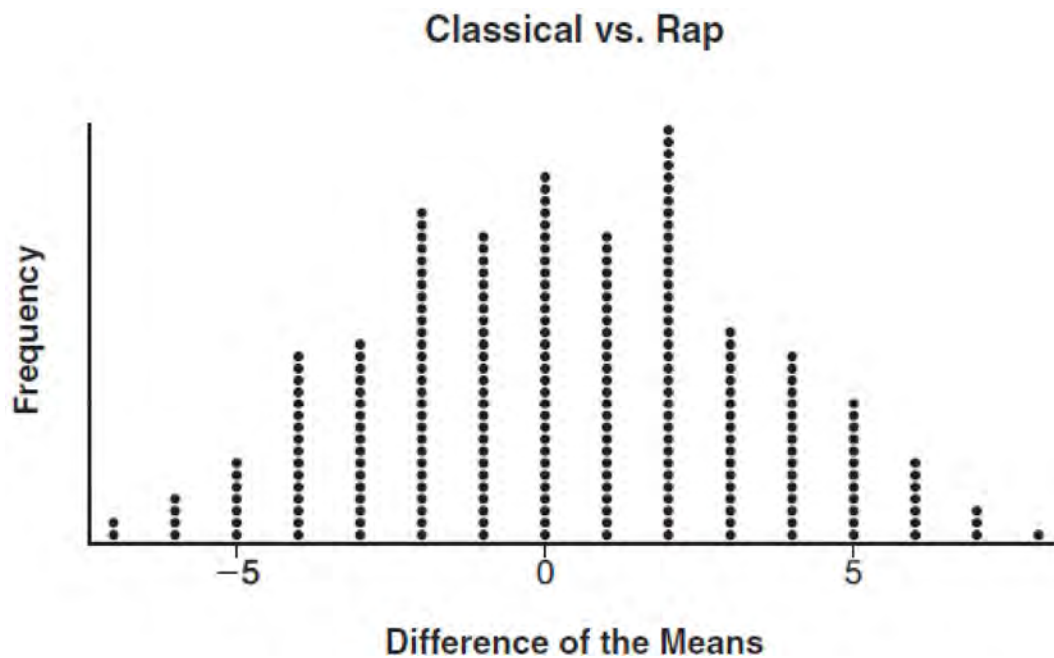
**Algebra II 4 Point Regents Exam Questions**

501 To determine if the type of music played while taking a quiz has a relationship to results, 16 students were randomly assigned to either a room softly playing classical music or a room softly playing rap music. The results on the quiz were as follows:

Classical: 74, 83, 77, 77, 84, 82, 90, 89

Rap: 77, 80, 78, 74, 69, 72, 78, 69

John correctly rounded the difference of the means of his experimental groups as 7. How did John obtain this value and what does it represent in the given context? Justify your answer. To determine if there is any significance in this value, John rerandomized the 16 scores into two groups of 8, calculated the difference of the means, and simulated this process 250 times as shown below.



Does the simulation support the theory that there may be a significant difference in quiz scores? Explain.

502 Solve the following system of equations algebraically for all values of  $x$ ,  $y$ , and  $z$ :

$$2x + 3y - 4z = -1$$

$$x - 2y + 5z = 3$$

$$-4x + y + z = 16$$

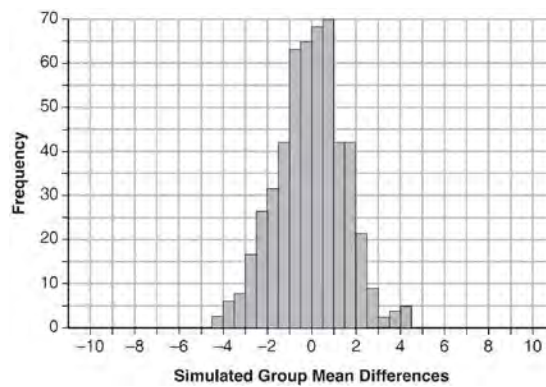
Algebra II 4 Point Regents Exam Questions

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- 503 Seventy-two students are randomly divided into two equally-sized study groups. Each member of the first group (group 1) is to meet with a tutor after school twice each week for one hour. The second group (group 2), is given an online subscription to a tutorial account that they can access for a maximum of two hours each week. Students in both groups are given the same tests during the year. A summary of the two groups' final grades is shown below:

	Group 1	Group 2
$\bar{x}$	80.16	83.8
$S_x$	6.9	5.2

Calculate the mean difference in the final grades (group 1 – group 2) and explain its meaning in the context of the problem. A simulation was conducted in which the students' final grades were rerandomized 500 times. The results are shown below.



Use the simulation to determine if there is a significant difference in the final grades. Explain your answer.

- 504 The height,  $h(t)$  in cm, of a piston, is given by the equation  $h(t) = 12 \cos\left(\frac{\pi}{3} t\right) + 8$ , where  $t$  represents the number of seconds since the measurements began. Determine the average rate of change, in cm/sec, of the piston's height on the interval  $1 \leq t \leq 2$ . At what value(s) of  $t$ , to the nearest tenth of a second, does  $h(t) = 0$  in the interval  $1 \leq t \leq 5$ ? Justify your answer.
- 505 a) Algebraically determine the roots, in simplest  $a + bi$  form, to the equation below.  

$$x^2 - 2x + 7 = 4x - 10$$
 b) Consider the system of equations below.  

$$y = x^2 - 2x + 7$$

$$y = 4x - 10$$
 The graph of this system confirms the solution from part a is imaginary. Explain why.

Algebra II 4 Point Regents Exam Questions

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- 506 Using a microscope, a researcher observed and recorded the number of bacteria spores on a large sample of uniformly sized pieces of meat kept at room temperature. A summary of the data she recorded is shown in the table below.

Hours (x)	Average Number of Spores (y)
0	4
0.5	10
1	15
2	60
3	260
4	1130
6	16,380

Using these data, write an exponential regression equation, rounding all values to the *nearest thousandth*. The researcher knows that people are likely to suffer from food-borne illness if the number of spores exceeds 100. Using the exponential regression equation, determine the maximum amount of time, to the *nearest quarter hour*, that the meat can be kept at room temperature safely.

- 507 Using the formula below, determine the monthly payment on a 5-year car loan with a monthly percentage rate of 0.625% for a car with an original cost of \$21,000 and a \$1000 down payment, to the *nearest cent*.

$$P_n = PMT \left( \frac{1 - (1 + i)^{-n}}{i} \right)$$

$P_n$  = present amount borrowed

$n$  = number of monthly pay periods

$PMT$  = monthly payment

$i$  = interest rate per month

The affordable monthly payment is \$300 for the same time period. Determine an appropriate down payment, to the *nearest dollar*.

- 508 Solve the given equation algebraically for all values of  $x$ .  $3\sqrt{x} - 2x = -5$

- 509 Evaluate  $j(-1)$  given

$j(x) = 2x^4 - x^3 - 35x^2 + 16x + 48$ . Explain what your answer tells you about  $x + 1$  as a factor. Algebraically find the remaining zeros of  $j(x)$ .

- 510 A population of 950 bacteria grows continuously at a rate of 4.75% per day. Write an exponential function,  $N(t)$ , that represents the bacterial population after  $t$  days and explain the reason for your choice of base. Determine the bacterial population after 36 hours, to the *nearest bacterium*.

- 511 Solve the following system of equations algebraically for all values of  $x$ ,  $y$ , and  $z$ :

$$x + y + z = 1$$

$$2x + 4y + 6z = 2$$

$$-x + 3y - 5z = 11$$

Algebra II 4 Point Regents Exam Questions

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- 512 After sitting out of the refrigerator for a while, a turkey at room temperature ( $68^{\circ}\text{F}$ ) is placed into an oven at 8 a.m., when the oven temperature is  $325^{\circ}\text{F}$ . Newton's Law of Heating explains that the temperature of the turkey will increase proportionally to the difference between the temperature of the turkey and the temperature of the oven, as given by the formula below:

$$T = T_a + (T_0 - T_a)e^{-kt}$$

$T_a$  = the temperature surrounding the object

$T_0$  = the initial temperature of the object

$t$  = the time in hours

$T$  = the temperature of the object after  $t$  hours

$k$  = decay constant

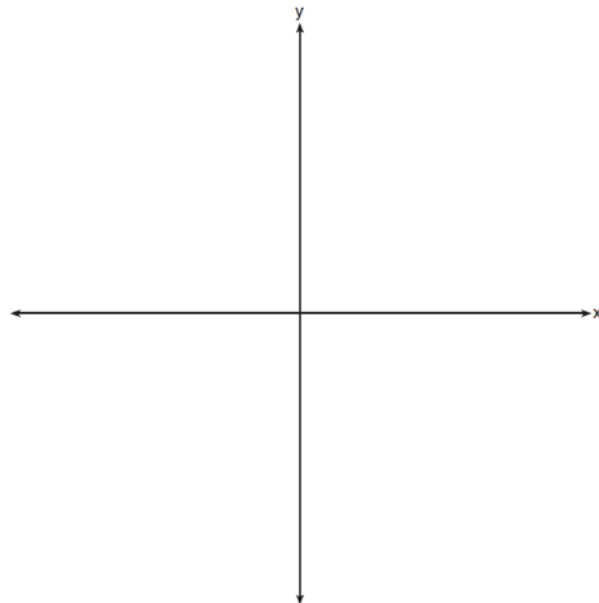
The turkey reaches the temperature of approximately  $100^{\circ}\text{F}$  after 2 hours. Find the value of  $k$ , to the *nearest thousandth*, and write an equation to determine the temperature of the turkey after  $t$  hours. Determine the Fahrenheit temperature of the turkey, to the *nearest degree*, at 3 p.m.

- 513 A Foucault pendulum can be used to demonstrate that the Earth rotates. The time,  $t$ , in seconds, that it takes for one swing or period of the pendulum

can be modeled by the equation  $t = 2\pi\sqrt{\frac{L}{g}}$  where

$L$  is the length of the pendulum in meters and  $g$  is a constant of  $9.81\text{ m/s}^2$ . The first Foucault pendulum was constructed in 1851 and has a pendulum length of 67 m. Determine, to the *nearest tenth of a second*, the time it takes this pendulum to complete one swing. Another Foucault pendulum at the United Nations building takes 9.6 seconds to complete one swing. Determine, to the *nearest tenth of a meter*, the length of this pendulum.

- 514 a) On the axes below, sketch *at least one* cycle of a sine curve with an amplitude of 2, a midline at  $y = -\frac{3}{2}$ , and a period of  $2\pi$ .



- b) Explain any differences between a sketch of  $y = 2\sin\left(x - \frac{\pi}{3}\right) - \frac{3}{2}$  and the sketch from part a.

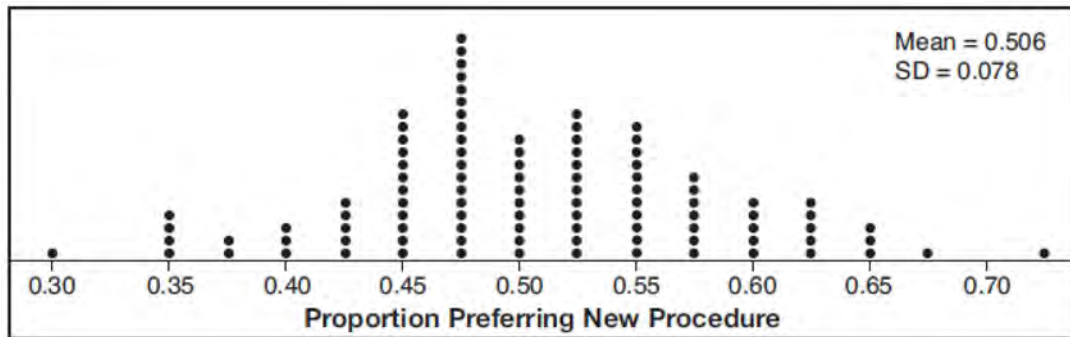
- 515 Given  $z(x) = 6x^3 + bx^2 - 52x + 15$ ,  $z(2) = 35$ , and  $z(-5) = 0$ , algebraically determine all the zeros of  $z(x)$ .

- 516 Solve the system of equations algebraically.

$$x^2 + y^2 = 25$$

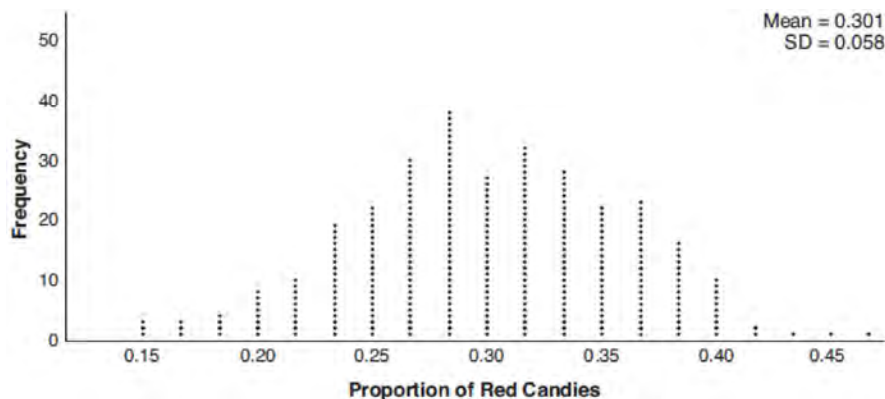
$$y + 5 = 2x$$

- 517 Charlie's Automotive Dealership is considering implementing a new check-in procedure for customers who are bringing their vehicles for routine maintenance. The dealership will launch the procedure if 50% or more of the customers give the new procedure a favorable rating when compared to the current procedure. The dealership devises a simulation based on the minimal requirement that 50% of the customers prefer the new procedure. Each dot on the graph below represents the proportion of the customers who preferred the new check-in procedure, each of sample size 40, simulated 100 times.



Assume the set of data is approximately normal and the dealership wants to be 95% confident of its results. Determine an interval containing the plausible sample values for which the dealership will launch the new procedure. Round your answer to the *nearest hundredth*. Forty customers are selected randomly to undergo the new check-in procedure and the proportion of customers who prefer the new procedure is 32.5%. The dealership decides *not* to implement the new check-in procedure based on the results of the study. Use statistical evidence to explain this decision.

- 518 Mary bought a pack of candy. The manufacturer claims that 30% of the candies manufactured are red. In her pack, 14 of the 60 candies are red. She ran a simulation of 300 samples, assuming the manufacturer is correct. The results are shown below.



Based on the simulation, determine the middle 95% of plausible values that the proportion of red candies in a pack is within. Based on the simulation, is it unusual that Mary's pack had 14 red candies out of a total of 60? Explain.



Algebra II 4 Point Regents Exam Questions

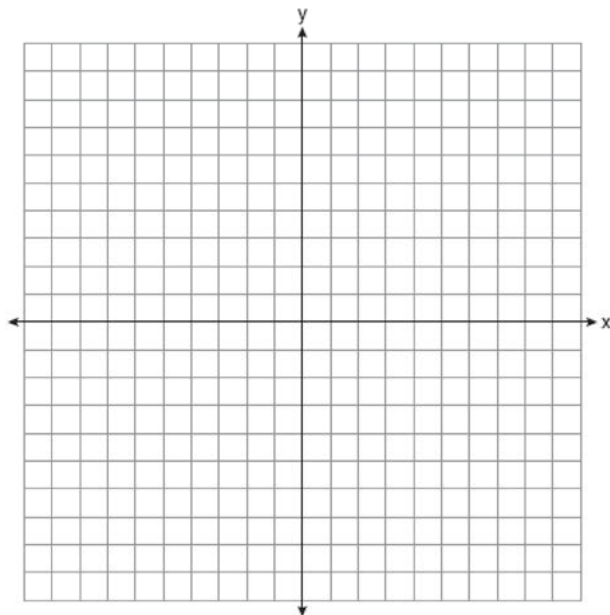
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- 519 Juan and Felipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

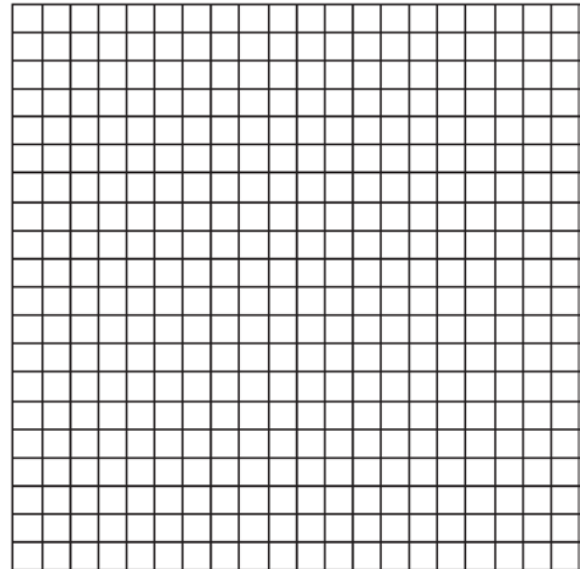
	Juan Wins	Felipe Wins
Short Practice Time	8	10
Long Practice Time	15	12

Given that the practice time was long, determine the exact probability that Felipe wins the next match. Determine whether or not the two events “Felipe wins” and “long practice time” are independent. Justify your answer.

- 520 Find algebraically the zeros for  $p(x) = x^3 + x^2 - 4x - 4$ . On the set of axes below, graph  $y = p(x)$ .



- 522 Write an equation for a sine function with an amplitude of 2 and a period of  $\frac{\pi}{2}$ . On the grid below, sketch the graph of the equation in the interval 0 to  $2\pi$ .



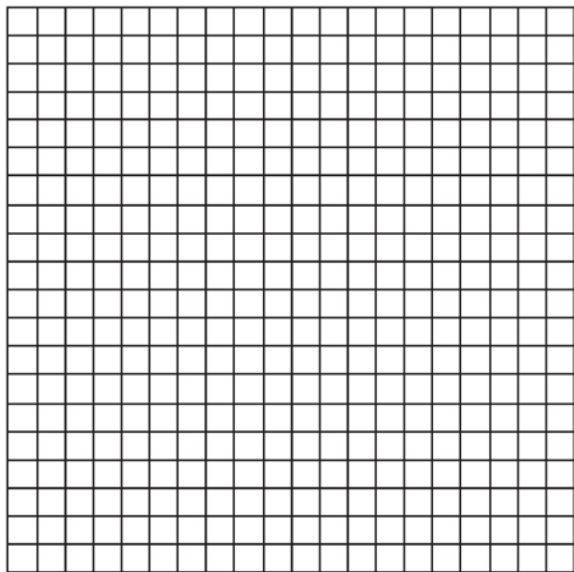
- 521 Given  $f(x) = 3x^3 - 4x^2 + 2x - 1$  and  $g(x) = x - 4$ , state the quotient and remainder of  $\frac{f(x)}{g(x)}$ , in the form  $q(x) + \frac{r(x)}{g(x)}$ . Is  $x = 4$  a root of  $f(x)$ ? Explain your answer.

- 523 Solve for all values of  $p$ :  $\frac{3p}{p-5} - \frac{2}{p+3} = \frac{p}{p+3}$

Algebra II 4 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 524 Determine an equation for the parabola with focus  $(4, -1)$  and directrix  $y = -5$ . (Use of the grid below is optional.)



- 525 Solve the system of equations shown below algebraically.

$$(x - 3)^2 + (y + 2)^2 = 16$$

$$2x + 2y = 10$$

- 526 The guidance department has reported that of the senior class, 2.3% are members of key club,  $K$ , 8.6% are enrolled in AP Physics,  $P$ , and 1.9% are in both. Determine the probability of  $P$  given  $K$ , to the *nearest tenth of a percent*. The principal would like a basic interpretation of these results. Write a statement relating your calculated probabilities to student enrollment in the given situation.

- 527 Given  $a(x) = x^4 + 2x^3 + 4x - 10$  and  $b(x) = x + 2$ , determine  $\frac{a(x)}{b(x)}$  in the form  $q(x) + \frac{r(x)}{b(x)}$ . Is  $b(x)$  a factor of  $a(x)$ ? Explain.

- 528 Monthly mortgage payments can be found using the formula below:

$$M = \frac{P \left( \frac{r}{12} \right) \left( 1 + \frac{r}{12} \right)^n}{\left( 1 + \frac{r}{12} \right)^n - 1}$$

$M$  = monthly payment

$P$  = amount borrowed

$r$  = annual interest rate

$n$  = number of monthly payments

The Banks family would like to borrow \$120,000 to purchase a home. They qualified for an annual interest rate of 4.8%. Algebraically determine the *fewest* number of whole years the Banks family would need to include in the mortgage agreement in order to have a monthly payment of no more than \$720.

- 529 Jim is looking to buy a vacation home for \$172,600 near his favorite southern beach. The formula to compute a mortgage payment,  $M$ , is

$$M = P \cdot \frac{r(1+r)^N}{(1+r)^N - 1}$$

where  $P$  is the principal

amount of the loan,  $r$  is the monthly interest rate, and  $N$  is the number of monthly payments. Jim's bank offers a monthly interest rate of 0.305% for a 15-year mortgage. With no down payment, determine Jim's mortgage payment, rounded to the *nearest dollar*. Algebraically determine and state the down payment, rounded to the *nearest dollar*, that Jim needs to make in order for his mortgage payment to be \$1100.

- 530 Determine, to the *nearest tenth of a year*, how long it would take an investment to double at a  $3\frac{3}{4}\%$  interest rate, compounded continuously.

Algebra II 4 Point Regents Exam Questions

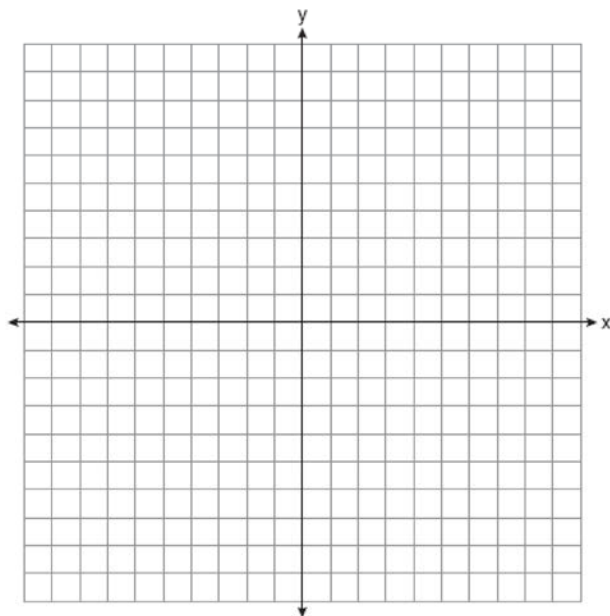
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531 The table below gives air pressures in kPa at selected altitudes above sea level measured in kilometers.

<b>x</b>	<b>Altitude (km)</b>	0	1	2	3	4	5
<b>y</b>	<b>Air Pressure (kPa)</b>	101	90	79	70	62	54

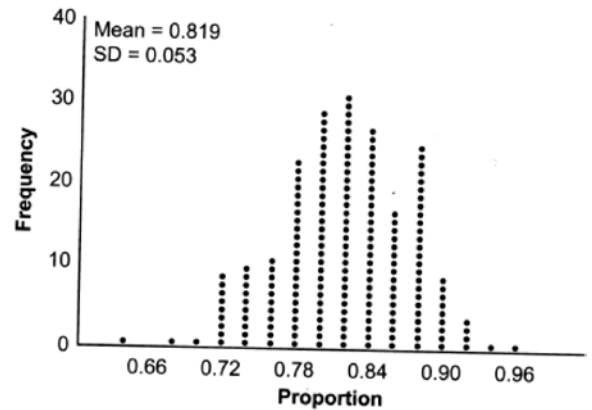
Write an exponential regression equation that models these data rounding all values to the *nearest thousandth*. Use this equation to algebraically determine the altitude, to the *nearest hundredth* of a kilometer, when the air pressure is 29 kPa.

532 Graph  $y = \log_2(x + 3) - 5$  on the set of axes below. Use an appropriate scale to include *both* intercepts.



Describe the behavior of the given function as  $x$  approaches  $-3$  and as  $x$  approaches positive infinity.

533 State officials claim 82% of a community want to repeal the 30 mph speed limit on an expressway. A community organization devises a simulation based on the claim that 82% of the community supports the repeal. Each dot on the graph below represents the proportion of community members who support the repeal. The graph shows 200 simulated surveys, each of sample size 60.

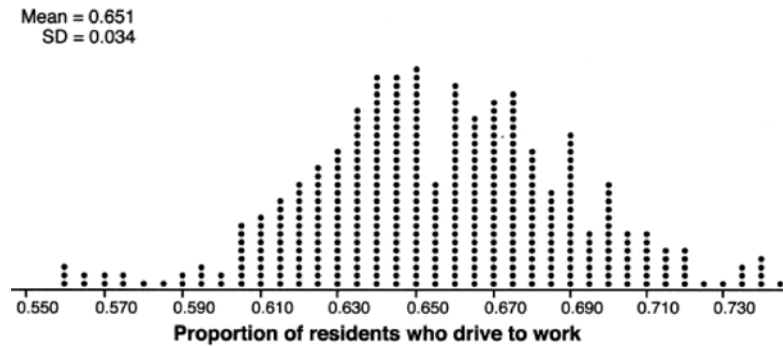


Based on the simulation, determine an interval containing the middle 95% of plausible proportions. Round your answer to the *nearest thousandth*. The community organization conducted its own sample survey of 60 people and found 70% supported the repeal. Based on the results of the simulation, explain why the organization should question the State officials' claim.

Algebra II 4 Point Regents Exam Questions

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- 534 In order to decrease the percentage of its residents who drive to work, a large city launches a campaign to encourage people to use public transportation instead. Before starting the campaign, the city's Department of Transportation uses census data to estimate that 65% of its residents drive to work. The Department of Transportation conducts a simulation, shown below, run 400 times based on this estimate. Each dot represents the proportion of 200 randomly selected residents who drive to work.

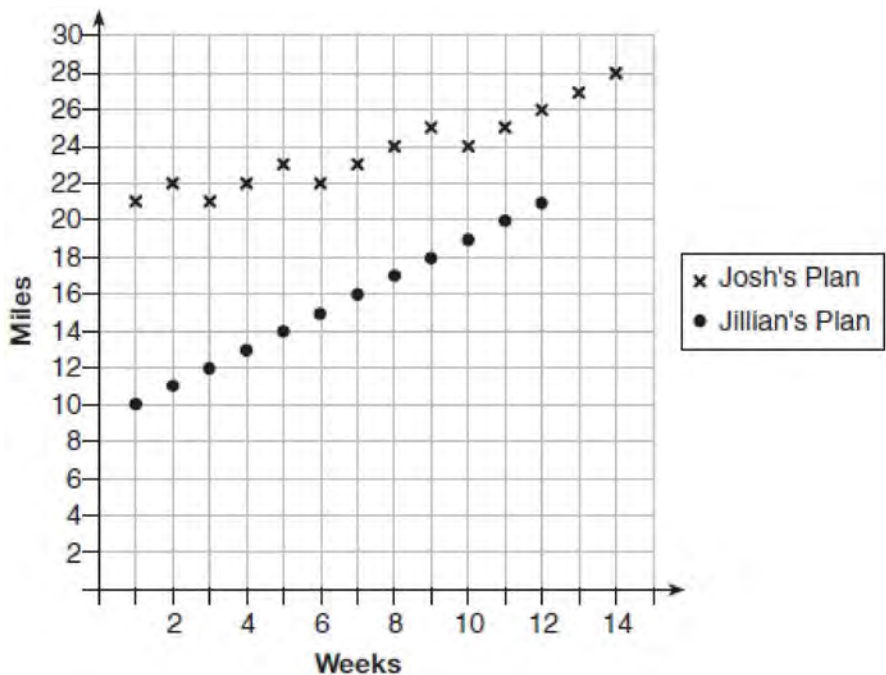


- Use the simulation results to construct a plausible interval containing the middle 95% of the data. Round your answer to the *nearest hundredth*. One year after launching the campaign, the Department of Transportation conducts a survey of 200 randomly selected city residents and finds that 122 of them drive to work. Should the department conclude that the city's campaign was effective? Use statistical evidence from the simulation to explain your answer.
- 535 Two versions of a standardized test are given, an April version and a May version. The statistics for the April version show a mean score of 480 and a standard deviation of 24. The statistics for the May version show a mean score of 510 and a standard deviation of 20. Assume the scores are normally distributed. Joanne took the April version and scored in the interval 510-540. What is the probability, to the *nearest ten thousandth*, that a test paper selected at random from the April version scored in the same interval? Maria took the May version. In what interval must Maria score to claim she scored as well as Joanne?
- 536 Alexa earns \$33,000 in her first year of teaching and earns a 4% increase in each successive year. Write a geometric series formula,  $S_n$ , for Alexa's total earnings over  $n$  years. Use this formula to find Alexa's total earnings for her first 15 years of teaching, to the *nearest cent*.
- 537 One of the medical uses of Iodine-131 (I-131), a radioactive isotope of iodine, is to enhance x-ray images. The half-life of I-131 is approximately 8.02 days. A patient is injected with 20 milligrams of I-131. Determine, to the *nearest day*, the amount of time needed before the amount of I-131 in the patient's body is approximately 7 milligrams.

Algebra II 4 Point Regents Exam Questions

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538 Elaina has decided to run the Buffalo half-marathon in May. She researched training plans on the Internet and is looking at two possible plans: Jillian's 12-week plan and Josh's 14-week plan. The number of miles run per week for each plan is plotted below.



Which one of the plans follows an arithmetic pattern? Explain how you arrived at your answer. Write a recursive definition to represent the number of miles run each week for the duration of the plan you chose. Jillian's plan has an alternative if Elaina wanted to train instead for a full 26-mile marathon. Week one would start at 13 miles and follow the same pattern for the half-marathon, but it would continue for 14 weeks. Write an explicit formula, in *simplest form*, to represent the number of miles run each week for the full-marathon training plan.

539 Carla wants to start a college fund for her daughter Lila. She puts \$63,000 into an account that grows at a rate of 2.55% per year, compounded monthly. Write a function,  $C(t)$ , that represents the amount of money in the account  $t$  years after the account is opened, given that no more money is deposited into or withdrawn from the account. Calculate algebraically the number of years it will take for the account to reach \$100,000, to the *nearest hundredth of a year*.

540 In contract negotiations between a local government agency and its workers, it is estimated that there is a 50% chance that an agreement will be reached on the salaries of the workers. It is estimated that there is a 70% chance that there will be an agreement on the insurance benefits. There is a 20% chance that no agreement will be reached on either issue. Find the probability that an agreement will be reached on *both* issues. Based on this answer, determine whether the agreement on salaries and the agreement on insurance are independent events. Justify your answer.

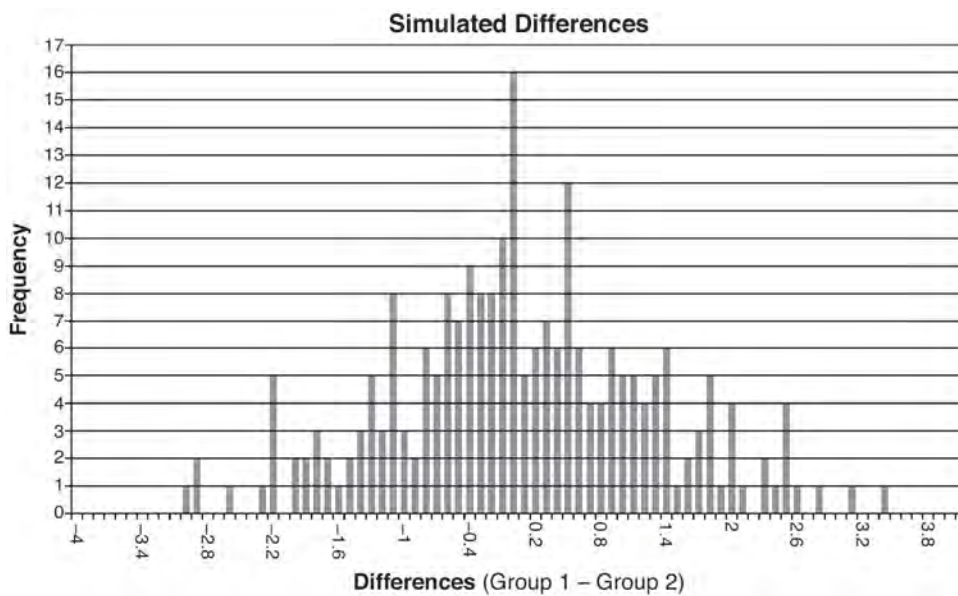
Algebra II 4 Point Regents Exam Questions

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- 541 Ayva designed an experiment to determine the effect of a new energy drink on a group of 20 volunteer students. Ten students were randomly selected to form group 1 while the remaining 10 made up group 2. Each student in group 1 drank one energy drink, and each student in group 2 drank one cola drink. Ten minutes later, their times were recorded for reading the same paragraph of a novel. The results of the experiment are shown below.

Group 1 (seconds)	Group 2 (seconds)
17.4	23.3
18.1	18.8
18.2	22.1
19.6	12.7
18.6	16.9
16.2	24.4
16.1	21.2
15.3	21.2
17.8	16.3
19.7	14.5
Mean = 17.7	Mean = 19.1

Ayva thinks drinking energy drinks makes students read faster. Using information from the experimental design or the results, explain why Ayva's hypothesis may be *incorrect*. Using the given results, Ayva randomly mixes the 20 reading times, splits them into two groups of 10, and simulates the difference of the means 232 times.

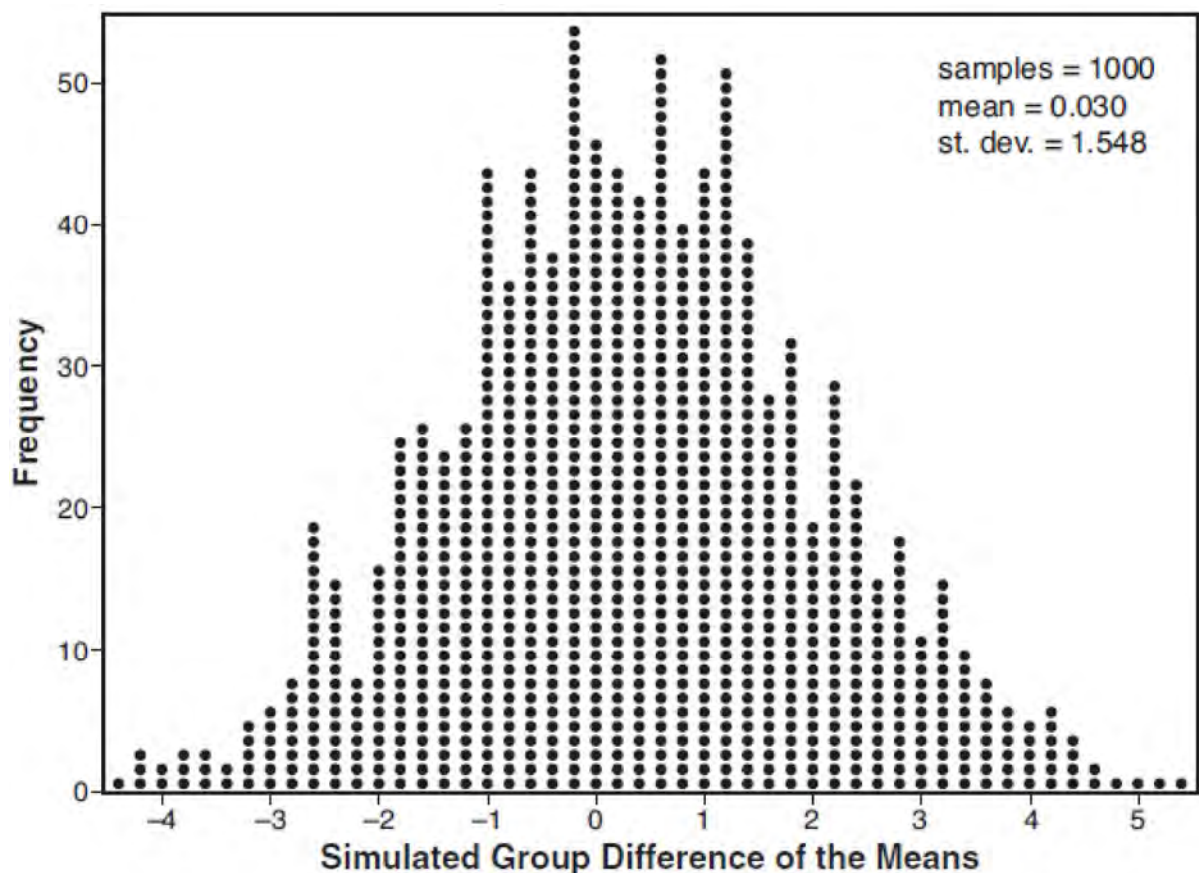


Ayva has decided that the difference in mean reading times is not an unusual occurrence. Support her decision using the results of the simulation. Explain your reasoning.

- 542 Joseph was curious to determine if scent improves memory. A test was created where better memory is indicated by higher test scores. A controlled experiment was performed where one group was given the test on scented paper and the other group was given the test on unscented paper. The summary statistics from the experiment are given below.

	Scented Paper	Unscented Paper
$\bar{x}$	23	18
$s_x$	2.898	2.408

Calculate the difference in means in the experimental test grades (scented -unscented). A simulation was conducted in which the subjects' scores were rerandomized into two groups 1000 times. The differences of the group means were calculated each time. The results are shown below.



Use the simulation results to determine the interval representing the middle 95% of the difference in means, to the nearest hundredth. Is the difference in means in Joseph's experiment statistically significant based on the simulation? Explain.

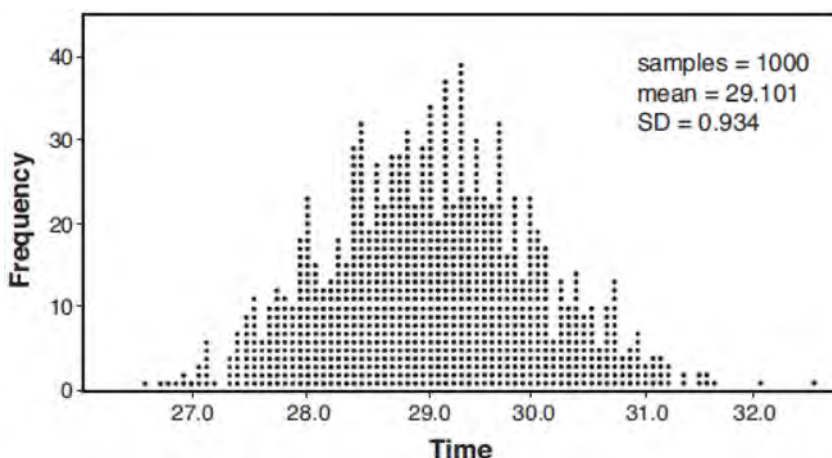
Algebra II 4 Point Regents Exam Questions

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- 543 A radio station claims to its advertisers that the mean number of minutes commuters listen to the station is 30. The station conducted a survey of 500 of their listeners who commute. The sample statistics are shown below.

$\bar{x}$	29.11
$s_x$	20.718

A simulation was run 1000 times based upon the results of the survey. The results of the simulation appear below.



Based on the simulation results, is the claim that commuters listen to the station on average 30 minutes plausible? Explain your response including an interval containing the middle 95% of the data, rounded to the *nearest hundredth*.

- 544 A student is chosen at random from the student body at a given high school. The probability that the student selects Math as the favorite subject is  $\frac{1}{4}$ . The probability that the student chosen is a junior is  $\frac{116}{459}$ . If the probability that the student selected is a junior or that the student chooses Math as the favorite subject is  $\frac{47}{108}$ , what is the exact probability that the student selected is a junior whose favorite subject is Math? Are the events "the student is a junior" and "the student's favorite subject is Math" independent of each other? Explain your answer.

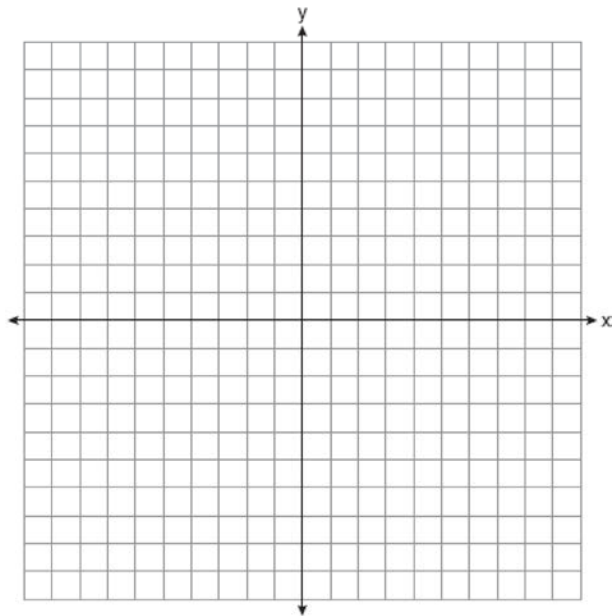
- 545 Simon lost his library card and has an overdue library book. When the book was 5 days late, he owed \$2.25 to replace his library card and pay the fine for the overdue book. When the book was 21 days late, he owed \$6.25 to replace his library card and pay the fine for the overdue book. Suppose the total amount Simon owes when the book is  $n$  days late can be determined by an arithmetic sequence. Determine a formula for  $a_n$ , the  $n$ th term of this sequence. Use the formula to determine the amount of money, in dollars, Simon needs to pay when the book is 60 days late.



Algebra II 4 Point Regents Exam Questions

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- 546 Graph the following function on the axes below.  
 $f(x) = \log_3(2 - x)$



State the domain of  $f$ . State the equation of the asymptote.

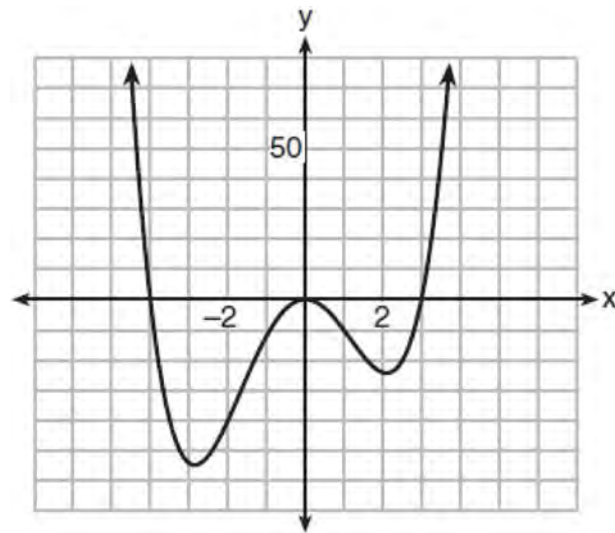
- 547 The monthly high temperature ( $^{\circ}\text{F}$ ) in Buffalo, New York can be modeled by  $B(m) = 24.9 \sin(0.5m - 2.05) + 55.25$ , where  $m$  is the number of the month and January = 1. Find the average rate of change in the monthly high temperature between June and October, to the nearest hundredth. Explain what this value represents in the given context.

- 548 When observed by researchers under a microscope, a smartphone screen contained approximately 11,000 bacteria per square inch. Bacteria, under normal conditions, double in population every 20 minutes.

a) Assuming an initial value of 11,000 bacteria, write a function,  $p(t)$ , that can be used to model the population of bacteria,  $p$ , on a smartphone screen, where  $t$  represents the time in minutes after it is first observed under a microscope.

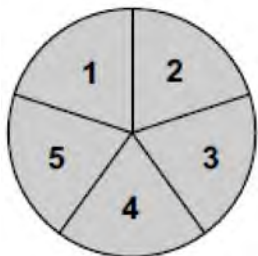
b) Using  $p(t)$  from part a, determine algebraically, to the nearest hundredth of a minute, the amount of time it would take for a smartphone screen that was not touched or cleaned to have a population of 1,000,000 bacteria per square inch.

- 549 The graph of  $y = f(x)$  is shown below. The function has a leading coefficient of 1.

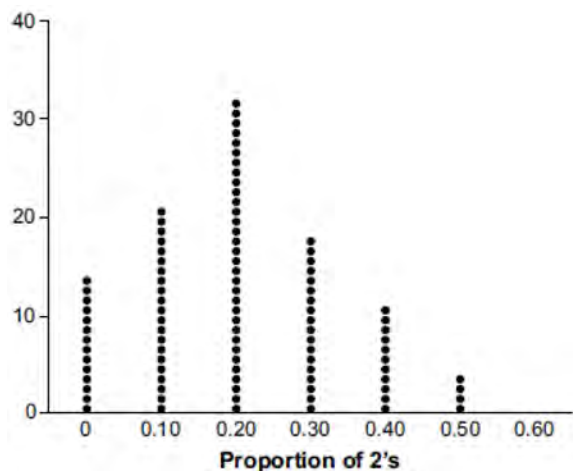


Write an equation for  $f(x)$ . The function  $g$  is formed by translating function  $f$  left 2 units. Write an equation for  $g(x)$ .

- 550 Joette is playing a carnival game. To win a prize, one has to correctly guess which of five equally sized regions a spinner will land on, as shown in the diagram below.

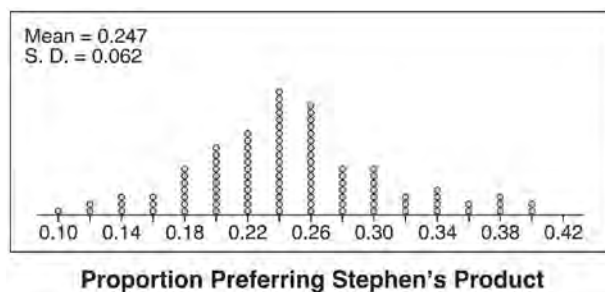


She complains that the game is unfair because her favorite number, 2, has only been spun once in ten times she played the game. State the proportion of 2's that were spun. State the theoretical probability of spinning a 2. The simulation output below shows the results of simulating ten spins of a fair spinner, repeated 100 times.



Does the output indicate that the carnival game was unfair? Explain your answer.

- 551 Stephen's Beverage Company is considering whether to produce a new brand of cola. The company will launch the product if at least 25% of cola drinkers will buy the product. Fifty cola drinkers are randomly selected to take a blind taste-test of products A, B, and the new product. Nine out of fifty participants preferred Stephen's new cola to products A and B. The company then devised a simulation based on the requirement that 25% of cola drinkers will buy the product. Each dot in the graph shown below represents the proportion of people who preferred Stephen's new product, each of sample size 50, simulated 100 times.



Assume the set of data is approximately normal and the company wants to be 95% confident of its results. Does the sample proportion obtained from the blind taste-test, nine out of fifty, fall within the margin of error developed from the simulation? Justify your answer. The company decides to continue developing the product even though only nine out of fifty participants preferred its brand of cola in the taste-test. Describe how the simulation data could be used to support this decision.

- 552 Solve the following system of equations algebraically for all values of  $a$ ,  $b$ , and  $c$ .

$$a + 4b + 6c = 23$$

$$a + 2b + c = 2$$

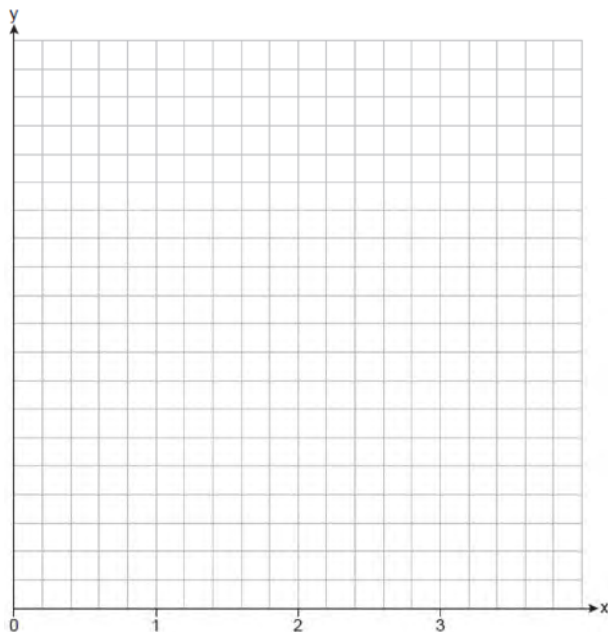
$$6b + 2c = a + 14$$

Algebra II 4 Point Regents Exam Questions

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553 Solve the equation  $\sqrt{49 - 10x} + 5 = 2x$  algebraically.

554 The function  $v(x) = x(3 - x)(x + 4)$  models the volume, in cubic inches, of a rectangular solid for  $0 \leq x \leq 3$ . Graph  $y = v(x)$  over the domain  $0 \leq x \leq 3$ .



To the *nearest tenth of a cubic inch*, what is the maximum volume of the rectangular solid?

555 Algebraically determine the values of  $h$  and  $k$  to correctly complete the identity stated below.

$$2x^3 - 10x^2 + 11x - 7 = (x - 4)(2x^2 + hx + 3) + k$$

556 Solve the equation  $\sqrt{2x - 7} + x = 5$  algebraically, and justify the solution set.

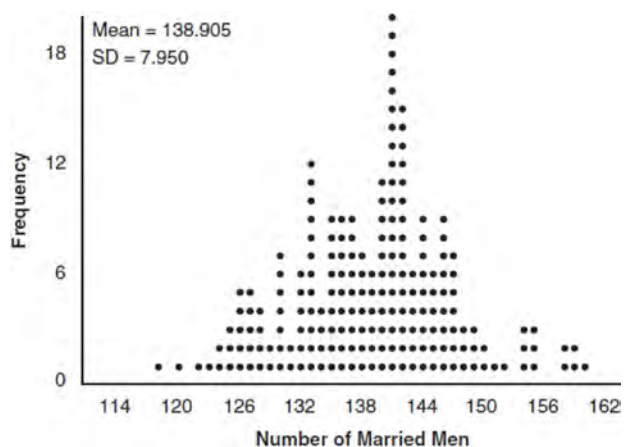
557 Write an explicit formula for  $a_n$ , the  $n$ th term of the recursively defined sequence below.

$$a_1 = x + 1$$

$$a_n = x(a_{n-1})$$

For what values of  $x$  would  $a_n = 0$  when  $n > 1$ ?

558 In a random sample of 250 men in the United States, age 21 or older, 139 are married. The graph below simulated samples of 250 men, 200 times, assuming that 139 of the men are married.



a) Based on the simulation, create an interval in which the middle 95% of the number of married men may fall. Round your answer to the *nearest integer*.

b) A study claims "50 percent of men 21 and older in the United States are married." Do your results from part a contradict this claim? Explain.

559 Solve algebraically for all values of  $x$ :

$$\sqrt{6 - 2x} + x = 2(x + 15) - 9$$

560 Given:  $f(x) = 2x^2 + x - 3$  and  $g(x) = x - 1$   
Express  $f(x) \cdot g(x) - [f(x) + g(x)]$  as a polynomial in standard form.

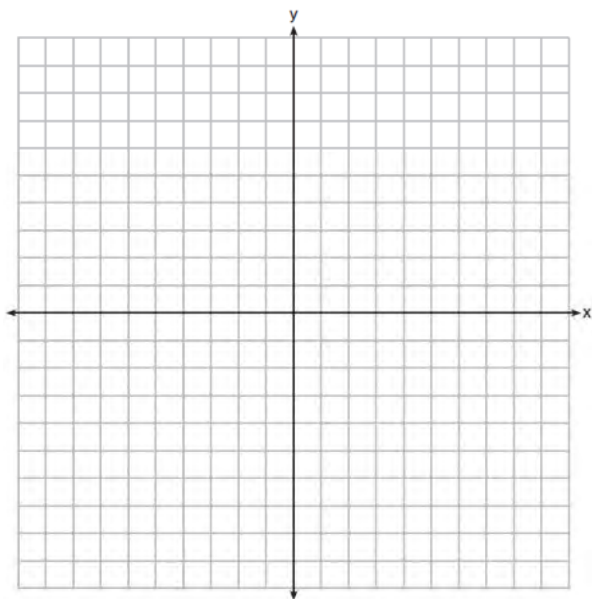
Algebra II 4 Point Regents Exam Questions

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- 561 On the set of axes below, graph  $y = f(x)$  and  $y = g(x)$  for the given functions.

$$f(x) = x^3 - 3x^2$$

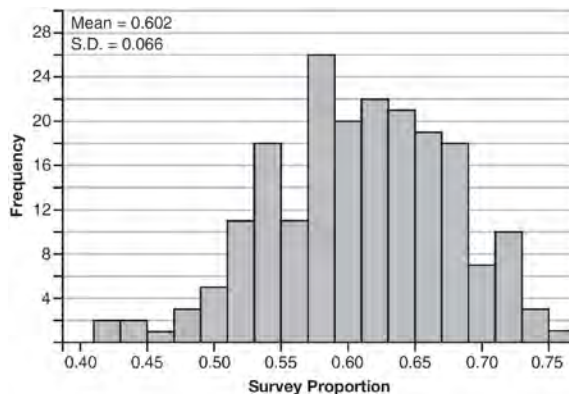
$$g(x) = 2x - 5$$



State the number of solutions to the equation  $f(x) = g(x)$ .

- 562 Sonja is cutting wire to construct a mobile. She cuts 100 inches for the first piece, 80 inches for the second piece, and 64 inches for the third piece. Assuming this pattern continues, write an explicit equation for  $a_n$ , the length in inches of the  $n$ th piece. Sonja only has 40 feet of wire to use for the project and wants to cut 20 pieces total for the mobile using her pattern. Will she have enough wire? Justify your answer.

- 563 Fifty-five students attending the prom were randomly selected to participate in a survey about the music choice at the prom. Sixty percent responded that a DJ would be preferred over a band. Members of the prom committee thought that the vote would have 50% for the DJ and 50% for the band. A simulation was run 200 times, each of sample size 55, based on the premise that 60% of the students would prefer a DJ. The approximate normal simulation results are shown below.



Using the results of the simulation, determine a plausible interval containing the middle 95% of the data. Round all values to the *nearest hundredth*. Members of the prom committee are concerned that a vote of all students attending the prom may produce a 50% – 50% split. Explain what statistical evidence supports this concern.

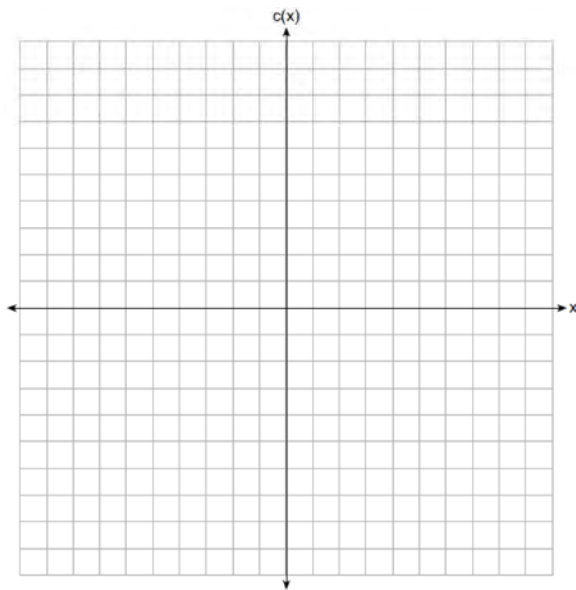
- 564 Factor completely over the set of integers:  $16x^4 - 81$ . Sara graphed the polynomial  $y = 16x^4 - 81$  and stated “All the roots of  $y = 16x^4 - 81$  are real.” Is Sara correct? Explain your reasoning.

565 Which function shown below has a greater average rate of change on the interval  $[-2,4]$ ? Justify your answer.

$x$	$f(x)$
-4	0.3125
-3	0.625
-2	1.25
-1	2.5
0	5
1	10
2	20
3	40
4	80
5	160
6	320

$$g(x) = 4x^3 - 5x^2 + 3$$

566 Graph  $c(x) = -9(3)^{x-4} + 2$  on the axes below.



Describe the end behavior of  $c(x)$  as  $x$  approaches positive infinity. Describe the end behavior of  $c(x)$  as  $x$  approaches negative infinity.

567 Algebraically solve the following system of equations.

$$(x-2)^2 + (y-3)^2 = 16$$

$$x + y - 1 = 0$$

568 The half-life of a radioactive substance is 15 years. Write an equation that can be used to determine the amount,  $s(t)$ , of 200 grams of this substance that remains after  $t$  years. Determine algebraically, to the *nearest year*, how long it will take for  $\frac{1}{10}$  of this substance to remain.

569 Solve the following system of equations algebraically for all values of  $x$ ,  $y$ , and  $z$ :

$$x + 3y + 5z = 45$$

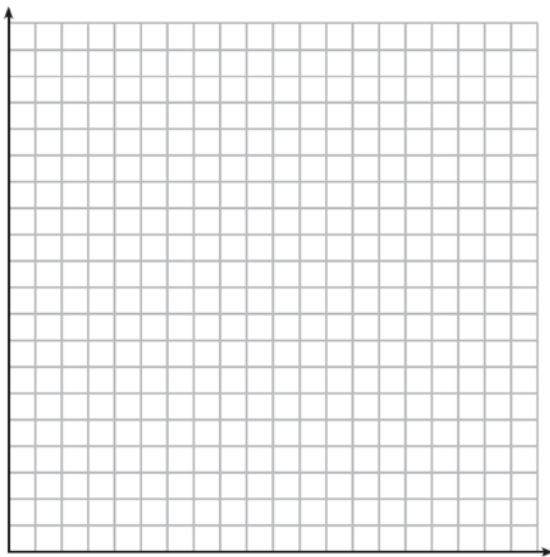
$$6x - 3y + 2z = -10$$

$$-2x + 3y + 8z = 72$$

**Algebra II 6 Point Regents Exam Questions**

570 The value of a certain small passenger car based on its use in years is modeled by

$V(t) = 28482.698(0.684)^t$ , where  $V(t)$  is the value in dollars and  $t$  is the time in years. Zach had to take out a loan to purchase the small passenger car. The function  $Z(t) = 22151.327(0.778)^t$ , where  $Z(t)$  is measured in dollars, and  $t$  is the time in years, models the unpaid amount of Zach's loan over time. Graph  $V(t)$  and  $Z(t)$  over the interval  $0 \leq t \leq 5$ , on the set of axes below.



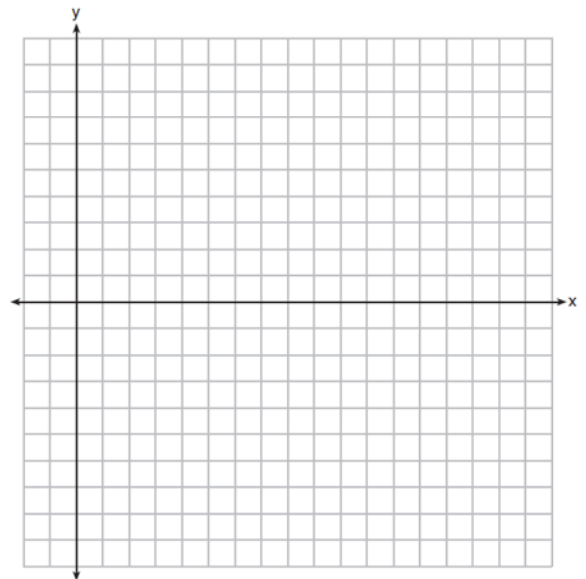
State when  $V(t) = Z(t)$ , to the *nearest hundredth*, and interpret its meaning in the context of the problem. Zach takes out an insurance policy that requires him to pay a \$3000 deductible in case of a collision. Zach will cancel the collision policy when the value of his car equals his deductible. To the *nearest year*, how long will it take Zach to cancel this policy? Justify your answer.

571 A major car company analyzes its revenue,  $R(x)$ , and costs  $C(x)$ , in millions of dollars over a fifteen-year period. The company represents its revenue and costs as a function of time, in years,  $x$ , using the given functions.

$$R(x) = 550x^3 - 12,000x^2 + 83,000x + 7000$$

$$C(x) = 880x^3 - 21,000x^2 + 150,000x - 160,000$$

The company's profits can be represented as the difference between its revenue and costs. Write the profit function,  $P(x)$ , as a polynomial in standard form. Graph  $y = P(x)$  on the set of axes below over the domain  $2 \leq x \leq 16$ .

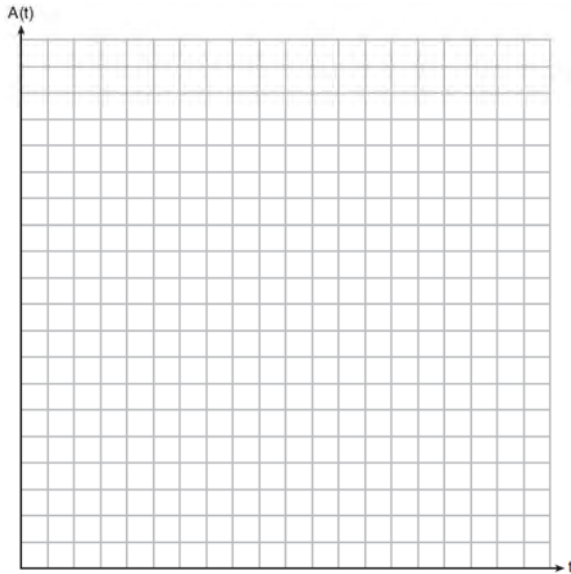


Over the given domain, state when the company was the least profitable and the most profitable, to the *nearest year*. Explain how you determined your answer.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 572 Tony is evaluating his retirement savings. He currently has \$318,000 in his account, which earns an interest rate of 7% compounded annually. He wants to determine how much he will have in the account in the future, even if he makes no additional contributions to the account. Write a function,  $A(t)$ , to represent the amount of money that will be in his account in  $t$  years. Graph  $A(t)$  where  $0 \leq t \leq 20$  on the set of axes below.



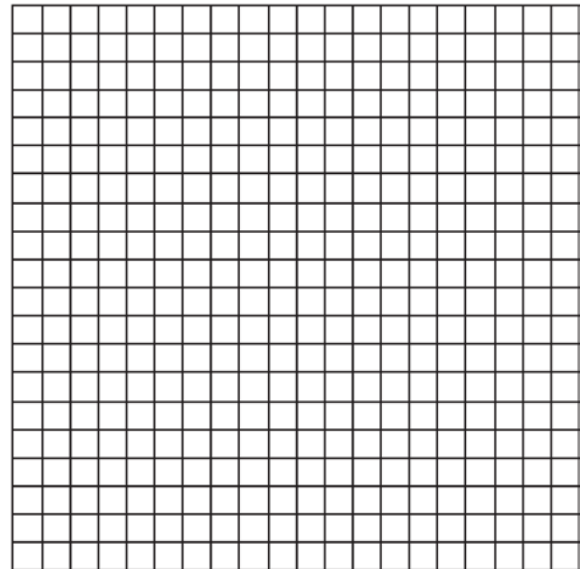
Tony's goal is to save \$1,000,000. Determine algebraically, to the *nearest year*, how many years it will take for him to achieve his goal. Explain how your graph of  $A(t)$  confirms your answer.

- 573 A radioactive substance has a mass of 140 g at 3 p.m. and 100 g at 8 p.m. Write an equation in the

form  $A = A_0 \left( \frac{1}{2} \right)^{\frac{t}{h}}$  that models this situation,

where  $h$  is the constant representing the number of hours in the half-life,  $A_0$  is the initial mass, and  $A$  is the mass  $t$  hours after 3 p.m. Using this equation, solve for  $h$ , to the *nearest ten thousandth*. Determine when the mass of the radioactive substance will be 40 g. Round your answer to the *nearest tenth of an hour*.

- 574 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function  $f(t) = -13 \cos(0.8\pi t) + 13$ , where  $t$  represents the time (in seconds) since the nail first became caught in the tire. Determine the period of  $f(t)$ . Interpret what the period represents in this context. On the grid below, graph *at least one* cycle of  $f(t)$  that includes the y-intercept of the function.



Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

- 575 The Beaufort Wind Scale was devised by British Rear Admiral Sir Francis Beaufort, in 1805 based upon observations of the effects of the wind. Beaufort numbers,  $B$ , are determined by the equation  $B = 1.69\sqrt{s + 4.45} - 3.49$ , where  $s$  is the speed of the wind in mph, and  $B$  is rounded to the nearest integer from 0 to 12.

Beaufort Wind Scale	
Beaufort Number	Force of Wind
0	Calm
1	Light air
2	Light breeze
3	Gentle breeze
4	Moderate breeze
5	Fresh breeze
6	Steady breeze
7	Moderate gale
8	Fresh gale
9	Strong gale
10	Whole gale
11	Storm
12	Hurricane

Using the table above, classify the force of wind at a speed of 30 mph. Justify your answer. In 1946, the scale was extended to accommodate strong hurricanes. A strong hurricane received a  $B$  value of exactly 15. Algebraically determine the value of  $s$ , to the *nearest mph*. Any  $B$  values that round to 10 receive a Beaufort number of 10. Using technology, find an approximate range of wind speeds, to the *nearest mph*, associated with a Beaufort number of 10.

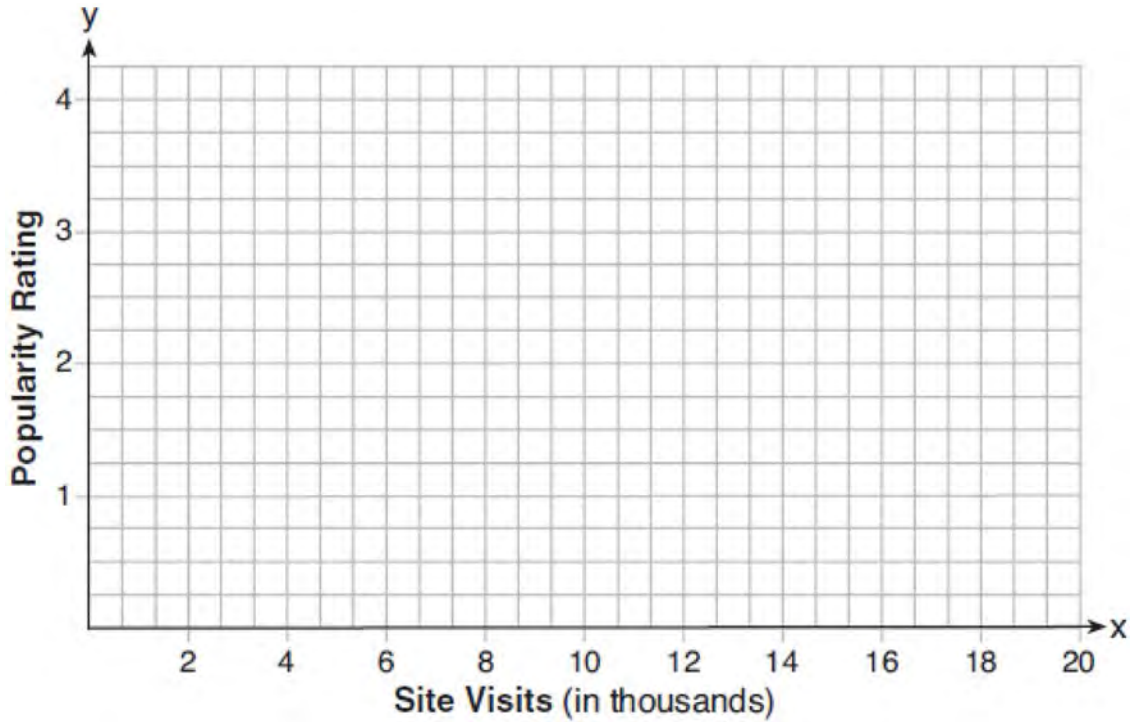
- 576 Titanium-44 is a radioactive isotope such that every 63 years, its mass decreases by half. For a sample of titanium-44 with an initial mass of 100 grams, write a function that will give the mass of the sample remaining after any amount of time. Define all variables. Scientists sometimes use the average yearly decrease in mass for estimation purposes. Use the average yearly decrease in mass of the sample between year 0 and year 10 to predict the amount of the sample remaining after 40 years. Round your answer to the *nearest tenth*. Is the actual mass of the sample or the estimated mass greater after 40 years? Justify your answer.
- 577 The population, in millions of people, of the United States can be represented by the recursive formula below, where  $a_0$  represents the population in 1910 and  $n$  represents the number of years since 1910.
- $$a_0 = 92.2$$
- $$a_n = 1.015a_{n-1}$$
- Identify the percentage of the annual rate of growth from the equation  $a_n = 1.015a_{n-1}$ . Write an exponential function,  $P$ , where  $P(t)$  represents the United States population in millions of people, and  $t$  is the number of years since 1910. According to this model, determine algebraically the number of years it takes for the population of the United States to be approximately 300 million people. Round your answer to the *nearest year*.



Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 578 Website popularity ratings are often determined using models that incorporate the number of visits per week a website receives. One model for ranking websites is  $P(x) = \log(x - 4)$ , where  $x$  is the number of visits per week in thousands and  $P(x)$  is the website's popularity rating. According to this model, if a website is visited 16,000 times in one week, what is its popularity rating, rounded to the *nearest tenth*? Graph  $y = P(x)$  on the axes below.

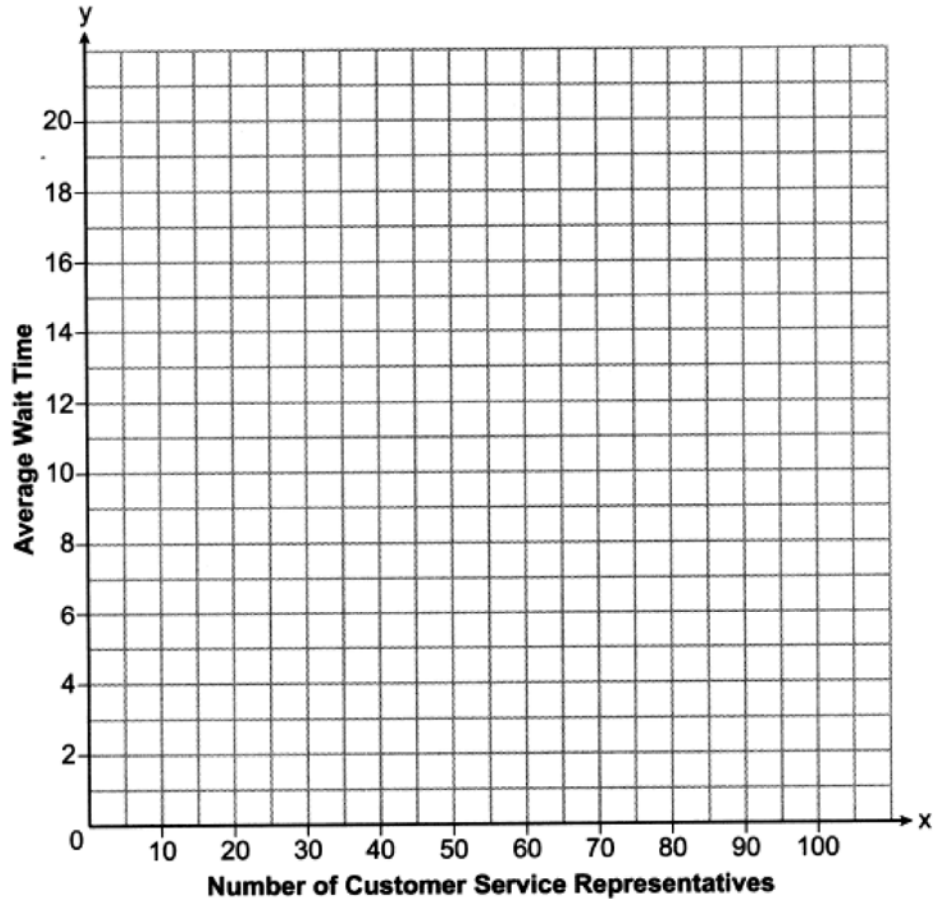


An alternative rating model is represented by  $R(x) = \frac{1}{2}x - 6$ , where  $x$  is the number of visits per week in thousands. Graph  $R(x)$  on the same set of axes. For what number of weekly visits will the two models provide the same rating?

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 579 A technology company is comparing two plans for speeding up its technical support time. Plan A can be modeled by the function  $A(x) = 15.7(0.98)^x$  and plan B can be modeled by the function  $B(x) = 11(0.99)^x$  where  $x$  is the number of customer service representatives employed by the company and  $A(x)$  and  $B(x)$  represent the average wait time, in minutes, of each customer. Graph  $A(x)$  and  $B(x)$  in the interval  $0 \leq x \leq 100$  on the set of axes below.

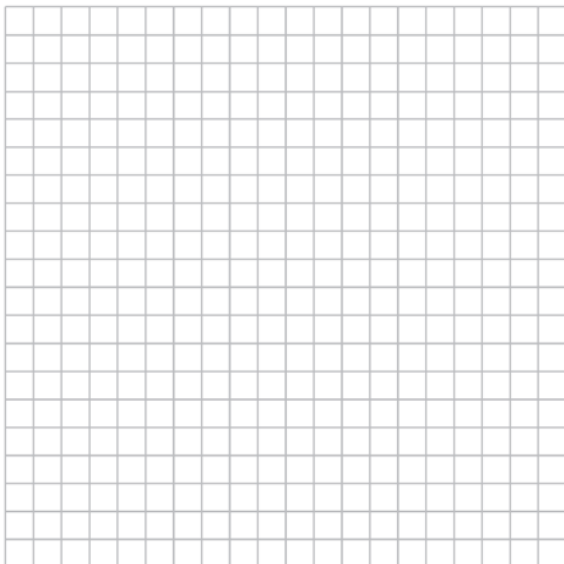


To the *nearest integer*, solve the equation  $A(x) = B(x)$ . Determine, to the *nearest minute*,  $B(100) - A(100)$ . Explain what this value represents in the given context.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 580 The ocean tides near Carter Beach follow a repeating pattern over time, with the amount of time between each low and high tide remaining relatively constant. On a certain day, low tide occurred at 8:30 a.m. and high tide occurred at 3:00 p.m. At high tide, the water level was 12 inches above the average local sea level; at low tide it was 12 inches below the average local sea level. Assume that high tide and low tide are the maximum and minimum water levels each day, respectively. Write a cosine function of the form  $f(t) = A \cos(Bt)$ , where  $A$  and  $B$  are real numbers, that models the water level,  $f(t)$ , in inches above or below the average Carter Beach sea level, as a function of the time measured in  $t$  hours since 8:30 a.m. On the grid below, graph one cycle of this function.



People who fish in Carter Beach know that a certain species of fish is most plentiful when the water level is increasing. Explain whether you would recommend fishing for this species at 7:30 p.m. or 10:30 p.m. using evidence from the given context.

- 581 Sarah is fighting a sinus infection. Her doctor prescribed a nasal spray and an antibiotic to fight the infection. The active ingredients, in milligrams, remaining in the bloodstream from the nasal spray,  $n(t)$ , and the antibiotic,  $a(t)$ , are modeled in the functions below, where  $t$  is the time in hours since the medications were taken.

$$n(t) = \frac{t+1}{t+5} + \frac{18}{t^2 + 8t + 15}$$

$$a(t) = \frac{9}{t+3}$$

Determine which drug is made with a greater initial amount of active ingredient. Justify your answer. Sarah's doctor told her to take both drugs at the same time. Determine algebraically the number of hours after taking the medications when both medications will have the same amount of active ingredient remaining in her bloodstream.

- 582 Seth's parents gave him \$5000 to invest for his 16th birthday. He is considering two investment options. Option  $A$  will pay him 4.5% interest compounded annually. Option  $B$  will pay him 4.6% compounded quarterly. Write a function of option  $A$  and option  $B$  that calculates the value of each account after  $n$  years. Seth plans to use the money after he graduates from college in 6 years. Determine how much more money option  $B$  will earn than option  $A$  to the nearest cent. Algebraically determine, to the nearest tenth of a year, how long it would take for option  $B$  to double Seth's initial investment.

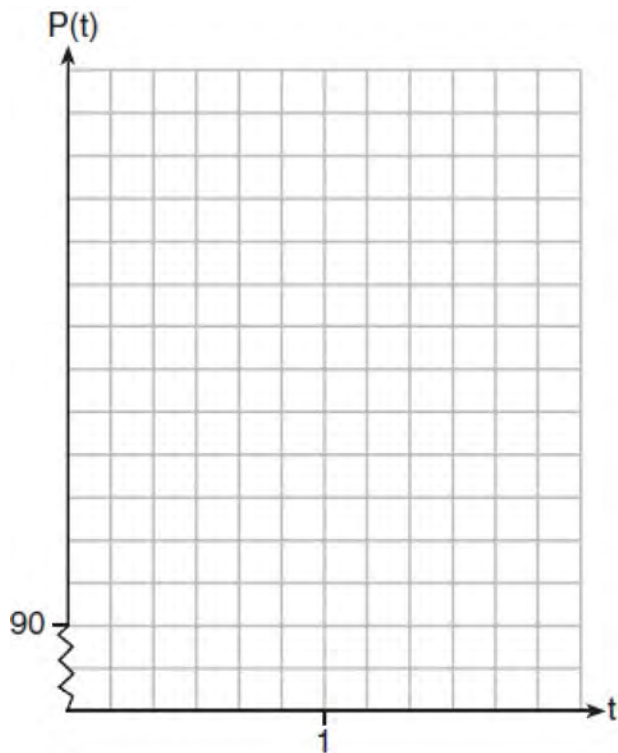
Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 583 The resting blood pressure of an adult patient can be modeled by the function  $P$  below, where  $P(t)$  is the pressure in millimeters of mercury after time  $t$  in seconds.

$$P(t) = 24 \cos(3\pi t) + 120$$

On the set of axes below, graph  $y = P(t)$  over the domain  $0 \leq t \leq 2$ .



Determine the period of  $P$ . Explain what this value represents in the given context. Normal resting blood pressure for an adult is 120 over 80. This means that the blood pressure oscillates between a maximum of 120 and a minimum of 80. Adults with high blood pressure (above 140 over 90) and adults with low blood pressure (below 90 over 60) may be at risk for health disorders. Classify the given patient's blood pressure as low, normal, or high and explain your reasoning.

- 584 The speed of a tidal wave,  $s$ , in hundreds of miles per hour, can be modeled by the equation  $s = \sqrt{t} - 2t + 6$ , where  $t$  represents the time from its origin in hours. Algebraically determine the time when  $s = 0$ . How much faster was the tidal wave traveling after 1 hour than 3 hours, to the nearest mile per hour? Justify your answer.

- 585 Objects cool at different rates based on the formula below.

$$T = (T_0 - T_R)e^{-rt} + T_R$$

$T_0$ : initial temperature

$T_R$ : room temperature

$r$ : rate of cooling of the object

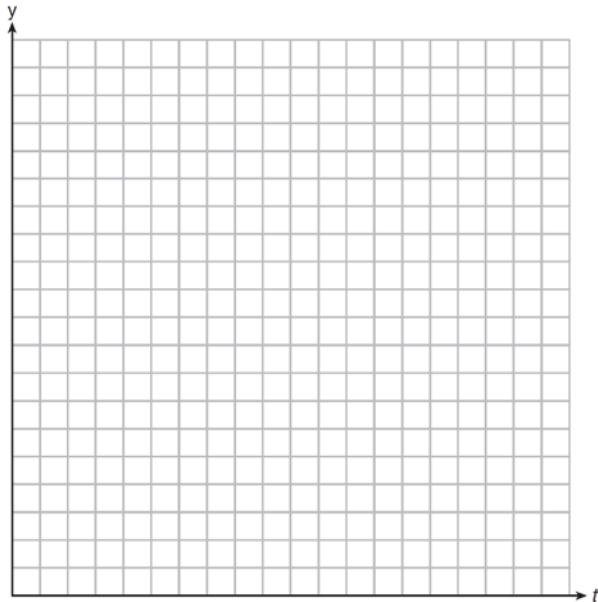
$t$ : time in minutes that the object cools to a temperature,  $T$

Mark makes T-shirts using a hot press to transfer designs to the shirts. He removes a shirt from a press that heats the shirt to  $400^\circ\text{F}$ . The rate of cooling for the shirt is 0.0735 and the room temperature is  $75^\circ\text{F}$ . Using this information, write an equation for the temperature of the shirt,  $T$ , after  $t$  minutes. Use the equation to find the temperature of the shirt, to the nearest degree, after five minutes. At the same time, Mark's friend Jeanine removes a hoodie from a press that heats the hoodie to  $450^\circ\text{F}$ . After eight minutes, the hoodie measured  $270^\circ\text{F}$ . The room temperature is still  $75^\circ\text{F}$ . Determine the rate of cooling of the hoodie, to the nearest ten thousandth. The T-shirt and hoodie were removed at the same time. Determine when the temperature will be the same, to the nearest minute.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

586 Drugs break down in the human body at different rates and therefore must be prescribed by doctors carefully to prevent complications, such as overdosing. The breakdown of a drug is represented by the function  $N(t) = N_0(e)^{-rt}$ , where  $N(t)$  is the amount left in the body,  $N_0$  is the initial dosage,  $r$  is the decay rate, and  $t$  is time in hours. Patient A,  $A(t)$ , is given 800 milligrams of a drug with a decay rate of 0.347. Patient B,  $B(t)$ , is given 400 milligrams of another drug with a decay rate of 0.231. Write two functions,  $A(t)$  and  $B(t)$ , to represent the breakdown of the respective drug given to each patient. Graph each function on the set of axes below.



To the *nearest hour*,  $t$ , when does the amount of the given drug remaining in patient B begin to exceed the amount of the given drug remaining in patient A? The doctor will allow patient A to take another 800 milligram dose of the drug once only 15% of the original dose is left in the body. Determine, to the *nearest tenth of an hour*, how long patient A will have to wait to take another 800 milligram dose of the drug.

## Algebra II Multiple Choice Regents Exam Questions Answer Section

1 ANS: 1

$$2) (x^4 - x^2y^2 + y^4) \neq (x^2 - y^2)(x^2 - y^2); 3) x^6 + y^6 \neq (x^3 + y^3)^2; 4) \frac{x^6 + y^6}{x^2 + y^2} \neq x^6 + y^6 - (x^2 + y^2)$$

REF: 082219aai NAT: A.APR.C.4 TOP: Polynomial Identities

2 ANS: 4

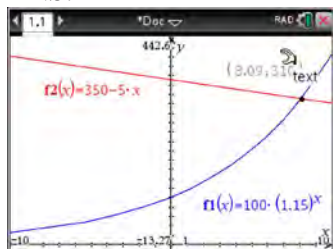
The scenario represents a decreasing geometric sequence with a common ratio of 0.80.

REF: 061610aai NAT: F.BF.A.2 TOP: Sequences

3 ANS: 3

REF: 061623aai NAT: F.BF.A.2 TOP: Sequences

4 ANS: 2



REF: 011716aai NAT: A.REI.D.11 TOP: Other Systems

5 ANS: 2

$$\begin{array}{r} x^2 + 2x + 4 \\ x - 2 \overline{) x^3 - 0x^2 + 0x - 2} \\ \underline{x^3 - 2x^2} \phantom{+ 0x - 2} \\ 2x^2 + 0x \phantom{- 2} \\ \underline{2x^2 - 4x} \phantom{- 2} \\ 4x - 2 \\ \underline{4x - 8} \\ 6 \end{array}$$

REF: 082217aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

6 ANS: 3

$$x = \frac{1}{2}y + 2$$

$$2x = y + 4$$

$$y = 2x - 4$$

REF: 012315aia NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

7 ANS: 4

$$(x - 2i)(x - 2i) = x^2 - 4xi + 4i^2 = x^2 - 4xi - 4$$

REF: 082202aia NAT: N.CN.A.2 TOP: Operations with Complex Numbers

8 ANS: 2

$$1 = \frac{2\pi}{k}$$

$$k = 2\pi$$

REF: 012313aia NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

9 ANS: 3

$$x^2 + 2x + 1 = -5 + 1$$

$$(x + 1)^2 = -4$$

$$x + 1 = \pm 2i$$

$$x = -1 \pm 2i$$

REF: 081703aia NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | completing the square

10 ANS: 3

$$S_{20} = \frac{-2 - (-2)(-3)^{20}}{1 - (-3)} = 1,743,392,200$$

REF: 012306aia NAT: A.SSE.B.4 TOP: Series KEY: geometric

11 ANS: 1 REF: 081609aia NAT: F.BF.B.6 TOP: Sigma Notation

KEY: represent

12 ANS: 3 REF: 082201aia NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

13 ANS: 2 REF: 011709aia NAT: S.IC.B.5 TOP: Analysis of Data

14 ANS: 3

$$\left(\frac{1}{2}\right)^{\frac{1}{73.83}} \approx 0.990656$$

REF: 081710aia NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

15 ANS: 4 REF: 081624aia NAT: F.BF.A.2 TOP: Sequences

16 ANS: 3

$$\sqrt{56-x} = x \quad -8 \text{ is extraneous.}$$

$$56-x = x^2$$

$$0 = x^2 + x - 56$$

$$0 = (x+8)(x-7)$$

$$x = 7$$

REF: 061605aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

17 ANS: 3

$$\frac{x+2}{x} + \frac{x}{3} = \frac{2x^2+6}{3x} \quad 0 \text{ is extraneous.}$$

$$\frac{x^2+3x+6}{3x} = \frac{2x^2+6}{3x}$$

$$x^2+3x+6 = 2x^2+6$$

$$x^2-3x = 0$$

$$x(x-3) = 0$$

$$x = 0, 3$$

REF: 012309aii NAT: A.REI.A.2 TOP: Solving Rationals

18 ANS: 1

$$x+2 \overline{) \begin{array}{r} x^3 - 2x^2 - x + 6 \\ x^4 + 0x^3 - 5x^2 + 4x + 14 \end{array}}$$

$$\underline{x^4 + 2x^3}$$

$$-2x^3 - 5x^2$$

$$\underline{-2x^3 - 4x^2}$$

$$-x^2 + 4x$$

$$\underline{-x^2 - 2x}$$

$$6x + 14$$

$$\underline{6x + 12}$$

$$2$$

REF: 012305aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division



19 ANS: 4

$$\text{period} = \frac{2\pi}{B}$$

$$\frac{1}{60} = \frac{2\pi}{B}$$

$$B = 120\pi$$

REF: 061624aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

20 ANS: 4

$$m^5 + m^3 - 6m = m(m^4 + m^2 - 6) = m(m^2 + 3)(m^2 - 2)$$

REF: 011703aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

21 ANS: 1

The probability of rain equals the probability of rain, given that Sean pitches.

REF: 061611aai NAT: S.CP.A.3 TOP: Conditional Probability

22 ANS: 4 REF: 081622aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

23 ANS: 3 REF: 061602aai NAT: A.CED.A.1 TOP: Modeling Rationals

24 ANS: 1

$$P(28) = 5(2)^{\frac{98}{28}} \approx 56$$

REF: 011702aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions

25 ANS: 3

$$M = \frac{240000 \left( \frac{4.5\%}{12} \right) \left( 1 + \frac{4.5\%}{12} \right)^{15 \times 12}}{\left( 1 + \frac{4.5\%}{12} \right)^{15 \times 12} - 1} \approx 1835.98$$

REF: 062209aai NAT: F.IF.B.4 TOP: Evaluating Exponential Expressions

26 ANS: 1

$$x + y + z = 9 \quad 4 - y - z = -1 \quad 4 - 6 + z = 9$$

$$\underline{x - y - z = -1} \quad 4 - y + z = 21 \quad z = 11$$

$$2x = 8 \quad -y - z = -5$$

$$x = 4 \quad \underline{-y + z = 17}$$

$$-2y = 12$$

$$y = -6$$

REF: 012018aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

27 ANS: 1

$$0.5^{\frac{1}{0.0803}} \approx 0.000178$$

REF: 082224aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

28 ANS: 4

$$\log 2^t = \log \sqrt{10} \quad 2) \frac{\log \sqrt{10}}{\log 2} = \log_2 \sqrt{10}, \quad 1) \log_2 \sqrt{10} = \log_2 10^{\frac{1}{2}} = \frac{1}{2} \log_2 10, \quad 3) \log_4 10 = \frac{\log_2 10}{\log_2 4} = \frac{1}{2} \log_2 10$$

$$t \log 2 = \log \sqrt{10}$$

$$t = \frac{\log \sqrt{10}}{\log 2}$$

REF: 012009aai NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

29 ANS: 1

$$\left(a^{\sqrt[3]{2b^2}}\right)\left(\sqrt[3]{4a^2b}\right) = a^{\sqrt[3]{8a^2b^3}} = 2ab^{\sqrt[3]{a^2}}$$

REF: 082213aai NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

30 ANS: 4 REF: 081708aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

31 ANS: 2

1)  $x \rightarrow \infty, f(x) \rightarrow \infty$ ; 3) quartic polynomial; 4) three real roots

REF: 012318aai NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

32 ANS: 2

$$6xi^3(-4xi+5) = -24x^2i^4 + 30xi^3 = -24x^2(1) + 30x(-1) = -24x^2 - 30xi$$

REF: 061704aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

33 ANS: 4

(1) and (3) are not recursive

REF: 012013aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

34 ANS: 1

II. Ninth graders drive to school less often; III. Students know little about adults; IV. Calculus students love math!

REF: 081602aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

35 ANS: 2 REF: 012321aai NAT: F.BF.A.2 TOP: Sequences

36 ANS: 1

$$7 - 3i + x^2 - 4xi + 4i^2 - 4i - 2x^2 = 7 - 7i - x^2 - 4xi - 4 = 3 - x^2 - 4xi - 7i = (3 - x^2) - (4x + 7)i$$

REF: 012022aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

37 ANS: 2

$$ME = \left( z \sqrt{\frac{p(1-p)}{n}} \right) = \left( 1.96 \sqrt{\frac{(0.55)(0.45)}{900}} \right) \approx 0.03 \text{ or } \frac{1}{\sqrt{900}} \approx 0.03$$

REF: 081612aai NAT: S.IC.B.4 TOP: Analysis of Data

38 ANS: 1

$$8(2^{x+3}) = 48$$

$$2^{x+3} = 6$$

$$(x+3)\ln 2 = \ln 6$$

$$x+3 = \frac{\ln 6}{\ln 2}$$

$$x = \frac{\ln 6}{\ln 2} - 3$$

REF: 061702aai NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

39 ANS: 1

$$d = 18; r = \pm \frac{5}{4}$$

REF: 011714aai NAT: F.IF.A.3 TOP: Sequences KEY: explicit

40 ANS: 2

Combining (1) and (3):  $-6c = -18$  Combining (1) and (2):  $5a + 3c = -1$  Using (3):  $-(-2) - 5b - 5(3) = 2$ 

$$c = 3$$

$$5a + 3(3) = -1$$

$$2 - 5b - 15 = 2$$

$$5a = -10$$

$$b = -3$$

$$a = -2$$

REF: 081623aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

41 ANS: 2

$$\frac{x^2 + 3x}{x^2 + 5x + 6} = \frac{x(x+3)}{(x+2)(x+3)}$$

REF: 082215aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: factoring

42 ANS: 1



REF: 081711aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

43 ANS: 3

$f(x) = -f(x)$ , so  $f(x)$  is odd.  $g(-x) \neq g(x)$ , so  $g(x)$  is not even.  $g(-x) \neq -g(x)$ , so  $g(x)$  is not odd.  $h(-x) = h(x)$ , so  $h(x)$  is even.

REF: fall1502aai NAT: F.BF.B.3 TOP: Even and Odd Functions

44 ANS: 2

$$x = \frac{y+1}{y-2}$$

$$xy - 2x = y + 1$$

$$xy - y = 2x + 1$$

$$y(x-1) = 2x + 1$$

$$y = \frac{2x+1}{x-1}$$

REF: 081714aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

45 ANS: 1

$$\sqrt[4]{81x^8y^6} = 81^{\frac{1}{4}} x^{\frac{8}{4}} y^{\frac{6}{4}} = 3x^2y^{\frac{3}{2}}$$

REF: 012001aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

46 ANS: 3

$$-2\left(-\frac{1}{2}x^2 = -6x + 20\right)$$

$$x^2 - 12x = -40$$

$$x^2 - 12x + 36 = -40 + 36$$

$$(x - 6)^2 = -4$$

$$x - 6 = \pm 2i$$

$$x = 6 \pm 2i$$

REF: fall1504aii NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | completing the square

47 ANS: 2

$$4300e^{0.07x} = 5123$$

$$\ln e^{0.07x} = \ln \frac{5123}{4300}$$

$$0.07x = \ln \frac{5123}{4300}$$

$$x = \frac{\ln \frac{5123}{4300}}{0.07}$$

$$x \approx 2.5$$

REF: 012302aii NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

48 ANS: 3 REF: 012003aii NAT: A.APR.C.4 TOP: Polynomial Identities

49 ANS: 3

between 000 and 449, inclusive  $\rightarrow \frac{450}{1000} = 45\%$

REF: 012024aii NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

50 ANS: 2 REF: 061620aii NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

51 ANS: 2 REF: 062206aii NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

52 ANS: 3 REF: 012002aii NAT: F.BF.A.1 TOP: Operations with Functions

53 ANS: 1 REF: 061701aii NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

54 ANS: 4 REF: 012008aii NAT: S.CP.A.3 TOP: Conditional Probability

55 ANS: 3

$$(m - 2)^2(m + 3) = (m^2 - 4m + 4)(m + 3) = m^3 + 3m^2 - 4m^2 - 12m + 4m + 12 = m^3 - m^2 - 8m + 12$$

REF: 081605aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

56 ANS: 3 REF: 012005aii NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

- 57 ANS: 3 REF: 061722aai NAT: A.CED.A.1 TOP: Modeling Rationals  
 58 ANS: 2 REF: 082203aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
 KEY: amplitude

- 59 ANS: 4  
 The maximum volume of  $p(x) = -(x+2)(x-10)(x-14)$  is about 56, at  $x = 12.1$

- REF: 081712aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions  
 60 ANS: 2 REF: 011720aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems  
 61 ANS: 2

$$B(t) = 750 \left( 1.16^{\frac{1}{12}} \right)^{12t} \approx 750(1.012)^{12t} \quad B(t) = 750 \left( 1 + \frac{0.16}{12} \right)^{12t} \text{ is wrong, because the growth is an annual rate}$$

that is not compounded monthly.

- REF: spr1504aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions  
 62 ANS: 2

The events are independent because  $P(A \text{ and } B) = P(A) \cdot P(B)$ .

$$0.125 = 0.5 \cdot 0.25$$

If  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = 0.25 + 0.5 - .125 = 0.625$ , then the events are not mutually exclusive because  $P(A \text{ or } B) = P(A) + P(B)$

$$0.625 \neq 0.5 + 0.25$$

- REF: 061714aai NAT: S.CP.B.7 TOP: Theoretical Probability  
 63 ANS: 4

$$k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$$

$$k^2(k^2 - 4) + 8k(k^2 - 4) + 12(k^2 - 4)$$

$$(k^2 - 4)(k^2 + 8k + 12)$$

$$(k+2)(k-2)(k+6)(k+2)$$

- REF: fall1505aai NAT: A.SSE.A.2 TOP: Factoring Polynomials  
 KEY: factoring by grouping

- 64 ANS: 1  
 The graph of  $y = \sin x$  is unchanged when rotated  $180^\circ$  about the origin.

- REF: 081614aai NAT: F.BF.B.3 TOP: Even and Odd Functions

65 ANS: 3

$$\frac{4}{k^2 - 8k + 12} = \frac{k(k-6) + (k-2)}{k^2 - 8k + 12} \quad k = 6 \text{ is extraneous}$$

$$4 = k^2 - 6k + k - 2$$

$$0 = k^2 - 5k - 6$$

$$0 = (k-6)(k+1)$$

$$k = 6, -1$$

REF: 082218aai NAT: A.REI.A.2 TOP: Solving Rationals

66 ANS: 1 REF: 011704aai NAT: F.TF.C.8 TOP: Simplifying Trigonometric Expressions

67 ANS: 4

$$\frac{-3x^2 - 5x + 2}{x^3 + 2x^2} = \frac{(-3x+1)(x+2)}{x^2(x+2)} = \frac{-3x}{x^2} + \frac{1}{x^2} = -3x^{-1} + x^{-2}$$

REF: 061723aai NAT: A.APR.D.6 TOP: Expressions with Negative Exponents

KEY: variables

68 ANS: 1

$$\begin{array}{r} 3x^2 + 4x - 1 \\ 2x + 3 \overline{) 6x^3 + 17x^2 + 10x + 2} \\ \underline{6x^3 + 9x^2} \phantom{+ 2} \\ 8x^2 + 10x \phantom{+ 2} \\ \underline{8x^2 + 12x} \phantom{+ 2} \\ -2x + 2 \phantom{+ 2} \\ \underline{-2x - 3} \\ 5 \end{array}$$

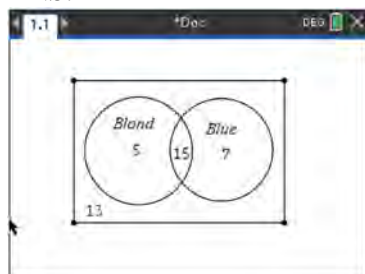
REF: fall1503aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

69 ANS: 3 REF: 012015aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

70 ANS: 2



$$40 - (20 + 22 - 15) = 13$$

REF: 062204aai NAT: S.CP.A.1 TOP: Venn Diagrams

71 ANS: 4

1)  $d(2) = 2$ ; 2)  $d(1) = 12$ ; 3)  $d(9) \approx 11$ ; 4)  $d(-1) = 2$ 

REF: 062220aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

72 ANS: 2

$$(2 - yi)(2 - yi) = 4 - 4yi + y^2 i^2 = -y^2 - 4yi + 4$$

REF: 061603aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

73 ANS: 4 REF: 082220aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

74 ANS: 3

$$\frac{f(7) - f(-7)}{7 - (-7)} = \frac{2^{-0.25(7)} \cdot \sin\left(\frac{\pi}{2}(7)\right) - 2^{-0.25(-7)} \cdot \sin\left(\frac{\pi}{2}(-7)\right)}{14} \approx -0.26$$

REF: 061721aai NAT: F.IF.B.6 TOP: Rate of Change

75 ANS: 4 REF: 061716aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

76 ANS: 3

$$d = 10 \log \frac{6.3 \times 10^{-3}}{1.0 \times 10^{-12}} \approx 98$$

REF: 011715aai NAT: F.IF.B.4 TOP: Evaluating Logarithmic Expressions

77 ANS: 3

$$y = -6x + \frac{1}{2}$$

$$x = -6y + \frac{1}{2}$$

$$x - \frac{1}{2} = -6y$$

$$-\frac{1}{6} \left( x - \frac{1}{2} \right) = y$$

REF: 062217aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

78 ANS: 4

$$x = \frac{8 \pm \sqrt{(-8)^2 - 4(6)(29)}}{2(6)} = \frac{8 \pm \sqrt{-632}}{12} = \frac{8 \pm i\sqrt{4}\sqrt{158}}{12} = \frac{2}{3} \pm \frac{1}{6}i\sqrt{158}$$

REF: 011711aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula



79 ANS: 4

$$\frac{15000}{12000} = \frac{12000e^{.025t}}{12000}$$

$$1.25 = e^{.025t}$$

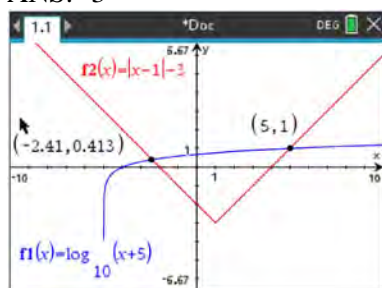
$$\ln 1.25 = \ln e^{.025t}$$

$$\ln 1.25 = .025t$$

$$\frac{\ln 1.25}{.025} = t$$

REF: 082209aia NAT: F.LE.A.4 TOP: Exponential Growth

80 ANS: 3



REF: 012317aia NAT: A.REI.D.11 TOP: Other Systems

81 ANS: 4

1) is a correct formula, but not recursive

REF: 082216aia NAT: F.LE.A.2 TOP: Sequences KEY: recursive

82 ANS: 3

The pattern suggests an exponential pattern, not linear or sinusoidal. A 4% growth rate is accurate, while a 43% growth rate is not.

REF: 011713aia NAT: S.ID.B.6 TOP: Regression KEY: choose model

83 ANS: 1

$$\begin{array}{r|rrrrr} 2 & 1 & 0 & -4 & -4 & 8 \\ & & 2 & 4 & 0 & -8 \\ \hline & 1 & 2 & 0 & -4 & 0 \end{array}$$

Since there is no remainder when the quartic is divided by  $x - 2$ , this binomial is a factor.

REF: 061711aia NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

84 ANS: 3

REF: 082214aia NAT: F.IF.C.7 TOP: Graphing Exponential Functions

85 ANS: 2

The mass of the carbon-14 is decreasing by half every 5715 years.

REF: 062211aia NAT: F.LE.B.5 TOP: Modeling Exponential Functions

86 ANS: 1

$$\frac{A}{P} = e^{rt}$$

$$0.42 = e^{rt}$$

$$\ln 0.42 = \ln e^{rt}$$

$$-0.87 \approx rt$$

REF: 011723aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

87 ANS: 2

$$p(x) = 4^x, q(x) = \left(\frac{5}{9}\right)^x, r(x) = 5.29^x, s(x) = 2^x$$

REF: 012304aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

88 ANS: 4

$$y = g(x) = (x-2)^2 \quad (x-2)^2 = 3x-2 \quad y = 3(6)-2 = 16$$

$$x^2 - 4x + 4 = 3x - 2 \quad y = 3(1) - 2 = 1$$

$$x^2 - 7x + 6 = 0$$

$$(x-6)(x-1) = 0$$

$$x = 6, 1$$

REF: 011705aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

89 ANS: 3

$$1.0525^{\frac{1}{12}} \approx 1.00427$$

REF: 061621aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

90 ANS: 3 REF: 061710aai NAT: S.IC.A.2 TOP: Analysis of Data

91 ANS: 2

$$2x^3 + x^2 - 18x - 9$$

$$x^2(2x+1) - 9(2x+1)$$

$$(x^2 - 9)(2x+1)$$

$$(x+3)(x-3)(2x+1)$$

REF: 082206aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

92 ANS: 1

1) let  $y = x + 2$ , then  $y^2 + 2y - 8$ 

$$(y + 4)(y - 2)$$

$$(x + 2 + 4)(x + 2 - 2)$$

$$(x + 6)x$$

REF: 081715aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: multivariable

93 ANS: 2

$$2x + 4y - 2z = 2 \quad -x - 3y + 2z = 0 \quad x + y = 2 \quad 3 + 2y - z = 1 \quad 2y - z = -2$$

$$\underline{-x - 3y + 2z = 0} \quad \underline{4x - 8y + 2z = 20} \quad \underline{x - y = 4} \quad 6 - 4y + z = 10 \quad \underline{2(-1) - z = -2}$$

$$x + y = 2 \quad 5x - 5y = 20 \quad 2x = 6 \quad 2y - z = -2 \quad z = 0$$

$$x - y = 4 \quad x = 3 \quad \underline{-4y + z = 4}$$

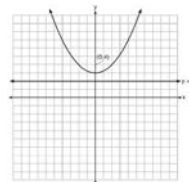
$$-2y = 2$$

$$y = -1$$

REF: 062208aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

94 ANS: 4



A parabola with a focus of  $(0, 4)$  and a directrix of  $y = 2$  is sketched as follows: By inspection, it is determined that the vertex of the parabola is  $(0, 3)$ . It is also evident that the distance,  $p$ , between the vertex and the focus is 1. It is possible to use the formula  $(x - h)^2 = 4p(y - k)$  to derive the equation of the parabola as follows:  $(x - 0)^2 = 4(1)(y - 3)$

$$x^2 = 4y - 12$$

$$x^2 + 12 = 4y$$

$$\frac{x^2}{4} + 3 = y$$

or A point  $(x, y)$  on the parabola must be the same distance from the focus as it is from the directrix. For any such point  $(x, y)$ , the distance to the focus is  $\sqrt{(x - 0)^2 + (y - 4)^2}$  and the distance to the directrix is  $y - 2$ . Setting this equal leads to:  $x^2 + y^2 - 8y + 16 = y^2 - 4y + 4$

$$x^2 + 16 = 4y + 4$$

$$\frac{x^2}{4} + 3 = y$$

REF: spr1502aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

95 ANS: 1

The zeros of the polynomial are at  $-b$ , and  $c$ . The sketch of a polynomial of degree 3 with a negative leading coefficient should have end behavior showing as  $x$  goes to negative infinity,  $f(x)$  goes to positive infinity. The multiplicities of the roots are correctly represented in the graph.

REF: spr1501aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

KEY: bimodalgraph

96 ANS: 4

The distance between the focus and directrix is  $1 - -3 = 4$ .  $p$  is half this distance, or 2. The vertex of the parabola is  $(4, -1)$ . Since the directrix is above the focus, the parabola faces downward.  $y = -\frac{1}{4p}(x - h)^2 + k$

$$y = -\frac{1}{4(2)}(x - 4)^2 - 1$$

$$y + 1 = -\frac{1}{8}(x - 4)^2$$

REF: 012322aii NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

97 ANS: 1

REF: 081616aii NAT: F.TF.A.1 TOP: Unit Circle

KEY: bimodalgraph

98 ANS: 1

$$\frac{N(6) - N(0)}{6 - 0} \approx -8.93$$

REF: 012012aii NAT: F.IF.B.6 TOP: Rate of Change

99 ANS: 3

$$0.75^{\frac{1}{10}} \approx .9716$$

REF: 061713aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

100 ANS: 4

REF: 082205aii NAT: F.TF.A.2 TOP: Unit Circle

101 ANS: 3

$$(x + a)^2 + 5(x + a) + 4 \quad \text{let } u = x + a$$

$$u^2 + 5u + 4$$

$$(u + 4)(u + 1)$$

$$(x + a + 4)(x + a + 1)$$

REF: 012006aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: multivariable

102 ANS: 4

REF: 081707aii NAT: F.TF.A.2 TOP: Reference Angles

KEY: bimodalgraph

103 ANS: 1

$$\ln e^{x+2} = \ln \frac{7}{5}$$

$$(x+2)\ln e = \ln \frac{7}{5}$$

$$x = -2 + \ln \frac{7}{5}$$

REF: 062207aai NAT: F.LE.A.4 TOP: Exponential Equations

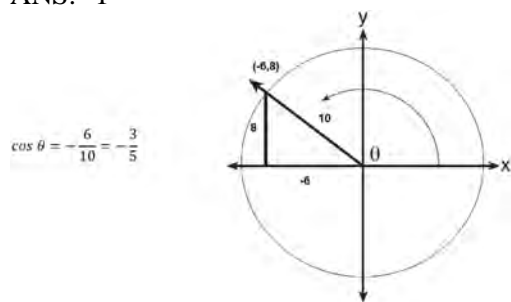
KEY: without common base

104 ANS: 4

1)  $-1$  is also a zero. 2)  $x^2(x-a) + 16(x-a) = (x^2 + 16)(x-a)$   $a$  is the only zero. 3)  $-a$  is the only zero. 4)  $x^2(x-a) - 9(x-a) = (x^2 - 9)(x-a)$ .

REF: 012019aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

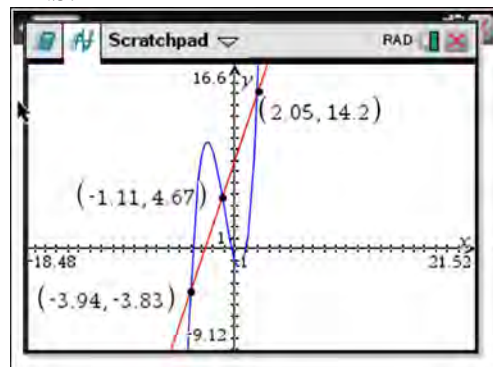
105 ANS: 1



REF: 061617aai NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: extension to reals

106 ANS: 4



REF: 061622aai NAT: A.REI.D.11 TOP: Other Systems

107 ANS: 4

$$2 \times 0.035 = 0.07 \text{ or } ME = \left( z \sqrt{\frac{p(1-p)}{n}} \right) = \left( 1.96 \sqrt{\frac{(0.65)(0.35)}{200}} \right) \approx 0.07$$

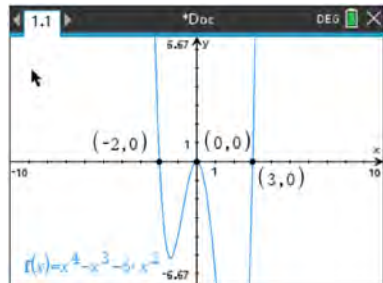
REF: 012319aai NAT: S.IC.B.4 TOP: Analysis of Data

- 108 ANS: 1 REF: 082221aii NAT: F.BF.B.6 TOP: Sigma Notation  
KEY: represent
- 109 ANS: 1  
The car lost approximately 19% of its value each year.  
  
REF: 081613aii NAT: F.LE.B.5 TOP: Modeling Exponential Functions
- 110 ANS: 4 REF: 081718aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: amplitude
- 111 ANS: 3 REF: 062205aii NAT: F.BF.B.3 TOP: Transformations with Functions
- 112 ANS: 2 REF: 061724aii NAT: A.SSE.B.4 TOP: Series  
KEY: geometric
- 113 ANS: 2  
 $h(x)$  does not have a  $y$ -intercept.  
  
REF: 011719aii NAT: F.IF.C.9 TOP: Comparing Functions
- 114 ANS: 1 REF: 081722aii NAT: S.IC.B.6 TOP: Analysis of Data
- 115 ANS: 2 REF: 062219aii NAT: F.TF.A.1 TOP: Unit Circle
- 116 ANS: 4  
 $(x+y)^3 = x^3 + 3x^2y + 3xy^2 + y^3 \neq x^3 + 3xy + y^3$   
  
REF: 081620aii NAT: A.APR.C.4 TOP: Polynomial Identities
- 117 ANS: 4  
If  $1-i$  is one solution, the other is  $1+i$ .  $(x-(1-i))(x-(1+i)) = 0$   
 $x^2 - x - ix - x + ix + (1-i^2) = 0$   
 $x^2 - 2x + 2 = 0$
- REF: 081601aii NAT: A.REI.B.4 TOP: Complex Conjugate Root Theorem
- 118 ANS: 4 REF: 012014aii NAT: S.IC.B.5 TOP: Analysis of Data
- 119 ANS: 2  
 $a_2 = 8 + \log_{2+1} 1 = 8 + 0 = 8$   
 $a_3 = 8 + \log_{3+1} 2 = 8 + \frac{1}{2} = 8.5$
- REF: 062221aii NAT: F.IF.A.3 TOP: Sequences
- 120 ANS: 2  
 $x^2 = 3x + 40$ .  $x = -5$  is an extraneous solution.  
 $x^2 - 3x - 40 = 0$   
 $(x-8)(x+5) = 0$   
 $x = 8, -5$
- REF: 012010aii NAT: A.REI.A.2 TOP: Solving Radicals  
KEY: extraneous solutions
- 121 ANS: 2 REF: 062222aii NAT: F.IF.C.9 TOP: Comparing Functions

122 ANS: 2 REF: 081717aia NAT: S.IC.B.3 TOP: Analysis of Data  
KEY: type

123 ANS: 2 REF: 081610aia NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions  
KEY: increasing/decreasing

124 ANS: 2



REF: 012316aia NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

125 ANS: 4  
Translate the parent log function 2 to the right and reflect over the  $x$ -axis.

REF: 082207aia NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

126 ANS: 1  
(1)  $\frac{9-0}{2-1} = 9$  (2)  $\frac{17-0}{3.5-1} = 6.8$  (3)  $\frac{0-0}{5-1} = 0$  (4)  $\frac{17--5}{3.5-1} \approx 6.3$

REF: 011724aia NAT: F.IF.B.6 TOP: Rate of Change

127 ANS: 1  
 $(x+3)^2 + (2x-4)^2 = 8 \quad b^2 - 4ac$   
 $x^2 + 6x + 9 + 4x^2 - 16x + 16 = 8 \quad 100 - 4(5)(17) < 0$   
 $5x^2 - 10x + 17 = 0$

REF: 081719aia NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

128 ANS: 3 REF: 011710aia NAT: F.BF.A.1 TOP: Operations with Functions

129 ANS: 2  
 $x = -\frac{3}{4}y + 2$

$$-4x = 3y - 8$$

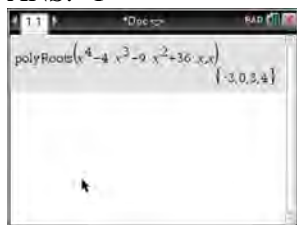
$$-4x + 8 = 3y$$

$$-\frac{4}{3}x + \frac{8}{3} = y$$

REF: 061616aia NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

130 ANS: 1



$$x^4 - 4x^3 - 9x^2 + 36x = 0$$

$$x^3(x-4) - 9x(x-4) = 0$$

$$(x^3 - 9x)(x-4) = 0$$

$$x(x^2 - 9)(x-4) = 0$$

$$x(x+3)(x-3)(x-4) = 0$$

$$x = 0, \pm 3, 4$$

REF: 061606aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

131 ANS: 2

$$5x^2 - 4x + 2 = 0 \quad \frac{4 \pm \sqrt{(-4)^2 - 4(5)(2)}}{2(5)} = \frac{4 \pm \sqrt{-24}}{10} = \frac{4 \pm 2i\sqrt{6}}{10} = \frac{2 \pm i\sqrt{6}}{5}$$

REF: 012020aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

132 ANS: 4 REF: 012303aai NAT: F.LE.B.5 TOP: Modeling Exponential Functions

133 ANS: 3

$$\sin^2 A + \left(\frac{\sqrt{5}}{3}\right)^2 = 1 \quad \text{Since } \tan A < 0, \sin A = -\frac{2}{3}$$

$$\sin^2 A + \frac{5}{9} = \frac{9}{9}$$

$$\sin^2 A = \frac{4}{9}$$

$$\sin A = \pm \frac{2}{3}$$

REF: 012320aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

134 ANS: 3 REF: 061720aai NAT: F.LE.A.2 TOP: Sequences

KEY: explicit

135 ANS: 2

$$\frac{212}{1334} \approx .16 \quad ME = \left( z \sqrt{\frac{p(1-p)}{n}} \right) = \left( 1.96 \sqrt{\frac{(0.16)(0.84)}{1334}} \right) \approx 0.02 \quad \text{or} \quad \frac{1}{\sqrt{1334}} \approx .027$$

REF: 081716aai NAT: S.IC.B.4 TOP: Analysis of Data



136 ANS: 3

Self selection causes bias.

REF: 061703aii NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

137 ANS: 1

REF: 062201aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

138 ANS: 2

$$\begin{array}{r|rrrr}
 -4 & 1 & -11 & 16 & 84 \\
 & & -4 & 60 & -304 \\
 \hline
 & 1 & -15 & 76 & 
 \end{array}$$

Since there is a remainder when the cubic is divided by  $x + 4$ , this binomial is not a factor.

REF: 081720aii NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

139 ANS: 4

REF: 062215aii NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

140 ANS: 4

$$\frac{13}{13+11} = \frac{13}{24}$$

REF: 012011aii NAT: S.CP.A.4 TOP: Conditional Probability

141 ANS: 3

$$\frac{1}{J} = \frac{1}{F} - \frac{1}{W}$$

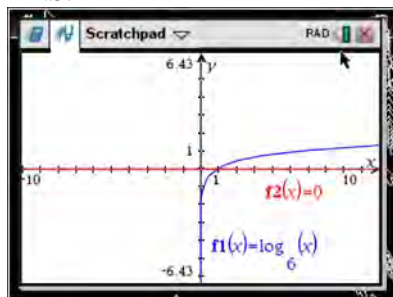
$$\frac{1}{J} = \frac{W-F}{FW}$$

$$J = \frac{FW}{W-F}$$

REF: 081617aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

142 ANS: 1



REF: 061618aii NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

143 ANS: 1

$$\frac{x(x^2 - 9)}{-(x^2 - 9)} = -x$$

REF: 012023aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: factoring

144 ANS: 2 REF: 011701aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

145 ANS: 3

$$x^2 - 6x + 9 - (x^2 + 6x + 9) = -12x$$

REF: 062210aai NAT: F.BF.A.1 TOP: Operations with Functions

146 ANS: 4

$$4(x^2 - 6x + 9) + 4(y^2 + 18y + 81) = 76 + 36 + 324$$

$$4(x - 3)^2 + 4(y + 9)^2 = 436$$

REF: 061619aai NAT: G.GPE.A.1 TOP: Equations of Circles

KEY: completing the square

147 ANS: 2 REF: 082222aai NAT: A.CED.A.1 TOP: Modeling Rationals

148 ANS: 4

$$496 \pm 2(115)$$

REF: 011718aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: interval

149 ANS: 3 REF: 011706aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

150 ANS: 3

$$x = -\frac{2y}{5} + 4 \quad y = -\frac{5}{2}(6) + 10 = -5$$

$$5x = -2y + 20$$

$$2y = -5x + 20$$

$$y = -\frac{5}{2}x + 10$$

REF: 082223aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

151 ANS: 1

$$\frac{2x}{x-2} \left( \frac{x}{x} \right) - \frac{11}{x} \left( \frac{x-2}{x-2} \right) = \frac{8}{x^2 - 2x}$$

$$2x^2 - 11x + 22 = 8$$

$$2x^2 - 11x + 14 = 0$$

$$(2x - 7)(x - 2) = 0$$

$$x = \frac{7}{2}, 2$$

REF: 061719aai NAT: A.REI.A.2 TOP: Solving Rationals

152 ANS: 2

$$2x^4 - x^3 - 16x + 8 = 0$$

$$x^3(2x - 1) - 8(2x - 1) = 0$$

$$(x^3 - 8)(2x - 1) = 0$$

$$x = 2, \frac{1}{2}$$

REF: 012307aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

153 ANS: 2

1) 1 real, mult. 2; 3) not a quadratic; 4) not a function.

REF: 012324aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

154 ANS: 1

The product of the roots equals  $(3 + i)(3 - i) = 9 - i^2 = 10 = \frac{c}{a}$ . OR

$$(x - (3 + i))(x - (3 - i)) = 0$$

$$(x - 3 - i)(x - 3 + i) = 0$$

$$((x - 3) - i)((x - 3) + i) = 0$$

$$(x - 3)^2 - i^2 = 0$$

$$x^2 - 6x + 9 + 1 = 0$$

$$x^2 - 6x + 10 = 0$$

REF: 082208aai NAT: A.REI.B.4 TOP: Complex Conjugate Root Theorem

155 ANS: 3



REF: 081604aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: probability

156 ANS: 2

$$\begin{array}{r}
 2x^2 - 3x + 7 \\
 2x + 3 \overline{) 4x^3 + 0x^2 + 5x + 10} \\
 \underline{4x^3 + 6x^2} \phantom{+ 5x + 10} \\
 -6x^2 + 5x \phantom{+ 10} \\
 \underline{-6x^2 - 9x} \phantom{+ 10} \\
 14x + 10 \\
 \underline{14x + 21} \\
 -11
 \end{array}$$

REF: 061614aai NAT: A.APR.D.6 TOP: Rational Expressions  
 KEY: division

157 ANS: 1

$$\begin{array}{r}
 2x^2 + x - 6 \\
 x + 3 \overline{) 2x^3 + 7x^2 - 3x - 25} \\
 \underline{2x^3 + 6x^2} \phantom{- 3x - 25} \\
 x^2 - 3x \phantom{- 25} \\
 \underline{x^2 + 3x} \phantom{- 25} \\
 -6x - 25 \\
 \underline{-6x - 18} \\
 -7
 \end{array}$$

REF: 062203aai NAT: A.APR.D.6 TOP: Rational Expressions  
 KEY: division

158 ANS: 2



REF: 081603aai NAT: A.REI.D.11 TOP: Other Systems

159 ANS: 4

$$g(x): \frac{10-6}{4-2} = 2 \quad t(x): \frac{3-5}{4-2} = 4$$

REF: 062212ai NAT: F.IF.C.9 TOP: Comparing Functions

160 ANS: 4 REF: 012314aii NAT: S.IC.B.3 TOP: Analysis of Data

161 ANS: 1

$$\left(1.03^{\frac{1}{12}}\right)^{12t} \approx 1.00247^{12t}$$

REF: 062224aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

162 ANS: 1

The vertical distance from the directrix to the vertex,  $p$ , is 2. The vertical distance from the vertex to the focus must also be 2.

REF: 062213aii NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

163 ANS: 2

The 2010 population is 110 million.

REF: 061718aii NAT: F.LE.B.5 TOP: Modeling Exponential Functions

164 ANS: 3 REF: 081705aii NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: increasing/decreasing

165 ANS: 1

$$\frac{2(x-4)}{(x+3)(x-4)} + \frac{3(x+3)}{(x-4)(x+3)} = \frac{2x-2}{x^2-x-12}$$

$$2x - 8 + 3x + 9 = 2x - 2$$

$$3x = -3$$

$$x = -1$$

REF: 011717aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

166 ANS: 3

Since  $x + 4$  is a factor of  $p(x)$ , there is no remainder.

REF: 081621aii NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

167 ANS: 1

$$1.0325^{\frac{1}{12}} \approx 1.0027$$

REF: 012323aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

168 ANS: 1

$$\frac{157}{25 + 47 + 157}$$

REF: 081607aii NAT: S.CP.A.4 TOP: Conditional Probability

169 ANS: 2 REF: 012311aii NAT: A.APR.C.4 TOP: Polynomial Identities

170 ANS: 4

	Bar Harbor	Phoenix
<b>Minimum</b>	31.386	66.491
<b>Midline</b>	55.3	86.729
<b>Maximum</b>	79.214	106.967
<b>Range</b>	47.828	40.476

REF: 061715aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions  
KEY: maximum/minimum

171 ANS: 3

(3) repeats 3 times over  $2\pi$ .

REF: 011722aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: recognize | bimodalgraph

172 ANS: 3 REF: 081618aai NAT: F.LE.A.2 TOP: Sequences

KEY: recursive

173 ANS: 4 REF: 061601aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

174 ANS: 2 REF: 082204aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

175 ANS: 2



$\bar{x} + 2\sigma$  represents approximately 48% of the data.

REF: 061609aai NAT: S.ID.A.4 TOP: Normal Distributions  
KEY: percent

176 ANS: 4 REF: 061706aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

177 ANS: 3

The distance from the vertex to the focus,  $p$ , is 4. Since the focus is below the vertex,  $p$  is negative.

$$y = -\frac{1}{4(4)}(x-2)^2 + 1$$

REF: 082212aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

178 ANS: 4

$$\frac{1}{2}x^2 + 2x = \frac{1}{4}x - 8 \quad b^2 - 4ac$$

$$2x^2 + 8x = x - 32 \quad 7^2 - 4(2)(32) < 0$$

$$2x^2 + 7x + 32 = 0$$

REF: 012310aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

179 ANS: 1 REF: 061708aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

180 ANS: 1

1)  $A(20) > 0$ ; 2)  $.5 \times .5 = .25$ ; 3) true; 4)  $A(7) \approx 9.9$ 

REF: 082211aii NAT: F.LE.B.5 TOP: Modeling Exponential Functions

181 ANS: 3

$$(6 - ki)^2 = 27 - 36i$$

$$36 - 12ki + k^2i^2 = 27 - 36i$$

$$9 - k^2 - 12ki = -36i$$

Set real part equal to real part:  $9 - k^2 = 0$  Set imaginary part equal to imaginary part:  $-12ki = -36i$ 

$$k = \pm 3$$

$$\frac{-12ki}{-12i} = \frac{-36i}{-12i}$$

$$k = 3$$

REF: 012308aii NAT: N.CN.A.2 TOP: Operations with Complex Numbers

182 ANS: 3

$$2d(d^3 + 3d^2 - 9d - 27)$$

$$2d(d^2(d+3) - 9(d+3))$$

$$2d(d^2 - 9)(d+3)$$

$$2d(d+3)(d-3)(d+3)$$

$$2d(d+3)^2(d-3)$$

REF: 081615aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

183 ANS: 3

REF: 011708aii

NAT: F.BF.B.4

TOP: Inverse of Functions

KEY: other

184 ANS: 3

$$\begin{array}{r} 2x+1 \\ x+2 \overline{) 2x^2+5x+8} \end{array}$$

$$\underline{2x^2+4x}$$

$$x+8$$

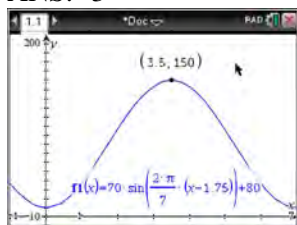
$$\underline{x+2}$$

$$6$$

REF: 012007aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

185 ANS: 3



$H(t)$  is at a minimum at  $70(-1) + 80 = 10$

REF: 061613aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

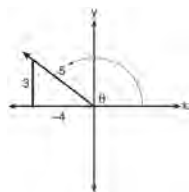
KEY: maximum/minimum

186 ANS: 4 REF: 012016aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: increasing/decreasing

187 ANS: 1

A reference triangle can be sketched using the coordinates  $(-4, 3)$  in the second quadrant to find the value of  $\sin \theta$ .



REF: spr1503aai NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: extension to reals

188 ANS: 2

$$\begin{aligned} x(30 - 0.01x) - (0.15x^3 + 0.01x^2 + 2x + 120) &= 30x - 0.01x^2 - 0.15x^3 - 0.01x^2 - 2x - 120 \\ &= -0.15x^3 - 0.02x^2 + 28x - 120 \end{aligned}$$

REF: 061709aai NAT: F.BF.A.1 TOP: Operations with Functions

189 ANS: 2

$$\begin{aligned} \sqrt{x+14} &= \sqrt{2x+5} + 1 & \sqrt{22+14} - \sqrt{2(22)+5} &= 1 \\ x+14 &= 2x+5+2\sqrt{2x+5}+1 & 6-7 &\neq 1 \\ -x+8 &= 2\sqrt{2x+5} \end{aligned}$$

$$x^2 - 16x + 64 = 8x + 20$$

$$x^2 - 24x + 44 = 0$$

$$(x-22)(x-2) = 0$$

$$x = 2, 22$$

REF: 081704aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: advanced

190 ANS: 4

$$x^3 - x^2yi - xy^2 + x^2yi - xy^2i^2 - y^3i = x^3 - xy^2 - xy^2(-1) - y^3i = x^3 - y^3i$$

REF: 062223aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers



191 ANS: 3

To determine student opinion, survey the widest range of students.

REF: 062202aia NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

192 ANS: 2



REF: 011712aia NAT: A.REI.D.11 TOP: Other Systems

193 ANS: 4

The vertex is (1,0) and  $p = 2$ .  $y = \frac{1}{4(2)}(x-1)^2 + 0$ 

REF: 061717aia NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

194 ANS: 2

$$\begin{array}{r} \phantom{x^2+3} \overline{) x^2 + 0x + 12} \\ \underline{x^2 + 0x + 3} \phantom{0} \\ 9 \phantom{0} \end{array}$$

REF: 062218aia NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

195 ANS: 2

$$\begin{array}{r} \phantom{x+2} \overline{) \frac{x^2 + 0x + 1}{x^3 + 2x^2 + x + 6}} \\ \underline{x^3 + 2x^2} \phantom{+ x + 6} \\ 0x^2 + x \phantom{+ 6} \\ \underline{0x^2 + 0x} \phantom{+ 6} \\ x + 6 \\ \underline{x + 2} \\ 4 \end{array}$$

REF: 081611aia NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

196 ANS: 2

$$\cos \theta = \pm \sqrt{1 - \left(\frac{-\sqrt{2}}{5}\right)^2} = \pm \sqrt{\frac{25}{25} - \frac{2}{25}} = \pm \frac{\sqrt{23}}{5}$$

REF: 061712aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

197 ANS: 2

The vertex of the parabola is (0,0). The distance,  $p$ , between the vertex and the focus or the vertex and thedirectrix is 1.  $y = \frac{-1}{4p}(x-h)^2 + k$ 

$$y = \frac{-1}{4(1)}(x-0)^2 + 0$$

$$y = -\frac{1}{4}x^2$$

REF: 081706aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

198 ANS: 3

REF: 061607aai NAT: S.IC.A.2 TOP: Analysis of Data

199 ANS: 1

$$\begin{aligned} u &= x + 2 & u^2 - 5u + 6 \\ & & (u-3)(u-2) \\ & & (x+2-3)(x+2-2) \\ & & (x-1)x \end{aligned}$$

REF: 012301aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

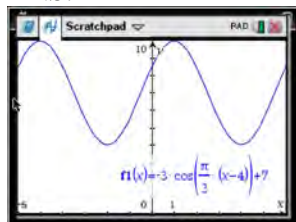
KEY: higher power

200 ANS: 4

REF: 062216aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

201 ANS: 4

As the range is  $[4,10]$ , the midline is  $y = \frac{4+10}{2} = 7$ .

REF: fall1506aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

202 ANS: 4

The vertex is (2,-1) and  $p = 2$ .  $y = -\frac{1}{4(2)}(x-2)^2 - 1$ 

REF: 081619aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

203 ANS: 1

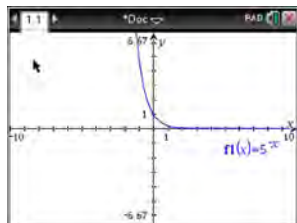
$$x^2 + 2x - 8 = 0$$

$$(x + 4)(x - 2) = 0$$

$$x = -4, 2$$

REF: 081701aai NAT: A.APR.D.6 TOP: Undefined Rationals

204 ANS: 4



$$y = 5^{-x} = \left(\frac{1}{5}\right)^x$$

REF: 061615aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

205 ANS: 1

$$x = \frac{-3 \pm \sqrt{3^2 - 4(2)(2)}}{2(2)} = \frac{-3 \pm \sqrt{-7}}{4} = -\frac{3}{4} \pm \frac{i\sqrt{7}}{4}$$

REF: 061612aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

206 ANS: 3

$$\frac{x^{\frac{1}{5}}}{x^{\frac{1}{2}}} = x^{\frac{1}{5} - \frac{1}{2}} = x^{-\frac{3}{10}} = \frac{1}{x^{\frac{3}{10}}} = \frac{1}{\sqrt[10]{x^3}}$$

REF: 012312aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

207 ANS: 4

$$d = 32(.8)^{b-1} \quad S_n = \frac{32 - 32(.8)^{12}}{1 - .8} \approx 149$$

REF: 081721aai NAT: A.SSE.B.4 TOP: Series KEY: geometric

208 ANS: 1

(2) is not recursive

REF: 081608aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

209 ANS: 3 REF: 081724aai NAT: F.BF.A.2 TOP: Sequences

210 ANS: 1

$$\frac{-12}{16} = \frac{9}{-12} = \frac{-6.75}{9}$$

REF: 012017aai NAT: F.IF.A.3 TOP: Sequences KEY: difference or ratio

211 ANS: 3

$$-33t^2 + 360t = 700 + 5t$$

$$-33t^2 + 355t - 700 = 0$$

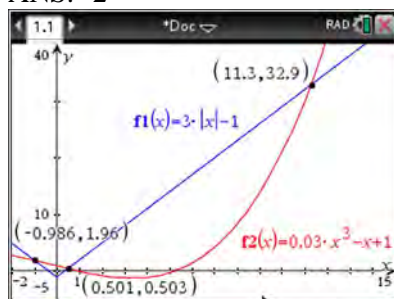
$$t = \frac{-355 \pm \sqrt{355^2 - 4(-33)(-700)}}{2(-33)} \approx 3,8$$

REF: 081606aai NAT: A.REI.D.11 TOP: Quadratic-Linear Systems

212 ANS: 1 REF: 062214aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: predict

213 ANS: 2



REF: 061705aai NAT: A.REI.D.11 TOP: Other Systems

214 ANS: 3

$$(3k - 2i)^2 = 9k^2 - 12ki + 4i^2 = 9k^2 - 12ki - 4$$

REF: 081702aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

215 ANS: 3

The graph shows three real zeros, and has end behavior matching the given end behavior.

REF: 061604aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

KEY: bimodalgraph

216 ANS: 4

$$4x^2 = -98$$

$$x^2 = -\frac{98}{4}$$

$$x^2 = -\frac{49}{2}$$

$$x = \pm \sqrt{-\frac{49}{2}} = \pm \frac{7i}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \pm \frac{7i\sqrt{2}}{2}$$

REF: 061707aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | taking square roots

217 ANS: 4

$$x(x+7) \left[ \frac{3x+25}{x+7} - 5 = \frac{3}{x} \right]$$

$$x(3x+25) - 5x(x+7) = 3(x+7)$$

$$3x^2 + 25x - 5x^2 - 35x = 3x + 21$$

$$2x^2 + 13x + 21 = 0$$

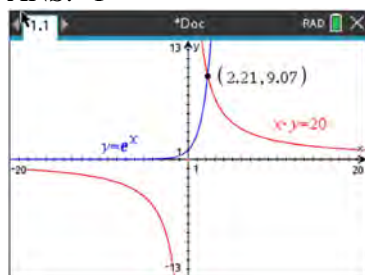
$$(2x+7)(x+3) = 0$$

$$x = -\frac{7}{2}, -3$$

REF: fall1501aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

218 ANS: 1



REF: 082210aii NAT: A.REI.D.11 TOP: Other Systems

219 ANS: 4

$$\left( \frac{-54x^9}{y^4} \right)^{\frac{2}{3}} = \frac{(2 \cdot -27)^{\frac{2}{3}} x^{\frac{18}{3}}}{y^{\frac{8}{3}}} = \frac{2^{\frac{2}{3}} \cdot 9x^6}{y^2 \cdot y^{\frac{2}{3}}} = \frac{9x^6 \sqrt[3]{4}}{y^2 \sqrt[3]{y^2}}$$

REF: 081723aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

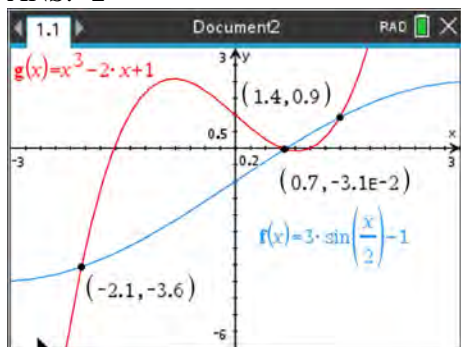
KEY: variables

220 ANS: 4

$$(1) \frac{B(60) - B(10)}{60 - 10} \approx 28\% \quad (2) \frac{B(69) - B(19)}{69 - 19} \approx 33\% \quad (3) \frac{B(72) - B(36)}{72 - 36} \approx 38\% \quad (4) \frac{B(73) - B(60)}{73 - 60} \approx 46\%$$

REF: 011721aii NAT: F.IF.B.6 TOP: Rate of Change

221 ANS: 2



REF: 012021aai NAT: A.REI.D.11 TOP: Other Systems

222 ANS: 3

$$\log_{0.8} \left( \frac{V}{17000} \right) = t \qquad \frac{17,000(0.8)^3 - 17,000(0.8)^1}{3 - 1} \approx -2450$$

$$0.8^t = \frac{V}{17000}$$

$$V = 17000(0.8)^t$$

REF: 081709aai NAT: F.IF.B.6 TOP: Rate of Change

223 ANS: 2

$$\left( m^{\frac{5}{3}} \right)^{-\frac{1}{2}} = m^{-\frac{5}{6}} = \frac{1}{\sqrt[6]{m^5}}$$

REF: 011707aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

224 ANS: 4

$$\frac{m(c)}{g(c)} = \frac{c+1}{1-c^2} = \frac{c+1}{(1+c)(1-c)} = \frac{1}{1-c}$$

REF: 061608aai NAT: F.BF.A.1 TOP: Operations with Functions

## Algebra II Multiple Choice Regents Exam Questions

### Answer Section

225 ANS: 1 REF: 081813aai NAT: A.SSE.B.4 TOP: Series

KEY: geometric

226 ANS: 2

$$y = \frac{1}{2}x + 8 \quad x = \frac{1}{2}y + 8$$

$$2x = y + 16$$

$$y = 2x - 16$$

REF: 081806aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

227 ANS: 3 REF: 061824aai NAT: A.CED.A.1 TOP: Modeling Rationals

228 ANS: 3 REF: 011824aai NAT: F.BF.A.2 TOP: Sequences

229 ANS: 2 REF: 081802aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

230 ANS: 4 REF: 011801aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

231 ANS: 1

The time of the next high tide will be the midpoint of consecutive low tides.

REF: 011907aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

232 ANS: 1

$$p(x) = r(x) - c(x)$$

$$-0.5x^2 + 250x - 300 = -0.3x^2 + 150x - c(x)$$

$$c(x) = 0.2x^2 - 100x + 300$$

REF: 061813aai NAT: F.BF.A.1 TOP: Operations with Functions

233 ANS: 1

$$-\sqrt{1 - \left(-\frac{3}{4}\right)^2} = -\sqrt{\frac{16}{16} - \frac{9}{16}} = -\sqrt{\frac{7}{16}} = -\frac{\sqrt{7}}{4}$$

REF: 081905aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

234 ANS: 3

$$\frac{x^{\frac{2}{3}} \cdot x^{\frac{5}{2}}}{x^{\frac{1}{6}}} = \frac{x^{\frac{4}{6}} \cdot x^{\frac{15}{6}}}{x^{\frac{1}{6}}} = x^{\frac{18}{6}} = x^3$$

REF: 081812aai NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index > 2

235 ANS: 3

$$8r^3 = 216 \quad S_{12} = \frac{8 - 8(3)^{12}}{1 - 3} = 2125760$$

$$r^3 = 27$$

$$r = 3$$

REF: 081902aai NAT: A.SSE.B.4 TOP: Series KEY: geometric

236 ANS: 4

The vertex is (2,2) and  $p = 3$ .  $3 + 2 = 5$ 

REF: 081823aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

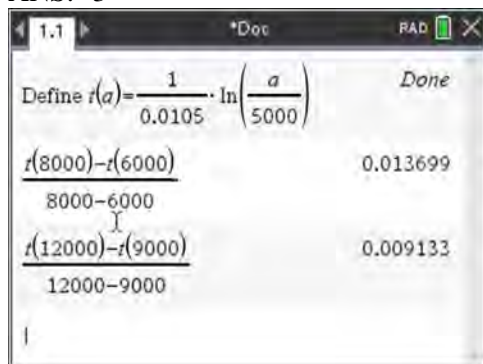
237 ANS: 2

REF: 081904aai

NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

238 ANS: 3



REF: 081922aai NAT: F.IF.B.6 TOP: Rate of Change

239 ANS: 2

$$P(B) \cdot P(A|B) = P(A \text{ and } B)$$

$$P(B) \cdot 0.8 = 0.2$$

$$P(B) = 0.25$$

REF: 081913aai NAT: S.CP.A.3 TOP: Conditional Probability

240 ANS: 3

$$1^3 - k(1)^2 + 2(1) = 0$$

$$k = 3$$

REF: 061812aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

241 ANS: 2

REF: 011901aai

NAT: S.ID.A.4 TOP: Normal Distributions

KEY: mean and standard deviation



242 ANS: 3

$$\frac{2}{3x+1} = \frac{1}{x} - \frac{6x}{3x+1} - \frac{1}{3} \text{ is extraneous.}$$

$$\frac{6x+2}{3x+1} = \frac{1}{x}$$

$$6x^2 + 2x = 3x + 1$$

$$6x^2 - x - 1 = 0$$

$$(2x-1)(3x+1) = 0$$

$$x = \frac{1}{2}, -\frac{1}{3}$$

REF: 011915aai NAT: A.REI.A.2 TOP: Solving Rationals

243 ANS: 4

$$\frac{5+9}{2} = 7, \text{ vertex: } (-2, 7); p = 7 - 9 = -2, y = \frac{1}{4(-2)}(x+2)^2 + 7$$

$$y - 7 = \frac{1}{-8}(x+2)^2$$

$$-8(y - 7) = (x + 2)^2$$

REF: 061821aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

244 ANS: 4

There is no  $x$ -intercept.

REF: 011823aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

245 ANS: 1

REF: 081804aai NAT: F.IF.C.9 TOP: Comparing Functions

246 ANS: 4

$$(a + b + c)^2 = a^2 + ab + ac + ab + b^2 + bc + ac + ab + c^2$$

$$x = a^2 + b^2 + c^2 + 2(ab + bc + ac)$$

$$x = y + 2z$$

REF: 061822aai NAT: A.APR.C.4 TOP: Polynomial Identities

247 ANS: 1

REF: 011902aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

248 ANS: 2

REF: 011910aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

249 ANS: 4

$$a_1 = 2.5 + 0.5(1) = 3$$

REF: 011916aai NAT: F.BF.A.2 TOP: Sequences

250 ANS: 1

$$6 - (3x - 2i)(3x - 2i) = 6 - (9x^2 - 12xi + 4i^2) = 6 - 9x^2 + 12xi + 4 = -9x^2 + 12xi + 10$$

REF: 061915aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

251 ANS: 1  
2) linear, 3) quadratic, 4) cubic

REF: 061920aai NAT: F.LE.A.2 TOP: Families of Functions

252 ANS: 4  
 $400 \cdot .954 \approx 380$

REF: 061918aai NAT: S.ID.A.4 TOP: Normal Distributions  
KEY: predict

253 ANS: 4

$$\frac{n}{m} = \frac{\sqrt{a^5}}{a} = \frac{a^{\frac{5}{2}}}{a^{\frac{2}{2}}} = a^{\frac{3}{2}} = \sqrt{a^3}$$

REF: 011811aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents  
KEY: variables

254 ANS: 2 REF: 061917aai NAT: F.LE.B.5 TOP: Modeling Exponential Functions

255 ANS: 1  
 $1.025^{\frac{1}{12}} \approx 1.00206$

REF: 081924aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

256 ANS: 1  
 $2000 \left( 1 + \frac{.032}{12} \right)^{12t} \approx 2000(1.003)^{12t}$

REF: 012004aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

257 ANS: 2  
 $1.00643^{12} \approx 1.08$

REF: 081808aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

258 ANS: 1 REF: 061904aai NAT: F.IF.B.6 TOP: Rate of Change

259 ANS: 2  
 $S_{20} = \frac{.01 - .01(3)^{20}}{1 - 3} = 17,433,922$

REF: 011822aai NAT: A.SSE.B.4 TOP: Series KEY: geometric

260 ANS: 2 REF: 061816aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions  
KEY: bimodalgraph

261 ANS: 2

$$2 - \frac{x-1}{x+2}$$

$$1 + \frac{x+2}{x+2} - \frac{x-1}{x+2}$$

$$1 + \frac{x+2-(x-1)}{x+2}$$

$$1 + \frac{3}{x+2}$$

REF: 081907aai NAT: A.APR.D.7 TOP: Addition and Subtraction of Rationals

262 ANS: 4

$$1 + \frac{.009}{12} = 1.00075$$

REF: 011918aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

263 ANS: 4

$$\frac{x^2 - 4x}{2x} = \frac{x(x-4)}{2x} = \frac{x-4}{2} = \frac{x}{2} - 2 = \frac{x-1}{2} - \frac{3}{2} = \frac{x-1-3}{2} = \frac{x-4}{2}$$

REF: 011921aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: factoring

264 ANS: 3

$$y = x^3 - 2$$

$$x = y^3 - 2$$

$$x + 2 = y^3$$

$$\sqrt[3]{x+2} = y$$

REF: 061815aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

265 ANS: 4

The maximum of  $p$  is 5. The minimum of  $f$  is  $-\frac{21}{4}$  ( $x = \frac{-6}{2(4)} = -\frac{3}{4}$ )

$$f\left(-\frac{3}{4}\right) = 4\left(-\frac{3}{4}\right)^2 + 6\left(-\frac{3}{4}\right) - 3 = 4\left(\frac{9}{16}\right) - \frac{18}{4} - \frac{12}{4} = -\frac{21}{4}. \quad \frac{20}{4} - \left(-\frac{21}{4}\right) = \frac{41}{4} = 10.25$$

REF: 011922aai NAT: F.IF.C.9 TOP: Comparing Functions

266 ANS: 3

REF: 061901aai NAT: S.IC.B.3 TOP: Analysis of Data

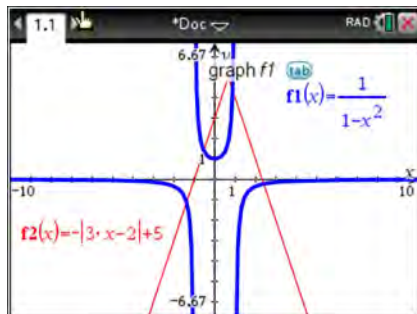
KEY: type

267 ANS: 1

$$\frac{N(10) - N(1)}{10 - 1} \approx -2.03, \frac{N(20) - N(10)}{20 - 10} \approx -1.63, \frac{N(25) - N(15)}{25 - 15} \approx -1.46, \frac{N(30) - N(1)}{30 - 1} \approx -1.64$$

REF: 061807aia NAT: F.IF.B.6 TOP: Rate of Change

268 ANS: 4



REF: 011924aia NAT: A.REI.D.11 TOP: Other Systems

269 ANS: 2

$$x^2 + 4x - 1 = x - 3 \quad y + 3 = -1$$

$$x^2 + 3x + 2 = 0 \quad y = -4$$

$$(x + 2)(x + 1) = 0$$

$$x = -2, -1$$

REF: 061801aia NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

270 ANS: 3

$$x^2 - 4x - 5 = 4x^2 - 40x + 100$$

$$3x^2 - 36x + 105 = 0$$

$$x^2 - 12x + 35 = 0$$

$$(x - 7)(x - 5) = 0$$

$$x = 5, 7$$

REF: 081807aia NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

271 ANS: 4 REF: 011805aia NAT: F.LE.B.5 TOP: Modeling Exponential Functions

272 ANS: 2

$$0.254 \pm 2(0.060) \rightarrow (0.134, 0.374)$$

REF: 061913aia NAT: S.IC.B.5 TOP: Analysis of Data

273 ANS: 2



REF: 061817aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: probability

274 ANS: 2

$$\text{If } \cos \theta = \frac{7}{25}, \sin \theta = \pm \frac{24}{25}, \text{ and } \tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\pm \frac{24}{25}}{\frac{7}{25}} = \pm \frac{24}{7}$$

REF: 081811aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

275 ANS: 1

$$x - \frac{20}{x} = 8$$

$$x^2 - 8x - 20 = 0$$

$$(x - 10)(x + 2) = 0$$

$$x = 10, -2$$

REF: 061916aai NAT: A.CED.A.1 TOP: Modeling Rationals

276 ANS: 2

$$x = \frac{2 \pm \sqrt{(-2)^2 - 4(5)(4)}}{2(5)} = \frac{2 \pm \sqrt{-76}}{10} = \frac{2 \pm i\sqrt{4}\sqrt{19}}{10} = \frac{1}{5} \pm \frac{i\sqrt{19}}{5}$$

REF: 011905aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

277 ANS: 2 REF: 011806aai NAT: A.APR.C.4 TOP: Polynomial Identities

278 ANS: 4

$$f(x) = (x + 1)(x - 1)(x - 2) = (x^2 - 1)(x - 2) = x^3 - 2x^2 - x + 2$$

REF: 081921aai NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

279 ANS: 4 REF: 081912aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

280 ANS: 1 REF: 081903aai NAT: F.LE.A.2 TOP: Families of Functions

281 ANS: 4

$$(x^6y^4 - 9)(x^4 - 16)$$

$$(x^3y^2 + 3)(x^3y^2 - 3)(x^2 + 4)(x^2 - 4)$$

REF: 081814aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

282 ANS: 2

$$u = x + 2 \quad u^2 + 4u + 3$$

$$(u + 3)(u + 1)$$

$$(x + 2 + 3)(x + 2 + 1)$$

$$(x + 5)(x + 3)$$

REF: 081901aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

283 ANS: 4 REF: 061921aai NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

284 ANS: 1

In vertex form, the parabola is  $y = -\frac{1}{4(2)}(x + 4)^2 + 3$ . The vertex is  $(-4, 3)$  and  $p = 2$ .  $3 + 2 = 5$

REF: 011816aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

285 ANS: 1

$$(2x - i)^2 - (2x - i)(2x + 3i)$$

$$(2x - i)[(2x - i) - (2x + 3i)]$$

$$(2x - i)(-4i)$$

$$-8xi + 4i^2$$

$$-8xi - 4$$

REF: 011911aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

286 ANS: 3

$$\sqrt{x+1} = x+1$$

$$x+1 = x^2 + 2x + 1$$

$$0 = x^2 + x$$

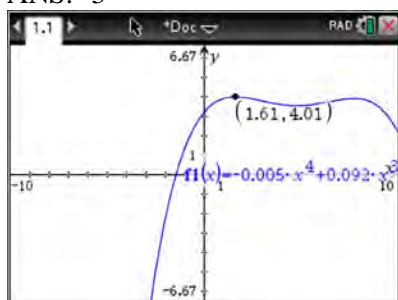
$$0 = x(x+1)$$

$$x = -1, 0$$

REF: 011802aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

287 ANS: 3



REF: 011817aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

288 ANS: 3

$$x = \frac{-2 \pm \sqrt{2^2 - 4(3)(7)}}{2(3)} = \frac{-2 \pm \sqrt{-80}}{6} = \frac{-2 \pm i\sqrt{16}\sqrt{5}}{6} = -\frac{1}{3} \pm \frac{2i\sqrt{5}}{3}$$

REF: 081809aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

289 ANS: 1

$$(x+7)(x-1) = x^2 + 6x - 7 = x^2 + 6x + 9 - 7 - 9 = (x+3)^2 - 16$$

REF: 061808aai NAT: A.APR.C.4 TOP: Polynomial Identities

290 ANS: 2

$$f(x) = f(-x)$$

$$x^2 - 4 = (-x)^2 - 4$$

$$x^2 - 4 = x^2 - 4$$

REF: 061806aai NAT: F.BF.B.3 TOP: Even and Odd Functions

291 ANS: 4

$$m^3 - 2m^2 + 4m - 8 = 0$$

$$m^2(m-2) + 4(m-2) = 0$$

$$(m^2 + 4)(m-2) = 0$$

REF: 081821aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

292 ANS: 4

$$\log_2(x-1) - 1 = 0$$

$$\log_2(x-1) = 1$$

$$x-1 = 2^1$$

$$x = 3$$

REF: 061819aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

293 ANS: 4  
1 year = 365 days

REF: 061823aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

294 ANS: 2

$$x = \frac{y}{y+2}$$

$$xy + 2x = y$$

$$xy - y = -2x$$

$$y(x - 1) = -2x$$

$$y = \frac{-2x}{x-1}$$

REF: 081924aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

295 ANS: 4 REF: 081824aai NAT: S.CP.A.3 TOP: Conditional Probability

296 ANS: 1

The cosine function has been translated +3. Since the maximum is 5 and the minimum is 1, the amplitude is 2.

$$\frac{\pi}{3} = \frac{2\pi}{b}$$

$$b = 6$$

REF: 011913aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

297 ANS: 4 REF: 061914aai NAT: A.REI.D.11 TOP: Other Systems

298 ANS: 3

$$x^2 + (2x)^2 = 5 \quad y = 2x = \pm 2$$

$$x^2 + 4x^2 = 5$$

$$5x^2 = 5$$

$$x = \pm 1$$

REF: 081916aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

299 ANS: 3 REF: 061910aai NAT: F.BF.A.2 TOP: Sequences

300 ANS: 2

(1)  $0.4 \cdot 0.3 \neq 0.2$ , (2)  $0.8 \cdot 0.25 = 0.2$ , (3)  $P(A|B) = P(A) = 0.2$ , (4)  $0.2 \neq 0.15 \cdot 0.05$

$$0.2 \neq 0.2 \cdot 0.2$$

REF: 011912aai NAT: S.CP.A.3 TOP: Conditional Probability

301 ANS: 4 REF: 081810aai NAT: F.BF.A.2 TOP: Sequences



302 ANS: 3

$$T(19) = 8 \sin(0.3(19) - 3) + 74 \approx 77$$

REF: 061922aai NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: radians

303 ANS: 1

$$x - \frac{4}{x-1} = 2 \quad x = \frac{3 \pm \sqrt{(-3)^2 - 4(1)(-2)}}{2(1)} = \frac{3 \pm \sqrt{17}}{2}$$

$$x(x-1) - 4 = 2(x-1)$$

$$x^2 - x - 4 = 2x - 2$$

$$x^2 - 3x - 2 = 0$$

REF: 011812aai NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

304 ANS: 4 REF: 011808aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

305 ANS: 4

$$1.06^{\frac{1}{52}}$$

REF: 061924aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

306 ANS: 1

$$x^3 + 2x^2 - 9x - 18 = 0 \quad x^3 - 9x + 2x^2 - 18 = 0 \quad x^3 - 9x + 2x^2 - 18 = 0$$

$$x^2(x+2) - 9(x+2) = 0 \quad x(x^2 - 9) + 2(x^2 - 9) = 0 \quad x(x^2 - 9) + 2(x^2 - 9) = 0$$

$$(x+2)(x^2 - 9) = 0$$

REF: 011903aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

307 ANS: 4

$$\sqrt{3x^2y} \cdot \sqrt[3]{27x^3y^2} = 3^{\frac{1}{2}}x^{\frac{1}{2}}y^{\frac{1}{2}} \cdot 3^{\frac{2}{3}}xy^{\frac{2}{3}} = 3^{\frac{3}{2}}x^{\frac{5}{2}}y^{\frac{7}{6}}$$

REF: 081914aai NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

308 ANS: 4

$$a = \frac{14-4}{2} = 5, d = \frac{14+4}{2} = 9$$

REF: 061810aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

309 ANS: 4

$$5000 \left( 1 + \frac{.035}{12} \right)^{12 \cdot 6} \approx 6166.50$$

REF: 081917aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions

310 ANS: 2

$$P = \frac{2\pi}{\frac{\pi}{45}} = 90$$

REF: 081822aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: period

311 ANS: 4

$$p(5) = 2(5)^3 - 3(5) + 5 = 240$$

REF: 011819aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

312 ANS: 3

$$\frac{c^2 - d^2}{d^2 + cd - 2c^2} = \frac{(c+d)(c-d)}{(d+2c)(d-c)} = \frac{-(c+d)}{d+2c} = \frac{-c-d}{d+2c}$$

REF: 011818aai NAT: A.APR.D.6 TOP: Rational Expressions  
KEY: factoring

313 ANS: 4

$$3x - (-2x + 14) = 16 \quad 3(6) - 4z = 2$$

$$5x = 30 \quad -4z = -16$$

$$x = 6 \quad z = 4$$

REF: 011803aai NAT: A.REI.C.6 TOP: Solving Linear Systems  
KEY: three variables

314 ANS: 2

$$4x \cdot x^{\frac{2}{3}} + 2x^{\frac{5}{3}} = 4x^{\frac{5}{3}} + 2x^{\frac{5}{3}} = 6x^{\frac{5}{3}} = 6\sqrt[3]{x^5}$$

REF: 061820aai NAT: N.RN.A.2 TOP: Operations with Radicals  
KEY: with variables, index > 2

315 ANS: 2

$$121(b)^2 = 64 \quad 64\left(\frac{8}{11}\right)^2 \approx 34$$

$$b = \frac{8}{11}$$

REF: 011904aai NAT: F.IF.A.3 TOP: Sequences KEY: explicit

316 ANS: 2

$$n^2(n^2 - 9) + 4n(n^2 - 9) - 12(n^2 - 9)$$

$$(n^2 + 4n - 12)(n^2 - 9)$$

$$(n + 6)(n - 2)(n + 3)(n - 3)$$

REF: 061911aii NAT: A.SSE.A.2 TOP: Factoring Polynomials  
KEY: factoring by grouping

317 ANS: 4

$$wx^2 + w = 0$$

$$w(x^2 + 1) = 0$$

$$x^2 = -1$$

$$x = \pm i$$

REF: 061912aii NAT: A.REI.B.4 TOP: Solving Quadratics  
KEY: complex solutions | taking square roots

318 ANS: 3 REF: 011917aii NAT: F.BF.B.4 TOP: Inverse of Functions  
KEY: other

319 ANS: 4

$$(x - y)^2 = x^2 - 2xy + y^2 \quad (x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

REF: 061902aii NAT: A.APR.C.4 TOP: Polynomial Identities

320 ANS: 1

$$-4(-1) - 3 = 1 \quad 8 = \frac{2\pi}{b}$$

$$b = \frac{\pi}{4}$$

REF: 081820aii NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions  
KEY: maximum/minimum

321 ANS: 2 REF: 081908aii NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

322 ANS: 1

$$1240(1.06)^x = 890(1.11)^x$$

$$x \approx 7$$

REF: 061814aii NAT: A.REI.D.11 TOP: Other Systems

323 ANS: 2

$$x + y - z = 6 \quad 2x + 2y - 2z = 12 \quad 5y - 4z = 31 \quad 5y - 2(-4) = 23 \quad x + 3 - (-4) = 6$$

$$\underline{-x + 4y - z = 17} \quad \underline{2x - 3y + 2z = -19} \quad \underline{5y - 2z = 23} \quad 5y = 15 \quad x = -1$$

$$5y - 2z = 23 \quad 5y - 4z = 31 \quad -2z = 8 \quad y = 3$$

$$z = -4$$

REF: 061923aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

324 ANS: 1

$$(x^{\frac{3}{2}})^2 = x^3$$

REF: 061908aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

325 ANS: 2

$$x = -6(y - 2)$$

$$-\frac{x}{6} = y - 2$$

$$-\frac{x}{6} + 2 = y$$

REF: 011821aii NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

326 ANS: 4

$$S_7 = \frac{85000 - 85000(1.06)^7}{1 - 1.06} \approx 713476.20$$

REF: 061905aii NAT: A.SSE.B.4 TOP: Series KEY: geometric

327 ANS: 2 REF: 081816aii NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

KEY: bimodalgraph

328 ANS: 2

$$x = 4y + 5$$

$$x - 5 = 4y$$

$$\frac{1}{4}x - \frac{5}{4} = y$$

REF: 061909aii NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

329 ANS: 3

$$\begin{array}{r}
 2x^3 - 4x^2 - x + \frac{14}{x+6} \\
 x+6 \overline{) 2x^4 + 8x^3 - 25x^2 - 6x + 14} \\
 \underline{2x^4 + 12x^3} \phantom{- 25x^2 - 6x + 14} \\
 -4x^3 - 25x^2 \phantom{- 6x + 14} \\
 \underline{-4x^3 - 24x^2} \phantom{- 6x + 14} \\
 -x^2 - 6x + 14 \\
 \underline{-x^2 - 6x} \phantom{+ 14} \\
 14
 \end{array}$$

REF: 081805aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

330 ANS: 1

$$\begin{array}{r}
 2x^2 + x + 5 \\
 2x-1 \overline{) 4x^3 + 0x^2 + 9x - 5} \\
 \underline{4x^3 - 2x^2} \phantom{+ 9x - 5} \\
 2x^2 + 9x - 5 \\
 \underline{2x^2 - x} \phantom{- 5} \\
 10x - 5 \\
 \underline{10x - 5} \\
 0
 \end{array}$$

REF: 081713aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

331 ANS: 1

$$84.1\% \times 750 \approx 631$$

REF: 011923aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: predict

332 ANS: 4

$$\begin{aligned}
 \ln e^{0.3x} &= \ln \frac{5918}{87} \\
 x &= \frac{\ln \frac{5918}{87}}{0.3}
 \end{aligned}$$

REF: 081801aai NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

333 ANS: 3

$$1.04^{\frac{1}{12}} \approx 1.0032737$$

REF: 011906aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

334 ANS: 3

$$(x + 3i)^2 - (2x - 3i)^2 = x^2 + 6xi + 9i^2 - (4x^2 - 12xi + 9i^2) = -3x^2 + 18xi$$

REF: 061805aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

335 ANS: 4

REF: 081803aai NAT: F.BF.A.1 TOP: Operations with Functions

336 ANS: 1

REF: 011815aai NAT: F.TF.A.2 TOP: Unit Circle

337 ANS: 1

$$x^2 + 2x + 1 = (x + 1)^2$$

REF: 011919aai NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

338 ANS: 3

$$y = 278(0.5)^{\frac{18}{1.8}} \approx 0.271$$

REF: 011920aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions

339 ANS: 4

(1) quadratic has two roots and both are real  $(-2,0)$  and  $(-0.5,0)$ , (2)  $x = \pm\sqrt{32} - 3$ , (3) the real root is 3, with a multiplicity of 2, (4)  $x = \pm 4i$

REF: 011909aai NAT: A.REI.B.4 TOP: Using the Discriminant

KEY: determine nature of roots given equation, graph, table

340 ANS: 3

$$(x + 4)^2 - 10 = 3x + 6 \quad y = 3(-5) + 6 = -9$$

$$x^2 + 8x + 16 - 10 = 3x + 6 \quad y = 3(0) + 6 = 6$$

$$x^2 + 5x = 0$$

$$x(x + 5) = 0$$

$$x = -5, 0$$

REF: 061903aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

341 ANS: 4

$$120 = 68 + (195 - 68)e^{-0.05t}$$

$$52 = 127e^{-0.05t}$$

$$\ln \frac{52}{127} = \ln e^{-0.05t}$$

$$\ln \frac{52}{127} = -0.05t$$

$$\frac{\ln \frac{52}{127}}{-0.05} = t$$

$$18 \approx t$$

REF: 081918aai NAT: F.LE.A.4 TOP: Exponential Decay

342 ANS: 4

$$\frac{2}{x} = \frac{4x}{x+3}$$

$$2x + 6 = 4x^2$$

$$4x^2 - 2x - 6 = 0$$

$$2(2x^2 - x - 3) = 0$$

$$(2x - 3)(x + 1) = 0$$

$$x = \frac{3}{2}, -1$$

REF: 061809aai NAT: A.REI.A.2 TOP: Solving Rationals

343 ANS: 1 REF: 011814aai NAT: A.REI.D.11 TOP: Other Systems

344 ANS: 1

$$100 \left( \frac{1}{2} \right)^{\frac{d}{8}} = 100e^{kd}$$

$$\left( \frac{1}{2} \right)^{\frac{1}{8}} = e^k$$

$$k \approx -0.087$$

REF: 061818aai NAT: F.LE.A.4 TOP: Exponential Decay

345 ANS: 3 REF: 081819aai NAT: A.REI.D.11 TOP: Other Systems

346 ANS: 4

$$0.48 \cdot 0.25 = 0.12$$

REF: 061811aai NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: probability

347 ANS: 2 REF: 061804aai NAT: S.ID.B.6 TOP: Regression

KEY: choose model

348 ANS: 4

$$\begin{array}{r}
 5x^2 + x - 3 \\
 2x - 1 \overline{) 10x^3 - 3x^2 - 7x + 3} \\
 \underline{10x^3 - 5x^2} \phantom{- 7x + 3} \\
 2x^2 - 7x \phantom{+ 3} \\
 \underline{2x^2 - x} \phantom{+ 3} \\
 -6x + 3 \\
 \underline{-6x + 3} \\
 0
 \end{array}$$

REF: 011809aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

349 ANS: 2

$$b^2 = 2b^2 - 64 \quad -8 \text{ is extraneous.}$$

$$-b^2 = -64$$

$$b = \pm 8$$

REF: 061919aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

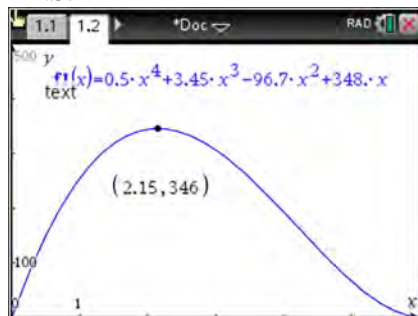
350 ANS: 3

REF: 061906aai

NAT: F.LE.A.2

TOP: Families of Functions

351 ANS: 1



REF: 011908aai NAT: F.IF.B.4

TOP: Graphing Polynomial Functions

352 ANS: 2

$$\begin{array}{r}
 85 \\
 \hline
 210 + 85
 \end{array}$$

REF: 081818aai NAT: S.CP.A.1

TOP: Venn Diagrams

353 ANS: 4

REF: 061907aai

NAT: A.APR.B.2

TOP: Remainder and Factor Theorems

354 ANS: 4

REF: 081906aai

NAT: S.IC.B.3

TOP: Analysis of Data

KEY: type

355 ANS: 4

REF: 081817aai

NAT: F.BF.B.3

TOP: Transformations with Functions



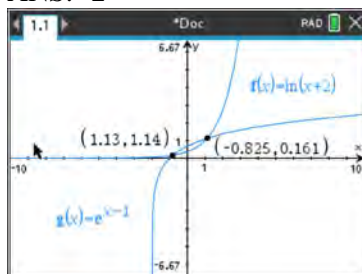
356 ANS: 1

$$\begin{array}{r}
 3x - 1 \\
 3x + 1 \overline{) 9x^2 + 0x - 2} \\
 \underline{9x^2 + 3x} \phantom{- 2} \\
 -3x - 2 \\
 \underline{-3x - 1} \\
 -1
 \end{array}$$

REF: 081910aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

357 ANS: 2



REF: 081920aai NAT: A.REI.D.11 TOP: Other Systems

358 ANS: 1



REF: 081919aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

359 ANS: 2

REF: 081911aai

NAT: F.BF.B.3

TOP: Even and Odd Functions

360 ANS: 1

$$9110 = 5000e^{30r}$$

$$\ln \frac{911}{500} = \ln e^{30r}$$

$$\frac{\ln \frac{911}{500}}{30} = r$$

$$r \approx .02$$

REF: 011810aai NAT: F.LE.A.4 TOP: Exponential Growth

- 361 ANS: 3                      REF: 081909aai      NAT: F.BF.A.2      TOP: Sequences  
 KEY: recursive
- 362 ANS: 2                      REF: 061802aai      NAT: F.IF.C.7      TOP: Graphing Exponential Functions
- 363 ANS: 2                      REF: 011804aai      NAT: F.TF.A.2      TOP: Determining Trigonometric Functions  
 KEY: radians

364 ANS: 4

$$x(x-2)\left(\frac{10}{x^2-2x} + \frac{4}{x} = \frac{5}{x-2}\right) \text{ 2 is extraneous.}$$

$$10 + 4(x-2) = 5x$$

$$10 + 4x - 8 = 5x$$

$$2 = x$$

REF: 081915aai      NAT: A.REI.A.2      TOP: Solving Rationals  
 KEY: rational solutions

365 ANS: 3  
 $440 \times 2.3\% \approx 10$

REF: 011807aai      NAT: S.ID.A.4      TOP: Normal Distributions  
 KEY: predict

366 ANS: 3

$$e^{bt} = \frac{c}{a}$$

$$\ln e^{bt} = \ln \frac{c}{a}$$

$$bt \ln e = \ln \frac{c}{a}$$

$$t = \frac{\ln \frac{c}{a}}{b}$$

REF: 011813aai      NAT: F.LE.A.4      TOP: Exponential Equations  
 KEY: without common base

367 ANS: 3

$$\frac{x^2(x+2) - 9(x+2)}{x(x^2 - x - 6)} = \frac{(x^2 - 9)(x+2)}{x(x-3)(x+2)} = \frac{(x+3)(x-3)}{x(x-3)} = \frac{x+3}{x}$$

REF: 061803aai      NAT: A.APR.D.6      TOP: Rational Expressions  
 KEY: factoring

368 ANS: 2                      REF: 011820aai      NAT: S.IC.A.2      TOP: Analysis of Data

369 ANS: 3

$$-3 + 5i - (4 + 24i - 2i - 12i^2) = -3 + 5i - (16 + 22i) = -19 - 17i$$

REF: 081815aia NAT: N.CN.A.2 TOP: Operations with Complex Numbers

370 ANS: 3

The vertex is  $(-3, 5)$  and  $p = 2$ .  $y = \frac{-1}{4(2)}(x + 3)^2 + 5$

REF: 011914aia NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

## Algebra II 2 Point Regents Exam Questions

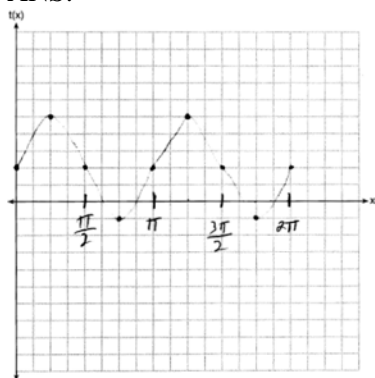
## Answer Section

371 ANS:

A student is more likely to jog if both siblings jog. 1 jogs:  $\frac{416}{2239} \approx 0.19$ . both jog:  $\frac{400}{1780} \approx 0.22$

REF: 061732aai NAT: S.CP.A.4 TOP: Conditional Probability

372 ANS:



REF: 081830aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

373 ANS:

$$3x^3 + x^2 + 3xy + y = x^2(3x + 1) + y(3x + 1) = (x^2 + y)(3x + 1)$$

REF: 011828aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

374 ANS:

Randomly assign participants to two groups. One group uses the toothpaste with ingredient X and the other group uses the toothpaste without ingredient X.

REF: 061626aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

375 ANS:

$$\frac{p(8) - p(4)}{8 - 4} \approx 48.78$$

REF: 081827aai NAT: F.IF.B.6 TOP: Rate of Change

376 ANS:

$250(1) + 2450 = 2700$  The maximum lung capacity of a person is 2700 mL.

REF: 081928aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

377 ANS:

$$\begin{array}{r}
 3x + 13 \\
 x - 2 \overline{) 3x^2 + 7x - 20} \quad 3x + 13 + \frac{6}{x - 2} \\
 \underline{3x^2 - 6x} \phantom{- 20} \\
 13x - 20 \\
 \underline{13x - 26} \\
 6
 \end{array}$$

REF: 011732aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

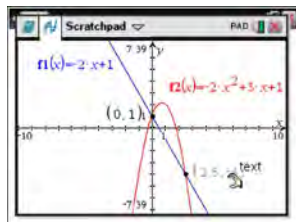
378 ANS:

period is  $\frac{2}{3}$ . The wheel rotates once every  $\frac{2}{3}$  second.

REF: 061728aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: period

379 ANS:



$$-2x + 1 = -2x^2 + 3x + 1$$

$$2x^2 - 5x = 0$$

$$x(2x - 5) = 0$$

$$x = 0, \frac{5}{2}$$

REF: fall1507aii NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

380 ANS:

$$\frac{60 - 20}{4 - 2} = \frac{40}{2} = 20$$

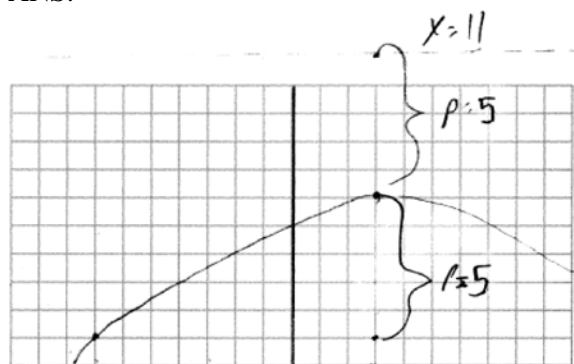
REF: 082225aii NAT: F.IF.B.6 TOP: Rate of Change

381 ANS:

Translation 3 units right and 4 units up

REF: 012027aii NAT: F.IF.C.7 TOP: Graphing Exponential Functions

382 ANS:

vertex (3, 6), focus (3, 1),  $p = 5$ , directrix  $y = 6 + 5 = 11$ 

REF: 012028aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

383 ANS:

 $2(0.042) = 0.084 \approx 0.08$  The percent of users making in-app purchases will be within 8% of 35%.

REF: 081832aai NAT: S.IC.B.4 TOP: Analysis of Data

384 ANS:

 $0.133696 \times 9256 \approx 1237$ 

REF: 082230aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: predict

385 ANS:

$$\left(p^2 n^{\frac{1}{2}}\right)^8 \sqrt{p^5 n^4} = (p^{16} n^4) p^2 n^2 \sqrt{p} = p^{18} n^6 \sqrt{p}$$

REF: 012025aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

386 ANS:

$$\frac{1}{3} \times \frac{5}{12} = \frac{5}{36}$$

REF: 012327aai NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: probability

387 ANS:

Since there are six flavors, each flavor can be assigned a number, 1-6. Use the simulation to see the number of times the same number is rolled 4 times in a row.

REF: 081728aai NAT: S.IC.A.2 TOP: Analysis of Data

388 ANS:

$$(4 - 3i)(5 + 2yi - 5 + 2yi)$$

$$(4 - 3i)(4yi)$$

$$16yi - 12yi^2$$

$$12y + 16yi$$

REF: spr1506aii NAT: N.CN.A.2 TOP: Operations with Complex Numbers

389 ANS:

$$M = \frac{(152500 - 15250) \left( \frac{.036}{12} \right) \left( 1 + \frac{.036}{12} \right)^{360}}{\left( 1 + \frac{.036}{12} \right)^{360} - 1} \approx 624$$

REF: 061831aii NAT: F.IF.B.4 TOP: Evaluating Exponential Expressions

390 ANS:

$$P(S \cap M) = P(S) + P(M) - P(S \cup M) = \frac{649}{1376} + \frac{433}{1376} - \frac{974}{1376} = \frac{108}{1376}$$

REF: 061629aii NAT: S.CP.B.7 TOP: Theoretical Probability

391 ANS:

$$\frac{\left( \ln \frac{1}{2} \right)}{1590} \text{ is negative, so } M(t) \text{ represents decay.}$$

REF: 011728aii NAT: F.IF.C.7 TOP: Graphing Exponential Functions

392 ANS:

$$t^2 + \left( \frac{4}{7} \right)^2 = 1 \quad -\frac{\sqrt{33}}{7}$$

$$t^2 + \frac{16}{49} = \frac{49}{49}$$

$$t^2 = \frac{33}{49}$$

$$t = \frac{\pm\sqrt{33}}{7}$$

REF: 011931aii NAT: F.TF.A.2 TOP: Unit Circle

393 ANS:

The denominator of the rational exponent represents the index of a root, and the 4th root of 81 is 3 and  $3^3$  is 27.

REF: 011832aii NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

394 ANS:

Self selection is a cause of bias because people with more free time are more likely to respond.

REF: 061828aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

395 ANS:

$\csc \theta = \frac{1}{\sin \theta}$ , and  $\sin \theta$  on a unit circle represents the  $y$  value of a point on the unit circle. Since  $y = \sin \theta$ ,

$$\csc \theta = \frac{1}{y}.$$

REF: 011727aai NAT: F.TF.A.2 TOP: Reciprocal Trigonometric Relationships

396 ANS:

$0 = \log_{10}(x-4)$  The  $x$ -intercept of  $h$  is  $(2,0)$ .  $f$  has the larger value.

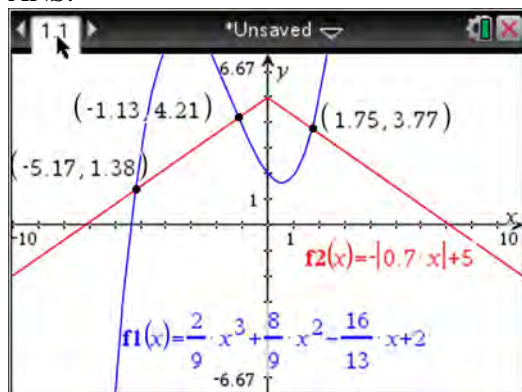
$$10^0 = x - 4$$

$$1 = x - 4$$

$$x = 5$$

REF: 081630aai NAT: F.IF.C.9 TOP: Comparing Functions

397 ANS:



REF: fall1510aai NAT: A.REI.D.11 TOP: Other Systems

398 ANS:

$$\frac{1}{x} - \frac{1}{3} = -\frac{1}{3x}$$

$$\frac{3-x}{3x} = -\frac{1}{3x}$$

$$3-x = -1$$

$$x = 4$$

REF: 061625aai NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions



399 ANS:

$$xi(-6i)^2 = xi(36i^2) = 36xi^3 = -36xi$$

REF: 081627aii NAT: N.CN.A.2 TOP: Operations with Complex Numbers

400 ANS:

$$\frac{x^{\frac{8}{3}}}{\frac{4}{x^3}} = x^y$$

$$x^{\frac{4}{3}} = x^y$$

$$\frac{4}{3} = y$$

REF: spr1505aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: numbers

401 ANS:



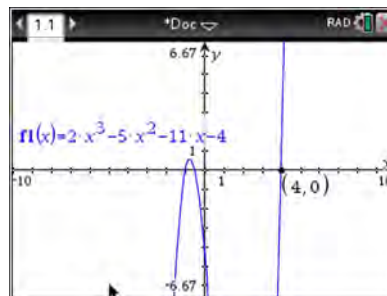
69

REF: 061726aii NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

402 ANS:

$f(4) = 2(4)^3 - 5(4)^2 - 11(4) - 4 = 128 - 80 - 44 - 4 = 0$  Any method that demonstrates 4 is a zero of  $f(x)$  confirms



that  $x - 4$  is a factor, as suggested by the Remainder Theorem.

REF: spr1507aii NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

403 ANS:

$$r = \frac{360}{300} = 1.2 \quad S_n = \frac{300 - 300(1.2)^n}{1 - 1.2} \quad S_{10} = \frac{300 - 300(1.2)^{10}}{1 - 1.2} \approx 7787.6$$

REF: 012029aii NAT: A.SSE.B.4 TOP: Series KEY: geometric

404 ANS:

$$(a+b)^3 = a^3 + b^3 \quad \text{No. Erin's shortcut only works if } a = 0, b = 0 \text{ or } a = -b.$$

$$a^3 + 3a^2b + 3ab^2 + b^3 = a^3 + b^3$$

$$3ab^2 + 3a^2b = 0$$

$$3ab(b+a) = 0$$

$$a = 0, b = 0, a = -b$$

REF: 011927aia NAT: A.APR.C.4 TOP: Polynomial Identities

405 ANS:

$$\begin{array}{r} 2a^2 + 5a + 2 \\ 3a - 2 \overline{) 6a^3 + 11a^2 - 4a - 9} \quad 2a^2 + 5a + 2 - \frac{5}{3a - 2} \\ \underline{6a^3 - 4a^2} \phantom{- 9} \\ 15a^2 - 4a \phantom{- 9} \\ \underline{15a^2 - 10a} \phantom{- 9} \\ 6a - 9 \\ \underline{6a - 4} \\ -5 \end{array}$$

REF: 061829aia NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

406 ANS:

$$\cos A = \frac{\cos A}{\sin A}$$

$$-3 = \frac{3}{\sqrt{10} \sin A}$$

$$\sin A = \frac{3}{-3\sqrt{10}} = -\frac{1}{\sqrt{10}}$$

REF: 082229aia NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

407 ANS:

$$\frac{10.1 - -2}{2} - \frac{2.5 - -0.1}{2} = 6.05 - 1.3 = 4.75$$

REF: 081930aia NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: amplitude

408 ANS:

$$-6(x+3)\left(\frac{-3}{x+3} - \frac{x}{6} + 1 = 0\right)$$

$$18 + x(x+3) - 6(x+3) = 0$$

$$18 + x^2 + 3x - 6x - 18 = 0$$

$$x^2 - 3x = 0$$

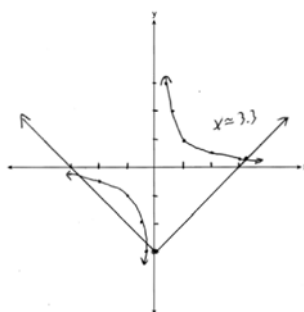
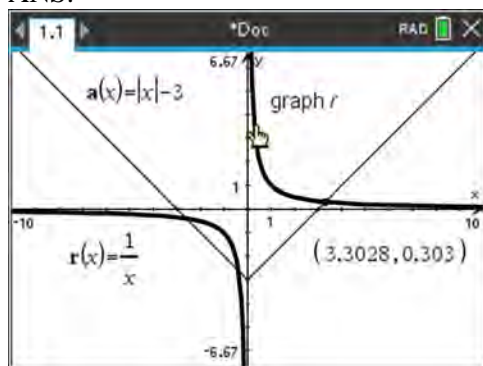
$$x(x-3) = 0$$

$$x = 0, 3$$

REF: 081829aia NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

409 ANS:



REF: 081932aia NAT: A.REI.D.11 TOP: Other Systems

410 ANS:

$$-x(2x^3 - x^2 - 18x + 9)$$

$$-x(x^2(2x-1) - 9(2x-1))$$

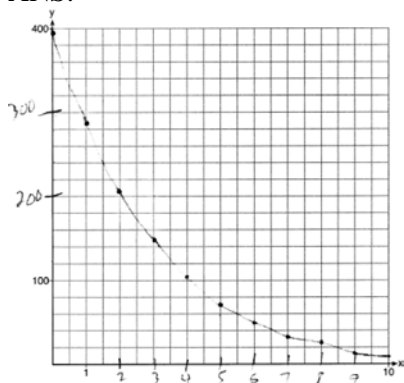
$$-x(x^2 - 9)(2x - 1)$$

$$-x(x+3)(x-3)(2x-1)$$

REF: 062228aia NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

411 ANS:



REF: 061729aia NAT: F.IF.C.7 TOP: Graphing Exponential Functions

412 ANS:

$$1200 \cdot 0.784 \approx 941$$

REF: 081828aia NAT: S.ID.A.4 TOP: Normal Distributions

KEY: predict

413 ANS:

$$A = Pe^{rt}$$

$$135000 = 100000e^{5r}$$

$$1.35 = e^{5r}$$

$$\ln 1.35 = \ln e^{5r}$$

$$\ln 1.35 = 5r$$

$$.06 \approx r \text{ or } 6\%$$

REF: 061632aia NAT: F.LE.A.4 TOP: Exponential Growth

414 ANS:

$$\frac{7}{2x} - \frac{2}{x+1} = \frac{1}{4}$$

$$\frac{7x+7-4x}{2x^2+2x} = \frac{1}{4}$$

$$2x^2 + 2x = 12x + 28$$

$$x^2 - 5x - 14 = 0$$

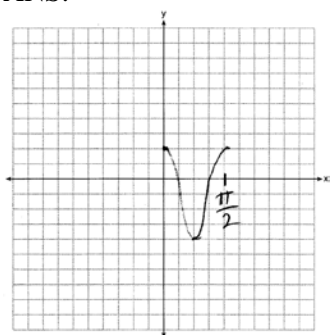
$$(x-7)(x+2) = 0$$

$$x = 7, -2$$

REF: 061926aia NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

415 ANS:



REF: 061628aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: graph

416 ANS:

$$a_1 = 4$$

$$a_n = 3a_{n-1}$$

REF: 081931aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

417 ANS:

$$\sqrt{4x+1} = 11-x \quad 20 \text{ is extraneous.}$$

$$4x+1 = 121-22x+x^2$$

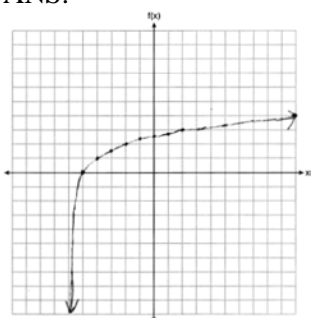
$$0 = x^2 - 26x + 120$$

$$0 = (x-6)(x-20)$$

$$x = 6, 20$$

REF: 082227aai NAT: A.REI.A.2 TOP: Solving Radicals  
KEY: extraneous solutions

418 ANS:



REF: 061927aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

419 ANS:

$$\frac{p(x)}{x-1} = x^2 + 7 + \frac{5}{x-1}$$

$$p(x) = x^3 - x^2 + 7x - 7 + 5$$

$$p(x) = x^3 - x^2 + 7x - 2$$

REF: 061930aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

420 ANS:

$P(-2) = 60$   $Q(-2) = 0$   $(x+2)$  is a factor of  $Q(x)$  since  $Q(-2) = 0$ .

REF: 081929aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

421 ANS:



43

REF: 012328aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

422 ANS:

No, because  $P(M/R) \neq P(M)$

$$\frac{70}{180} \neq \frac{230}{490}$$

$$0.38 \neq 0.47$$

REF: 011731aai NAT: S.CP.A.4 TOP: Conditional Probability

423 ANS:

No.  $0.499 \pm 2(0.049) \rightarrow 0.401 - 0.597$ . Since 0.43 falls within this interval, Robin's coin is likely not unfair.

REF: 061932aai NAT: S.IC.A.2 TOP: Analysis of Data

424 ANS:

$$\frac{\sqrt[3]{x^2 y^5}}{\sqrt[4]{x^3 y^4}} = \frac{x^{\frac{2}{3}} y^{\frac{5}{3}}}{x^{\frac{3}{4}} y^{\frac{12}{4}}} = \frac{x^{\frac{8}{12}} y^{\frac{20}{12}}}{x^{\frac{9}{12}} y^{\frac{12}{12}}} = x^{-\frac{1}{12}} y^{\frac{2}{3}}$$

REF: 011925aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

425 ANS:

$$S_5 = \frac{6 - 6(.8)^5}{1 - .8} \approx 20.17$$

REF: 062226aai NAT: A.SSE.B.4 TOP: Series KEY: geometric

426 ANS:

$$\frac{2x^{\frac{3}{2}}}{2x^{\frac{2}{2}}} = x^{\frac{1}{2}} = \sqrt{x}$$

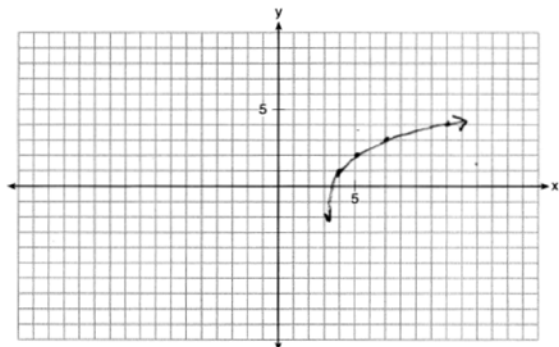
REF: 081826aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents  
KEY: variables

427 ANS:

sample: pails of oranges; population: truckload of oranges. It is likely that about 5% of all the oranges are unsatisfactory.

REF: 011726aai NAT: S.IC.A.2 TOP: Analysis of Data

428 ANS:



REF: 011932aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

429 ANS:

Yes.  $P(B) = P(B|G)$ 

$$0.14 + 0.26 = \frac{.14}{.35}$$

$$.4 = .4$$

REF: 062229aai NAT: S.CP.A.4 TOP: Conditional Probability

430 ANS:

$$\sqrt[3]{81} = \sqrt[3]{3^4} = 3^{\frac{4}{3}} \quad a = \frac{4}{3}$$

REF: 062230aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents  
KEY: variables

431 ANS:

Let  $x$  equal the first integer and  $x + 1$  equal the next.  $(x + 1)^2 - x^2 = x^2 + 2x + 1 - x^2 = 2x + 1$ .  $2x + 1$  is an odd integer.

REF: fall1511aii NAT: A.APR.C.4 TOP: Polynomial Identities

432 ANS:

$$2x^2 - 7x + 4 = 11 - 2x \quad y = 11 - 2\left(\frac{7}{2}\right) = 4 \quad \left\{\left(\frac{7}{2}, 4\right), (-1, 13)\right\}$$

$$2x^2 - 5x - 7 = 0 \quad y = 11 - 2(-1) = 13$$

$$(2x - 7)(x + 1) = 0$$

$$x = \frac{7}{2}, -1$$

REF: 082232aii NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

433 ANS:

$$\sqrt{x-4} = -x+6 \quad \sqrt{x-4} = -8+6 = -2 \text{ is extraneous.}$$

$$x-4 = x^2 - 12x + 36$$

$$0 = x^2 - 13x + 40$$

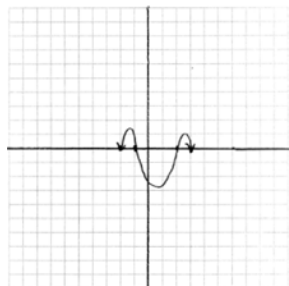
$$0 = (x-8)(x-5)$$

$$x = 5, 8$$

REF: 061730aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

434 ANS:



REF: 011831aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

435 ANS:

The denominator of the rational exponent represents the index of a root, and the numerator of the rational exponent represents the power of the base.  $\left(\sqrt{9}\right)^5 = 243$

REF: 081926aii NAT: N.RN.A.1 TOP: Radicals and Rational Exponents



436 ANS:

$$\left( \frac{y^{\frac{17}{8}}}{y^{\frac{10}{8}}} \right)^{-4} = y^n \quad n = -\frac{7}{2}$$

$$\left( y^{\frac{7}{8}} \right)^{-4} = y^n$$

$$y^{-\frac{7}{2}} = y^n$$

REF: 082228aii    NAT: A.APR.D.6    TOP: Expressions with Negative Exponents  
KEY: variables

437 ANS:

$$\frac{-1}{\sqrt{2^2 + (-1)^2}} = -\frac{1}{\sqrt{5}}$$

REF: 061832aii    NAT: F.TF.A.2    TOP: Determining Trigonometric Functions  
KEY: extension to reals

438 ANS:

$$\sin^2 \theta + (-0.7)^2 = 1 \quad \text{Since } \theta \text{ is in Quadrant II, } \sin \theta = \sqrt{.51} \text{ and } \tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\sqrt{.51}}{-0.7} \approx -1.02$$

$$\sin^2 \theta = .51$$

$$\sin \theta = \pm \sqrt{.51}$$

REF: 081628aii    NAT: F.TF.C.8    TOP: Determining Trigonometric Functions

439 ANS:

$$\frac{1}{8} + \frac{1}{6} = \frac{1}{t_b}; \quad \frac{24t_b}{8} + \frac{24t_b}{6} = \frac{24t_b}{t_b}$$

$$3t_b + 4t_b = 24$$

$$t_b = \frac{24}{7} \approx 3.4$$

REF: 011827aii    NAT: A.REI.A.2    TOP: Solving Rationals

440 ANS:

$$x = (y - 3)^3 + 1$$

$$x - 1 = (y - 3)^3$$

$$\sqrt[3]{x - 1} = y - 3$$

$$\sqrt[3]{x - 1} + 3 = y$$

$$f^{-1}(x) = \sqrt[3]{x - 1} + 3$$

REF: fall1509aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

441 ANS:

$$a^{x+1} = a^{\frac{2}{3}}$$

$$x + 1 = \frac{2}{3}$$

$$x = -\frac{1}{3}$$

REF: 012326aai NAT: A.CED.A.1 TOP: Exponential Equations

KEY: common base shown

442 ANS:

$$a_1 = 4 \quad a_8 = 639$$

$$a_n = 2a_{n-1} + 1$$

REF: 081729aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

443 ANS:

$$y = 2.459(1.616)^x$$

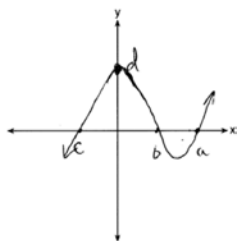
REF: 012329aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

444 ANS:

$$\frac{103}{110 + 103} = \frac{103}{213}$$

REF: 061825aai NAT: S.CP.A.4 TOP: Conditional Probability

445 ANS:



REF: 081732aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

446 ANS:

$$x^3 - 2x^2 - 9x + 18 = x^2(x-2) - 9(x-2) = (x^2 - 9)(x-2) = (x+3)(x-3)(x-2)$$

REF: 082226aia NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

447 ANS:

$$4\% \quad 8.75 = 1.25(1+r)^{49} \quad \text{or} \quad 8.75 = 1.25e^{49r}$$

$$7 = (1+r)^{49} \quad \ln 7 = \ln e^{49r}$$

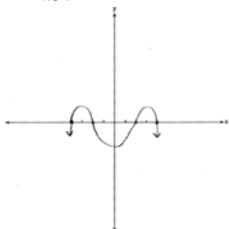
$$r+1 = \sqrt[49]{7} \quad \ln 7 = 49r$$

$$r \approx .04 \quad r = \frac{\ln 7}{49}$$

$$r \approx .04$$

REF: 081730aia NAT: F.LE.A.4 TOP: Exponential Growth

448 ANS:



REF: 011926aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

449 ANS:

$$S_{10} = \frac{15 - 15(1.03)^{10}}{1 - 1.03} \approx 171.958$$

REF: 011929aia NAT: A.SSE.B.4 TOP: Series KEY: geometric

450 ANS:

$$\left(x^{\frac{5}{3}}\right)^{\frac{6}{5}} = \left(y^{\frac{5}{6}}\right)^{\frac{6}{5}}$$

$$x^2 = y$$

REF: 011730aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents  
KEY: variables

451 ANS:

$$x^2(4x - 1) + 4(4x - 1) = (x^2 + 4)(4x - 1)$$

REF: 061727aii NAT: A.SSE.A.2 TOP: Factoring Polynomials  
KEY: factoring by grouping

452 ANS:

$$j(-x) = (-x)^4 - 3(-x)^2 - 4 = x^2 - 3x^2 - 4 \quad \text{Since } j(x) = j(-x), \text{ the function is even.}$$

REF: 081731aii NAT: F.BF.B.3 TOP: Even and Odd Functions

453 ANS:

$$3(x^3 + 4x^2 - x - 4) = 0$$

$$(x^2(x + 4) - (x + 4)) = 0$$

$$(x^2 - 1)(x + 4) = 0$$

$$x = \pm 1, -4$$

REF: 012325aii NAT: A.APR.B.3 TOP: Solving Polynomial Equations

454 ANS:

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{-7/25}{-24/25} \quad \cos \theta = \frac{-24}{25}$$

REF: 061928aii NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

455 ANS:

$$(1 - i)(1 - i)(1 - i) = (1 - 2i + i^2)(1 - i) = -2i(1 - i) = -2i + 2i^2 = -2 - 2i$$

REF: 011725aii NAT: N.CN.A.2 TOP: Operations with Complex Numbers

456 ANS:

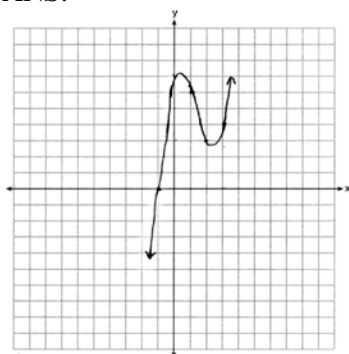
$$x^4 - 5x^2 + 4$$

$$(x^2 - 4)(x^2 - 1)$$

$$(x + 2)(x - 2)(x + 1)(x - 1)$$

REF: 012331aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

457 ANS:



REF: 012032aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

458 ANS:

$$\sqrt[3]{x} \cdot \sqrt{x} = x^{\frac{1}{3}} \cdot x^{\frac{1}{2}} = x^{\frac{3}{6}} \cdot x^{\frac{3}{6}} = x^{\frac{5}{6}}$$

REF: 061731aia NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

459 ANS:

No, because  $P(F/CR) \neq P(F)$ 

$$\frac{36}{42+36} \neq \frac{17+37+36+15}{39+17+42+12+17+37+36+15}$$

$$\frac{36}{78} \neq \frac{105}{215}$$

$$\frac{6}{13} \neq \frac{21}{43}$$

REF: 082231aia NAT: S.CP.A.4 TOP: Conditional Probability

460 ANS:

Light wave C. The periods for A, B, and C are 280, 220 and 320.

REF: 012030aia NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

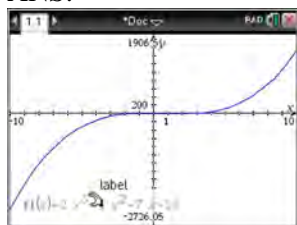
KEY: period

461 ANS:

 $q$  has the smaller minimum value for the domain  $[-2, 2]$ .  $h$ 's minimum is  $-1(2(-1)+1)$  and  $q$ 's minimum is  $-8$ .

REF: 011830aia NAT: F.IF.C.9 TOP: Comparing Functions

462 ANS:

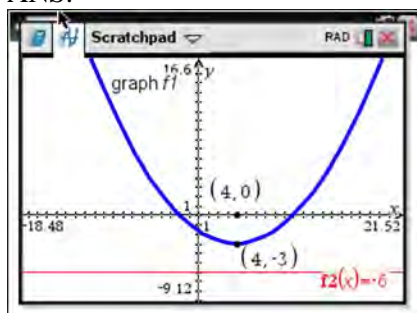


$$\begin{array}{r}
 2x^2 + 6x + 23 \\
 x - 5 \overline{) 2x^3 - 4x^2 - 7x - 10} \\
 \underline{2x^3 - 10x^2} \phantom{- 7x - 10} \\
 6x^2 - 7x \phantom{- 10} \\
 \underline{6x^2 - 30x} \phantom{- 10} \\
 23x - 10 \\
 \underline{23x - 115} \\
 105
 \end{array}$$

Since there is a remainder,  $x - 5$  is not a factor.

REF: 061627aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

463 ANS:



The vertex of the parabola is  $(4, -3)$ . The  $x$ -coordinate of the focus and the vertex is the same. Since the distance from the vertex to the directrix is 3, the distance from the vertex to the focus is 3, so the  $y$ -coordinate of the focus is 0. The coordinates of the focus are  $(4, 0)$ .

REF: 061630aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

464 ANS:

$m(3) = 3^3 - 3^2 - 5(3) - 3 = 27 - 9 - 15 - 3 = 0$  Since  $m(3) = 0$ , there is no remainder when  $m(x)$  is divided by  $x - 3$ , and so  $x - 3$  is a factor.

REF: 012026aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

465 ANS:

$r(2) = -6$ . Since there is a remainder when the cubic is divided by  $x - 2$ , this binomial is not a factor.

$$\begin{array}{r}
 2 \overline{) \begin{array}{cccc} 1 & -4 & 4 & 6 \\ & 2 & -4 & 0 \\ \hline 1 & -2 & 0 & -6 \end{array}}
 \end{array}$$

REF: 061725aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

466 ANS:

$a_1 = 3$   $a_2 = 7$   $a_3 = 15$   $a_4 = 31$ ; No, because there is no common ratio:  $\frac{7}{3} \neq \frac{15}{7}$

REF: 061830aai NAT: F.IF.A.3 TOP: Sequences KEY: recursive

467 ANS:

$\frac{306.25 - 156.25}{70 - 50} = \frac{150}{20} = 7.5$  Between 50-70 mph, each additional mph in speed requires 7.5 more feet to stop.

REF: 081631aai NAT: F.IF.B.6 TOP: Rate of Change

468 ANS:

$$\begin{aligned} & (x^3 + 2x - 1)(x^2 + 7) - 3(x^4 - 5x) \\ & x^5 + 7x^3 + 2x^3 + 14x - x^2 - 7 - 3x^4 + 15x \\ & x^5 - 3x^4 + 9x^3 - x^2 + 29x - 7 \end{aligned}$$

REF: 012330aai NAT: F.BF.A.1 TOP: Operations with Functions

469 ANS:

$$(x^2 - 6)(x^2 + 2)$$

REF: 081825aai NAT: A.SSE.A.2 TOP: Factoring Polynomials  
KEY: higher power

470 ANS:

$$P(W/D) = \frac{P(W \cap D)}{P(D)} = \frac{.4}{.5} = .8$$

REF: 081726aai NAT: S.CP.B.6 TOP: Conditional Probability

471 ANS:

$$B(t) = 100(2)^{\frac{t}{30}}$$

REF: 012031aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

472 ANS:

Amplitude, because the height of the graph shows the volume of the air.

REF: 081625aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: mixed

473 ANS:

Applying the commutative property,  $\left(3^{\frac{1}{5}}\right)^2$  can be rewritten as  $\left(3^2\right)^{\frac{1}{5}}$  or  $9^{\frac{1}{5}}$ . A fractional exponent can be rewritten as a radical with the denominator as the index, or  $9^{\frac{1}{5}} = \sqrt[5]{9}$ .

REF: 081626aai NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

474 ANS:

$$20e^{.05t} = 30e^{.03t}$$

$$\frac{\frac{2}{3}e^{.05t}}{e^{.05t}} = \frac{e^{.03t}}{e^{.05t}}$$

$$\ln \frac{2}{3} = \ln e^{-.02t}$$

$$\ln \frac{2}{3} = -.02t \ln e$$

$$\frac{\ln \frac{2}{3}}{-.02} = t$$

$$20.3 \approx t$$

REF: 011829aai NAT: A.REI.D.11 TOP: Other Systems

475 ANS:

$$\text{No. } \left( \sqrt[7]{x^2} \right) \left( \sqrt[5]{x^3} \right) = x^{\frac{2}{7}} \cdot x^{\frac{3}{5}} = x^{\frac{31}{35}} = \sqrt[35]{x^{31}}$$

REF: 061929aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

476 ANS:

$$\frac{13.9 - 9.4}{4 - 1} = 1.5 \text{ The average rate of change in the number of hours of daylight from January 1-April 1 is 1.5.}$$

REF: 061925aai NAT: F.IF.B.6 TOP: Rate of Change

477 ANS:

$$D = 1.223(2.652)^A$$

REF: 011826aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

478 ANS:

Rewrite  $\frac{4}{3}$  as  $\frac{1}{3} \cdot \frac{4}{1}$ , using the power of a power rule.

REF: 081725aai NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

479 ANS:

$$x = \frac{-5 \pm \sqrt{5^2 - 4(2)(8)}}{2(2)} = -\frac{5}{4} \pm \frac{i\sqrt{39}}{4}$$

REF: 061827aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula



480 ANS:

$$\frac{9}{6} = 1.5 \quad a_1 = 6$$

$$a_n = 1.5 \cdot a_{n-1}$$

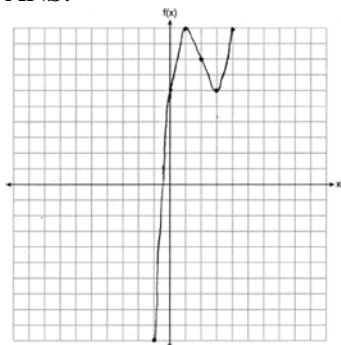
REF: 061931aii NAT: F.LE.A.2 TOP: Sequences KEY: recursive

481 ANS:

$$\frac{165 + 66 - 33}{825} = \frac{198}{825}$$

REF: 081925aii NAT: S.CP.B.6 TOP: Conditional Probability

482 ANS:



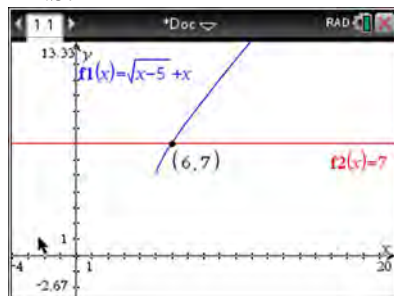
REF: 061826aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

483 ANS:

Using a 95% level of confidence,  $x \pm 2$  standard deviations sets the usual wait time as 150-302 seconds. 360 seconds is unusual.

REF: 081629aii NAT: S.IC.B.6 TOP: Analysis of Data

484 ANS:



$$\sqrt{x-5} = -x+7 \quad \sqrt{x-5} = -9+7 = -2 \text{ is extraneous.}$$

$$x-5 = x^2 - 14x + 49$$

$$0 = x^2 - 15x + 54$$

$$0 = (x-6)(x-9)$$

$$x = 6, 9$$

REF: spr1508aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

485 ANS:

$$\frac{3}{n} = \frac{2}{n^2} \quad 0 \text{ is an extraneous solution.}$$

$$3n^2 = 2n$$

$$3n^2 - 2n = 0$$

$$n(3n - 2) = 0$$

$$n = 0, \frac{2}{3}$$

REF: 062227aai NAT: A.REI.A.2 TOP: Solving Rationals

486 ANS:

$$i^2 = -1, \text{ and not } 1; 10 + 10i$$

REF: 011825aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

487 ANS:

$\pi < \theta < 2\pi \rightarrow$  Quadrant III or IV  $\theta$  must be in Quadrant IV, where  $\tan \theta$  is negative.

$$\cos \theta = \frac{\sqrt{3}}{4} \rightarrow \text{Quadrant I or IV}$$

REF: 012332aai NAT: F.TF.A.2 TOP: Finding the Terminal Side of an Angle

488 ANS:

$\frac{B(11) - B(8)}{11 - 8} \approx -10.1$  The average monthly high temperature decreases  $10.1^\circ$  each month from August to November.

REF: 011930aai NAT: F.IF.B.6 TOP: Rate of Change

489 ANS:

$$-\frac{1}{2}i^3(3i - 4) - 3i^2 = -\frac{3}{2}i^4 + 2i^3 - 3i^2 = -\frac{3}{2} - 2i + 3 = \frac{3}{2} - 2i$$

REF: 081927aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

490 ANS:

Based on these data, the two events do not appear to be independent.  $P(F) = \frac{106}{200} = 0.53$ , while

$P(F|T) = \frac{54}{90} = 0.6$ ,  $P(F|R) = \frac{25}{65} = 0.39$ , and  $P(F|C) = \frac{27}{45} = 0.6$ . The probability of being female are not the same as the conditional probabilities. This suggests that the events are not independent.

REF: fall1508aai NAT: S.CP.A.4 TOP: Conditional Probability

491 ANS:

$$F(t) = 169.136(.971)^t$$

REF: 062232aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

492 ANS:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B) \quad A \text{ and } B \text{ are independent since } P(A \cap B) = P(A) \cdot P(B)$$

$$0.8 = 0.6 + 0.5 - P(A \cap B)$$

$$0.3 = 0.6 \cdot 0.5$$

$$P(A \cap B) = 0.3$$

$$0.3 = 0.3$$

REF: 081632aii NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: independence

493 ANS:

$$b^2 - 4ac = (-4)^2 - 4(1)(13) = 16 - 52 = -36 \quad \text{imaginary}$$

REF: 062225aii NAT: A.REI.B.4 TOP: Using the Discriminant

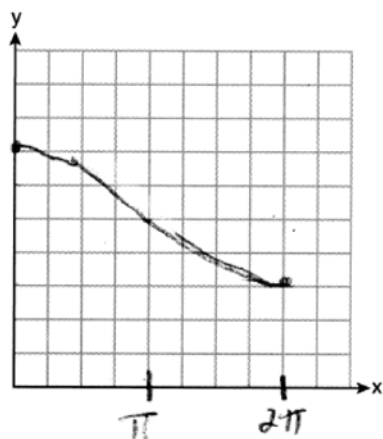
KEY: determine nature of roots given equation, graph, table

494 ANS:

$$P(A + B) = P(A) \cdot P(B|A) = 0.8 \cdot 0.85 = 0.68$$

REF: 011928aii NAT: S.CP.A.3 TOP: Conditional Probability

495 ANS:



REF: 062231aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

496 ANS:

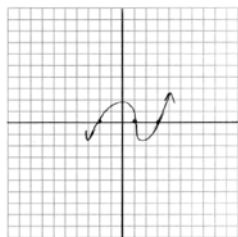
$$(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$$

$$x^4 + 2x^2y^2 + y^4 = x^4 - 2x^2y^2 + y^4 + 4x^2y^2$$

$$x^4 + 2x^2y^2 + y^4 = x^4 + 2x^2y^2 + y^4$$

REF: 081727aii NAT: A.APR.C.4 TOP: Polynomial Identities

497 ANS:



REF: 011729aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

498 ANS:

$$x^2 + (x - 28)^2 = 400 \quad y = 12 - 28 = -16 \quad y = 16 - 28 = -12$$

$$x^2 + x^2 - 56x + 784 = 400$$

$$2x^2 - 56x + 384 = 0$$

$$x^2 - 28x + 192 = 0$$

$$(x - 16)(x - 12) = 0$$

$$x = 12, 16$$

REF: 081831aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

499 ANS:

$$\frac{x^3 + 9}{x^3 + 8} = \frac{x^3 + 8}{x^3 + 8} + \frac{1}{x^3 + 8}$$

$$\frac{x^3 + 9}{x^3 + 8} = \frac{x^3 + 9}{x^3 + 8}$$

REF: 061631aai NAT: A.APR.C.4 TOP: Polynomial Identities

500 ANS:

The expression is of the form  $y^2 - 5y - 6$  or  $(y - 6)(y + 1)$ . Let  $y = 4x^2 + 5x$ :

$$(4x^2 + 5x - 6)(4x^2 + 5x + 1)$$

$$(4x - 3)(x + 2)(4x + 1)(x + 1)$$

REF: fall1512aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: a&gt;1

**Algebra II 4 Point Regents Exam Questions  
Answer Section**

501 ANS:

John found the means of the scores of the two rooms and subtracted the means. The mean score for the classical room was 7 higher than the rap room (82-75). Yes, there is less than a 5% chance this difference occurring due to random chance. It is likely the difference was due to the music.

REF: 081836aai NAT: S.IC.B.5 TOP: Analysis of Data

502 ANS:

$$\begin{array}{r}
 4x + 6y - 8z = -2 \quad 4x + 6y - 8z = -2 \quad 4x - 8y + 20z = 12 \quad z + 2 = 3z - 4 \quad y = 3 + 2 \quad -4x + 5 + 3 = 16 \\
 4x - 8y + 20z = 12 \quad \underline{-4x + y + z = 16} \quad \underline{-4x + y + z = 16} \quad 6 = 2z \quad = 5 \quad -4x = 8 \\
 -4x + y + z = 16 \quad 7y - 7z = 14 \quad -7y + 21z = 28 \quad z = 3 \quad x = -2 \\
 y - z = 2 \quad y - 3z = -4 \\
 y = z + 2 \quad y = 3z - 4
 \end{array}$$

REF: 081833aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

503 ANS:

The mean difference between the students' final grades in group 1 and group 2 is  $-3.64$ . This value indicates that students who met with a tutor had a mean final grade of 3.64 points less than students who used an on-line subscription. One can infer whether this difference is due to the differences in intervention or due to which students were assigned to each group by using a simulation to rerandomize the students' final grades many (500) times. If the observed difference  $-3.64$  is the result of the assignment of students to groups alone, then a difference of  $-3.64$  or less should be observed fairly regularly in the simulation output. However, a difference of  $-3$  or less occurs in only about 2% of the rerandomizations. Therefore, it is quite unlikely that the assignment to groups alone accounts for the difference; rather, it is likely that the difference between the interventions themselves accounts for the difference between the two groups' mean final grades.

REF: fall1514aai NAT: S.IC.B.5 TOP: Analysis of Data

504 ANS:

$$\frac{h(2) - h(1)}{2 - 1} = -12, \quad h(t) = 0 \text{ at } t \approx 2.2, 3.8, \text{ using a graphing calculator to find where } h(t) = 0.$$

REF: 061836aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

505 ANS:

$$x^2 - 6x = -17 \quad \text{The solution is imaginary because the parabola and line do not intersect.}$$

$$x^2 - 6x + 9 = -17 + 9$$

$$(x - 3)^2 = -8$$

$$x - 3 = \pm 2i\sqrt{2}$$

$$x = 3 \pm 2i\sqrt{2}$$

REF: 081936aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | completing the square

506 ANS:

$$y = 4.168(3.981)^x \quad 100 = 4.168(3.981)^x$$

$$\log \frac{100}{4.168} = \log(3.981)^x$$

$$\log \frac{100}{4.168} = x \log(3.981)$$

$$\frac{\log \frac{100}{4.168}}{\log(3.981)} = x$$

$$x \approx 2.25$$

REF: 081736aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

507 ANS:

$$20000 = PMT \left( \frac{1 - (1 + 0.00625)^{-60}}{0.00625} \right) \quad 21000 - x = 300 \left( \frac{1 - (1 + 0.00625)^{-60}}{0.00625} \right)$$

$$PMT \approx 400.76$$

$$x \approx 6028$$

REF: 011736aai NAT: F.IF.B.4 TOP: Evaluating Exponential Expressions

508 ANS:

$$3\sqrt{x} - 2x = -5 \quad 1 \text{ is extraneous.}$$

$$3\sqrt{x} = 2x - 5$$

$$9x = 4x^2 - 20x + 25$$

$$4x^2 - 29x + 25 = 0$$

$$(4x - 25)(x - 1) = 0$$

$$x = \frac{25}{4}, 1$$

REF: 011936aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

509 ANS:

$$j(-1) = 2(-1)^4 - (-1)^3 - 35(-1)^2 + 16(-1) + 48 = 2 + 1 - 35 - 16 + 48 = 0; \quad x + 1 \text{ is a factor of } j(x);$$

$$2x^3 - 3x^2 - 32x + 48 = 0$$

$$x^2(2x - 3) - 16(2x - 3) = 0$$

$$(x^2 - 16)(2x - 3) = 0$$

$$x = \pm 4, \frac{3}{2}$$

REF: 081834aai NAT: A.APR.B.2 TOP: Remainder and Factor Theorems

510 ANS:

$$N(t) = 950e^{0.0475t} \quad \text{The base is } e \text{ because growth is continuous. } N\left(\frac{36}{24}\right) \approx 1020$$

REF: 081933aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions

511 ANS:

$$x + y + z = 1 \quad x + y + z = 1 \quad x + y + z = 1 \quad -2z - z = 3 \quad y - (-1) = 3 \quad x + 2 - 1 = 1$$

$$x + 2y + 3z = 1 \quad \underline{x + 2y + 3z = 1} \quad \underline{-x + 3y - 5z = 11} \quad -3z = 3 \quad y = 2 \quad x = 0$$

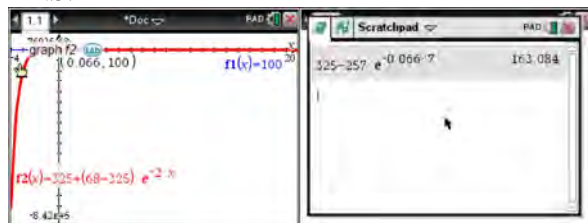
$$-x + 3y - 5z = 11 \quad y + 2z = 0 \quad 4y - 4z = 12 \quad z = -1$$

$$y = -2z \quad y - z = 3$$

REF: 061733aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

512 ANS:



$$100 = 325 + (68 - 325)e^{-2k} \quad T = 325 - 257e^{-0.066t}$$

$$-225 = -257e^{-2k} \quad T = 325 - 257e^{-0.066(7)} \approx 163$$

$$k = \frac{\ln\left(\frac{-225}{-257}\right)}{-2}$$

$$k \approx 0.066$$

REF: fall1513aai NAT: F.LE.A.4 TOP: Exponential Growth

513 ANS:

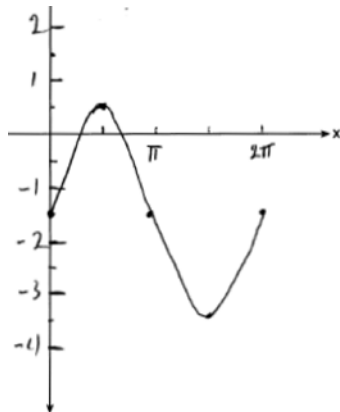
$$t = 2\pi\sqrt{\frac{67}{9.81}} \approx 16.4 \quad 9.6 = 2\pi\sqrt{\frac{L}{9.81}}$$

$$L \approx 22.9$$

REF: 062234aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: context

514 ANS:

Part a sketch is shifted  $\frac{\pi}{3}$  units right.

REF: 081735aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

515 ANS:

$$0 = 6(-5)^3 + b(-5)^2 - 52(-5) + 15 \quad z(x) = 6x^3 + 19x^2 - 52x + 15$$

$$0 = -750 + 25b + 260 + 15$$

$$475 = 25b$$

$$19 = b$$

-5	6	19	-52	15
		-30	55	15
	6	-11	3	0

$$6x^2 - 11x + 3 = 0$$

$$(2x - 3)(3x - 1) = 0$$

$$x = \frac{3}{2}, \frac{1}{3}, -5$$

REF: fall1515aii NAT: A.APR.B.2 TOP: Remainder and Factor Theorems



516 ANS:

$$x^2 + (2x - 5)^2 = 25 \quad y + 5 = 2(0) \quad y + 5 = 2(4) \quad (0, -5), (4, 3)$$

$$x^2 + 4x^2 - 20x + 25 = 25 \quad y = -5 \quad y = 3$$

$$5x^2 - 20x = 0$$

$$5x(x - 4) = 0$$

$$x = 0, 4$$

REF: 062236aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

517 ANS:

$0.506 \pm 2 \cdot 0.078 = 0.35 - 0.66$ . The 32.5% value falls below the 95% confidence level.

REF: 061736aai NAT: S.IC.B.5 TOP: Analysis of Data

518 ANS:

$0.301 \pm 2(0.058) \rightarrow 0.185 - 0.417 \frac{14}{60} \approx 0.23$ . It is not unusual because 0.23 falls within this interval.

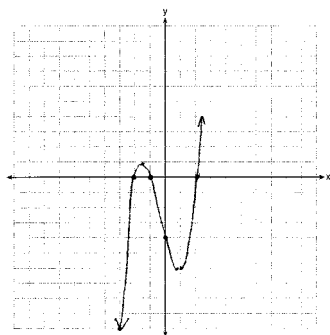
REF: 081935aai NAT: S.IC.B.5 TOP: Analysis of Data

519 ANS:

$P(F|L) = \frac{12}{27}$   $P(F) = \frac{22}{45}$  Since  $P(F|L) \neq P(F)$ , the events are not independent.

REF: 061936aai NAT: S.CP.A.4 TOP: Conditional Probability

520 ANS:



$$0 = x^2(x + 1) - 4(x + 1)$$

$$0 = (x^2 - 4)(x + 1)$$

$$0 = (x + 2)(x - 2)(x + 1)$$

$$x = -2, -1, 2$$

REF: 081633aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

521 ANS:

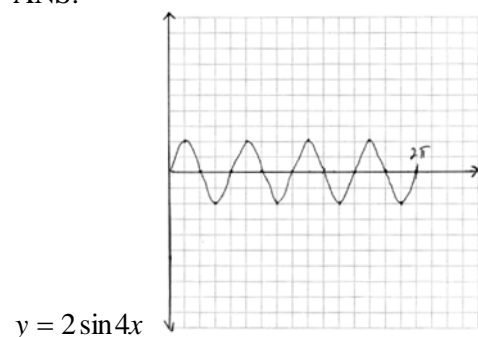
$$\begin{array}{r}
 3x^2 + 8x + 34 \\
 x - 4 \overline{) 3x^3 - 4x^2 + 2x - 1} \\
 \underline{3x^3 - 12x^2} \phantom{+ 2x - 1} \\
 8x^2 + 2x \phantom{- 1} \\
 \underline{8x^2 - 32x} \phantom{- 1} \\
 34x - 1 \\
 \underline{34x - 136} \\
 135
 \end{array}$$

$x = 4$  is not a root of  $f(x)$  because  $\frac{f(x)}{g(x)}$  has a remainder.

REF: 082235aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

522 ANS:



REF: 081934aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

523 ANS:

$$\frac{3p}{p-5} = \frac{p+2}{p+3}$$

$$3p^2 + 9p = p^2 - 3p - 10$$

$$2p^2 + 12p + 10 = 0$$

$$p^2 + 6p + 5 = 0$$

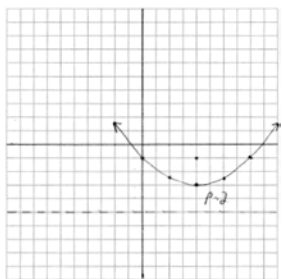
$$(p+5)(p+1) = 0$$

$$p = -5, -1$$

REF: 081733aai NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

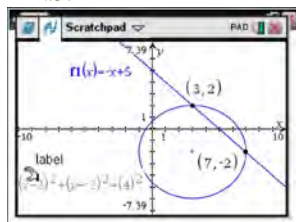
524 ANS:



$$y = \frac{1}{4(2)}(x-4)^2 - 3 \quad y = \frac{-1 + -5}{2} = -3. \text{ The vertex is } (4, -3) \text{ and } p = 2.$$

REF: 061935aia NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

525 ANS:



$$y = -x + 5 \quad y = -7 + 5 = -2$$

$$(x-3)^2 + (-x+5+2)^2 = 16 \quad y = -3 + 5 = 2$$

$$x^2 - 6x + 9 + x^2 - 14x + 49 = 16$$

$$2x^2 - 20x + 42 = 0$$

$$x^2 - 10x + 21 = 0$$

$$(x-7)(x-3) = 0$$

$$x = 7, 3$$

REF: 061633aia NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

526 ANS:

$$P(P/K) = \frac{P(P \cap K)}{P(K)} = \frac{1.9}{2.3} \approx 82.6\% \text{ A key club member has an 82.6\% probability of being enrolled in AP Physics.}$$

REF: 011735aia NAT: S.CP.B.6 TOP: Conditional Probability

527 ANS:

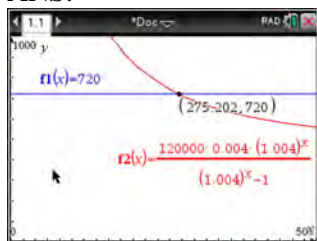
$$x+2 \overline{) \begin{array}{r} x^3 + 4 \\ x^4 + 2x^3 + 4x - 10 \end{array}} \quad x^3 + 4 - \frac{18}{x+2}. \text{ No, because there is a remainder.}$$

$$\begin{array}{r} x^4 + 2x^3 \\ \underline{x^4 + 2x^3} \\ 4x - 10 \\ \underline{4x + 8} \\ -18 \end{array}$$

REF: 011934aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

528 ANS:



$$720 = \frac{120000 \left( \frac{.048}{12} \right) \left( 1 + \frac{.048}{12} \right)^n}{\left( 1 + \frac{.048}{12} \right)^n - 1} \quad \frac{275.2}{12} \approx 23 \text{ years}$$

$$720(1.004)^n - 720 = 480(1.004)^n$$

$$240(1.004)^n = 720$$

$$1.004^n = 3$$

$$n \log 1.004 = \log 3$$

$$n \approx 275.2 \text{ months}$$

REF: spr1509aii NAT: A.CED.A.1 TOP: Exponential Growth

529 ANS:

$$M = 172600 \cdot \frac{0.00305(1 + 0.00305)^{12 \cdot 15}}{(1 + 0.00305)^{12 \cdot 15} - 1} \approx 1247 \quad 1100 = (172600 - x) \cdot \frac{0.00305(1 + 0.00305)^{12 \cdot 15}}{(1 + 0.00305)^{12 \cdot 15} - 1}$$

$$1100 \approx (172600 - x) \cdot (0.007228)$$

$$152193 \approx 172600 - x$$

$$20407 \approx x$$

REF: 061734aii NAT: F.IF.B.4 TOP: Evaluating Exponential Expressions

530 ANS:

$$2 = e^{0.0375t}$$

$$t \approx 18.5$$

REF: 081835aai NAT: F.LE.A.4 TOP: Exponential Growth

531 ANS:

$$y = 101.523(.883)^x \quad 29 = 101.523(.883)^x$$

$$\frac{29}{101.523} = (.883)^x$$

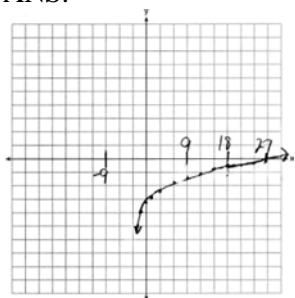
$$\log \frac{29}{101.523} = x \log(.883)$$

$$\frac{\log \frac{29}{101.523}}{\log(.883)} = x$$

$$x \approx 10.07$$

REF: 012036aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

532 ANS:

As  $x \rightarrow -3$ ,  $y \rightarrow -\infty$ . As  $x \rightarrow \infty$ ,  $y \rightarrow \infty$ .

REF: 061735aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

533 ANS:

.819  $\pm$  2  $\cdot$  .053 = .713 – .925. Since .70 does not fall within the 95% interval.

REF: 082236aai NAT: S.IC.A.2 TOP: Analysis of Data

534 ANS:

.651  $\pm$  2  $\cdot$  .034 = .58 – .72. No, since .61 (122/200) falls within the 95% interval.

REF: 062235aai NAT: S.IC.A.2 TOP: Analysis of Data

535 ANS:

$$\text{normcdf}(510, 540, 480, 24) = 0.0994 \quad z = \frac{510 - 480}{24} = 1.25 \quad 1.25 = \frac{x - 510}{20} \quad 2.5 = \frac{x - 510}{20} \quad 535-560$$

$$z = \frac{540 - 480}{24} = 2.5 \quad x = 535 \quad x = 560$$

REF: fall1516aai NAT: S.ID.A.4 TOP: Normal Distributions  
KEY: probability

536 ANS:

$$S_n = \frac{33000 - 33000(1.04)^n}{1 - 1.04} \quad S_{15} = \frac{33000 - 33000(1.04)^{15}}{1 - 1.04} \approx 660778.39$$

REF: 061634aai NAT: A.SSE.B.4 TOP: Series KEY: geometric

537 ANS:

$$7 = 20(0.5)^{\frac{t}{8.02}}$$

$$\log 0.35 = \log 0.5^{\frac{t}{8.02}}$$

$$\log 0.35 = \frac{t \log 0.5}{8.02}$$

$$\frac{8.02 \log 0.35}{\log 0.5} = t$$

$$t \approx 12$$

REF: 081634aai NAT: F.LE.A.4 TOP: Exponential Decay

538 ANS:

Jillian's plan, because distance increases by one mile each week.  $a_1 = 10$        $a_n = n + 12$ 

$$a_n = a_{n-1} + 1$$

REF: 011734aai NAT: F.BF.A.2 TOP: Sequences KEY: recursive

539 ANS:

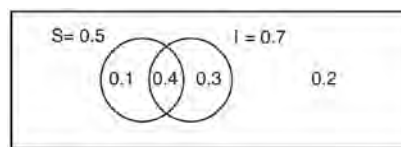
$$C(t) = 63000 \left( 1 + \frac{0.0255}{12} \right)^{12t} \quad 63000 \left( 1 + \frac{0.0255}{12} \right)^{12t} = 100000$$

$$12t \log(1.002125) = \log \frac{100}{63}$$

$$t \approx 18.14$$

REF: 061835aai NAT: A.CED.A.1 TOP: Exponential Growth

540 ANS:



This scenario can be modeled with a Venn Diagram: Since  $P(S \cup I) = 0.2$ ,  $P(S \cup I) = 0.8$ . Then,  $P(S \cap I) = P(S) + P(I) - P(S \cup I)$ . If  $S$  and  $I$  are independent, then the

$$= 0.5 + 0.7 - 0.8$$

$$= 0.4$$

Product Rule must be satisfied. However,  $(0.5)(0.7) \neq 0.4$ . Therefore, salary and insurance have not been treated independently.

REF: spr1513aii NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: independence

541 ANS:

Some of the students who did not drink energy drinks read faster than those who did drink energy drinks.

$17.7 - 19.1 = -1.4$  Differences of -1.4 and less occur  $\frac{25}{232}$  or about 10% of the time, so the difference is not unusual.

REF: 081636aii NAT: S.IC.B.5 TOP: Analysis of Data

542 ANS:

$23 - 18 = 5$ ,  $\bar{x} \pm 2\sigma = -3.07 - 3.13$ , Yes, a difference of 5 or more occurred three times out of a thousand, which is statistically significant.

REF: 061834aii NAT: S.IC.B.5 TOP: Analysis of Data

543 ANS:

$29.101 \pm 2 \cdot 0.934 = 27.23 - 30.97$ . Yes, since 30 falls within the 95% interval.

REF: 011935aii NAT: S.IC.A.2 TOP: Analysis of Data

544 ANS:

$$\frac{47}{108} = \frac{1}{4} + \frac{116}{459} - P(M \text{ and } J); \text{ No, because } \frac{31}{459} \neq \frac{1}{4} \cdot \frac{116}{459}$$

$$P(M \text{ and } J) = \frac{31}{459}$$

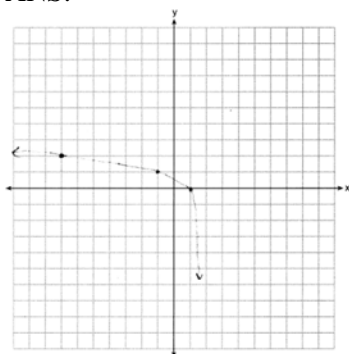
REF: 011834aii NAT: S.CP.A.3 TOP: Conditional Probability

545 ANS:

$\frac{6.25 - 2.25}{21 - 5} = \frac{4}{16} = \$0.25$  fine per day.  $2.25 - 5(.25) = \$1$  replacement fee.  $a_n = 1.25 + (n - 1)(.25)$ .  $a_{60} = \$16$

REF: 081734aii NAT: F.BF.A.2 TOP: Sequences

546 ANS:

Domain:  $x < 2$ , Asymptote  $x = 2$ 

REF: 012034aii NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

547 ANS:

$\frac{B(10) - B(6)}{10 - 6} \approx -3.88$ . The average monthly high temperature decreases about  $4^\circ$  each month from June and October.

REF: 012336aii NAT: F.IF.B.6 TOP: Rate of Change

548 ANS:

$$\text{a) } p(t) = 11000(2)^{\frac{t}{20}}; \text{ b) } \frac{1000000}{11000} = \frac{11000(2)^{\frac{t}{20}}}{11000}$$

$$\log \frac{1000}{11} = \log 2^{\frac{t}{20}}$$

$$\log \frac{1000}{11} = \frac{t \cdot \log 2}{20}$$

$$\frac{20 \log \frac{1000}{11}}{\log 2} = t$$

$$t \approx 130.13$$

REF: 082233aii NAT: F.LE.A.4 TOP: Exponential Growth

549 ANS:

$$f(x) = x^2(x+4)(x-3); g(x) = (x+2)^2(x+6)(x-1)$$

REF: 011836aii NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

550 ANS:

$\frac{1}{10}, \frac{1}{5}$ , and no, since 0.10 clearly falls within 95% of 0.20.

REF: 012334aii NAT: S.IC.A.2 TOP: Analysis of Data



551 ANS:

Yes. The margin of error from this simulation indicates that 95% of the observations fall within  $\pm 0.12$  of the simulated proportion, 0.25. The margin of error can be estimated by multiplying the standard deviation, shown to

be 0.06 in the dotplot, by 2, or applying the estimated standard error formula,  $\left(\sqrt{\frac{p(1-p)}{n}}\right)$  or  $\left(\sqrt{\frac{(0.25)(0.75)}{50}}\right)$

and multiplying by 2. The interval  $0.25 \pm 0.12$  includes plausible values for the true proportion of people who prefer Stephen's new product. The company has evidence that the population proportion could be at least 25%. As seen in the dotplot, it can be expected to obtain a sample proportion of 0.18 (9 out of 50) or less several times, even when the population proportion is 0.25, due to sampling variability. Given this information, the results of the survey do not provide enough evidence to suggest that the true proportion is not at least 0.25, so the development of the product should continue at this time.

REF: spr1512aii NAT: S.IC.B.4 TOP: Analysis of Data

552 ANS:

$$\begin{array}{rclcl}
 a + 4b + 6c = 23 & a + 2b + c = 2 & 8b + 3c = 16 & 2b + 5(4) = 21 & a + 4\left(\frac{1}{2}\right) + 6(4) = 23 \\
 \underline{a + 2b + c = 2} & \underline{-a + 6b + 2c = 14} & \underline{8b + 20c = 84} & 2b = 1 & \\
 2b + 5c = 21 & 8b + 3c = 16 & 17c = 68 & b = \frac{1}{2} & a + 2 + 24 = 23 \\
 & & c = 4 & & a = -3
 \end{array}$$

REF: 011933aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

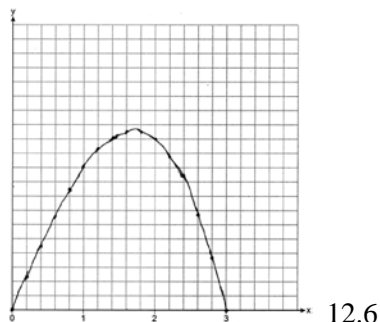
553 ANS:

$$\begin{array}{l}
 \sqrt{49 - 10x} = 2x - 5 \quad -\frac{3}{2} \text{ is extraneous.} \\
 49 - 10x = 4x^2 - 20x + 25 \\
 0 = 4x^2 - 10x - 24 \\
 0 = 2x^2 - 5x - 12 \\
 0 = (2x + 3)(x - 4) \\
 x = -\frac{3}{2}, 4
 \end{array}$$

REF: 012333aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

554 ANS:



REF: 082234aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

555 ANS:

$$2x^3 - 10x^2 + 11x - 7 = 2x^3 + hx^2 + 3x - 8x^2 - 4hx - 12 + k \quad h = -2$$

$$-2x^2 + 8x + 5 = hx^2 - 4hx + k \quad k = 5$$

REF: 011733aai NAT: A.APR.C.4 TOP: Polynomial Identities

556 ANS:

$$\left(\sqrt{2x-7}\right)^2 = (5-x)^2 \quad \sqrt{2(4)-7} + 4 = 5 \quad \sqrt{2(8)-7} + 8 = 5$$

$$2x - 7 = 25 - 10x + x^2 \quad \sqrt{1} = 1 \quad \sqrt{9} \neq -3$$

$$0 = x^2 - 12x + 32$$

$$0 = (x-8)(x-4)$$

$$x = 4, 8$$

REF: 081635aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

557 ANS:

$$a_n = x^{n-1}(x+1) \quad x^{n-1} = 0 \quad x+1 = 0$$

$$x = 0 \quad x = -1$$

REF: spr1511aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

558 ANS:

138.905  $\pm$  2  $\cdot$  7.95 = 123 – 155. No, since 125 (50% of 250) falls within the 95% interval.

REF: 011835aai NAT: S.IC.A.2 TOP: Analysis of Data

559 ANS:

$$\sqrt{6-2x} + x = 2x + 30 - 9 \quad \sqrt{6-2(-29)} \neq -29 + 21, \text{ so } -29 \text{ is extraneous.}$$

$$\sqrt{6-2x} = x + 21 \quad \sqrt{64} \neq -8$$

$$6 - 2x = x^2 + 42x + 441$$

$$x^2 + 44x + 435 = 0$$

$$(x + 29)(x + 15) = 0$$

$$x = -29, -15$$

REF: 061833aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

560 ANS:

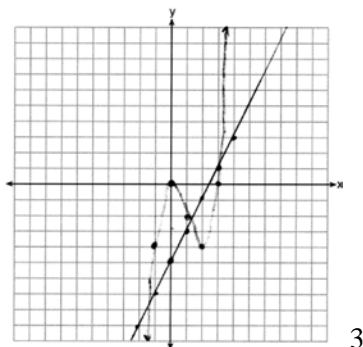
$$(2x^2 + x - 3) \bullet (x - 1) - \left[ (2x^2 + x - 3) + (x - 1) \right]$$

$$(2x^3 - 2x^2 + x^2 - x - 3x + 3) - (2x^2 + 2x - 4)$$

$$2x^3 - 3x^2 - 6x + 7$$

REF: 011833aii NAT: F.BF.A.1 TOP: Operations with Functions

561 ANS:



REF: 062233aii NAT: A.REI.D.11 TOP: Other Systems

562 ANS:

$$a_n = 100(.8)^{n-1} \quad S_{20} = \frac{100 - 100(.8)^{20}}{1 - .8} \approx 494 \text{ No, because } 494 > 40 \times 12.$$

REF: 012033aii NAT: A.SSE.B.4 TOP: Series KEY: geometric

563 ANS:

$0.602 \pm 2 \cdot 0.066 = 0.47 - 0.73$ . Since 0.50 falls within the 95% interval, this supports the concern there may be an even split.

REF: 061635aii NAT: S.IC.B.5 TOP: Analysis of Data

564 ANS:

$$16x^4 - 81 = (4x^2 + 9)(4x^2 - 9) = (4x^2 + 9)(2x + 3)(2x - 3). \text{ No, because } \pm \frac{3i}{2} \text{ are roots.}$$

REF: 061933aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

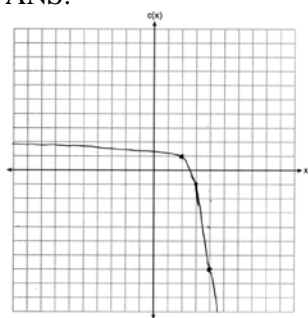
565 ANS:

$$\frac{f(4) - f(-2)}{4 - (-2)} = \frac{80 - 1.25}{6} = 13.125 \text{ } g(x) \text{ has a greater rate of change}$$

$$\frac{g(4) - g(-2)}{4 - (-2)} = \frac{179 - (-49)}{6} = 38$$

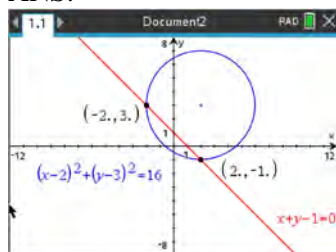
REF: 061636aai NAT: F.IF.C.9 TOP: Comparing Functions

566 ANS:

As  $x \rightarrow \infty, c(x) \rightarrow -\infty$ . As  $x \rightarrow -\infty, c(x) \rightarrow 2$ .

REF: 012335aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

567 ANS:



$$y = -x + 1 \quad y = -2 + 1 = -1 \quad (2, -1)$$

$$(x - 2)^2 + (-x + 1 - 3)^2 = 16 \quad y = 2 + 1 = 3 \quad (-2, 3)$$

$$x^2 - 4x + 4 + x^2 + 4x + 4 = 16$$

$$2x^2 = 8$$

$$x = -2, 2$$

REF: 012035aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

568 ANS:

$$s(t) = 200(0.5)^{\frac{t}{15}} \quad \frac{1}{10} = (0.5)^{\frac{t}{15}}$$

$$\log \frac{1}{10} = \log(0.5)^{\frac{t}{15}}$$

$$-1 = \frac{t \cdot \log(0.5)}{15}$$

$$t = \frac{-15}{\log(0.5)} \approx 50$$

REF: 061934aii NAT: F.LE.A.4 TOP: Exponential Decay

569 ANS:

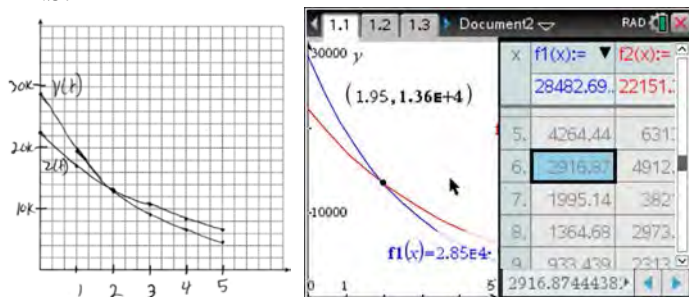
$$\begin{array}{cccccc} 6x - 3y + 2z = -10 & x + 3y + 5z = 45 & 4x + 10z = 62 & 4x + 4(7) = 20 & 6(-2) - 3y + 2(7) = -10 & \\ -2x + 3y + 8z = 72 & 6x - 3y + 2z = -10 & 4x + 4z = 20 & 4x = -8 & -3y = -12 & \\ 4x + 10z = 62 & 7x + 7z = 35 & 6z = 42 & x = -2 & y = 4 & \\ & 4x + 4z = 20 & z = 7 & & & \end{array}$$

REF: spr1510aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

**Algebra II 6 Point Regents Exam Questions  
Answer Section**

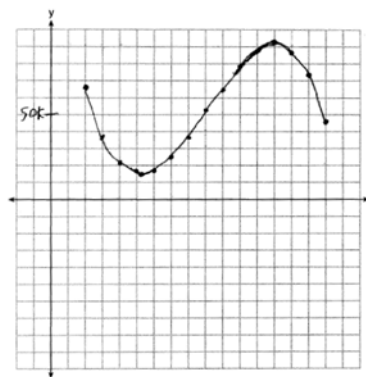
570 ANS:



At 1.95 years, the value of the car equals the loan balance. Zach can cancel the policy after 6 years.

REF: 081737aia NAT: A.REI.D.11 TOP: Other Systems

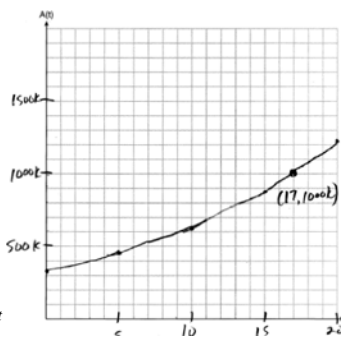
571 ANS:



$P(x) = R(x) - C(x) = -330x^3 + 9000x^2 - 67000x + 167000$   
 Least profitable at year 5 because there is a minimum in  $P(x)$ . Most profitable at year 13 because there is a maximum in  $P(x)$ .

REF: 081837aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

572 ANS:



$$A(t) = 318000(1.07)^t$$

$$318000(1.07)^t = 1000000$$

The graph of  $A(t)$  nearly intersects

$$1.07^t = \frac{1000}{318}$$

$$t \log 1.07 = \log \frac{1000}{318}$$

$$t = \frac{\log \frac{1000}{318}}{\log 1.07}$$

$$t \approx 17$$

the point (17, 1000000).

REF: 011937aia NAT: A.CED.A.1 TOP: Exponential Growth

573 ANS:

$$100 = 140 \left( \frac{1}{2} \right)^{\frac{5}{h}} \quad \log \frac{100}{140} = \log \left( \frac{1}{2} \right)^{\frac{5}{h}} \quad 40 = 140 \left( \frac{1}{2} \right)^{\frac{t}{10.3002}}$$

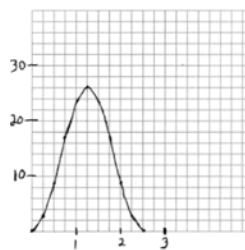
$$\log \frac{5}{7} = \frac{5}{h} \log \frac{1}{2} \quad \log \frac{2}{7} = \log \left( \frac{1}{2} \right)^{\frac{t}{10.3002}}$$

$$h = \frac{5 \log \frac{1}{2}}{\log \frac{5}{7}} \approx 10.3002 \quad \log \frac{2}{7} = \frac{t \log \left( \frac{1}{2} \right)}{10.3002}$$

$$t = \frac{10.3002 \log \frac{2}{7}}{\log \frac{1}{2}} \approx 18.6$$

REF: 061737aia NAT: F.LE.A.4 TOP: Exponential Decay

574 ANS:



period =  $\frac{2\pi}{0.8\pi} = 2.5$ . The wheel rotates once every 2.5 seconds.  
of  $f(t) = 26$ .

No, because the maximum

REF: 061937aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

575 ANS:

$B = 1.69\sqrt{30 + 4.45} - 3.49 \approx 6$ , which is a steady breeze.

$$15 = 1.69\sqrt{s + 4.45} - 3.49$$

$$18.49 = 1.69\sqrt{s + 4.45}$$

$$\frac{18.49}{1.69} = \sqrt{s + 4.45}$$

$$\left(\frac{18.49}{1.69}\right)^2 = s + 4.45$$

$$s = \left(\frac{18.49}{1.69}\right)^2 - 4.45$$

$$s \approx 115$$

$$9.5 = 1.69\sqrt{s + 4.45} - 3.49$$

$$10.49 = 1.69\sqrt{s + 4.45} - 3.49 \quad 55-64$$

$$12.99 = 1.69\sqrt{s + 4.45}$$

$$13.98 = 1.69\sqrt{s + 4.45}$$

$$\frac{12.99}{1.69} = \sqrt{s + 4.45}$$

$$\frac{13.98}{1.69} = \sqrt{s + 4.45}$$

$$\left(\frac{12.99}{1.69}\right)^2 = s + 4.45$$

$$\left(\frac{13.98}{1.69}\right)^2 = s + 4.45$$

$$s = \left(\frac{12.99}{1.69}\right)^2 - 4.45$$

$$s = \left(\frac{13.98}{1.69}\right)^2 - 4.45$$

$$s \approx 55$$

$$s \approx 64$$

REF: 081937aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: context



576 ANS:

$A(t) = 100(0.5)^{\frac{t}{63}}$ , where  $t$  is time in years, and  $A(t)$  is the amount of titanium-44 left after  $t$  years.

$\frac{A(10) - A(0)}{10 - 0} = \frac{89.58132 - 100}{10} = -1.041868$  The estimated mass at  $t = 40$  is  $100 - 40(-1.041868) \approx 58.3$ . The

actual mass is  $A(40) = 100(0.5)^{\frac{40}{63}} \approx 64.3976$ . The estimated mass is less than the actual mass.

REF: fall1517aii NAT: F.LE.A.2 TOP: Modeling Exponential Functions

577 ANS:

1.5%;  $P(t) = 92.2(1.015)^t$ ;  $\frac{300}{92.2} = (1.015)^t$

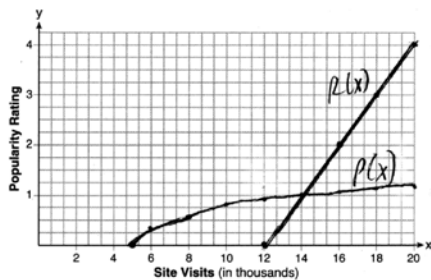
$$\log \frac{300}{92.2} = t \log(1.015)$$

$$\frac{\log \frac{300}{92.2}}{\log(1.015)} = t$$

$$t \approx 79$$

REF: 062237aii NAT: F.LE.A.2 TOP: Sequences KEY: recursive

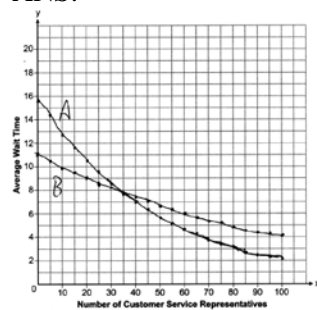
578 ANS:



$P(16) = \log(16 - 4) \approx 1.1$ , 14000

REF: 061837aii NAT: A.REI.D.11 TOP: Other Systems

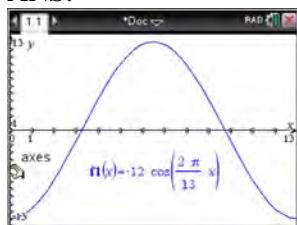
579 ANS:



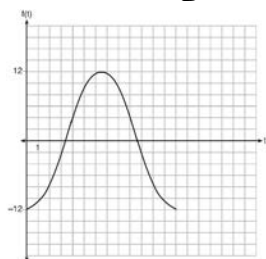
35;  $B(100) - A(100) \approx 2$ , which represents the difference of the average wait time when there are 100 CSRs between the plans.

REF: 082237aii NAT: A.REI.D.11 TOP: Other Systems

580 ANS:



The amplitude, 12, can be interpreted from the situation, since the water level has a minimum of  $-12$  and a maximum of  $12$ . The value of  $A$  is  $-12$  since at 8:30 it is low tide. The period of the function is 13 hours, and is expressed in the function through the parameter  $B$ . By experimentation with technology or using the relation  $P = \frac{2\pi}{B}$  (where  $P$  is the period), it is determined that  $B = \frac{2\pi}{13}$ .



$$f(t) = -12 \cos\left(\frac{2\pi}{13} t\right)$$

In order to answer the question about when to fish, the student must interpret the function and determine which choice, 7:30 pm or 10:30 pm, is on an increasing interval. Since the function is increasing from  $t = 13$  to  $t = 19.5$  (which corresponds to 9:30 pm to 4:00 am), 10:30 is the appropriate choice.

REF: spr1514aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

581 ANS:

$$\text{antibiotic } n(0) = \frac{0+1}{0+5} + \frac{18}{0^2 + 8(0) + 15} = \frac{3}{15} + \frac{18}{15} = \frac{21}{15}$$

$$\frac{t+1}{t+5} + \frac{18}{t^2 + 8t + 15} = \frac{9}{t+3}$$

$$a(0) = \frac{9}{0+3} = 3$$

$$\frac{(t+1)(t+3)}{(t+5)(t+3)} + \frac{18}{(t+3)(t+5)} = \frac{9(t+5)}{(t+3)(t+5)}$$

$$t^2 + 4t + 3 + 18 = 9t + 45$$

$$t^2 - 5t - 24 = 0$$

$$(t-8)(t+3) = 0$$

$$t = 8$$

REF: 012037aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

582 ANS:

$$A = 5000(1.045)^n \quad 5000\left(1 + \frac{.046}{4}\right)^{4(6)} - 5000(1.045)^6 \approx 6578.87 - 6511.30 \approx 67.57 \quad 10000 = 5000\left(1 + \frac{.046}{4}\right)^{4n}$$

$$B = 5000\left(1 + \frac{.046}{4}\right)^{4n}$$

$$2 = 1.0115^{4n}$$

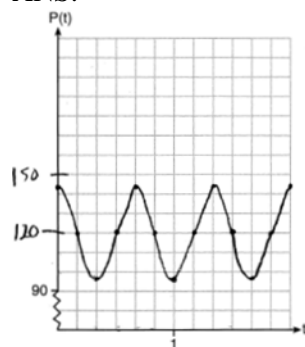
$$\log 2 = 4n \cdot \log 1.0115$$

$$n = \frac{\log 2}{4 \log 1.0115}$$

$$n \approx 15.2$$

REF: 081637aii NAT: A.CED.A.1 TOP: Exponential Growth

583 ANS:



The period of  $P$  is  $\frac{2}{3}$ , which means the patient's blood pressure reaches a high every  $\frac{2}{3}$

second and a low every  $\frac{2}{3}$  second. The patient's blood pressure is high because 144 over 96 is greater than 120 over 80.

REF: 011837aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

584 ANS:

$$0 = \sqrt{t} - 2t + 6 \quad 2\left(\frac{9}{4}\right) - 6 < 0, \text{ so } \frac{9}{4} \text{ is extraneous.}$$

$$2t - 6 = \sqrt{t}$$

$$4t^2 - 24t + 36 = t$$

$$4t^2 - 25t + 36 = 0$$

$$(4t - 9)(t - 4) = 0$$

$$t = \frac{9}{4}, 4$$

$$(\sqrt{1} - 2(1) + 6) - (\sqrt{3} - 2(3) + 6) = 5 - \sqrt{3} \approx 3.268 \quad 327 \text{ mph}$$

REF: 011737aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: context

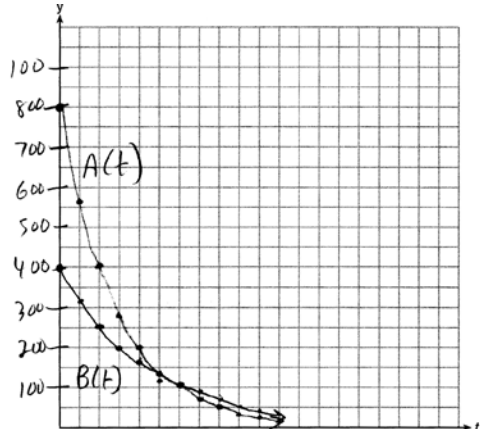
585 ANS:

$$T = (400 - 75)e^{-0.0735t} + 75, \quad 325e^{-0.0735(5)} + 75 \approx 300, \quad 270 = (450 - 75)e^{-8r} + 75, \quad 325e^{-0.0735t} + 75 = 375e^{-0.0817t} + 75$$

$$r \approx 0.0817 \qquad t \approx 17$$

REF: 012337aia NAT: A.CED.A.1 TOP: Exponential Decay

586 ANS:



$$A(t) = 800e^{-0.347t}$$

$$800e^{-0.347t} = 400e^{-0.231t} \quad 0.15 = e^{-0.347t}$$

$$B(t) = 400e^{-0.231t}$$

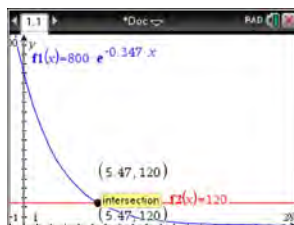
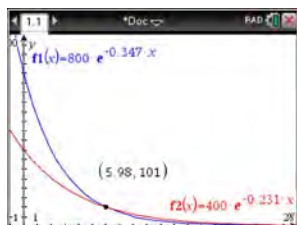
$$\ln 2e^{-0.347t} = \ln e^{-0.231t} \quad \ln 0.15 = \ln e^{-0.347t}$$

$$\ln 2 + \ln e^{-0.347t} = \ln e^{-0.231t} \quad \ln 0.15 = -0.347t \cdot \ln e$$

$$\ln 2 - 0.347t = -0.231t \quad 5.5 \approx t$$

$$\ln 2 = 0.116t$$

$$6 \approx t$$



REF: 061637aia NAT: A.REI.D.11 TOP: Other Systems