JMAP
REGENTS BY DATE

The NY Geometry Regents Exams
Fall, 2008-January, 2014

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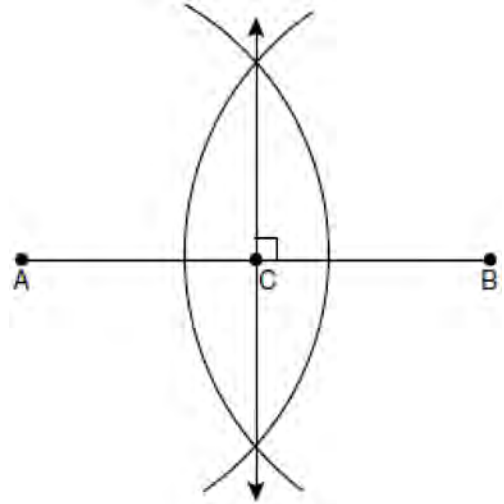
fall08ge

1 Isosceles trapezoid $ABCD$ has diagonals $\overline{AC}$ and $\overline{BD}$. If $AC = 5x + 13$ and $BD = 11x - 5$, what is the value of x?
1) 28
2) $10\frac{3}{4}$
3) 3
4) $\frac{1}{2}$

2 What is the negation of the statement "The Sun is shining"?
1) It is cloudy.
2) It is daytime.
3) It is not raining.
4) The Sun is not shining.

3 Triangle ABC has vertices $A(1,3)$, $B(0,1)$, and $C(4,0)$. Under a translation, A', the image point of A, is located at $(4,4)$. Under this same translation, point C' is located at
1) $(7,1)$
2) $(5,3)$
3) $(3,2)$
4) $(1,-1)$

4 The diagram below shows the construction of the perpendicular bisector of $\overline{AB}$.

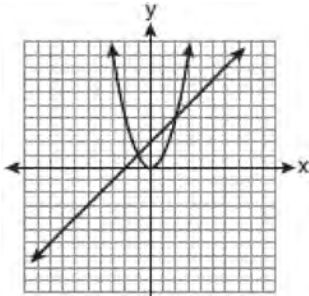

Which statement is *not* true?
1) $AC = CB$
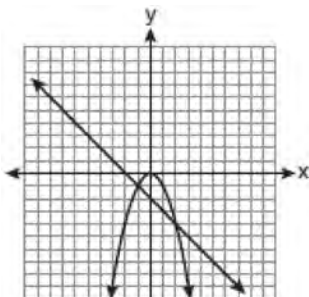2) $CB = \frac{1}{2}AB$
3) $AC = 2AB$
4) $AC + CB = AB$

5   Which graph could be used to find the solution to the following system of equations?
$$y = -x + 2$$
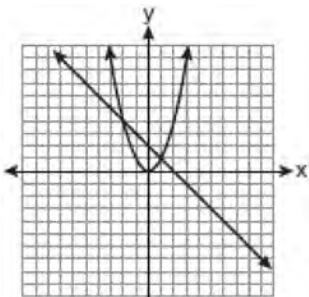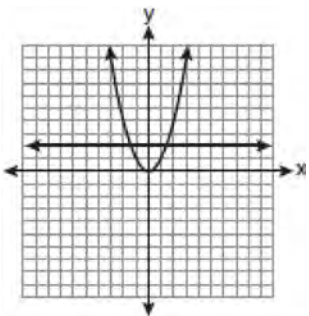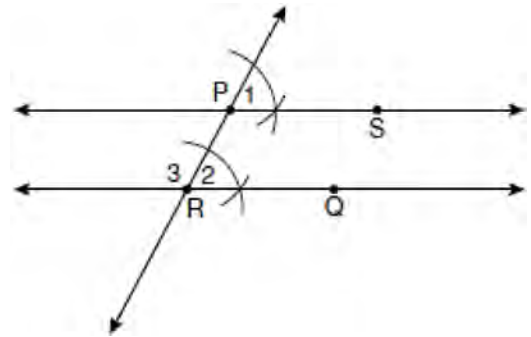$$y = x^2$$

1)

2)

3)

4)

6   Line k is drawn so that it is perpendicular to two distinct planes, P and R. What must be true about planes P and R?
1)   Planes P and R are skew.
2)   Planes P and R are parallel.
3)   Planes P and R are perpendicular.
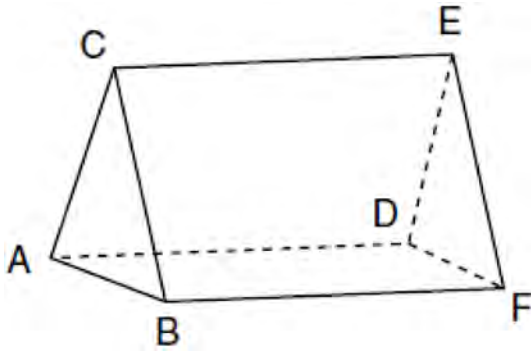4)   Plane P intersects plane R but is not perpendicular to plane R.

7   The diagram below illustrates the construction of $\overleftrightarrow{PS}$ parallel to $\overleftrightarrow{RQ}$ through point P.

Which statement justifies this construction?
1) $m\angle 1 = m\angle 2$
2) $m\angle 1 = m\angle 3$
3) $\overline{PR} \cong \overline{RQ}$
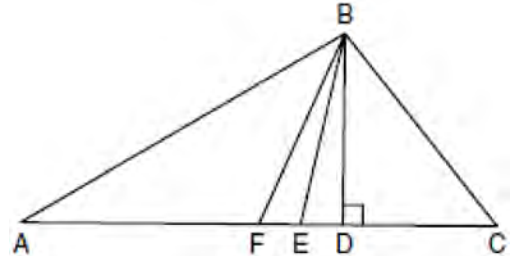4) $\overline{PS} \cong \overline{RQ}$

2

8 The figure in the diagram below is a triangular prism.
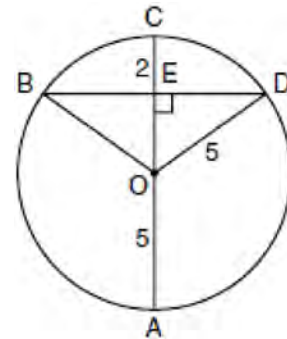

Which statement must be true?
1) $\overline{DE} \cong \overline{AB}$
2) $\overline{AD} \cong \overline{BC}$
3) $\overline{AD} \parallel \overline{CE}$
4) $\overline{DE} \parallel \overline{BC}$

9 The vertices of $\triangle ABC$ are $A(-1,-2)$, $B(-1,2)$ and $C(6,0)$. Which conclusion can be made about the angles of $\triangle ABC$?
1) $m\angle A = m\angle B$
2) $m\angle A = m\angle C$
3) $m\angle ACB = 90$
4) $m\angle ABC = 60$

10 Given $\triangle ABC$ with base $\overline{AFEDC}$, median $\overline{BF}$, altitude $\overline{BD}$, and $\overline{BE}$ bisects $\angle ABC$, which conclusion is valid?

1) $\angle FAB \cong \angle ABF$
2) $\angle ABF \cong \angle CBD$
3) $\overline{CE} \cong \overline{EA}$
4) $\overline{CF} \cong \overline{FA}$

11 In the diagram below, circle O has a radius of 5, and $CE = 2$. Diameter $\overline{AC}$ is perpendicular to chord $\overline{BD}$ at E.

What is the length of $\overline{BD}$?
1) 12
2) 10
3) 8
4) 4

3

12 What is the equation of a line that passes through the point $(-3, -11)$ and is parallel to the line whose equation is $2x - y = 4$?
1) $y = 2x + 5$
2) $y = 2x - 5$
3) $y = \dfrac{1}{2}x + \dfrac{25}{2}$
4) $y = -\dfrac{1}{2}x - \dfrac{25}{2}$

13 Line segment AB has endpoints $A(2, -3)$ and $B(-4, 6)$. What are the coordinates of the midpoint of $\overline{AB}$?
1) $(-2, 3)$
2) $\left(-1, 1\dfrac{1}{2}\right)$
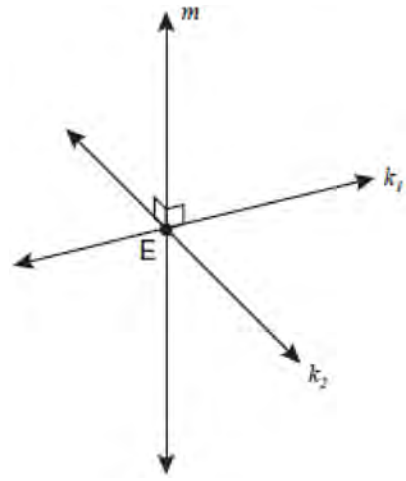3) $(-1, 3)$
4) $\left(3, 4\dfrac{1}{2}\right)$

14 What are the center and radius of a circle whose equation is $(x - A)^2 + (y - B)^2 = C$?
1) center $= (A, B)$; radius $= C$
2) center $= (-A, -B)$; radius $= C$
3) center $= (A, B)$; radius $= \sqrt{C}$
4) center $= (-A, -B)$; radius $= \sqrt{C}$

15 A rectangular prism has a volume of $3x^2 + 18x + 24$. Its base has a length of $x + 2$ and a width of 3. Which expression represents the height of the prism?
1) $x + 4$
2) $x + 2$
3) 3
4) $x^2 + 6x + 8$

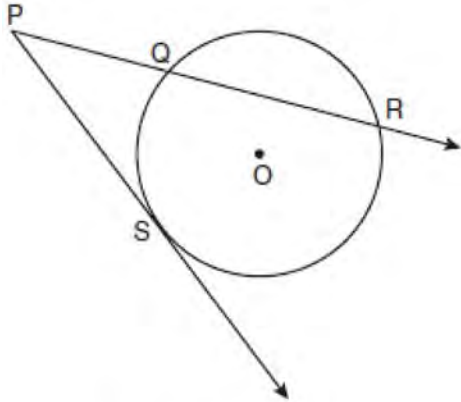16 Lines k_1 and k_2 intersect at point E. Line m is perpendicular to lines k_1 and k_2 at point E.

Which statement is always true?
1) Lines k_1 and k_2 are perpendicular.
2) Line m is parallel to the plane determined by lines k_1 and k_2.
3) Line m is perpendicular to the plane determined by lines k_1 and k_2.
4) Line m is coplanar with lines k_1 and k_2.

17 In the diagram below, $\overline{PS}$ is a tangent to circle O at point S, $\overline{PQR}$ is a secant, $PS = x$, $PQ = 3$, and $PR = x + 18$.
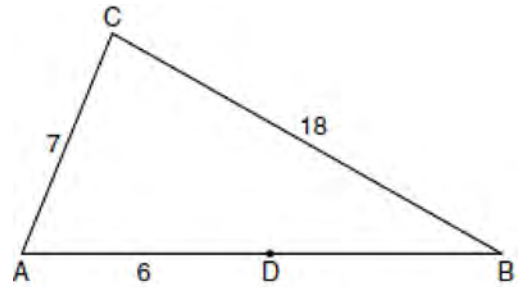

(Not drawn to scale)

What is the length of $\overline{PS}$?
1) 6
2) 9
3) 3
4) 27

18 A polygon is transformed according to the rule: $(x, y) \rightarrow (x + 2, y)$. Every point of the polygon moves two units in which direction?
1) up
2) down
3) left
4) right

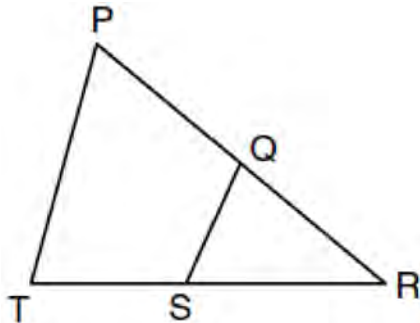19 In the diagram below of $\triangle ABC$, D is a point on $\overline{AB}$, $AC = 7$, $AD = 6$, and $BC = 18$.

(Not drawn to scale)

The length of $\overline{DB}$ could be
1) 5
2) 12
3) 19
4) 25

20 The diameter of a circle has endpoints at $(-2, 3)$ and $(6, 3)$. What is an equation of the circle?
1) $(x - 2)^2 + (y - 3)^2 = 16$
2) $(x - 2)^2 + (y - 3)^2 = 4$
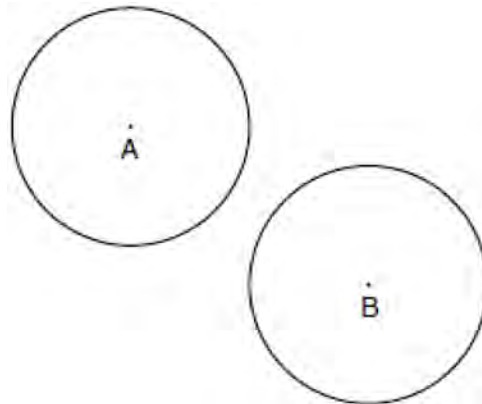3) $(x + 2)^2 + (y + 3)^2 = 16$
4) $(x + 2)^2 + (y + 3)^2 = 4$

5

21 In the diagram below of $\triangle PRT$, Q is a point on $\overline{PR}$, S is a point on $\overline{TR}$, $\overline{QS}$ is drawn, and $\angle RPT \cong \angle RSQ$.

Which reason justifies the conclusion that $\triangle PRT \sim \triangle SRQ$?
1) AA
2) ASA
3) SAS
4) SSS

22 The lines $3y + 1 = 6x + 4$ and $2y + 1 = x - 9$ are
1) parallel
2) perpendicular
3) the same line
4) neither parallel nor perpendicular

23 The endpoints of $\overline{AB}$ are $A(3, 2)$ and $B(7, 1)$. If $\overline{A''B''}$ is the result of the transformation of $\overline{AB}$ under $D_2 \circ T_{-4, 3}$ what are the coordinates of A'' and B''?
1) $A''(-2, 10)$ and $B''(6, 8)$
2) $A''(-1, 5)$ and $B''(3, 4)$
3) $A''(2, 7)$ and $B''(10, 5)$
4) $A''(14, -2)$ and $B''(22, -4)$

24 In the diagram below, circle A and circle B are shown.

What is the total number of lines of tangency that are common to circle A and circle B?
1) 1
2) 2
3) 3
4) 4

25 In which triangle do the three altitudes intersect outside the triangle?
1) a right triangle
2) an acute triangle
3) an obtuse triangle
4) an equilateral triangle

26 Two triangles are similar, and the ratio of each pair of corresponding sides is $2:1$. Which statement regarding the two triangles is *not* true?
1) Their areas have a ratio of $4:1$.
2) Their altitudes have a ratio of $2:1$.
3) Their perimeters have a ratio of $2:1$.
4) Their corresponding angles have a ratio of $2:1$.

27 What is the measure of an interior angle of a regular octagon?
1) 45°
2) 60°
3) 120°
4) 135°

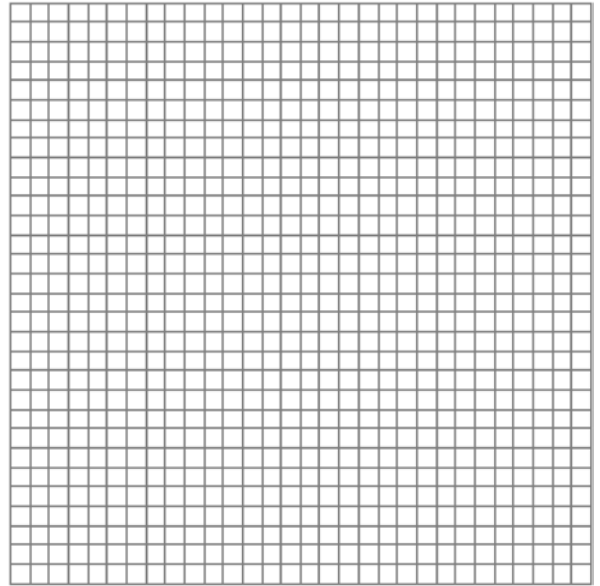28 What is the slope of a line perpendicular to the line whose equation is $5x + 3y = 8$?

1) $\frac{5}{3}$

2) $\frac{3}{5}$

3) $-\frac{3}{5}$

4) $-\frac{5}{3}$

29 In the diagram below of right triangle ACB, altitude $\overline{CD}$ intersects $\overline{AB}$ at D. If $AD = 3$ and $DB = 4$, find the length of $\overline{CD}$ in simplest radical form.

30 The vertices of $\triangle ABC$ are $A(3,2)$, $B(6,1)$, and $C(4,6)$. Identify and graph a transformation of $\triangle ABC$ such that its image, $\triangle A'B'C'$, results in $\overline{AB} \parallel \overline{A'B'}$.
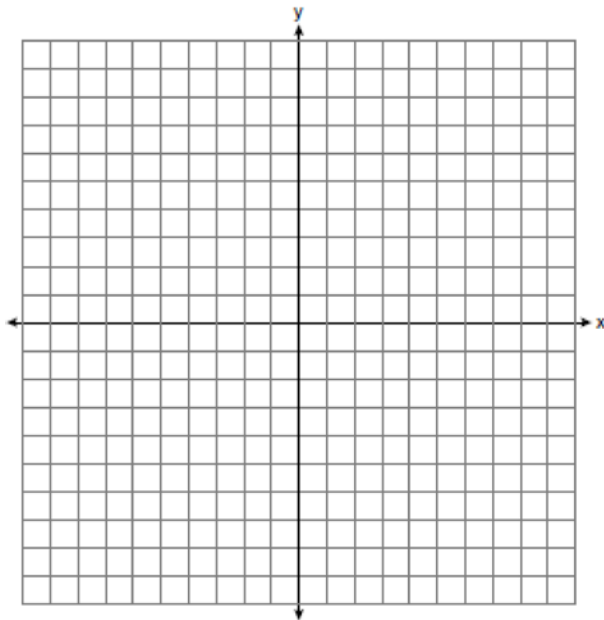

31 The endpoints of $\overline{PQ}$ are $P(-3, 1)$ and $Q(4, 25)$. Find the length of $\overline{PQ}$.
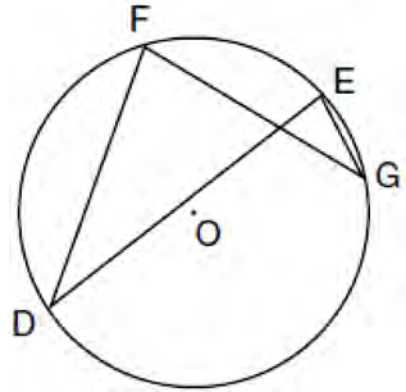
32 Using a compass and straightedge, construct the bisector of the angle shown below. [*Leave all construction marks*.]
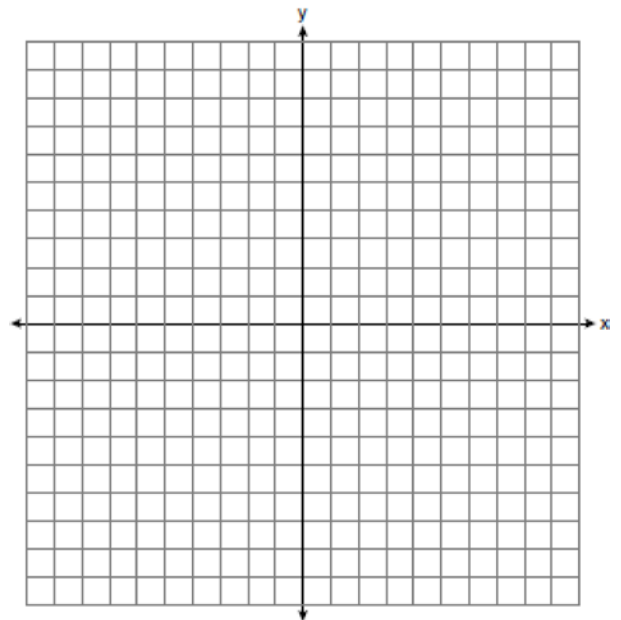
33 The volume of a cylinder is 12,566.4 cm³. The height of the cylinder is 8 cm. Find the radius of the cylinder to the *nearest tenth of a centimeter*.

34 Write a statement that is logically equivalent to the statement "If two sides of a triangle are congruent, the angles opposite those sides are congruent." Identify the new statement as the converse, inverse, or contrapositive of the original statement.

35 On the set of axes below, graph and label $\triangle DEF$ with vertices at $D(-4,-4)$, $E(-2,2)$, and $F(8,-2)$. If G is the midpoint of $\overline{EF}$ and H is the midpoint of $\overline{DF}$, state the coordinates of G and H and label each point on your graph. Explain why $\overline{GH} \parallel \overline{DE}$.

36 In the diagram below of circle O, chords $\overline{DF}$, $\overline{DE}$, $\overline{FG}$, and $\overline{EG}$ are drawn such that $m\overparen{DF}:m\overparen{FE}:m\overparen{EG}:m\overparen{GD} = 5:2:1:7$. Identify one pair of inscribed angles that are congruent to each other and give their measure.

37 A city is planning to build a new park. The park must be equidistant from school A at $(3,3)$ and school B at $(3,-5)$. The park also must be exactly 5 miles from the center of town, which is located at the origin on the coordinate graph. Each unit on the graph represents 1 mile. On the set of axes below, sketch the compound loci and label with an **X** all possible locations for the new park.

38 In the diagram below, quadrilateral *ABCD* is inscribed in circle *O*, $\overline{AB} \parallel \overline{DC}$, and diagonals $\overline{AC}$ and $\overline{BD}$ are drawn. Prove that $\triangle ACD \cong \triangle BDC$.

0609ge

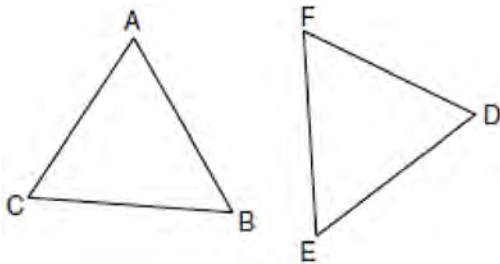1 Juliann plans on drawing $\triangle ABC$, where the measure of $\angle A$ can range from 50° to 60° and the measure of $\angle B$ can range from 90° to 100°. Given these conditions, what is the correct range of measures possible for $\angle C$?
   1) 20° to 40°
   2) 30° to 50°
   3) 80° to 90°
   4) 120° to 130°

2 In the diagram of $\triangle ABC$ and $\triangle DEF$ below, $\overline{AB} \cong \overline{DE}$, $\angle A \cong \angle D$, and $\angle B \cong \angle E$.

   Which method can be used to prove $\triangle ABC \cong \triangle DEF$?
   1) SSS
   2) SAS
   3) ASA
   4) HL

3 In the diagram below, under which transformation will $\triangle A'B'C'$ be the image of $\triangle ABC$?

   1) rotation
   2) dilation
   3) translation
   4) glide reflection

4 The lateral faces of a regular pyramid are composed of
   1) squares
   2) rectangles
   3) congruent right triangles
   4) congruent isosceles triangles

5 Point A is located at $(4,-7)$. The point is reflected in the x-axis. Its image is located at
   1) $(-4,7)$
   2) $(-4,-7)$
   3) $(4,7)$
   4) $(7,-4)$

1

6 In the diagram of circle O below, chords $\overline{AB}$ and $\overline{CD}$ are parallel, and $\overline{BD}$ is a diameter of the circle.

If $m\overarc{AD} = 60$, what is $m\angle CDB$?
1) 20
2) 30
3) 60
4) 120

7 What is an equation of the line that passes through the point $(-2,5)$ and is perpendicular to the line whose equation is $y = \frac{1}{2}x + 5$?

1) $y = 2x + 1$
2) $y = -2x + 1$
3) $y = 2x + 9$
4) $y = -2x - 9$

8 After a composition of transformations, the coordinates $A(4,2)$, $B(4,6)$, and $C(2,6)$ become $A''(-2,-1)$, $B''(-2,-3)$, and $C''(-1,-3)$, as shown on the set of axes below.
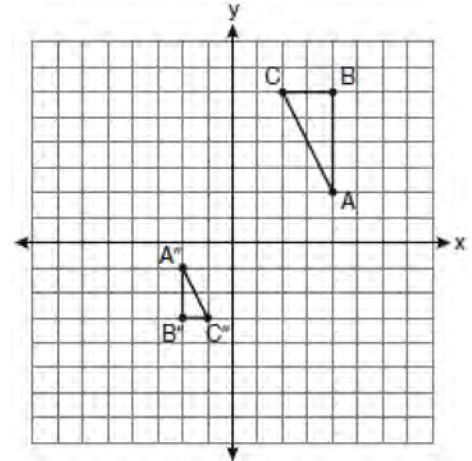

Which composition of transformations was used?
1) $R_{180°} \circ D_2$
2) $R_{90°} \circ D_2$
3) $D_{\frac{1}{2}} \circ R_{180°}$
4) $D_{\frac{1}{2}} \circ R_{90°}$

9 In an equilateral triangle, what is the difference between the sum of the exterior angles and the sum of the interior angles?
1) 180°
2) 120°
3) 90°
4) 60°

10 What is an equation of a circle with its center at $(-3,5)$ and a radius of 4?
1) $(x-3)^2 + (y+5)^2 = 16$
2) $(x+3)^2 + (y-5)^2 = 16$
3) $(x-3)^2 + (y+5)^2 = 4$
4) $(x+3)^2 + (y-5)^2 = 4$

11 In $\triangle ABC$, $m\angle A = 95$, $m\angle B = 50$, and $m\angle C = 35$. Which expression correctly relates the lengths of the sides of this triangle?
1) $AB < BC < CA$
2) $AB < AC < BC$
3) $AC < BC < AB$
4) $BC < AC < AB$

12 In a coordinate plane, how many points are both 5 units from the origin and 2 units from the *x*-axis?
1) 1
2) 2
3) 3
4) 4

13 What is the contrapositive of the statement, "If I am tall, then I will bump my head"?
1) If I bump my head, then I am tall.
2) If I do not bump my head, then I am tall.
3) If I am tall, then I will not bump my head.
4) If I do not bump my head, then I am not tall.

14 In the diagram of $\triangle ABC$ below, Jose found centroid *P* by constructing the three medians. He measured $\overline{CF}$ and found it to be 6 inches.

If $PF = x$, which equation can be used to find *x*?
1) $x + x = 6$
2) $2x + x = 6$
3) $3x + 2x = 6$
4) $x + \dfrac{2}{3}x = 6$

15 In the diagram below, the length of the legs $\overline{AC}$ and $\overline{BC}$ of right triangle *ABC* are 6 cm and 8 cm, respectively. Altitude $\overline{CD}$ is drawn to the hypotenuse of $\triangle ABC$.

What is the length of $\overline{AD}$ to the *nearest tenth of a centimeter*?
1) 3.6
2) 6.0
3) 6.4
4) 4.0

16 In the diagram below, tangent $\overline{AB}$ and secant $\overline{ACD}$ are drawn to circle *O* from an external point *A*, $AB = 8$, and $AC = 4$.

What is the length of $\overline{CD}$?
1) 16
2) 13
3) 12
4) 10

3

17 In the diagram of $\triangle ABC$ and $\triangle EDC$ below, $\overline{AE}$ and $\overline{BD}$ intersect at C, and $\angle CAB \cong \angle CED$.

Which method can be used to show that $\triangle ABC$ must be similar to $\triangle EDC$?
1) SAS
2) AA
3) SSS
4) HL

18 Point P is on line m. What is the total number of planes that are perpendicular to line m and pass through point P?
1) 1
2) 2
3) 0
4) infinite

19 Square $LMNO$ is shown in the diagram below.

What are the coordinates of the midpoint of diagonal $\overline{LN}$?

1) $\left(4\frac{1}{2}, -2\frac{1}{2}\right)$

2) $\left(-3\frac{1}{2}, 3\frac{1}{2}\right)$

3) $\left(-2\frac{1}{2}, 3\frac{1}{2}\right)$

4) $\left(-2\frac{1}{2}, 4\frac{1}{2}\right)$

20 Which graph represents a circle with the equation $(x-5)^2 + (y+1)^2 = 9$?

1)

2)

3)

4)

21 In the diagram below, a right circular cone has a diameter of 8 inches and a height of 12 inches.

8 inches

12 inches

What is the volume of the cone to the *nearest cubic inch*?
1) 201
2) 481
3) 603
4) 804

22 A circle is represented by the equation $x^2 + (y+3)^2 = 13$. What are the coordinates of the center of the circle and the length of the radius?
1) $(0,3)$ and 13
2) $(0,3)$ and $\sqrt{13}$
3) $(0,-3)$ and 13
4) $(0,-3)$ and $\sqrt{13}$

23 Given the system of equations: $y = x^2 - 4x$
$$x = 4$$
The number of points of intersection is
1) 1
2) 2
3) 3
4) 0

5

24 Side $\overline{PQ}$ of $\triangle PQR$ is extended through Q to point T. Which statement is *not* always true?
1) $m\angle RQT > m\angle R$
2) $m\angle RQT > m\angle P$
3) $m\angle RQT = m\angle P + m\angle R$
4) $m\angle RQT > m\angle PQR$

25 Which illustration shows the correct construction of an angle bisector?

1)

2)

3)

4)

26 Which equation represents a line perpendicular to the line whose equation is $2x + 3y = 12$?
1) $6y = -4x + 12$
2) $2y = 3x + 6$
3) $2y = -3x + 6$
4) $3y = -2x + 12$

27 In $\triangle ABC$, point D is on $\overline{AB}$, and point E is on $\overline{BC}$ such that $\overline{DE} \parallel \overline{AC}$. If $DB = 2$, $DA = 7$, and $DE = 3$, what is the length of $\overline{AC}$?
1) 8
2) 9
3) 10.5
4) 13.5

28 In three-dimensional space, two planes are parallel and a third plane intersects both of the parallel planes. The intersection of the planes is a
1) plane
2) point
3) pair of parallel lines
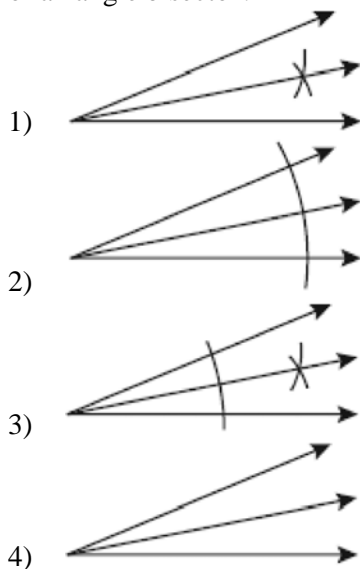4) pair of intersecting lines

29 In the diagram of $\triangle ABC$ below, $AB = 10$, $BC = 14$, and $AC = 16$. Find the perimeter of the triangle formed by connecting the midpoints of the sides of $\triangle ABC$.

30 Using a compass and straightedge, construct a line that passes through point P and is perpendicular to line m. [Leave all construction marks.]

$\cdot P$

$\longleftrightarrow m$

31 Find an equation of the line passing through the point $(5,4)$ and parallel to the line whose equation is $2x + y = 3$.

6

32 The length of $\overline{AB}$ is 3 inches. On the diagram below, sketch the points that are equidistant from A and B and sketch the points that are 2 inches from A. Label with an **X** all points that satisfy both conditions.

A •————————————————• B

33 Given: Two is an even integer or three is an even integer.
Determine the truth value of this disjunction. Justify your answer.

34 In the diagram below, $\triangle ABC \sim \triangle EFG$, $m\angle C = 4x + 30$, and $m\angle G = 5x + 10$. Determine the value of x.

35 In the diagram below, circles X and Y have two tangents drawn to them from external point T. The points of tangency are C, A, S, and E. The ratio of TA to AC is $1:3$. If $TS = 24$, find the length of $\overline{SE}$.

(Not drawn to scale)

36 Triangle *ABC* has coordinates $A(-6,2)$, $B(-3,6)$, and $C(5,0)$. Find the perimeter of the triangle. Express your answer in simplest radical form. [The use of the grid below is optional.]

37 The coordinates of the vertices of parallelogram *ABCD* are $A(-2,2)$, $B(3,5)$, $C(4,2)$, and $D(-1,-1)$. State the coordinates of the vertices of parallelogram $A''B''C''D''$ that result from the transformation $r_{y-axis} \circ T_{2,-3}$. [The use of the set of axes below is optional.]

38 Given: $\triangle ABC$ and $\triangle EDC$, *C* is the midpoint of $\overline{BD}$ and $\overline{AE}$
Prove: $\overline{AB} \parallel \overline{DE}$

0809ge

1 Based on the diagram below, which statement is true?

1) $a \parallel b$
2) $a \parallel c$
3) $b \parallel c$
4) $d \parallel e$

2 The diagram below shows the construction of the bisector of $\angle ABC$.

Which statement is *not* true?

1) $m\angle EBF = \frac{1}{2} m\angle ABC$

2) $m\angle DBF = \frac{1}{2} m\angle ABC$

3) $m\angle EBF = m\angle ABC$
4) $m\angle DBF = m\angle EBF$

3 In the diagram of $\triangle ABC$ below, $\overline{AB} \cong \overline{AC}$. The measure of $\angle B$ is $40°$.

What is the measure of $\angle A$?
1) $40°$
2) $50°$
3) $70°$
4) $100°$

4 In the diagram of circle O below, chord $\overline{CD}$ is parallel to diameter $\overline{AOB}$ and $m\overset{\frown}{AC} = 30$.

What is $m\overset{\frown}{CD}$?
1) 150
2) 120
3) 100
4) 60

1

5 In the diagram of trapezoid $ABCD$ below, diagonals $\overline{AC}$ and $\overline{BD}$ intersect at E and $\triangle ABC \cong \triangle DCB$.

Which statement is true based on the given information?
1) $\overline{AC} \cong \overline{BC}$
2) $\overline{CD} \cong \overline{AD}$
3) $\angle CDE \cong \angle BAD$
4) $\angle CDB \cong \angle BAC$

6 Which transformation produces a figure similar but not congruent to the original figure?
1) $T_{1,3}$
2) $D_{\frac{1}{2}}$
3) $R_{90°}$
4) $r_{y=x}$

7 In the diagram below of parallelogram $ABCD$ with diagonals $\overline{AC}$ and $\overline{BD}$, $m\angle 1 = 45$ and $m\angle DCB = 120$.

What is the measure of $\angle 2$?
1) 15°
2) 30°
3) 45°
4) 60°

8 On the set of axes below, Geoff drew rectangle $ABCD$. He will transform the rectangle by using the translation $(x, y) \rightarrow (x+2, y+1)$ and then will reflect the translated rectangle over the x-axis.

What will be the area of the rectangle after these transformations?
1) exactly 28 square units
2) less than 28 square units
3) greater than 28 square units
4) It cannot be determined from the information given.

2

9 What is the equation of a line that is parallel to the line whose equation is $y = x + 2$?
1) $x + y = 5$
2) $2x + y = -2$
3) $y - x = -1$
4) $y - 2x = 3$

10 The endpoints of $\overline{CD}$ are $C(-2, -4)$ and $D(6, 2)$. What are the coordinates of the midpoint of $\overline{CD}$?
1) $(2, 3)$
2) $(2, -1)$
3) $(4, -2)$
4) $(4, 3)$

11 What are the center and the radius of the circle whose equation is $(x - 3)^2 + (y + 3)^2 = 36$
1) center = $(3, -3)$; radius = 6
2) center = $(-3, 3)$; radius = 6
3) center = $(3, -3)$; radius = 36
4) center = $(-3, 3)$; radius = 36

12 Given the equations: $y = x^2 - 6x + 10$
$$y + x = 4$$
What is the solution to the given system of equations?
1) $(2, 3)$
2) $(3, 2)$
3) $(2, 2)$ and $(1, 3)$
4) $(2, 2)$ and $(3, 1)$

13 The diagonal $\overline{AC}$ is drawn in parallelogram $ABCD$. Which method can *not* be used to prove that $\triangle ABC \cong \triangle CDA$?
1) SSS
2) SAS
3) SSA
4) ASA

14 In the diagram below, line k is perpendicular to plane $\mathcal{P}$ at point T.

Which statement is true?
1) Any point in plane $\mathcal{P}$ also will be on line k.
2) Only one line in plane $\mathcal{P}$ will intersect line k.
3) All planes that intersect plane $\mathcal{P}$ will pass through T.
4) Any plane containing line k is perpendicular to plane $\mathcal{P}$.

3

15 In the diagram below, which transformation was used to map $\triangle ABC$ to $\triangle A'B'C'$?

1) dilation
2) rotation
3) reflection
4) glide reflection

16 Which set of numbers represents the lengths of the sides of a triangle?
1) $\{5, 18, 13\}$
2) $\{6, 17, 22\}$
3) $\{16, 24, 7\}$
4) $\{26, 8, 15\}$

17 What is the slope of a line perpendicular to the line whose equation is $y = -\frac{2}{3}x - 5$?

1) $-\frac{3}{2}$

2) $-\frac{2}{3}$

3) $\frac{2}{3}$

4) $\frac{3}{2}$

18 A quadrilateral whose diagonals bisect each other and are perpendicular is a
1) rhombus
2) rectangle
3) trapezoid
4) parallelogram

19 If the endpoints of $\overline{AB}$ are $A(-4, 5)$ and $B(2, -5)$, what is the length of $\overline{AB}$?
1) $2\sqrt{34}$
2) 2
3) $\sqrt{61}$
4) 8

20 In the diagram below of $\triangle ACT$, D is the midpoint of $\overline{AC}$, O is the midpoint of $\overline{AT}$, and G is the midpoint of $\overline{CT}$.

If $AC = 10$, $AT = 18$, and $CT = 22$, what is the perimeter of parallelogram $CDOG$?
1) 21
2) 25
3) 32
4) 40

21 Which equation represents circle K shown in the graph below?

1) $(x+5)^2 + (y-1)^2 = 3$
2) $(x+5)^2 + (y-1)^2 = 9$
3) $(x-5)^2 + (y+1)^2 = 3$
4) $(x-5)^2 + (y+1)^2 = 9$

22 In the diagram below of right triangle ACB, altitude $\overline{CD}$ is drawn to hypotenuse $\overline{AB}$.

If $AB = 36$ and $AC = 12$, what is the length of $\overline{AD}$?
1) 32
2) 6
3) 3
4) 4

23 In the diagram of circle O below, chord $\overline{AB}$ intersects chord $\overline{CD}$ at E, $DE = 2x + 8$, $EC = 3$, $AE = 4x - 3$, and $EB = 4$.

What is the value of x?
1) 1
2) 3.6
3) 5
4) 10.25

24 What is the negation of the statement "Squares are parallelograms"?
1) Parallelograms are squares.
2) Parallelograms are not squares.
3) It is not the case that squares are parallelograms.
4) It is not the case that parallelograms are squares.

5

25 The diagram below shows the construction of the center of the circle circumscribed about $\triangle ABC$.

This construction represents how to find the intersection of
1) the angle bisectors of $\triangle ABC$
2) the medians to the sides of $\triangle ABC$
3) the altitudes to the sides of $\triangle ABC$
4) the perpendicular bisectors of the sides of $\triangle ABC$

26 A right circular cylinder has a volume of 1,000 cubic inches and a height of 8 inches. What is the radius of the cylinder to the *nearest tenth of an inch*?
1) 6.3
2) 11.2
3) 19.8
4) 39.8

27 If two different lines are perpendicular to the same plane, they are
1) collinear
2) coplanar
3) congruent
4) consecutive

28 How many common tangent lines can be drawn to the two externally tangent circles shown below?

1) 1
2) 2
3) 3
4) 4

29 In the diagram below of isosceles trapezoid $DEFG$, $\overline{DE} \parallel \overline{GF}$, $DE = 4x - 2$, $EF = 3x + 2$, $FG = 5x - 3$, and $GD = 2x + 5$. Find the value of x.

6

30 A regular pyramid with a square base is shown in the diagram below.

A side, s, of the base of the pyramid is 12 meters, and the height, h, is 42 meters. What is the volume of the pyramid in cubic meters?

31 Write an equation of the line that passes through the point $(6, -5)$ and is parallel to the line whose equation is $2x - 3y = 11$.

32 Using a compass and straightedge, construct the angle bisector of $\angle ABC$ shown below. [Leave all construction marks.]

33 The degree measures of the angles of $\triangle ABC$ are represented by x, $3x$, and $5x - 54$. Find the value of x.

34 In the diagram below of $\triangle ABC$ with side $\overline{AC}$ extended through D, $m\angle A = 37$ and $m\angle BCD = 117$. Which side of $\triangle ABC$ is the longest side? Justify your answer.

(Not drawn to scale)

35 Write an equation of the perpendicular bisector of the line segment whose endpoints are $(-1, 1)$ and $(7, -5)$. [The use of the grid below is optional]

7

36 On the set of axes below, sketch the points that are 5 units from the origin and sketch the points that are 2 units from the line $y = 3$. Label with an ✘ all points that satisfy both conditions.

37 Triangle *DEG* has the coordinates $D(1,1)$, $E(5,1)$, and $G(5,4)$. Triangle *DEG* is rotated 90° about the origin to form $\triangle D'E'G'$. On the grid below, graph and label $\triangle DEG$ and $\triangle D'E'G'$. State the coordinates of the vertices D', E', and G'. Justify that this transformation preserves distance.

38 Given: Quadrilateral *ABCD*, diagonal $\overline{AFEC}$, $\overline{AE} \cong \overline{FC}$, $\overline{BF} \perp \overline{AC}$, $\overline{DE} \perp \overline{AC}$, $\angle 1 \cong \angle 2$
Prove: *ABCD* is a parallelogram.

8

0110ge

1 In the diagram below of trapezoid $RSUT$, $\overline{RS} \parallel \overline{TU}$, X is the midpoint of $\overline{RT}$, and V is the midpoint of $\overline{SU}$.

If $RS = 30$ and $XV = 44$, what is the length of $\overline{TU}$?
1) 37
2) 58
3) 74
4) 118

2 In $\triangle ABC$, $m\angle A = x$, $m\angle B = 2x + 2$, and $m\angle C = 3x + 4$. What is the value of x?
1) 29
2) 31
3) 59
4) 61

3 Which expression best describes the transformation shown in the diagram below?

1) same orientation; reflection
2) opposite orientation; reflection
3) same orientation; translation
4) opposite orientation; translation

4   Based on the construction below, which statement must be true?

1) $m\angle ABD = \frac{1}{2} m\angle CBD$

2) $m\angle ABD = m\angle CBD$

3) $m\angle ABD = m\angle ABC$

4) $m\angle CBD = \frac{1}{2} m\angle ABD$

5   In the diagram below, $\triangle ABC$ is inscribed in circle P. The distances from the center of circle P to each side of the triangle are shown.

Which statement about the sides of the triangle is true?

1) $AB > AC > BC$

2) $AB < AC$ and $AC > BC$

3) $AC > AB > BC$

4) $AC = AB$ and $AB > BC$

6   Which transformation is *not* always an isometry?

1)   rotation

2)   dilation

3)   reflection

4)   translation

7   In $\triangle ABC$, $\overline{AB} \cong \overline{BC}$. An altitude is drawn from B to $\overline{AC}$ and intersects $\overline{AC}$ at D. Which conclusion is *not* always true?

1) $\angle ABD \cong \angle CBD$

2) $\angle BDA \cong \angle BDC$

3) $\overline{AD} \cong \overline{BD}$

4) $\overline{AD} \cong \overline{DC}$

8   In the diagram below, tangent $\overline{PA}$ and secant $\overline{PBC}$ are drawn to circle O from external point P.

If $PB = 4$ and $BC = 5$, what is the length of $\overline{PA}$?

1)   20

2)   9

3)   8

4)   6

2

9 Which geometric principle is used to justify the construction below?

1) A line perpendicular to one of two parallel lines is perpendicular to the other.
2) Two lines are perpendicular if they intersect to form congruent adjacent angles.
3) When two lines are intersected by a transversal and alternate interior angles are congruent, the lines are parallel.
4) When two lines are intersected by a transversal and the corresponding angles are congruent, the lines are parallel.

10 Which equation represents the circle whose center is $(-2, 3)$ and whose radius is 5?

1) $(x - 2)^2 + (y + 3)^2 = 5$
2) $(x + 2)^2 + (y - 3)^2 = 5$
3) $(x + 2)^2 + (y - 3)^2 = 25$
4) $(x - 2)^2 + (y + 3)^2 = 25$

11 Towns A and B are 16 miles apart. How many points are 10 miles from town A and 12 miles from town B?

1) 1
2) 2
3) 3
4) 0

12 Lines j and k intersect at point P. Line m is drawn so that it is perpendicular to lines j and k at point P. Which statement is correct?

1) Lines j and k are in perpendicular planes.
2) Line m is in the same plane as lines j and k.
3) Line m is parallel to the plane containing lines j and k.
4) Line m is perpendicular to the plane containing lines j and k.

13 In the diagram below of parallelogram $STUV$, $SV = x + 3$, $VU = 2x - 1$, and $TU = 4x - 3$.

What is the length of $\overline{SV}$?

1) 5
2) 2
3) 7
4) 4

14 Which equation represents a line parallel to the line whose equation is $2y - 5x = 10$?

1) $5y - 2x = 25$
2) $5y + 2x = 10$
3) $4y - 10x = 12$
4) $2y + 10x = 8$

3

15 In the diagram below of circle O, chords $\overline{AD}$ and $\overline{BC}$ intersect at E, $m\overset{\frown}{AC} = 87$, and $m\overset{\frown}{BD} = 35$.

What is the degree measure of $\angle CEA$?
1) 87
2) 61
3) 43.5
4) 26

16 In the diagram below of $\triangle ADB$, $m\angle BDA = 90$, $AD = 5\sqrt{2}$, and $AB = 2\sqrt{15}$.

What is the length of $\overline{BD}$?
1) $\sqrt{10}$
2) $\sqrt{20}$
3) $\sqrt{50}$
4) $\sqrt{110}$

17 What is the distance between the points $(-3, 2)$ and $(1, 0)$?
1) $2\sqrt{2}$
2) $2\sqrt{3}$
3) $5\sqrt{2}$
4) $2\sqrt{5}$

18 What is an equation of the line that contains the point $(3, -1)$ and is perpendicular to the line whose equation is $y = -3x + 2$?
1) $y = -3x + 8$
2) $y = -3x$
3) $y = \frac{1}{3}x$
4) $y = \frac{1}{3}x - 2$

19 In the diagram below, $\overline{SQ}$ and $\overline{PR}$ intersect at T, $\overline{PQ}$ is drawn, and $\overline{PS} \parallel \overline{QR}$.

What technique can be used to prove that $\triangle PST \sim \triangle RQT$?
1) SAS
2) SSS
3) ASA
4) AA

20 The equation of a circle is $(x-2)^2 + (y+4)^2 = 4$. Which diagram is the graph of the circle?

1)

2)

3)

4)

21 In the diagram below, $\triangle ABC$ is shown with $\overline{AC}$ extended through point D.

If m$\angle BCD = 6x + 2$, m$\angle BAC = 3x + 15$, and m$\angle ABC = 2x - 1$, what is the value of x?
1) 12
2) $14\frac{10}{11}$
3) 16
4) $18\frac{1}{9}$

22 Given $\triangle ABC \sim \triangle DEF$ such that $\frac{AB}{DE} = \frac{3}{2}$. Which statement is *not* true?
1) $\frac{BC}{EF} = \frac{3}{2}$
2) $\frac{m\angle A}{m\angle D} = \frac{3}{2}$
3) $\frac{\text{area of } \triangle ABC}{\text{area of } \triangle DEF} = \frac{9}{4}$
4) $\frac{\text{perimeter of } \triangle ABC}{\text{perimeter of } \triangle DEF} = \frac{3}{2}$

5

23 The pentagon in the diagram below is formed by five rays.

What is the degree measure of angle x?
1) 72
2) 96
3) 108
4) 112

24 Through a given point, P, on a plane, how many lines can be drawn that are perpendicular to that plane?
1) 1
2) 2
3) more than 2
4) none

25 What is the slope of a line that is perpendicular to the line whose equation is $3x + 4y = 12$?

1) $\frac{3}{4}$

2) $-\frac{3}{4}$

3) $\frac{4}{3}$

4) $-\frac{4}{3}$

26 What is the image of point $A(4, 2)$ after the composition of transformations defined by $R_{90°} \circ r_{y = x}$?
1) $(-4, 2)$
2) $(4, -2)$
3) $(-4, -2)$
4) $(2, -4)$

27 Which expression represents the volume, in cubic centimeters, of the cylinder represented in the diagram below?

1) 162π
2) 324π
3) 972π
4) $3,888\pi$

28 What is the inverse of the statement "If two triangles are not similar, their corresponding angles are not congruent"?
1) If two triangles are similar, their corresponding angles are not congruent.
2) If corresponding angles of two triangles are not congruent, the triangles are not similar.
3) If two triangles are similar, their corresponding angles are congruent.
4) If corresponding angles of two triangles are congruent, the triangles are similar.

6

29 In $\triangle RST$, $m\angle RST = 46$ and $\overline{RS} \cong \overline{ST}$. Find $m\angle STR$.

30 Tim has a rectangular prism with a length of 10 centimeters, a width of 2 centimeters, and an unknown height. He needs to build another rectangular prism with a length of 5 centimeters and the same height as the original prism. The volume of the two prisms will be the same. Find the width, in centimeters, of the new prism.

31 In the diagram below of circle C, $\overline{QR}$ is a diameter, and $Q(1, 8)$ and $C(3.5, 2)$ are points on a coordinate plane. Find and state the coordinates of point R.

32 Using a compass and straightedge, and $\overline{AB}$ below, construct an equilateral triangle with all sides congruent to $\overline{AB}$. [Leave all construction marks.]

33 In the diagram below of $\triangle ACD$, E is a point on $\overline{AD}$ and B is a point on $\overline{AC}$, such that $\overline{EB} \parallel \overline{DC}$. If $AE = 3$, $ED = 6$, and $DC = 15$, find the length of EB.

34 In the diagram below of $\triangle TEM$, medians $\overline{TB}$, $\overline{EC}$, and $\overline{MA}$ intersect at D, and $TB = 9$. Find the length of $\overline{TD}$.

35 In $\triangle KLM$, $m\angle K = 36$ and $KM = 5$. The transformation D_2 is performed on $\triangle KLM$ to form $\triangle K'L'M'$. Find $m\angle K'$. Justify your answer. Find the length of $\overline{K'M'}$. Justify your answer.

36 Given: *JKLM* is a parallelogram.
$\overline{JM} \cong \overline{LN}$
$\angle LMN \cong \angle LNM$
Prove: *JKLM* is a rhombus.

37 On the grid below, graph the points that are
equidistant from both the *x* and *y* axes and the
points that are 5 units from the origin. Label with
an **X** all points that satisfy both conditions.

38 On the set of axes below, solve the following
system of equations graphically for all values of *x*
and *y*.

$$y = (x - 2)^2 + 4$$

$$4x + 2y = 14$$

0610ge

1   In the diagram below of circle O,
chord $\overline{AB} \parallel$ chord $\overline{CD}$, and chord $\overline{CD} \parallel$ chord $\overline{EF}$.

Which statement must be true?
1) $\overset{\frown}{CE} \cong \overset{\frown}{DF}$
2) $\overset{\frown}{AC} \cong \overset{\frown}{DF}$
3) $\overset{\frown}{AC} \cong \overset{\frown}{CE}$
4) $\overset{\frown}{EF} \cong \overset{\frown}{CD}$

2   What is the negation of the statement "I am not going to eat ice cream"?
1)   I like ice cream.
2)   I am going to eat ice cream.
3)   If I eat ice cream, then I like ice cream.
4)   If I don't like ice cream, then I don't eat ice cream.

3   The diagram below shows a right pentagonal prism.

Which statement is always true?
1) $\overline{BC} \parallel \overline{ED}$
2) $\overline{FG} \parallel \overline{CD}$
3) $\overline{FJ} \parallel \overline{IH}$
4) $\overline{GB} \parallel \overline{HC}$

4   In isosceles triangle ABC, $AB = BC$. Which statement will always be true?
1) $m\angle B = m\angle A$
2) $m\angle A > m\angle B$
3) $m\angle A = m\angle C$
4) $m\angle C < m\angle B$

1

5 The rectangle *ABCD* shown in the diagram below will be reflected across the *x*-axis.

What will *not* be preserved?

1) slope of $\overline{AB}$
2) parallelism of $\overline{AB}$ and $\overline{CD}$
3) length of $\overline{AB}$
4) measure of $\angle A$

6 A right circular cylinder has an altitude of 11 feet and a radius of 5 feet. What is the lateral area, in square feet, of the cylinder, to the *nearest tenth*?

1) 172.7
2) 172.8
3) 345.4
4) 345.6

7 A transversal intersects two lines. Which condition would always make the two lines parallel?

1) Vertical angles are congruent.
2) Alternate interior angles are congruent.
3) Corresponding angles are supplementary.
4) Same-side interior angles are complementary.

8 If the diagonals of a quadrilateral do *not* bisect each other, then the quadrilateral could be a

1) rectangle
2) rhombus
3) square
4) trapezoid

9 What is the converse of the statement "If Bob does his homework, then George gets candy"?

1) If George gets candy, then Bob does his homework.
2) Bob does his homework if and only if George gets candy.
3) If George does not get candy, then Bob does not do his homework.
4) If Bob does not do his homework, then George does not get candy.

10 In $\triangle PQR$, $PQ = 8$, $QR = 12$, and $RP = 13$. Which statement about the angles of $\triangle PQR$ must be true?

1) $m\angle Q > m\angle P > m\angle R$
2) $m\angle Q > m\angle R > m\angle P$
3) $m\angle R > m\angle P > m\angle Q$
4) $m\angle P > m\angle R > m\angle Q$

11 Given: $y = \frac{1}{4}x - 3$

$y = x^2 + 8x + 12$

In which quadrant will the graphs of the given equations intersect?

1) I
2) II
3) III
4) IV

2

12 Which diagram shows the construction of an equilateral triangle?

1)

2)

3)

4)

13 Line segment AB is tangent to circle O at A. Which type of triangle is always formed when points A, B, and O are connected?
1) right
2) obtuse
3) scalene
4) isosceles

14 What is an equation for the circle shown in the graph below?

1) $x^2 + y^2 = 2$
2) $x^2 + y^2 = 4$
3) $x^2 + y^2 = 8$
4) $x^2 + y^2 = 16$

15 Which transformation can map the letter **S** onto itself?
1) glide reflection
2) translation
3) line reflection
4) rotation

3

16 In isosceles trapezoid $ABCD$, $\overline{AB} \cong \overline{CD}$. If $BC = 20$, $AD = 36$, and $AB = 17$, what is the length of the altitude of the trapezoid?
1) 10
2) 12
3) 15
4) 16

17 In plane $\mathcal{P}$, lines m and n intersect at point A. If line k is perpendicular to line m and line n at point A, then line k is
1) contained in plane $\mathcal{P}$
2) parallel to plane $\mathcal{P}$
3) perpendicular to plane $\mathcal{P}$
4) skew to plane $\mathcal{P}$

18 The diagram below shows $\overline{AB}$ and $\overline{DE}$.

Which transformation will move $\overline{AB}$ onto $\overline{DE}$ such that point D is the image of point A and point E is the image of point B?
1) $T_{3,-3}$
2) $D_{\frac{1}{2}}$
3) $R_{90°}$
4) $r_{y=x}$

19 In the diagram below of circle O, chords $\overline{AE}$ and $\overline{DC}$ intersect at point B, such that $m\overset{\frown}{AC} = 36$ and $m\overset{\frown}{DE} = 20$.

What is $m\angle ABC$?
1) 56
2) 36
3) 28
4) 8

20 The diagram below shows the construction of a line through point P perpendicular to line m.

Which statement is demonstrated by this construction?
1) If a line is parallel to a line that is perpendicular to a third line, then the line is also perpendicular to the third line.
2) The set of points equidistant from the endpoints of a line segment is the perpendicular bisector of the segment.
3) Two lines are perpendicular if they are equidistant from a given point.
4) Two lines are perpendicular if they intersect to form a vertical line.

21 What is the length, to the *nearest tenth,* of the line segment joining the points $(-4, 2)$ and $(146, 52)$?
1) 141.4
2) 150.5
3) 151.9
4) 158.1

22 What is the slope of a line perpendicular to the line whose equation is $y = 3x + 4$?
1) $\dfrac{1}{3}$
2) $-\dfrac{1}{3}$
3) 3
4) -3

23 In the diagram below of circle O, secant $\overline{AB}$ intersects circle O at D, secant $\overline{AOC}$ intersects circle O at E, $AE = 4$, $AB = 12$, and $DB = 6$.

(Not drawn to scale)

What is the length of $\overline{OC}$?
1) 4.5
2) 7
3) 9
4) 14

24 The diagram below shows a pennant in the shape of an isosceles triangle. The equal sides each measure 13, the altitude is $x + 7$, and the base is $2x$.

What is the length of the base?
1) 5
2) 10
3) 12
4) 24

25 In the diagram below of $\triangle ABC$, $\overline{CD}$ is the bisector of $\angle BCA$, $\overline{AE}$ is the bisector of $\angle CAB$, and $\overline{BG}$ is drawn.

Which statement must be true?
1) $DG = EG$
2) $AG = BG$
3) $\angle AEB \cong \angle AEC$
4) $\angle DBG \cong \angle EBG$

26 In the diagram below of circle O, chords $\overline{AD}$ and $\overline{BC}$ intersect at E.

Which relationship must be true?
1) $\triangle CAE \cong \triangle DBE$
2) $\triangle AEC \sim \triangle BED$
3) $\angle ACB \cong \angle CBD$
4) $\overparen{CA} \cong \overparen{DB}$

27 Two lines are represented by the equations
$-\dfrac{1}{2}y = 6x + 10$ and $y = mx$. For which value of m
will the lines be parallel?
1) -12
2) -3
3) 3
4) 12

28 The coordinates of the vertices of parallelogram
$ABCD$ are $A(-3,2)$, $B(-2,-1)$, $C(4,1)$, and $D(3,4)$.
The slopes of which line segments could be
calculated to show that $ABCD$ is a rectangle?
1) $\overline{AB}$ and $\overline{DC}$
2) $\overline{AB}$ and $\overline{BC}$
3) $\overline{AD}$ and $\overline{BC}$
4) $\overline{AC}$ and $\overline{BD}$

29 Tim is going to paint a wooden sphere that has a
diameter of 12 inches. Find the surface area of the
sphere, to the *nearest square inch*.

30 In the diagram below of $\triangle ABC$, $\overline{DE}$ is a
midsegment of $\triangle ABC$, $DE = 7$, $AB = 10$, and
$BC = 13$. Find the perimeter of $\triangle ABC$.

31 In right $\triangle DEF$, $m\angle D = 90$ and $m\angle F$ is 12 degrees
less than twice $m\angle E$. Find $m\angle E$.

32 Triangle XYZ, shown in the diagram below, is
reflected over the line $x = 2$. State the coordinates
of $\triangle X'Y'Z'$, the image of $\triangle XYZ$.

33 Two lines, $\overleftrightarrow{AB}$ and $\overleftrightarrow{CRD}$, are parallel and 10 inches
apart. Sketch the locus of all points that are
equidistant from $\overleftrightarrow{AB}$ and $\overleftrightarrow{CRD}$ and 7 inches from
point R. Label with an **X** each point that satisfies
both conditions.

7

34 The base of a pyramid is a rectangle with a width of 6 cm and a length of 8 cm. Find, in centimeters, the height of the pyramid if the volume is 288 cm^3.

35 Given: Quadrilateral $ABCD$ with $\overline{AB} \cong \overline{CD}$, $\overline{AD} \cong \overline{BC}$, and diagonal $\overline{BD}$ is drawn
   Prove: $\angle BDC \cong \angle ABD$

36 Find an equation of the line passing through the point $(6, 5)$ and perpendicular to the line whose equation is $2y + 3x = 6$.

37 Write an equation of the circle whose diameter $\overline{AB}$ has endpoints $A(-4, 2)$ and $B(4, -4)$. [The use of the grid below is optional.]

38 In the diagram below, quadrilateral $STAR$ is a rhombus with diagonals $\overline{SA}$ and $\overline{TR}$ intersecting at E. $ST = 3x + 30$, $SR = 8x - 5$, $SE = 3z$, $TE = 5z + 5$, $AE = 4z - 8$, m$\angle RTA = 5y - 2$, and m$\angle TAS = 9y + 8$. Find SR, RT, and m$\angle TAS$.

8

0810ge

1 In the diagram below, $\triangle ABC \cong \triangle XYZ$.

Which two statements identify corresponding congruent parts for these triangles?
1) $\overline{AB} \cong \overline{XY}$ and $\angle C \cong \angle Y$
2) $\overline{AB} \cong \overline{YZ}$ and $\angle C \cong \angle X$
3) $\overline{BC} \cong \overline{XY}$ and $\angle A \cong \angle Y$
4) $\overline{BC} \cong \overline{YZ}$ and $\angle A \cong \angle X$

2 A support beam between the floor and ceiling of a house forms a 90° angle with the floor. The builder wants to make sure that the floor and ceiling are parallel. Which angle should the support beam form with the ceiling?
1) 45°
2) 60°
3) 90°
4) 180°

3 In the diagram below, the vertices of $\triangle DEF$ are the midpoints of the sides of equilateral triangle ABC, and the perimeter of $\triangle ABC$ is 36 cm.

What is the length, in centimeters, of $\overline{EF}$?
1) 6
2) 12
3) 18
4) 4

4 What is the solution of the following system of equations?
$$y = (x + 3)^2 - 4$$
$$y = 2x + 5$$
1) $(0, -4)$
2) $(-4, 0)$
3) $(-4, -3)$ and $(0, 5)$
4) $(-3, -4)$ and $(5, 0)$

5 One step in a construction uses the endpoints of $\overline{AB}$ to create arcs with the same radii. The arcs intersect above and below the segment. What is the relationship of $\overline{AB}$ and the line connecting the points of intersection of these arcs?
1) collinear
2) congruent
3) parallel
4) perpendicular

1

6   If $\triangle ABC \sim \triangle ZXY$, $m\angle A = 50$, and $m\angle C = 30$, what is $m\angle X$?
1) 30
2) 50
3) 80
4) 100

7   In the diagram below of $\triangle AGE$ and $\triangle OLD$, $\angle GAE \cong \angle LOD$, and $\overline{AE} \cong \overline{OD}$.

To prove that $\triangle AGE$ and $\triangle OLD$ are congruent by SAS, what other information is needed?
1) $\overline{GE} \cong \overline{LD}$
2) $\overline{AG} \cong \overline{OL}$
3) $\angle AGE \cong \angle OLD$
4) $\angle AEG \cong \angle ODL$

8   Point A is not contained in plane $\mathcal{B}$. How many lines can be drawn through point A that will be perpendicular to plane $\mathcal{B}$?
1) one
2) two
3) zero
4) infinite

9   The equation of a circle is $x^2 + (y - 7)^2 = 16$. What are the center and radius of the circle?
1) center = $(0, 7)$; radius = 4
2) center = $(0, 7)$; radius = 16
3) center = $(0, -7)$; radius = 4
4) center = $(0, -7)$; radius = 16

10 What is an equation of the line that passes through the point $(7, 3)$ and is parallel to the line $4x + 2y = 10$?
1) $y = \frac{1}{2}x - \frac{1}{2}$
2) $y = -\frac{1}{2}x + \frac{13}{2}$
3) $y = 2x - 11$
4) $y = -2x + 17$

11 In $\triangle ABC$, $AB = 7$, $BC = 8$, and $AC = 9$. Which list has the angles of $\triangle ABC$ in order from smallest to largest?
1) $\angle A, \angle B, \angle C$
2) $\angle B, \angle A, \angle C$
3) $\angle C, \angle B, \angle A$
4) $\angle C, \angle A, \angle B$

12 Tangents $\overline{PA}$ and $\overline{PB}$ are drawn to circle O from an external point, P, and radii $\overline{OA}$ and $\overline{OB}$ are drawn. If $m\angle APB = 40$, what is the measure of $\angle AOB$?
1) 140º
2) 100º
3) 70º
4) 50º

13 What is the length of the line segment with endpoints $(-6, 4)$ and $(2, -5)$?
1) $\sqrt{13}$
2) $\sqrt{17}$
3) $\sqrt{72}$
4) $\sqrt{145}$

14 The lines represented by the equations $y + \frac{1}{2}x = 4$

and $3x + 6y = 12$ are
1) the same line
2) parallel
3) perpendicular
4) neither parallel nor perpendicular

15 A transformation of a polygon that always preserves both length and orientation is
1) dilation
2) translation
3) line reflection
4) glide reflection

16 In which polygon does the sum of the measures of the interior angles equal the sum of the measures of the exterior angles?
1) triangle
2) hexagon
3) octagon
4) quadrilateral

17 In the diagram below of circle O, chords $\overline{AB}$ and $\overline{CD}$ intersect at E.

If $CE = 10$, $ED = 6$, and $AE = 4$, what is the length of $\overline{EB}$?
1) 15
2) 12
3) 6.7
4) 2.4

18 In the diagram below of $\triangle ABC$, medians $\overline{AD}$, $\overline{BE}$, and $\overline{CF}$ intersect at G.

If $CF = 24$, what is the length of $\overline{FG}$?
1) 8
2) 10
3) 12
4) 16

3

19 If a line segment has endpoints $A(3x + 5, 3y)$ and $B(x - 1, -y)$, what are the coordinates of the midpoint of $\overline{AB}$?
1) $(x + 3, 2y)$
2) $(2x + 2, y)$
3) $(2x + 3, y)$
4) $(4x + 4, 2y)$

20 If the surface area of a sphere is represented by 144π, what is the volume in terms of π?
1) 36π
2) 48π
3) 216π
4) 288π

21 Which transformation of the line $x = 3$ results in an image that is perpendicular to the given line?
1) $r_{x\text{-axis}}$
2) $r_{y\text{-axis}}$
3) $r_{y = x}$
4) $r_{x = 1}$

22 In the diagram below of regular pentagon *ABCDE, $\overline{EB}$* is drawn.

What is the measure of $\angle AEB$?
1) 36°
2) 54°
3) 72°
4) 108°

23 $\triangle ABC$ is similar to $\triangle DEF$. The ratio of the length of $\overline{AB}$ to the length of $\overline{DE}$ is $3:1$. Which ratio is also equal to $3:1$?
1) $\dfrac{m\angle A}{m\angle D}$
2) $\dfrac{m\angle B}{m\angle F}$
3) $\dfrac{\text{area of } \triangle ABC}{\text{area of } \triangle DEF}$
4) $\dfrac{\text{perimeter of } \triangle ABC}{\text{perimeter of } \triangle DEF}$

24 What is the slope of a line perpendicular to the line whose equation is $2y = -6x + 8$?
1) -3
2) $\dfrac{1}{6}$
3) $\dfrac{1}{3}$
4) -6

25 In the diagram below of circle C, $m\overset{\frown}{QT} = 140$, and $m\angle P = 40$.

What is $m\overset{\frown}{RS}$?
1) 50
2) 60
3) 90
4) 110

4

26 Which statement is logically equivalent to "If it is warm, then I go swimming"
1) If I go swimming, then it is warm.
2) If it is warm, then I do not go swimming.
3) If I do not go swimming, then it is not warm.
4) If it is not warm, then I do not go swimming.

27 In the diagram below of $\triangle ACT$, $\overleftrightarrow{BE} \parallel \overline{AT}$.

If $CB = 3$, $CA = 10$, and $CE = 6$, what is the length of $\overline{ET}$?
1) 5
2) 14
3) 20
4) 26

28 Which geometric principle is used in the construction shown below?

1) The intersection of the angle bisectors of a triangle is the center of the inscribed circle.
2) The intersection of the angle bisectors of a triangle is the center of the circumscribed circle.
3) The intersection of the perpendicular bisectors of the sides of a triangle is the center of the inscribed circle.
4) The intersection of the perpendicular bisectors of the sides of a triangle is the center of the circumscribed circle.

29 The diagram below shows isosceles trapezoid $ABCD$ with $\overline{AB} \parallel \overline{DC}$ and $\overline{AD} \cong \overline{BC}$. If $m\angle BAD = 2x$ and $m\angle BCD = 3x + 5$, find $m\angle BAD$.

30 A right circular cone has a base with a radius of 15 cm, a vertical height of 20 cm, and a slant height of 25 cm. Find, in terms of π, the number of square centimeters in the lateral area of the cone.

5

31 In the diagram below of $\triangle HQP$, side $\overline{HP}$ is extended through P to T, m$\angle QPT = 6x + 20$, m$\angle HQP = x + 40$, and m$\angle PHQ = 4x - 5$. Find m$\angle QPT$.

(Not drawn to scale)

32 On the line segment below, use a compass and straightedge to construct equilateral triangle ABC. [Leave all construction marks.]

33 In the diagram below, car A is parked 7 miles from car B. Sketch the points that are 4 miles from car A and sketch the points that are 4 miles from car B. Label with an **X** all points that satisfy both conditions.

34 Write an equation for circle O shown on the graph below.

35 In the diagram below of quadrilateral $ABCD$ with diagonal $\overline{BD}$, m$\angle A = 93$, m$\angle ADB = 43$, m$\angle C = 3x + 5$, m$\angle BDC = x + 19$, and m$\angle DBC = 2x + 6$. Determine if $\overline{AB}$ is parallel to $\overline{DC}$. Explain your reasoning.

36 The coordinates of the vertices of $\triangle ABC$ $A(1, 3)$, $B(-2, 2)$ and $C(0, -2)$. On the grid below, graph and label $\triangle A''B''C''$, the result of the composite transformation $D_2 \circ T_{3,-2}$. State the coordinates of A'', B'', and C''.

37 In the diagram below, $\triangle RST$ is a $3 - 4 - 5$ right triangle. The altitude, h, to the hypotenuse has been drawn. Determine the length of h.

38 Given: Quadrilateral $ABCD$ has vertices $A(-5, 6)$, $B(6, 6)$, $C(8, -3)$, and $D(-3, -3)$.
Prove: Quadrilateral $ABCD$ is a parallelogram but is neither a rhombus nor a rectangle. [The use of the grid below is optional.]

7

0111ge

1   In the diagram below, $\overline{AB}$, $\overline{BC}$, and $\overline{AC}$ are tangents to circle O at points F, E, and D, respectively, $AF = 6$, $CD = 5$, and $BE = 4$.

What is the perimeter of $\triangle ABC$?
1)   15
2)   25
3)   30
4)   60

2   Quadrilateral $MNOP$ is a trapezoid with $\overline{MN} \parallel \overline{OP}$. If $M'N'O'P'$ is the image of $MNOP$ after a reflection over the x-axis, which two sides of quadrilateral $M'N'O'P'$ are parallel?
1) $\overline{M'N'}$ and $\overline{O'P'}$
2) $\overline{M'N'}$ and $\overline{N'O'}$
3) $\overline{P'M'}$ and $\overline{O'P'}$
4) $\overline{P'M'}$ and $\overline{N'O'}$

3   In the diagram below of $\triangle ABC$, D is the midpoint of $\overline{AB}$, and E is the midpoint of $\overline{BC}$.

If $AC = 4x + 10$, which expression represents DE?
1) $x + 2.5$
2) $2x + 5$
3) $2x + 10$
4) $8x + 20$

4   Which statement is true about every parallelogram?
1)   All four sides are congruent.
2)   The interior angles are all congruent.
3)   Two pairs of opposite sides are congruent.
4)   The diagonals are perpendicular to each other.

1

5 The diagram below shows a rectangular prism.

Which pair of edges are segments of lines that are coplanar?
1) $\overline{AB}$ and $\overline{DH}$
2) $\overline{AE}$ and $\overline{DC}$
3) $\overline{BC}$ and $\overline{EH}$
4) $\overline{CG}$ and $\overline{EF}$

6 A line segment has endpoints $A(7,-1)$ and $B(-3,3)$. What are the coordinates of the midpoint of $\overline{AB}$?
1) $(1,2)$
2) $\left(2,1\right)$
3) $(-5,2)$
4) $\left(5,-2\right)$

7 What is the image of the point $(-5,2)$ under the translation $T_{3,-4}$?
1) $(-9,5)$
2) $(-8,6)$
3) $(-2,-2)$
4) $(-15,-8)$

8 When writing a geometric proof, which angle relationship could be used alone to justify that two angles are congruent?
1) supplementary angles
2) linear pair of angles
3) adjacent angles
4) vertical angles

9 Plane $\mathcal{R}$ is perpendicular to line k and plane $\mathcal{D}$ is perpendicular to line k. Which statement is correct?
1) Plane $\mathcal{R}$ is perpendicular to plane $\mathcal{D}$.
2) Plane $\mathcal{R}$ is parallel to plane $\mathcal{D}$.
3) Plane $\mathcal{R}$ intersects plane $\mathcal{D}$.
4) Plane $\mathcal{R}$ bisects plane $\mathcal{D}$.

10 The vertices of the triangle in the diagram below are $A(7,9)$, $B(3,3)$, and $C(11,3)$.

What are the coordinates of the centroid of $\triangle ABC$?
1) $(5,6)$
2) $(7,3)$
3) $(7,5)$
4) $(9,6)$

11 Which set of numbers does *not* represent the sides of a right triangle?
1) $\{6,8,10\}$
2) $\{8,15,17\}$
3) $\{8,24,25\}$
4) $\{15,36,39\}$

2

12 In the diagram below of rhombus $ABCD$, $m\angle C = 100$.

What is $m\angle DBC$?
1) 40
2) 45
3) 50
4) 80

13 In the diagram below of circle O, radius $\overline{OC}$ is 5 cm. Chord $\overline{AB}$ is 8 cm and is perpendicular to $\overline{OC}$ at point P.

What is the length of $\overline{OP}$, in centimeters?
1) 8
2) 2
3) 3
4) 4

14 What is an equation of the line that passes through the point $(-2, 3)$ and is parallel to the line whose equation is $y = \frac{3}{2}x - 4$?
1) $y = \frac{-2}{3}x$
2) $y = \frac{-2}{3}x + \frac{5}{3}$
3) $y = \frac{3}{2}x$
4) $y = \frac{3}{2}x + 6$

15 In scalene triangle ABC, $m\angle B = 45$ and $m\angle C = 55$. What is the order of the sides in length, from longest to shortest?
1) $\overline{AB}, \overline{BC}, \overline{AC}$
2) $\overline{BC}, \overline{AC}, \overline{AB}$
3) $\overline{AC}, \overline{BC}, \overline{AB}$
4) $\overline{BC}, \overline{AB}, \overline{AC}$

16 What is an equation of a circle with center $(7, -3)$ and radius 4?
1) $(x - 7)^2 + (y + 3)^2 = 4$
2) $(x + 7)^2 + (y - 3)^2 = 4$
3) $(x - 7)^2 + (y + 3)^2 = 16$
4) $(x + 7)^2 + (y - 3)^2 = 16$

17 What is the volume, in cubic centimeters, of a cylinder that has a height of 15 cm and a diameter of 12 cm?
1) 180π
2) 540π
3) 675π
4) $2,160\pi$

3

18 Which compound statement is true?
 1) A triangle has three sides and a quadrilateral has five sides.
 2) A triangle has three sides if and only if a quadrilateral has five sides.
 3) If a triangle has three sides, then a quadrilateral has five sides.
 4) A triangle has three sides or a quadrilateral has five sides.

19 The two lines represented by the equations below are graphed on a coordinate plane.

$$x + 6y = 12$$

$$3(x - 2) = -y - 4$$

Which statement best describes the two lines?
 1) The lines are parallel.
 2) The lines are the same line.
 3) The lines are perpendicular.
 4) The lines intersect at an angle other than 90°.

20 Which diagram shows the construction of the perpendicular bisector of $\overline{AB}$?

1)

2)

3)

4)

21 In circle O, a diameter has endpoints $(-5, 4)$ and $(3, -6)$. What is the length of the diameter?
 1) $\sqrt{2}$
 2) $2\sqrt{2}$
 3) $\sqrt{10}$
 4) $2\sqrt{41}$

4

22 In the diagram of quadrilateral $ABCD$, $\overline{AB} \parallel \overline{CD}$, $\angle ABC \cong \angle CDA$, and diagonal $\overline{AC}$ is drawn.

Which method can be used to prove $\triangle ABC$ is congruent to $\triangle CDA$?
1) AAS
2) SSA
3) SAS
4) SSS

23 In the diagram below of right triangle ABC, $\overline{CD}$ is the altitude to hypotenuse $\overline{AB}$, $CB = 6$, and $AD = 5$.

What is the length of $\overline{BD}$?
1) 5
2) 9
3) 3
4) 4

24 In the diagram below, quadrilateral $JUMP$ is inscribed in a circle..

Opposite angles J and M must be
1) right
2) complementary
3) congruent
4) supplementary

5

25 Which graph represents a circle with the equation $(x-3)^2 + (y+1)^2 = 4$?

1)

2)

3)

4)

26 The point $(3, -2)$ is rotated $90°$ about the origin and then dilated by a scale factor of 4. What are the coordinates of the resulting image?
1) $(-12, 8)$
2) $(12, -8)$
3) $(8, 12)$
4) $(-8, -12)$

27 In the diagram below of $\triangle ABC$, side $\overline{BC}$ is extended to point D, $m\angle A = x$, $m\angle B = 2x + 15$, and $m\angle ACD = 5x + 5$.

What is $m\angle B$?
1) 5
2) 20
3) 25
4) 55

28 Point P lies on line m. Point P is also included in distinct planes Q, R, S, and T. At most, how many of these planes could be perpendicular to line m?
1) 1
2) 2
3) 3
4) 4

29 In the diagram below of $\triangle ACD$, B is a point on $\overline{AC}$ such that $\triangle ADB$ is an equilateral triangle, and $\triangle DBC$ is an isosceles triangle with $\overline{DB} \cong \overline{BC}$. Find $m\angle C$.

30 Triangle ABC has vertices $A(-2, 2)$, $B(-1, -3)$, and $C(4, 0)$. Find the coordinates of the vertices of $\triangle A'B'C'$, the image of $\triangle ABC$ after the transformation $r_{x\text{-axis}}$. [The use of the grid is optional.]

31 Find, in degrees, the measures of both an interior angle and an exterior angle of a regular pentagon.

32 In the diagram below of circle O, chord $\overline{AB}$ bisects chord $\overline{CD}$ at E. If $AE = 8$ and $BE = 9$, find the length of $\overline{CE}$ in simplest radical form.

33 On the diagram below, use a compass and straightedge to construct the bisector of $\angle ABC$. [Leave all construction marks.]

34 Find the slope of a line perpendicular to the line whose equation is $2y - 6x = 4$.

35 On the set of axes below, graph the locus of points that are four units from the point $(2, 1)$. On the same set of axes, graph the locus of points that are two units from the line $x = 4$. State the coordinates of all points that satisfy both conditions.

36 In the diagram below, $\overline{BFCE}$, $\overline{AB} \perp \overline{BE}$, $\overline{DE} \perp \overline{BE}$, and $\angle BFD \cong \angle ECA$. Prove that $\triangle ABC \sim \triangle DEF$.

37 In the diagram below of $\triangle ADE$, B is a point on $\overline{AE}$ and C is a point on $\overline{AD}$ such that $\overline{BC} \parallel \overline{ED}$, $AC = x - 3$, $BE = 20$, $AB = 16$, and $AD = 2x + 2$. Find the length of $\overline{AC}$.

38 Quadrilateral $MATH$ has coordinates $M(1, 1)$, $A(-2, 5)$, $T(3, 5)$, and $H(6, 1)$. Prove that quadrilateral $MATH$ is a rhombus and prove that it is *not* a square. [The use of the grid is optional.]

0611ge

1   Line segment *AB* is shown in the diagram below.

Which two sets of construction marks, labeled I, II, III, and IV, are part of the construction of the perpendicular bisector of line segment *AB*?
1)   I and II
2)   I and III
3)   II and III
4)   II and IV

2   If $\triangle JKL \cong \triangle MNO$, which statement is always true?
1) $\angle KLJ \cong \angle NMO$
2) $\angle KJL \cong \angle MON$
3) $\overline{JL} \cong \overline{MO}$
4) $\overline{JK} \cong \overline{ON}$

3   In the diagram below, $\triangle A'B'C'$ is a transformation of $\triangle ABC$, and $\triangle A''B''C''$ is a transformation of $\triangle A'B'C'$.

The composite transformation of $\triangle ABC$ to $\triangle A''B''C''$ is an example of a
1)   reflection followed by a rotation
2)   reflection followed by a translation
3)   translation followed by a rotation
4)   translation followed by a reflection

4 In the diagram below of △*ACE*, medians $\overline{AD}$, $\overline{EB}$, and $\overline{CF}$ intersect at *G*. The length of $\overline{FG}$ is 12 cm.

What is the length, in centimeters, of $\overline{GC}$?
1) 24
2) 12
3) 6
4) 4

5 In the diagram below of circle *O*, chord $\overline{AB}$ is parallel to chord $\overline{CD}$.

Which statement must be true?
1) $\overparen{AC} \cong \overparen{BD}$
2) $\overparen{AB} \cong \overparen{CD}$
3) $\overline{AB} \cong \overline{CD}$
4) $\overparen{ABD} \cong \overparen{CDB}$

6 In the diagram below, line *p* intersects line *m* and line *n*.

If m∠1 = 7*x* and m∠2 = 5*x* + 30, lines *m* and *n* are parallel when *x* equals
1) 12.5
2) 15
3) 87.5
4) 105

7 In the diagram of △*KLM* below, m∠*L* = 70, m∠*M* = 50, and $\overline{MK}$ is extended through *N*.

What is the measure of ∠*LKN*?
1) 60°
2) 120°
3) 180°
4) 300°

2

8 If two distinct planes, $\mathcal{A}$ and $\mathcal{B}$, are perpendicular to line c, then which statement is true?
1) Planes $\mathcal{A}$ and $\mathcal{B}$ are parallel to each other.
2) Planes $\mathcal{A}$ and $\mathcal{B}$ are perpendicular to each other.
3) The intersection of planes $\mathcal{A}$ and $\mathcal{B}$ is a line parallel to line c.
4) The intersection of planes $\mathcal{A}$ and $\mathcal{B}$ is a line perpendicular to line c.

9 What is the length of the line segment whose endpoints are $A(-1, 9)$ and $B(7, 4)$?
1) $\sqrt{61}$
2) $\sqrt{89}$
3) $\sqrt{205}$
4) $\sqrt{233}$

10 What is an equation of circle O shown in the graph below?

1) $(x+1)^2 + (y-3)^2 = 25$
2) $(x-1)^2 + (y+3)^2 = 25$
3) $(x-5)^2 + (y+6)^2 = 25$
4) $(x+5)^2 + (y-6)^2 = 25$

11 In the diagram below, parallelogram $ABCD$ has diagonals $\overline{AC}$ and $\overline{BD}$ that intersect at point E.

Which expression is *not* always true?
1) $\angle DAE \cong \angle BCE$
2) $\angle DEC \cong \angle BEA$
3) $\overline{AC} \cong \overline{DB}$
4) $\overline{DE} \cong \overline{EB}$

12 The volume, in cubic centimeters, of a sphere whose diameter is 6 centimeters is
1) 12π
2) 36π
3) 48π
4) 288π

13 The equation of line k is $y = \frac{1}{3}x - 2$. The equation of line m is $-2x + 6y = 18$. Lines k and m are
1) parallel
2) perpendicular
3) the same line
4) neither parallel nor perpendicular

14 What are the center and the radius of the circle whose equation is $(x-5)^2 + (y+3)^2 = 16$?
1) $(-5, 3)$ and 16
2) $(5, -3)$ and 16
3) $(-5, 3)$ and 4
4) $(5, -3)$ and 4

15 Triangle ABC has vertices $A(0, 0)$, $B(3, 2)$, and $C(0, 4)$. The triangle may be classified as
1) equilateral
2) isosceles
3) right
4) scalene

3

16 In rhombus *ABCD*, the diagonals $\overline{AC}$ and $\overline{BD}$ intersect at *E*. If *AE* = 5 and *BE* = 12, what is the length of $\overline{AB}$?
1) 7
2) 10
3) 13
4) 17

17 In the diagram below of circle *O*, $\overline{PA}$ is tangent to circle *O* at *A*, and $\overline{PBC}$ is a secant with points *B* and *C* on the circle.

If *PA* = 8 and *PB* = 4, what is the length of $\overline{BC}$?
1) 20
2) 16
3) 15
4) 12

18 Lines *m* and *n* intersect at point *A*. Line *k* is perpendicular to both lines *m* and *n* at point *A*. Which statement *must* be true?
1) Lines *m*, *n*, and *k* are in the same plane.
2) Lines *m* and *n* are in two different planes.
3) Lines *m* and *n* are perpendicular to each other.
4) Line *k* is perpendicular to the plane containing lines *m* and *n*.

19 In $\triangle DEF$, m$\angle D$ = 3*x* + 5, m$\angle E$ = 4*x* − 15, and m$\angle F$ = 2*x* + 10. Which statement is true?
1) *DF* = *FE*
2) *DE* = *FE*
3) m$\angle E$ = m$\angle F$
4) m$\angle D$ = m$\angle F$

20 As shown in the diagram below, $\triangle ABC \sim \triangle DEF$, *AB* = 7*x*, *BC* = 4, *DE* = 7, and *EF* = *x*.

What is the length of $\overline{AB}$?
1) 28
2) 2
3) 14
4) 4

21 A man wants to place a new bird bath in his yard so that it is 30 feet from a fence, *f*, and also 10 feet from a light pole, *P*. As shown in the diagram below, the light pole is 35 feet away from the fence.

How many locations are possible for the bird bath?
1) 1
2) 2
3) 3
4) 0

4

22 As shown on the graph below, $\Delta R'S'T'$ is the image of ΔRST under a single transformation.

Which transformation does this graph represent?
1) glide reflection
2) line reflection
3) rotation
4) translation

23 Which line is parallel to the line whose equation is $4x + 3y = 7$ and also passes through the point $(-5, 2)$?
1) $4x + 3y = -26$
2) $4x + 3y = -14$
3) $3x + 4y = -7$
4) $3x + 4y = 14$

24 If the vertex angles of two isosceles triangles are congruent, then the triangles must be
1) acute
2) congruent
3) right
4) similar

25 Which quadrilateral has diagonals that always bisect its angles and also bisect each other?
1) rhombus
2) rectangle
3) parallelogram
4) isosceles trapezoid

26 When ΔABC is dilated by a scale factor of 2, its image is $\Delta A'B'C'$. Which statement is true?
1) $\overline{AC} \cong \overline{A'C'}$
2) $\angle A \cong \angle A'$
3) perimeter of ΔABC = perimeter of $\Delta A'B'C'$
4) 2(area of ΔABC) = area of $\Delta A'B'C'$

27 What is the slope of a line that is perpendicular to the line whose equation is $3x + 5y = 4$?
1) $-\dfrac{3}{5}$
2) $\dfrac{3}{5}$
3) $-\dfrac{5}{3}$
4) $\dfrac{5}{3}$

28 In the diagram below of right triangle ABC, altitude $\overline{BD}$ is drawn to hypotenuse $\overline{AC}$, $AC = 16$, and $CD = 7$.

What is the length of $\overline{BD}$?
1) $3\sqrt{7}$
2) $4\sqrt{7}$
3) $7\sqrt{3}$
4) 12

29 Given the true statement, "The medians of a triangle are concurrent," write the negation of the statement and give the truth value for the negation.

5

30 Using a compass and straightedge, on the diagram below of $\overleftrightarrow{RS}$, construct an equilateral triangle with $\overline{RS}$ as one side. [Leave all construction marks.]

31 The Parkside Packing Company needs a rectangular shipping box. The box must have a length of 11 inches and a width of 8 inches. Find, to the *nearest tenth of an inch*, the minimum height of the box such that the volume is *at least* 800 cubic inches.

32 A pentagon is drawn on the set of axes below. If the pentagon is reflected over the *y*-axis, determine if this transformation is an isometry. Justify your answer. [The use of the set of axes is optional.]

33 In the diagram below of $\triangle ABC$, D is a point on $\overline{AB}$, E is a point on $\overline{BC}$, $\overline{AC} \parallel \overline{DE}$, $CE = 25$ inches, $AD = 18$ inches, and $DB = 12$ inches. Find, to the *nearest tenth of an inch*, the length of $\overline{EB}$.

34 In circle O, diameter $\overline{RS}$ has endpoints $R(3a, 2b - 1)$ and $S(a - 6, 4b + 5)$. Find the coordinates of point O, in terms of a and b. Express your answer in simplest form.

35 On the set of coordinate axes below, graph the locus of points that are equidistant from the lines $y = 6$ and $y = 2$ and also graph the locus of points that are 3 units from the y-axis. State the coordinates of *all* points that satisfy *both* conditions.
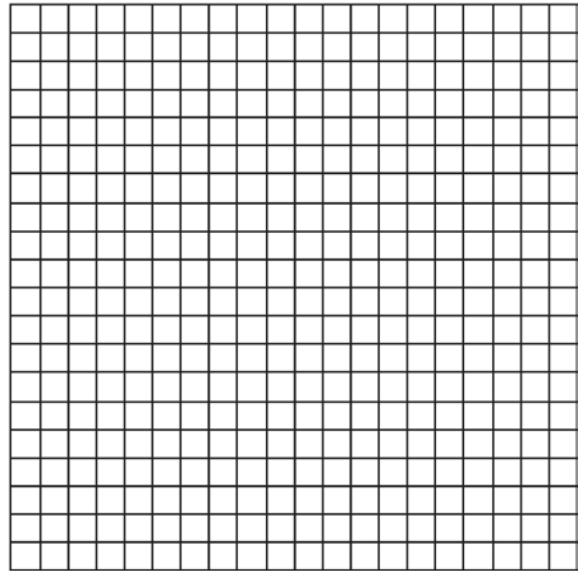

36 In the diagram below, tangent $\overline{ML}$ and secant $\overline{MNK}$ are drawn to circle O. The ratio $m\overset{\frown}{LN} : m\overset{\frown}{NK} : m\overset{\frown}{KL}$ is $3:4:5$. Find $m\angle LMK$.

37 Solve the following system of equations graphically.

$$2x^2 - 4x = y + 1$$
$$x + y = 1$$

38 In the diagram below, $\overline{PA}$ and $\overline{PB}$ are tangent to circle O, $\overline{OA}$ and $\overline{OB}$ are radii, and $\overline{OP}$ intersects the circle at C. Prove: $\angle AOP \cong \angle BOP$

0811ge

1 The statement "x is a multiple of 3, and x is an even integer" is true when x is equal to
1) 9
2) 8
3) 3
4) 6

2 In the diagram below, $\triangle ABC \cong \triangle XYZ$.

Which statement must be true?
1) $\angle C \cong \angle Y$
2) $\angle A \cong \angle X$
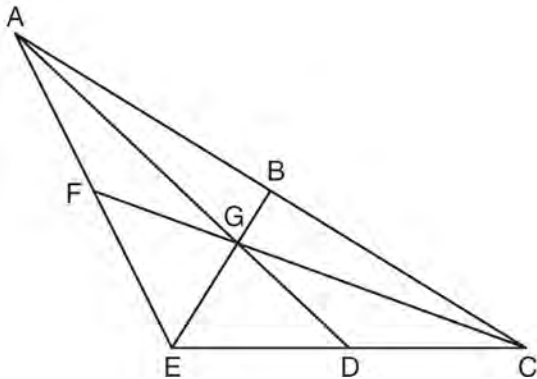3) $\overline{AC} \cong \overline{YZ}$
4) $\overline{CB} \cong \overline{XZ}$

3 In the diagram below of $\triangle ABC$, $\overleftrightarrow{TV} \parallel \overline{BC}$, $AT = 5$, $TB = 7$, and $AV = 10$.

What is the length of $\overline{VC}$?
1) $3\frac{1}{2}$
2) $7\frac{1}{7}$
3) 14
4) 24

4 Pentagon $PQRST$ has $\overline{PQ}$ parallel to $\overline{TS}$. After a translation of $T_{2,-5}$, which line segment is parallel to $\overline{P'Q'}$?
1) $\overline{R'Q'}$
2) $\overline{R'S'}$
3) $\overline{T'S'}$
4) $\overline{T'P'}$

5 In the diagram below of $\triangle PAO$, $\overline{AP}$ is tangent to circle O at point A, $OB = 7$, and $BP = 18$.

What is the length of $\overline{AP}$?
1) 10
2) 12
3) 17
4) 24

6 A straightedge and compass were used to create the construction below. Arc EF was drawn from point B, and arcs with equal radii were drawn from E and F.

Which statement is *false*?
1) $m\angle ABD = m\angle DBC$
2) $\frac{1}{2}(m\angle ABC) = m\angle ABD$
3) $2(m\angle DBC) = m\angle ABC$
4) $2(m\angle ABC) = m\angle CBD$

7 What is the length of the line segment whose endpoints are $(1, -4)$ and $(9, 2)$?
1) 5
2) $2\sqrt{17}$
3) 10
4) $2\sqrt{26}$

8 What is the image of the point $(2, -3)$ after the transformation $r_{y-\text{axis}}$?
1) $(2, 3)$
2) $(-2, -3)$
3) $(-2, 3)$
4) $(-3, 2)$

9 In the diagram below, lines n and m are cut by transversals p and q.

What value of x would make lines n and m parallel?
1) 110
2) 80
3) 70
4) 50

10 What is an equation of the circle with a radius of 5 and center at $(1, -4)$?
1) $(x + 1)^2 + (y - 4)^2 = 5$
2) $(x - 1)^2 + (y + 4)^2 = 5$
3) $(x + 1)^2 + (y - 4)^2 = 25$
4) $(x - 1)^2 + (y + 4)^2 = 25$

11 In the diagram below of $\triangle BCD$, side $\overline{DB}$ is extended to point A.

Which statement must be true?
1) $m\angle C > m\angle D$
2) $m\angle ABC < m\angle D$
3) $m\angle ABC > m\angle C$
4) $m\angle ABC > m\angle C + m\angle D$

2

12 Which equation represents the line parallel to the line whose equation is $4x + 2y = 14$ and passing through the point $(2, 2)$?

1) $y = -2x$
2) $y = -2x + 6$
3) $y = \frac{1}{2}x$
4) $y = \frac{1}{2}x + 1$

13 The coordinates of point A are $(-3a, 4b)$. If point A' is the image of point A reflected over the line $y = x$, the coordinates of A' are

1) $(4b, -3a)$
2) $(3a, 4b)$
3) $(-3a, -4b)$
4) $(-4b, -3a)$

14 As shown in the diagram below, $\overline{AC}$ bisects $\angle BAD$ and $\angle B \cong \angle D$.

Which method could be used to prove $\triangle ABC \cong \triangle ADC$?

1) SSS
2) AAA
3) SAS
4) AAS

15 Segment AB is the diameter of circle M. The coordinates of A are $(-4, 3)$. The coordinates of M are $(1, 5)$. What are the coordinates of B?

1) $(6, 7)$
2) $(5, 8)$
3) $(-3, 8)$
4) $(-5, 2)$

16 In the diagram below, $\overleftrightarrow{AB}$ is perpendicular to plane $AEFG$.

Which plane must be perpendicular to plane $AEFG$?

1) $ABCE$
2) $BCDH$
3) $CDFE$
4) $HDFG$

17 How many points are both 4 units from the origin and also 2 units from the line $y = 4$?

1) 1
2) 2
3) 3
4) 4

18 When solved graphically, what is the solution to the following system of equations?

$$y = x^2 - 4x + 6$$
$$y = x + 2$$

1) $(1, 4)$
2) $(4, 6)$
3) $(1, 3)$ and $(4, 6)$
4) $(3, 1)$ and $(6, 4)$

19 Triangle PQR has angles in the ratio of $2:3:5$. Which type of triangle is $\triangle PQR$?

1) acute
2) isosceles
3) obtuse
4) right

3

20 Plane $\mathcal{A}$ is parallel to plane $\mathcal{B}$. Plane $\mathcal{C}$ intersects plane $\mathcal{A}$ in line m and intersects plane $\mathcal{B}$ in line n. Lines m and n are
1) intersecting
2) parallel
3) perpendicular
4) skew

21 The diagonals of a quadrilateral are congruent but do not bisect each other. This quadrilateral is
1) an isosceles trapezoid
2) a parallelogram
3) a rectangle
4) a rhombus

22 What is the slope of a line that is perpendicular to the line represented by the equation $x + 2y = 3$?
1) -2
2) 2
3) $-\dfrac{1}{2}$
4) $\dfrac{1}{2}$

23 A packing carton in the shape of a triangular prism is shown in the diagram below.

What is the volume, in cubic inches, of this carton?
1) 20
2) 60
3) 120
4) 240

24 In the diagram below of circle O, diameter $\overline{AOB}$ is perpendicular to chord $\overline{CD}$ at point E, $OA = 6$, and $OE = 2$.

What is the length of $\overline{CE}$?
1) $4\sqrt{3}$
2) $2\sqrt{3}$
3) $8\sqrt{2}$
4) $4\sqrt{2}$

25 What is the measure of each interior angle of a regular hexagon?
1) $60°$
2) $120°$
3) $135°$
4) $270°$

26 Which equation represents the perpendicular bisector of $\overline{AB}$ whose endpoints are $A(8,2)$ and $B(0,6)$?
1) $y = 2x - 4$
2) $y = -\dfrac{1}{2}x + 2$
3) $y = -\dfrac{1}{2}x + 6$
4) $y = 2x - 12$

4

27 As shown in the diagram below, a kite needs a vertical and a horizontal support bar attached at opposite corners. The upper edges of the kite are 7 inches, the side edges are x inches, and the vertical support bar is $(x + 1)$ inches.

What is the measure, in inches, of the vertical support bar?
1) 23
2) 24
3) 25
4) 26

28 Given three distinct quadrilaterals, a square, a rectangle, and a rhombus, which quadrilaterals must have perpendicular diagonals?
1) the rhombus, only
2) the rectangle and the square
3) the rhombus and the square
4) the rectangle, the rhombus, and the square

29 In the diagram below, trapezoid $ABCD$, with bases $\overline{AB}$ and $\overline{DC}$, is inscribed in circle O, with diameter $\overline{DC}$. If m$\overarc{AB}$=80, find m$\overarc{BC}$.

30 On the diagram of $\triangle ABC$ shown below, use a compass and straightedge to construct the perpendicular bisector of $\overline{AC}$. [Leave all construction marks.]

31 A sphere has a diameter of 18 meters. Find the volume of the sphere, in cubic meters, in terms of π.

5

32 Write an equation of the circle graphed in the diagram below.

33 The diagram below shows $\triangle ABC$, with $\overline{AEB}$, $\overline{ADC}$, and $\angle ACB \cong \angle AED$. Prove that $\triangle ABC$ is similar to $\triangle ADE$.

34 Triangle ABC has vertices $A(3,3)$, $B(7,9)$, and $C(11,3)$. Determine the point of intersection of the medians, and state its coordinates. [The use of the set of axes below is optional.]

35 In the diagram below of $\triangle GJK$, H is a point on $\overline{GJ}$, $\overline{HJ} \cong \overline{JK}$, m$\angle G = 28$, and m$\angle GJK = 70$. Determine whether $\triangle GHK$ is an isosceles triangle and justify your answer.

36 As shown on the set of axes below, $\triangle GHS$ has vertices $G(3,1)$, $H(5,3)$, and $S(1,4)$. Graph and state the coordinates of $\triangle G''H''S''$, the image of $\triangle GHS$ after the transformation $T_{-3,1} \circ D_2$.

37 In the diagram below, $\triangle ABC \sim \triangle DEF$, $DE = 4$, $AB = x$, $AC = x + 2$, and $DF = x + 6$. Determine the length of $\overline{AB}$. [Only an algebraic solution can receive full credit.]

38 Given: $\triangle ABC$ with vertices $A(-6,-2)$, $B(2,8)$, and $C(6,-2)$. $\overline{AB}$ has midpoint D, $\overline{BC}$ has midpoint E, and $\overline{AC}$ has midpoint F.
Prove: $ADEF$ is a parallelogram
        $ADEF$ is *not* a rhombus
[The use of the grid is optional.]

0112ge

1 Line *n* intersects lines *l* and *m*, forming the angles shown in the diagram below.

Which value of *x* would prove *l* ∥ *m*?
1) 2.5
2) 4.5
3) 6.25
4) 8.75

2 In a given triangle, the point of intersection of the three medians is the same as the point of intersection of the three altitudes. Which classification of the triangle is correct?
1) scalene triangle
2) isosceles triangle
3) equilateral triangle
4) right isosceles triangle

3 A circle has the equation $(x-2)^2 + (y+3)^2 = 36$. What are the coordinates of its center and the length of its radius?
1) $(-2, 3)$ and 6
2) $(2, -3)$ and 6
3) $(-2, 3)$ and 36
4) $(2, -3)$ and 36

4 In the diagram below, *MATH* is a rhombus with diagonals $\overline{AH}$ and $\overline{MT}$.

If m∠*HAM* = 12, what is m∠*AMT*?
1) 12
2) 78
3) 84
4) 156

5 A line segment has endpoints $(4, 7)$ and $(1, 11)$. What is the length of the segment?
1) 5
2) 7
3) 16
4) 25

6 In △*FGH*, m∠*F* = 42 and an exterior angle at vertex *H* has a measure of 104. What is m∠*G*?
1) 34
2) 62
3) 76
4) 146

7 Which diagram represents a correct construction of equilateral $\triangle ABC$, given side $\overline{AB}$?

1)

2)

3)

4)

8 In the diagram below, $\triangle ABC$ is circumscribed about circle O and the sides of $\triangle ABC$ are tangent to the circle at points D, E, and F.

If $AB = 20$, $AE = 12$, and $CF = 15$, what is the length of $\overline{AC}$?
1) 8
2) 15
3) 23
4) 27

9 In $\triangle ABC$ and $\triangle DEF$, $\frac{AC}{DF} = \frac{CB}{FE}$. Which additional information would prove $\triangle ABC \sim \triangle DEF$?
1) $AC = DF$
2) $CB = FE$
3) $\angle ACB \cong \angle DFE$
4) $\angle BAC \cong \angle EDF$

10 The angles of triangle ABC are in the ratio of $8:3:4$. What is the measure of the *smallest* angle?
1) $12°$
2) $24°$
3) $36°$
4) $72°$

11 When a quadrilateral is reflected over the line $y = x$, which geometric relationship is *not* preserved?
1) congruence
2) orientation
3) parallelism
4) perpendicularity

2

12 Which equation represents circle O with center $(2, -8)$ and radius 9?

1) $(x + 2)^2 + (y - 8)^2 = 9$

2) $(x - 2)^2 + (y + 8)^2 = 9$

3) $(x + 2)^2 + (y - 8)^2 = 81$

4) $(x - 2)^2 + (y + 8)^2 = 81$

13 Which statement is the negation of "Two is a prime number" and what is the truth value of the negation?
1) Two is not a prime number; false
2) Two is not a prime number; true
3) A prime number is two; false
4) A prime number is two; true

14 In the diagram below of circle O, chords $\overline{AB}$ and $\overline{CD}$ intersect at E.

If m$\angle AEC = 34$ and m$\overarc{AC} = 50$, what is m$\overarc{DB}$?
1) 16
2) 18
3) 68
4) 118

15 The volume of a rectangular prism is 144 cubic inches. The height of the prism is 8 inches. Which measurements, in inches, could be the dimensions of the base?
1) 3.3 by 5.5
2) 2.5 by 7.2
3) 12 by 8
4) 9 by 9

16 The diagram below shows a pair of congruent triangles, with $\angle ADB \cong \angle CDB$ and $\angle ABD \cong \angle CBD$.

Which statement must be true?
1) $\angle ADB \cong \angle CBD$
2) $\angle ABC \cong \angle ADC$
3) $\overline{AB} \cong \overline{CD}$
4) $\overline{AD} \cong \overline{CD}$

17 What is an equation of the line that is perpendicular to the line whose equation is $y = \dfrac{3}{5}x - 2$ and that passes through the point $(3, -6)$?

1) $y = \dfrac{5}{3}x - 11$

2) $y = -\dfrac{5}{3}x + 11$

3) $y = -\dfrac{5}{3}x - 1$

4) $y = \dfrac{5}{3}x + 1$

18 Point A lies in plane $\mathcal{B}$. How many lines can be drawn perpendicular to plane $\mathcal{B}$ through point A?
1) one
2) two
3) zero
4) infinite

3

19 In the diagram below of isosceles trapezoid $ABCD$, $AB = CD = 25$, $AD = 26$, and $BC = 12$.

What is the length of an altitude of the trapezoid?
1) 7
2) 14
3) 19
4) 24

20 What is an equation of circle O shown in the graph below?

1) $(x + 2)^2 + (y - 2)^2 = 9$
2) $(x + 2)^2 + (y - 2)^2 = 3$
3) $(x - 2)^2 + (y + 2)^2 = 9$
4) $(x - 2)^2 + (y + 2)^2 = 3$

21 The diagram below represents a rectangular solid.

Which statement must be true?
1) $\overline{EH}$ and $\overline{BC}$ are coplanar
2) $\overline{FG}$ and $\overline{AB}$ are coplanar
3) $\overline{EH}$ and $\overline{AD}$ are skew
4) $\overline{FG}$ and $\overline{CG}$ are skew

22 In $\triangle RST$, $m\angle R = 58$ and $m\angle S = 73$. Which inequality is true?
1) $RT < TS < RS$
2) $RS < RT < TS$
3) $RT < RS < TS$
4) $RS < TS < RT$

23 The number of degrees in the sum of the interior angles of a pentagon is
1) 72
2) 360
3) 540
4) 720

24 What is the equation of a line passing through $(2, -1)$ and parallel to the line represented by the equation $y = 2x + 1$?

1) $y = -\dfrac{1}{2}x$

2) $y = -\dfrac{1}{2}x + 1$

3) $y = 2x - 5$
4) $y = 2x - 1$

25 The coordinates of the endpoints of $\overline{AB}$ are $A(0,0)$ and $B(0,6)$. The equation of the perpendicular bisector of $\overline{AB}$ is
1) $x = 0$
2) $x = 3$
3) $y = 0$
4) $y = 3$

26 In the diagram below, point P is the centroid of $\triangle ABC$.

If $PM = 2x + 5$ and $BP = 7x + 4$, what is the length of $\overline{PM}$?
1) 9
2) 2
3) 18
4) 27

27 In $\triangle PQR$, $\angle PRQ$ is a right angle and $\overline{RT}$ is drawn perpendicular to hypotenuse $\overline{PQ}$. If $PT = x$, $RT = 6$, and $TQ = 4x$, what is the length of $\overline{PQ}$?
1) 9
2) 12
3) 3
4) 15

28 In $\triangle ABC$, $AB = 5$ feet and $BC = 3$ feet. Which inequality represents all possible values for the length of $\overline{AC}$, in feet?
1) $2 \le AC \le 8$
2) $2 < AC < 8$
3) $3 \le AC \le 7$
4) $3 < AC < 7$

29 In the diagram below, two parallel lines intersect circle O at points A, B, C, and D, with $m\widehat{AB} = x + 20$ and $m\widehat{DC} = 2x - 20$. Find $m\widehat{AB}$.

30 In the diagram below, point M is located on $\overleftrightarrow{AB}$.

Sketch the locus of points that are 1 unit from $\overleftrightarrow{AB}$ and the locus of points 2 units from point M. Label with an **X** all points that satisfy both conditions.

31 Determine whether the two lines represented by the equations $y = 2x + 3$ and $2y + x = 6$ are parallel, perpendicular, or neither. Justify your response.

32 The coordinates of the vertices of $\triangle RST$ are $R(-2,3)$, $S(4,4)$, and $T(2,-2)$. Triangle $R'S'T'$ is the image of $\triangle RST$ after a rotation of 90° about the origin. State the coordinates of the vertices of $\triangle R'S'T'$. [The use of the set of axes below is optional.]

33 On the diagram below, use a compass and straightedge to construct the bisector of $\angle XYZ$. [Leave all construction marks.]

34 In the diagram below of circle O, diameter $\overline{AB}$ is perpendicular to chord $\overline{CD}$ at E. If $AO = 10$ and $BE = 4$, find the length of $\overline{CE}$.

35 Triangle ABC has coordinates $A(2,-2)$, $B(2,1)$, and $C(4,-2)$. Triangle $A'B'C'$ is the image of $\triangle ABC$ under $T_{5,-2}$. On the set of axes below, graph and label $\triangle ABC$ and its image, $\triangle A'B'C'$. Determine the relationship between the area of $\triangle ABC$ and the area of $\triangle A'B'C'$. Justify your response.

36 A paint can is in the shape of a right circular
    cylinder. The volume of the paint can is 600π
    cubic inches and its altitude is 12 inches. Find the
    radius, in inches, of the base of the paint can.
    Express the answer in simplest radical form. Find,
    to the *nearest tenth of a square inch*, the lateral
    area of the paint can.

37 Triangle *HKL* has vertices $H(-7, 2)$, $K(3, -4)$, and
    $L(5, 4)$. The midpoint of $\overline{HL}$ is *M* and the midpoint
    of $\overline{LK}$ is *N*. Determine and state the coordinates of
    points *M* and *N*. Justify the statement: $\overline{MN}$ is
    parallel to $\overline{HK}$. [The use of the set of axes below is
    optional.]

38 In the diagram below of quadrilateral *ABCD*,
    $\overline{AD} \cong \overline{BC}$ and $\angle DAE \cong \angle BCE$. Line segments *AC*,
    DB, and *FG* intersect at *E*.
    Prove: $\triangle AEF \cong \triangle CEG$

0612ge

1 Triangle *ABC* is graphed on the set of axes below.

Which transformation produces an image that is similar to, but *not* congruent to, $\triangle ABC$?

1) $T_{2,3}$
2) D_2
3) $r_{y=x}$
4) R_{90}

2 A student wrote the sentence "4 is an odd integer." What is the negation of this sentence and the truth value of the negation?

1) 3 is an odd integer; true
2) 4 is not an odd integer; true
3) 4 is not an even integer; false
4) 4 is an even integer; false

3 As shown in the diagram below, $\overleftrightarrow{EF}$ intersects planes $\mathcal{P}$, $\mathcal{Q}$, and $\mathcal{R}$.

If $\overleftrightarrow{EF}$ is perpendicular to planes $\mathcal{P}$ and $\mathcal{R}$, which statement must be true?

1) Plane $\mathcal{P}$ is perpendicular to plane $\mathcal{Q}$.
2) Plane $\mathcal{R}$ is perpendicular to plane $\mathcal{P}$.
3) Plane $\mathcal{P}$ is parallel to plane $\mathcal{Q}$.
4) Plane $\mathcal{R}$ is parallel to plane $\mathcal{P}$.

4 In the diagram below, *LATE* is an isosceles trapezoid with $\overline{LE} \cong \overline{AT}$, $LA = 24$, $ET = 40$, and $AT = 10$. Altitudes $\overline{LF}$ and $\overline{AG}$ are drawn.

What is the length of $\overline{LF}$?

1) 6
2) 8
3) 3
4) 4

5 In the diagram below of circle O, diameter $\overline{AB}$ is parallel to chord $\overline{CD}$.

If $m\widehat{CD} = 70$, what is $m\widehat{AC}$?
1) 110
2) 70
3) 55
4) 35

6 In the diagram below of $\overline{ABCD}$, $\overline{AC} \cong \overline{BD}$.

Using this information, it could be proven that
1) $BC = AB$
2) $AB = CD$
3) $AD - BC = CD$
4) $AB + CD = AD$

7 The diameter of a sphere is 15 inches. What is the volume of the sphere, to the *nearest tenth of a cubic inch*?
1) 706.9
2) 1767.1
3) 2827.4
4) 14,137.2

8 The diagram below shows the construction of $\overleftrightarrow{AB}$ through point P parallel to $\overleftrightarrow{CD}$.

Which theorem justifies this method of construction?
1) If two lines in a plane are perpendicular to a transversal at different points, then the lines are parallel.
2) If two lines in a plane are cut by a transversal to form congruent corresponding angles, then the lines are parallel.
3) If two lines in a plane are cut by a transversal to form congruent alternate interior angles, then the lines are parallel.
4) If two lines in a plane are cut by a transversal to form congruent alternate exterior angles, then the lines are parallel.

9 Parallelogram $ABCD$ has coordinates $A(1,5)$, $B(6,3)$, $C(3,-1)$, and $D(-2,1)$. What are the coordinates of E, the intersection of diagonals $\overline{AC}$ and $\overline{BD}$?
1) $(2,2)$
2) $(4.5,1)$
3) $(3.5,2)$
4) $(-1,3)$

10 What is the equation of a circle whose center is 4 units above the origin in the coordinate plane and whose radius is 6?
1) $x^2 + (y-6)^2 = 16$
2) $(x-6)^2 + y^2 = 16$
3) $x^2 + (y-4)^2 = 36$
4) $(x-4)^2 + y^2 = 36$

11 In the diagram of $\triangle ABC$ shown below, D is the midpoint of $\overline{AB}$, E is the midpoint of $\overline{BC}$, and F is the midpoint of $\overline{AC}$.

If $AB = 20$, $BC = 12$, and $AC = 16$, what is the perimeter of trapezoid $ABEF$?
1) 24
2) 36
3) 40
4) 44

12 In the diagram below, $\triangle LMO$ is isosceles with $LO = MO$.

If $m\angle L = 55$ and $m\angle NOM = 28$, what is $m\angle N$?
1) 27
2) 28
3) 42
4) 70

13 If $\overleftrightarrow{AB}$ is contained in plane $\mathcal{P}$, and $\overleftrightarrow{AB}$ is perpendicular to plane $\mathcal{R}$, which statement is true?
1) $\overleftrightarrow{AB}$ is parallel to plane $\mathcal{R}$.
2) Plane $\mathcal{P}$ is parallel to plane $\mathcal{R}$.
3) $\overleftrightarrow{AB}$ is perpendicular to plane $\mathcal{P}$.
4) Plane $\mathcal{P}$ is perpendicular to plane $\mathcal{R}$.

14 In the diagram below of $\triangle ABC$, $\overline{AE} \cong \overline{BE}$, $\overline{AF} \cong \overline{CF}$, and $\overline{CD} \cong \overline{BD}$.

Point P must be the
1) centroid
2) circumcenter
3) incenter
4) orthocenter

15 What is the equation of the line that passes through the point $(-9, 6)$ and is perpendicular to the line $y = 3x - 5$?
1) $y = 3x + 21$
2) $y = -\dfrac{1}{3}x - 3$
3) $y = 3x + 33$
4) $y = -\dfrac{1}{3}x + 3$

16 In the diagram of $\triangle ABC$ shown below, $\overline{DE} \parallel \overline{BC}$.

If $AB = 10$, $AD = 8$, and $AE = 12$, what is the length of $\overline{EC}$?
1) 6
2) 2
3) 3
4) 15

3

17 What is the length of $\overline{AB}$ with endpoints $A(-1,0)$ and $B(4,-3)$?

1) $\sqrt{6}$

2) $\sqrt{18}$

3) $\sqrt{34}$

4) $\sqrt{50}$

18 The sum of the interior angles of a polygon of n sides is

1) 360

2) $\dfrac{360}{n}$

3) $(n-2) \cdot 180$

4) $\dfrac{(n-2) \cdot 180}{n}$

19 What is the slope of a line perpendicular to the line whose equation is $20x - 2y = 6$?

1) -10

2) $-\dfrac{1}{10}$

3) 10

4) $\dfrac{1}{10}$

20 Which graph represents a circle whose equation is $(x+2)^2 + y^2 = 16$?

1)

2)

3)

4)

21 In circle O shown below, diameter $\overline{DB}$ is perpendicular to chord $\overline{AC}$ at E.

If $DB = 34$, $AC = 30$, and $DE > BE$, what is the length of $\overline{BE}$?
1) 8
2) 9
3) 16
4) 25

22 In parallelogram $ABCD$ shown below, diagonals $\overline{AC}$ and $\overline{BD}$ intersect at E.

Which statement must be true?
1) $\overline{AC} \cong \overline{DB}$
2) $\angle ABD \cong \angle CBD$
3) $\triangle AED \cong \triangle CEB$
4) $\triangle DCE \cong \triangle BCE$

23 Which equation of a circle will have a graph that lies entirely in the first quadrant?
1) $(x - 4)^2 + (y - 5)^2 = 9$
2) $(x + 4)^2 + (y + 5)^2 = 9$
3) $(x + 4)^2 + (y + 5)^2 = 25$
4) $(x - 5)^2 + (y - 4)^2 = 25$

24 In the diagram below, $\triangle ABC \sim \triangle RST$.

Which statement is *not* true?
1) $\angle A \cong \angle R$
2) $\dfrac{AB}{RS} = \dfrac{BC}{ST}$
3) $\dfrac{AB}{BC} = \dfrac{ST}{RS}$
4) $\dfrac{AB + BC + AC}{RS + ST + RT} = \dfrac{AB}{RS}$

25 In the diagram below of $\triangle ABC$, $\overline{BC}$ is extended to D.

(Not drawn to scale)

If $m\angle A = x^2 - 6x$, $m\angle B = 2x - 3$, and $m\angle ACD = 9x + 27$, what is the value of x?
1) 10
2) 2
3) 3
4) 15

26 An equation of the line that passes through $(2, -1)$ and is parallel to the line $2y + 3x = 8$ is
1) $y = \dfrac{3}{2}x - 4$
2) $y = \dfrac{3}{2}x + 4$
3) $y = -\dfrac{3}{2}x - 2$
4) $y = -\dfrac{3}{2}x + 2$

5

27 The graph below shows $\overline{JT}$ and its image, $\overline{J'T'}$, after a transformation.

Which transformation would map $\overline{JT}$ onto $\overline{J'T'}$?
1) translation
2) glide reflection
3) rotation centered at the origin
4) reflection through the origin

28 Which reason could be used to prove that a parallelogram is a rhombus?
1) Diagonals are congruent.
2) Opposite sides are parallel.
3) Diagonals are perpendicular.
4) Opposite angles are congruent.

29 Triangle *TAP* has coordinates $T(-1,4)$, $A(2,4)$, and $P(2,0)$. On the set of axes below, graph and label $\triangle T'A'P'$, the image of $\triangle TAP$ after the translation $(x,y) \rightarrow (x-5, y-1)$.

30 In the diagram below, $\ell \parallel m$ and $\overline{QR} \perp \overline{ST}$ at R.

If m$\angle 1$ = 63, find m$\angle 2$.

31 Two lines are represented by the equations $x + 2y = 4$ and $4y - 2x = 12$. Determine whether these lines are parallel, perpendicular, or neither. Justify your answer.

32 Using a compass and straightedge, construct the bisector of $\angle CBA$. [Leave all construction marks.]

33 The cylindrical tank shown in the diagram below is to be painted. The tank is open at the top, and the bottom does *not* need to be painted. Only the outside needs to be painted. Each can of paint covers 600 square feet. How many cans of paint must be purchased to complete the job?

34 On the set of axes below, graph the locus of points that are 4 units from the line $x = 3$ and the locus of points that are 5 units from the point $(0, 2)$. Label with an **X** all points that satisfy both conditions.

35 Given: $\overline{AD}$ bisects $\overline{BC}$ at E.
$\overline{AB} \perp \overline{BC}$
$\overline{DC} \perp \overline{BC}$
Prove: $\overline{AB} \cong \overline{DC}$

7

36 The coordinates of trapezoid $ABCD$ are $A(-4,5)$, $B(1,5)$, $C(1,2)$, and $D(-6,2)$. Trapezoid $A''B''C''D''$ is the image after the composition $r_{x-\text{axis}} \circ r_{y=x}$ is performed on trapezoid $ABCD$. State the coordinates of trapezoid $A''B''C''D''$. [The use of the set of axes below is optional.]

37 In the diagram below of circle O, chords $\overline{RT}$ and $\overline{QS}$ intersect at M. Secant $\overline{PTR}$ and tangent $\overline{PS}$ are drawn to circle O. The length of $\overline{RM}$ is two more than the length of $\overline{TM}$, $QM = 2$, $SM = 12$, and $PT = 8$.

Find the length of $\overline{RT}$. Find the length of $\overline{PS}$.

38 On the set of axes below, solve the system of equations graphically and state the coordinates of all points in the solution.

$$y = (x-2)^2 - 3$$
$$2y + 16 = 4x$$

8

0812ge

1 In the diagram below of circle O, chord $\overline{AB}$ is parallel to chord $\overline{GH}$. Chord $\overline{CD}$ intersects $\overline{AB}$ at E and $\overline{GH}$ at F.

Which statement must always be true?
1) $\overarc{AC} \cong \overarc{CB}$
2) $\overarc{DH} \cong \overarc{BH}$
3) $\overarc{AB} \cong \overarc{GH}$
4) $\overarc{AG} \cong \overarc{BH}$

2 The vertices of parallelogram $ABCD$ are $A(2,0)$, $B(0,-3)$, $C(3,-3)$, and $D(5,0)$. If $ABCD$ is reflected over the x-axis, how many vertices remain invariant?
1) 1
2) 2
3) 3
4) 0

3 Point M is the midpoint of $\overline{AB}$. If the coordinates of A are $(-3,6)$ and the coordinates of M are $(-5,2)$, what are the coordinates of B?
1) $(1,2)$
2) $(7,10)$
3) $(-4,4)$
4) $(-7,-2)$

4 When a dilation is performed on a hexagon, which property of the hexagon will *not* be preserved in its image?
1) parallelism
2) orientation
3) length of sides
4) measure of angles

5 As shown in the diagram below of $\triangle ABC$, a compass is used to find points D and E, equidistant from point A. Next, the compass is used to find point F, equidistant from points D and E. Finally, a straightedge is used to draw $\overrightarrow{AF}$. Then, point G, the intersection of $\overrightarrow{AF}$ and side $\overline{BC}$ of $\triangle ABC$, is labeled.

Which statement must be true?
1) $\overrightarrow{AF}$ bisects side $\overline{BC}$
2) $\overrightarrow{AF}$ bisects $\angle BAC$
3) $\overrightarrow{AF} \perp \overline{BC}$
4) $\triangle ABG \sim \triangle ACG$

6 In the diagram of $\triangle JEA$ below, m$\angle JEA = 90$ and m$\angle EAJ = 48$. Line segment MS connects points M and S on the triangle, such that m$\angle EMS = 59$.

What is m$\angle JSM$?
1) 163
2) 121
3) 42
4) 17

7 In $\triangle AED$ with $\overline{ABCD}$ shown in the diagram below, $\overline{EB}$ and $\overline{EC}$ are drawn.

If $\overline{AB} \cong \overline{CD}$, which statement could always be proven?
1) $\overline{AC} \cong \overline{DB}$
2) $\overline{AE} \cong \overline{ED}$
3) $\overline{AB} \cong \overline{BC}$
4) $\overline{EC} \cong \overline{EA}$

8 Given that $ABCD$ is a parallelogram, a student wrote the proof below to show that a pair of its opposite angles are congruent.

Statement	Reason
1. ABCD is a parallelogram.	1. Given
2. $\overline{BC} \cong \overline{AD}$ $\overline{AB} \cong \overline{DC}$	2. Opposite sides of a parallelogram are congruent.
3. $\overline{AC} \cong \overline{CA}$	3. Reflexive Postulate of Congruency
4. $\triangle ABC \cong \triangle CDA$	4. Side-Side-Side
5. $\angle B \cong \angle D$	5. _____

What is the reason justifying that $\angle B \cong \angle D$?
1) Opposite angles in a quadrilateral are congruent.
2) Parallel lines have congruent corresponding angles.
3) Corresponding parts of congruent triangles are congruent.
4) Alternate interior angles in congruent triangles are congruent.

9 The equation of a circle with its center at $(-3, 5)$ and a radius of 4 is
1) $(x + 3)^2 + (y - 5)^2 = 4$
2) $(x - 3)^2 + (y + 5)^2 = 4$
3) $(x + 3)^2 + (y - 5)^2 = 16$
4) $(x - 3)^2 + (y + 5)^2 = 16$

10 In the diagram below of $\triangle DAE$ and $\triangle BCE$, $\overline{AB}$ and $\overline{CD}$ intersect at E, such that $\overline{AE} \cong \overline{CE}$ and $\angle BCE \cong \angle DAE$.

Triangle DAE can be proved congruent to triangle BCE by
1) ASA
2) SAS
3) SSS
4) HL

11 As shown in the diagram below, $\overline{FJ}$ is contained in plane $\mathcal{R}$, $\overline{BC}$ and $\overline{DE}$ are contained in plane S, and $\overline{FJ}$, $\overline{BC}$, and $\overline{DE}$ intersect at A.

Which fact is sufficient to show that planes $\mathcal{R}$ and S are perpendicular?
1) $\overline{FA} \perp \overline{DE}$
2) $\overline{AD} \perp \overline{AF}$
3) $\overline{BC} \perp \overline{FJ}$
4) $\overline{DE} \perp \overline{BC}$

12 What is an equation of the circle shown in the graph below?

1) $(x-3)^2 + (y-4)^2 = 25$
2) $(x+3)^2 + (y+4)^2 = 25$
3) $(x-3)^2 + (y-4)^2 = 10$
4) $(x+3)^2 + (y+4)^2 = 10$

13 As shown in the diagram below, lines m and n are cut by transversal p.

If $m\angle 1 = 4x + 14$ and $m\angle 2 = 8x + 10$, lines m and n are parallel when x equals
1) 1
2) 6
3) 13
4) 17

3

14 The angle formed by the radius of a circle and a tangent to that circle has a measure of
1) 45°
2) 90°
3) 135°
4) 180°

15 A sphere is inscribed inside a cube with edges of 6 cm. In cubic centimeters, what is the volume of the sphere, in terms of π?
1) 12π
2) 36π
3) 48π
4) 288π

16 Scalene triangle *ABC* is similar to triangle *DEF*. Which statement is *false*?
1) $AB:BC=DE:EF$
2) $AC:DF=BC:EF$
3) $\angle ACB \cong \angle DFE$
4) $\angle ABC \cong \angle EDF$

17 Which equation represents a line that is parallel to the line whose equation is $y = \frac{3}{2}x - 3$ and passes through the point $(1, 2)$?
1) $y = \frac{3}{2}x + \frac{1}{2}$
2) $y = \frac{2}{3}x + \frac{4}{3}$
3) $y = \frac{3}{2}x - 2$
4) $y = -\frac{2}{3}x + \frac{8}{3}$

18 Lines *a* and *b* intersect at point *P*. Line *c* passes through *P* and is perpendicular to the plane containing lines *a* and *b*. Which statement must be true?
1) Lines *a*, *b*, and *c* are coplanar.
2) Line *a* is perpendicular to line *b*.
3) Line *c* is perpendicular to both line *a* and line *b*.
4) Line *c* is perpendicular to line *a* or line *b*, but not both.

19 As shown in the diagram of $\triangle ACD$ below, *B* is a point on $\overline{AC}$ and $\overline{DB}$ is drawn.

If m$\angle A$ = 66, m$\angle CDB$ = 18, and m$\angle C$ = 24, what is the longest side of $\triangle ABD$?
1) $\overline{AB}$
2) $\overline{DC}$
3) $\overline{AD}$
4) $\overline{BD}$

20 In $\triangle ABC$ shown below, *P* is the centroid and $BF = 18$.

What is the length of $\overline{BP}$?
1) 6
2) 9
3) 3
4) 12

4

21 In the diagram below, $\overline{EF}$ is the median of trapezoid $ABCD$.

If $AB = 5x - 9$, $DC = x + 3$, and $EF = 2x + 2$, what is the value of x?
1) 5
2) 2
3) 7
4) 8

22 In the diagram below of $\triangle ABC$, $\overline{AB} \cong \overline{AC}$, $m\angle A = 3x$, and $m\angle B = x + 20$.

What is the value of x?
1) 10
2) 28
3) 32
4) 40

23 For which polygon does the sum of the measures of the interior angles equal the sum of the measures of the exterior angles?
1) hexagon
2) pentagon
3) quadrilateral
4) triangle

24 For a triangle, which two points of concurrence could be located outside the triangle?
1) incenter and centroid
2) centroid and orthocenter
3) incenter and circumcenter
4) circumcenter and orthocenter

25 The slope of line ℓ is $-\frac{1}{3}$. What is an equation of a line that is perpendicular to line ℓ?
1) $y + 2 = \frac{1}{3}x$
2) $-2x + 6 = 6y$
3) $9x - 3y = 27$
4) $3x + y = 0$

26 Which type of triangle can be drawn using the points $(-2, 3)$, $(-2, -7)$, and $(4, -5)$?
1) scalene
2) isosceles
3) equilateral
4) no triangle can be drawn

27 In the diagram below, $\overline{DE}$ joins the midpoints of two sides of $\triangle ABC$.

Which statement is *not* true?
1) $CE = \frac{1}{2} CB$
2) $DE = \frac{1}{2} AB$
3) area of $\triangle CDE = \frac{1}{2}$ area of $\triangle CAB$
4) perimeter of $\triangle CDE = \frac{1}{2}$ perimeter of $\triangle CAB$

28 Which equation represents the line that is perpendicular to $2y = x + 2$ and passes through the point $(4, 3)$?
1) $y = \frac{1}{2}x - 5$
2) $y = \frac{1}{2}x + 1$
3) $y = -2x + 11$
4) $y = -2x - 5$

5

29 Write the negation of the statement "2 is a prime number," and determine the truth value of the negation.

30 The coordinates of the vertices of $\triangle ABC$ are $A(1,2)$, $B(-4,3)$, and $C(-3,-5)$. State the coordinates of $\triangle A'B'C'$, the image of $\triangle ABC$ after a rotation of 90° about the origin. [The use of the set of axes below is optional.]

31 A cylinder has a height of 7 cm and a base with a diameter of 10 cm. Determine the volume, in cubic centimeters, of the cylinder in terms of π.

32 The coordinates of the endpoints of $\overline{FG}$ are $(-4,3)$ and $(2,5)$. Find the length of $\overline{FG}$ in simplest radical form.

33 Using a compass and straightedge, construct a line perpendicular to $\overline{AB}$ through point P. [Leave all construction marks.]

34 The graph below shows the locus of points equidistant from the x-axis and y-axis. On the same set of axes, graph the locus of points 3 units from the line $x = 0$. Label with an **X** *all* points that satisfy both conditions.

6

35 As shown in the diagram below, the diagonals of parallelogram $QRST$ intersect at E. If $QE = x^2 + 6x$, $SE = x + 14$, and $TE = 6x - 1$, determine TE algebraically.

36 The vertices of $\triangle RST$ are $R(-6,5)$, $S(-7,-2)$, and $T(1,4)$. The image of $\triangle RST$ after the composition $T_{-2,3} \circ r_{y=x}$ is $\triangle R''S''T''$. State the coordinates of $\triangle R''S''T''$. [The use of the set of axes below is optional.]

37 On the set of axes below, solve the following system of equations graphically and state the coordinates of *all* points in the solution.

$$(x+3)^2 + (y-2)^2 = 25$$

$$2y + 4 = -x$$

38 Chords $\overline{AB}$ and $\overline{CD}$ intersect at E in circle O, as shown in the diagram below. Secant $\overline{FDA}$ and tangent $\overline{FB}$ are drawn to circle O from external point F and chord $\overline{AC}$ is drawn. The $m\widehat{DA} = 56$, $m\widehat{DB} = 112$, and the ratio of $m\widehat{AC}:m\widehat{CB} = 3:1$.

Determine $m\angle CEB$. Determine $m\angle F$. Determine $m\angle DAC$.

7

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1 If $\triangle MNP \cong \triangle VWX$ and $\overline{PM}$ is the shortest side of $\triangle MNP$, what is the shortest side of $\triangle VWX$?
1) $\overline{XV}$
2) $\overline{WX}$
3) $\overline{VW}$
4) $\overline{NP}$

2 In circle O shown in the diagram below, chords $\overline{AB}$ and $\overline{CD}$ are parallel.

If $m\overset{\frown}{AB} = 104$ and $m\overset{\frown}{CD} = 168$, what is $m\overset{\frown}{BD}$?
1) 38
2) 44
3) 88
4) 96

3 As shown in the diagram below, $\overline{CD}$ is a median of $\triangle ABC$.

Which statement is *always* true?
1) $\overline{AD} \cong \overline{DB}$
2) $\overline{AC} \cong \overline{AD}$
3) $\angle ACD \cong \angle CDB$
4) $\angle BCD \cong \angle ACD$

4 In the diagram below, under which transformation is $\triangle A'B'C'$ the image of $\triangle ABC$?

1) D_2
2) $r_{x\text{-axis}}$
3) $r_{y\text{-axis}}$
4) $(x, y) \rightarrow (x - 2, y)$

5 Line segment AB is a diameter of circle O whose center has coordinates $(6, 8)$. What are the coordinates of point B if the coordinates of point A are $(4, 2)$?
1) $(1, 3)$
2) $(5, 5)$
3) $(8, 14)$
4) $(10, 10)$

6 Plane $\mathcal{A}$ and plane $\mathcal{B}$ are two distinct planes that are both perpendicular to line ℓ. Which statement about planes $\mathcal{A}$ and $\mathcal{B}$ is true?
1) Planes $\mathcal{A}$ and $\mathcal{B}$ have a common edge, which forms a line.
2) Planes $\mathcal{A}$ and $\mathcal{B}$ are perpendicular to each other.
3) Planes $\mathcal{A}$ and $\mathcal{B}$ intersect each other at exactly one point.
4) Planes $\mathcal{A}$ and $\mathcal{B}$ are parallel to each other.

7   Triangle *ABC* is similar to triangle *DEF*. The lengths of the sides of $\triangle ABC$ are 5, 8, and 11. What is the length of the shortest side of $\triangle DEF$ if its perimeter is 60?
1)   10
2)   12.5
3)   20
4)   27.5

8   In the diagram below of right triangle *ABC*, altitude $\overline{CD}$ is drawn to hypotenuse $\overline{AB}$.

If *AD* = 3 and *DB* = 12, what is the length of altitude $\overline{CD}$?
1)   6
2) $6\sqrt{5}$
3)   3
4) $3\sqrt{5}$

9   The diagram below shows the construction of an equilateral triangle.

Which statement justifies this construction?
1) $\angle A + \angle B + \angle C = 180$
2) $m\angle A = m\angle B = m\angle C$
3) $AB = AC = BC$
4) $AB + BC > AC$

10   What is the slope of the line perpendicular to the line represented by the equation $2x + 4y = 12$?
1) -2
2)   2
3) $-\dfrac{1}{2}$
4) $\dfrac{1}{2}$

11   Triangle *ABC* is shown in the diagram below.

If $\overline{DE}$ joins the midpoints of $\overline{ADC}$ and $\overline{AEB}$, which statement is *not* true?
1) $DE = \dfrac{1}{2}CB$
2) $\overline{DE} \parallel \overline{CB}$
3) $\dfrac{AD}{DC} = \dfrac{DE}{CB}$
4) $\triangle ABC \sim \triangle AED$

12   The equations $x^2 + y^2 = 25$ and $y = 5$ are graphed on a set of axes. What is the solution of this system?
1) $(0,0)$
2) $(5,0)$
3) $(0,5)$
4) $(5,5)$

13   Square *ABCD* has vertices $A(-2,-3)$, $B(4,-1)$, $C(2,5)$, and $D(-4,3)$. What is the length of a side of the square?
1) $2\sqrt{5}$
2) $2\sqrt{10}$
3) $4\sqrt{5}$
4) $10\sqrt{2}$

14 The diagram below shows $\triangle ABD$, with $\overrightarrow{ABC}$, $\overline{BE} \perp \overline{AD}$, and $\angle EBD \cong \angle CBD$.

If $m\angle ABE = 52$, what is $m\angle D$?
1) 26
2) 38
3) 52
4) 64

15 As shown in the diagram below, $\overline{FD}$ and $\overline{CB}$ intersect at point A and $\overline{ET}$ is perpendicular to both $\overline{FD}$ and $\overline{CB}$ at A.

Which statement is *not* true?
1) $\overline{ET}$ is perpendicular to plane BAD.
2) $\overline{ET}$ is perpendicular to plane FAB.
3) $\overline{ET}$ is perpendicular to plane CAD.
4) $\overline{ET}$ is perpendicular to plane BAT.

16 Which set of numbers could *not* represent the lengths of the sides of a right triangle?
1) $\{1, 3, \sqrt{10}\}$
2) $\{2, 3, 4\}$
3) $\{3, 4, 5\}$
4) $\{8, 15, 17\}$

17 How many points are 5 units from a line and also equidistant from two points on the line?
1) 1
2) 2
3) 3
4) 0

18 The equation of a circle is $(x-2)^2 + (y+5)^2 = 32$. What are the coordinates of the center of this circle and the length of its radius?
1) $(-2, 5)$ and 16
2) $(2, -5)$ and 16
3) $(-2, 5)$ and $4\sqrt{2}$
4) $(2, -5)$ and $4\sqrt{2}$

19 The equation of a line is $y = \dfrac{2}{3}x + 5$. What is an equation of the line that is perpendicular to the given line and that passes through the point $(4, 2)$?
1) $y = \dfrac{2}{3}x - \dfrac{2}{3}$
2) $y = \dfrac{3}{2}x - 4$
3) $y = -\dfrac{3}{2}x + 7$
4) $y = -\dfrac{3}{2}x + 8$

3

20 Consider the relationship between the two statements below.

$$\text{If } \sqrt{16+9} \neq 4+3, \text{ then } 5 \neq 4+3$$

$$\text{If } \sqrt{16+9} = 4+3, \text{ then } 5 = 4+3$$

These statements are
1) inverses
2) converses
3) contrapositives
4) biconditionals

21 In the diagram of trapezoid $ABCD$ below, $\overline{AB} \parallel \overline{DC}$, $\overline{AD} \cong \overline{BC}$, m$\angle A = 4x + 20$, and m$\angle C = 3x - 15$.

What is m$\angle D$?
1) 25
2) 35
3) 60
4) 90

22 In circle R shown below, diameter $\overline{DE}$ is perpendicular to chord $\overline{ST}$ at point L.

Which statement is *not* always true?
1) $\overline{SL} \cong \overline{TL}$
2) $RS = DR$
3) $\overline{RL} \cong \overline{LE}$
4) $(DL)(LE) = (SL)(LT)$

23 Which equation represents circle A shown in the diagram below?

1) $(x-4)^2 + (y-1)^2 = 3$
2) $(x+4)^2 + (y+1)^2 = 3$
3) $(x-4)^2 + (y-1)^2 = 9$
4) $(x+4)^2 + (y+1)^2 = 9$

4

24 Which equation represents a line that is parallel to the line whose equation is $3x - 2y = 7$?

1) $y = -\dfrac{3}{2}x + 5$

2) $y = -\dfrac{2}{3}x + 4$

3) $y = \dfrac{3}{2}x - 5$

4) $y = \dfrac{2}{3}x - 4$

25 In the diagram below of circle O, $\overline{PAC}$ and $\overline{PBD}$ are secants.

If $m\overset{\frown}{CD} = 70$ and $m\overset{\frown}{AB} = 20$, what is the degree measure of $\angle P$?

1) 25
2) 35
3) 45
4) 50

26 The measure of an interior angle of a regular polygon is 120°. How many sides does the polygon have?

1) 5
2) 6
3) 3
4) 4

27 As shown in the diagram of rectangle $ABCD$ below, diagonals $\overline{AC}$ and $\overline{BD}$ intersect at E.

If $AE = x + 2$ and $BD = 4x - 16$, then the length of $\overline{AC}$ is

1) 6
2) 10
3) 12
4) 24

28 If the vertices of $\triangle ABC$ are $A(-2, 4)$, $B(-2, 8)$, and $C(-5, 6)$, then $\triangle ABC$ is classified as

1) right
2) scalene
3) isosceles
4) equilateral

29 After the transformation $r_{y = x}$, the image of $\triangle ABC$ is $\triangle A'B'C'$. If $AB = 2x + 13$ and $A'B' = 9x - 8$, find the value of x.

30 In the diagram below, circles A and B are tangent at point C and $\overline{AB}$ is drawn. Sketch all common tangent lines.

31 On the set of axes below, graph the locus of points 4 units from $(0, 1)$ and the locus of points 3 units from the origin. Label with an **X** *any* points that satisfy *both* conditions.

32 Write an equation of a circle whose center is $(-3, 2)$ and whose diameter is 10.

33 Using a compass and straightedge, construct a line perpendicular to line ℓ through point P. [Leave all construction marks.]

34 Write an equation of the line that is the perpendicular bisector of the line segment having endpoints $(3, -1)$ and $(3, 5)$. [The use of the grid below is optional]

35 A right circular cylinder with a height of 5 cm has a base with a diameter of 6 cm. Find the lateral area of the cylinder to the *nearest hundredth of a square centimeter*. Find the volume of the cylinder to the *nearest hundredth of a cubic centimeter*.

36 Triangle *ABC* has vertices $A(5, 1)$, $B(1, 4)$ and $C(1, 1)$. State and label the coordinates of the vertices of $\triangle A''B''C''$, the image of $\triangle ABC$, following the composite transformation $T_{1, -1} \circ D_2$.

[The use of the set of axes below is optional.]

37 In $\triangle ABC$, $m\angle A = x^2 + 12$, $m\angle B = 11x + 5$, and $m\angle C = 13x - 17$. Determine the longest side of $\triangle ABC$.

38 The diagram below shows rectangle *ABCD* with points *E* and *F* on side $\overline{AB}$. Segments *CE* and *DF* intersect at *G*, and $\angle ADG \cong \angle BCG$. Prove: $\overline{AE} \cong \overline{BF}$

0613ge

1 In trapezoid $RSTV$ with bases $\overline{RS}$ and $\overline{VT}$, diagonals $\overline{RT}$ and $\overline{SV}$ intersect at Q.

If trapezoid $RSTV$ is *not* isosceles, which triangle is equal in area to $\triangle RSV$?
1) $\triangle RQV$
2) $\triangle RST$
3) $\triangle RVT$
4) $\triangle SVT$

2 In the diagram below, $\triangle XYV \cong \triangle TSV$.

Which statement can *not* be proven?
1) $\angle XVY \cong \angle TVS$
2) $\angle VYX \cong \angle VUT$
3) $\overline{XY} \cong \overline{TS}$
4) $\overline{YV} \cong \overline{SV}$

3 In a park, two straight paths intersect. The city wants to install lampposts that are both equidistant from each path and also 15 feet from the intersection of the paths. How many lampposts are needed?
1) 1
2) 2
3) 3
4) 4

4 What are the coordinates of A', the image of $A(-3,4)$, after a rotation of $180°$ about the origin?
1) $(4,-3)$
2) $(-4,-3)$
3) $(3,4)$
4) $(3,-4)$

5 Based on the construction below, which conclusion is *not* always true?

1) $\overline{AB} \perp \overline{CD}$
2) $AB = CD$
3) $AE = EB$
4) $CE = DE$

1

6 Which equation represents the circle whose center is $(-5, 3)$ and that passes through the point $(-1, 3)$?

1) $(x+1)^2 + (y-3)^2 = 16$
2) $(x-1)^2 + (y+3)^2 = 16$
3) $(x+5)^2 + (y-3)^2 = 16$
4) $(x-5)^2 + (y+3)^2 = 16$

7 As shown in the diagram below, when right triangle DAB is reflected over the x-axis, its image is triangle DCB.

Which statement justifies why $\overline{AB} \cong \overline{CB}$?
1) Distance is preserved under reflection.
2) Orientation is preserved under reflection.
3) Points on the line of reflection remain invariant.
4) Right angles remain congruent under reflection.

8 In $\triangle ABC$, $m\angle A = 3x + 1$, $m\angle B = 4x - 17$, and $m\angle C = 5x - 20$. Which type of triangle is $\triangle ABC$?
1) right
2) scalene
3) isosceles
4) equilateral

9 What is the equation for circle O shown in the graph below?

1) $(x-3)^2 + (y+1)^2 = 6$
2) $(x+3)^2 + (y-1)^2 = 6$
3) $(x-3)^2 + (y+1)^2 = 9$
4) $(x+3)^2 + (y-1)^2 = 9$

10 Point A is on line m. How many distinct planes will be perpendicular to line m and pass through point A?
1) one
2) two
3) zero
4) infinite

2

11 In $\triangle ABC$, D is the midpoint of $\overline{AB}$ and E is the midpoint of $\overline{BC}$. If $AC = 3x - 15$ and $DE = 6$, what is the value of x?

1) 6
2) 7
3) 9
4) 12

12 What are the coordinates of the center of a circle if the endpoints of its diameter are $A(8, -4)$ and $B(-3, 2)$?
1) $(2.5, 1)$
2) $(2.5, -1)$
3) $(5.5, -3)$
4) $(5.5, 3)$

13 Which graph could be used to find the solution to the following system of equations?

$$y = (x + 3)^2 - 1$$

$$x + y = 2$$

1)

2)

3)

4)

14 What is the converse of "If an angle measures 90 degrees, then it is a right angle"?
1) If an angle is a right angle, then it measures 90 degrees.
2) An angle is a right angle if it measures 90 degrees.
3) If an angle is not a right angle, then it does not measure 90 degrees.
4) If an angle does not measure 90 degrees, then it is not a right angle.

15 As shown in the diagram below, a right pyramid has a square base, $ABCD$, and $\overline{EF}$ is the slant height.

Which statement is *not* true?
1) $\overline{EA} \cong \overline{EC}$
2) $\overline{EB} \cong \overline{EF}$
3) $\triangle AEB \cong \triangle BEC$
4) $\triangle CED$ is isosceles

16 The volume of a sphere is approximately 44.6022 cubic centimeters. What is the radius of the sphere, to the *nearest tenth of a centimeter*?
1) 2.2
2) 3.3
3) 4.4
4) 4.7

17 What is the equation of a line passing through the point $(6, 1)$ and parallel to the line whose equation is $3x = 2y + 4$?
1) $y = -\dfrac{2}{3}x + 5$
2) $y = -\dfrac{2}{3}x - 3$
3) $y = \dfrac{3}{2}x - 8$
4) $y = \dfrac{3}{2}x - 5$

18 Points $A(5,3)$ and $B(7,6)$ lie on $\overleftrightarrow{AB}$. Points $C(6,4)$ and $D(9,0)$ lie on $\overleftrightarrow{CD}$. Which statement is true?
1) $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$
2) $\overleftrightarrow{AB} \perp \overleftrightarrow{CD}$
3) $\overleftrightarrow{AB}$ and $\overleftrightarrow{CD}$ are the same line.
4) $\overleftrightarrow{AB}$ and $\overleftrightarrow{CD}$ intersect, but are not perpendicular.

19 Which set of equations represents two circles that have the same center?
1) $x^2 + (y + 4)^2 = 16$ and $(x + 4)^2 + y^2 = 16$
2) $(x + 3)^2 + (y - 3)^2 = 16$ and $(x - 3)^2 + (y + 3)^2 = 25$
3) $(x - 7)^2 + (y - 2)^2 = 16$ and $(x + 7)^2 + (y + 2)^2 = 25$
4) $(x - 2)^2 + (y - 5)^2 = 16$ and $(x - 2)^2 + (y - 5)^2 = 25$

4

20 Transversal $\overleftrightarrow{EF}$ intersects $\overleftrightarrow{AB}$ and $\overleftrightarrow{CD}$, as shown in the diagram below.

Which statement could always be used to prove $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$?

1) $\angle 2 \cong \angle 4$
2) $\angle 7 \cong \angle 8$
3) $\angle 3$ and $\angle 6$ are supplementary
4) $\angle 1$ and $\angle 5$ are supplementary

21 In $\triangle ABC$, $m\angle A = 60$, $m\angle B = 80$, and $m\angle C = 40$. Which inequality is true?

1) $AB > BC$
2) $AC > BC$
3) $AC < BA$
4) $BC < BA$

22 Circle O with $\angle AOC$ and $\angle ABC$ is shown in the diagram below.

What is the ratio of $m\angle AOC$ to $m\angle ABC$?

1) $1:1$
2) $2:1$
3) $3:1$
4) $1:2$

23 A rectangular prism has a base with a length of 25, a width of 9, and a height of 12. A second prism has a square base with a side of 15. If the volumes of the two prisms are equal, what is the height of the second prism?

1) 6
2) 8
3) 12
4) 15

24 In triangles ABC and DEF, $AB = 4$, $AC = 5$, $DE = 8$, $DF = 10$, and $\angle A \cong \angle D$. Which method could be used to prove $\triangle ABC \sim \triangle DEF$?

1) AA
2) SAS
3) SSS
4) ASA

5

25 Which graph represents a circle whose equation is $x^2 + (y-1)^2 = 9$?

1)

2)

3)

4)

26 What is the perimeter of a rhombus whose diagonals are 16 and 30?
1) 92
2) 68
3) 60
4) 17

27 In right triangle ABC shown in the diagram below, altitude $\overline{BD}$ is drawn to hypotenuse $\overline{AC}$, $CD = 12$, and $AD = 3$.

What is the length of $\overline{AB}$?
1) $5\sqrt{3}$
2) 6
3) $3\sqrt{5}$
4) 9

28 Secants $\overline{JKL}$ and $\overline{JMN}$ are drawn to circle O from an external point, J. If $JK = 8$, $LK = 4$, and $JM = 6$, what is the length of $\overline{JN}$?
1) 16
2) 12
3) 10
4) 8

29 A right circular cylinder has a height of 7 inches and the base has a diameter of 6 inches. Determine the lateral area, in square inches, of the cylinder in terms of π.

30 Determine, in degrees, the measure of each interior angle of a regular octagon.

31 Triangle ABC has vertices at $A(3,0)$, $B(9,-5)$, and $C(7,-8)$. Find the length of $\overline{AC}$ in simplest radical form.

32 On the ray drawn below, using a compass and straightedge, construct an equilateral triangle with a vertex at R. The length of a side of the triangle must be equal to a length of the diagonal of rectangle $ABCD$.

33 On the set of axes below, graph the locus of points 4 units from the x-axis and equidistant from the points whose coordinates are $(-2,0)$ and $(8,0)$.
Mark with an **X** all points that satisfy *both* conditions.

34 The coordinates of two vertices of square $ABCD$ are $A(2,1)$ and $B(4,4)$. Determine the slope of side $\overline{BC}$.

35 The coordinates of the vertices of parallelogram
$SWAN$ are $S(2, -2)$, $W(-2, -4)$, $A(-4, 6)$, and $N(0, 8)$.
State and label the coordinates of parallelogram
$S''W''A''N''$, the image of $SWAN$ after the
transformation $T_{4,-2} \circ D_{\frac{1}{2}}$. [The use of the set of

axes below is optional.]

36 In circle O shown below, chords $\overline{AB}$ and $\overline{CD}$ and
radius $\overline{OA}$ are drawn, such that $\overline{AB} \cong \overline{CD}$,
$\overline{OE} \perp \overline{AB}$, $\overline{OF} \perp \overline{CD}$, $OF = 16$, $CF = y + 10$, and
$CD = 4y - 20$.

Determine the length of $\overline{DF}$. Determine the length
of $\overline{OA}$.

37 If $\triangle RST \sim \triangle ABC$, $m\angle A = x^2 - 8x$, $m\angle C = 4x - 5$,
and $m\angle R = 5x + 30$, find $m\angle C$. [Only an algebraic
solution can receive full credit.]

38 In the diagram of $\triangle MAH$ below, $\overline{MH} \cong \overline{AH}$ and
medians $\overline{AB}$ and $\overline{MT}$ are drawn.
Prove: $\angle MBA \cong \angle ATM$

8

0813ge

1 Given: $\triangle ABD$, $\overline{BC}$ is the perpendicular bisector of $\overline{AD}$

Which statement can *not* always be proven?
1) $\overline{AC} \cong \overline{DC}$
2) $\overline{BC} \cong \overline{CD}$
3) $\angle ACB \cong \angle DCB$
4) $\triangle ABC \cong \triangle DBC$

2 In the diagram of circle O below, chord $\overline{CD}$ is parallel to diameter $\overline{AOB}$ and $\text{m}\overarc{CD} = 110$.

What is $\text{m}\overarc{DB}$?
1) 35
2) 55
3) 70
4) 110

3 Given the statement: One is a prime number.
What is the negation and the truth value of the negation?
1) One is not a prime number; true
2) One is not a prime number; false
3) One is a composite number; true
4) One is a composite number; false

4 Triangle ABC has the coordinates $A(1,2)$, $B(5,2)$, and $C(5,5)$. Triangle ABC is rotated 180° about the origin to form triangle $A'B'C'$. Triangle $A'B'C'$ is
1) acute
2) isosceles
3) obtuse
4) right

5 What is an equation of the circle with center $(-5,4)$ and a radius of 7?
1) $(x-5)^2 + (y+4)^2 = 14$
2) $(x-5)^2 + (y+4)^2 = 49$
3) $(x+5)^2 + (y-4)^2 = 14$
4) $(x+5)^2 + (y-4)^2 = 49$

6 In $\triangle ABC$, $\angle A \cong \angle B$ and $\angle C$ is an obtuse angle. Which statement is true?
1) $\overline{AC} \cong \overline{AB}$ and $\overline{BC}$ is the longest side.
2) $\overline{AC} \cong \overline{BC}$ and $\overline{AB}$ is the longest side.
3) $\overline{AC} \cong \overline{AB}$ and $\overline{BC}$ is the shortest side.
4) $\overline{AC} \cong \overline{BC}$ and $\overline{AB}$ is the shortest side.

7 In the diagram of $\triangle ABC$ below, medians $\overline{AD}$ and $\overline{BE}$ intersect at point F.

If $AF = 6$, what is the length of $\overline{FD}$?
1) 6
2) 2
3) 3
4) 9

8 In circle O, diameter $\overline{AB}$ intersects chord $\overline{CD}$ at E. If $CE = ED$, then $\angle CEA$ is which type of angle?
1) straight
2) obtuse
3) acute
4) right

1

9 If $\triangle ABC \cong \triangle JKL \cong \triangle RST$, then $\overline{BC}$ must be congruent to
1) $\overline{JL}$
2) $\overline{JK}$
3) $\overline{ST}$
4) $\overline{RS}$

10 In the diagram of $\triangle ABC$ below, $\overline{AB}$ is extended to point D.

If $m\angle CAB = x + 40$, $m\angle ACB = 3x + 10$, $m\angle CBD = 6x$, what is $m\angle CAB$?
1) 13
2) 25
3) 53
4) 65

11 The bases of a right triangular prism are $\triangle ABC$ and $\triangle DEF$. Angles A and D are right angles, $AB = 6$, $AC = 8$, and $AD = 12$. What is the length of edge $\overline{BE}$?
1) 10
2) 12
3) 14
4) 16
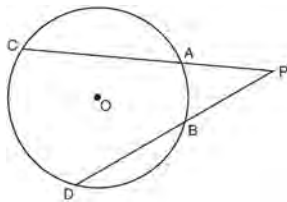
12 What is the equation of circle O shown in the diagram below?

1) $(x + 4)^2 + (y - 1)^2 = 3$
2) $(x - 4)^2 + (y + 1)^2 = 3$
3) $(x + 4)^2 + (y - 1)^2 = 9$
4) $(x - 4)^2 + (y + 1)^2 = 9$

13 The diagram below shows the construction of line m, parallel to line ℓ, through point P.

Which theorem was used to justify this construction?
1) If two lines are cut by a transversal and the alternate interior angles are congruent, the lines are parallel.
2) If two lines are cut by a transversal and the interior angles on the same side are supplementary, the lines are parallel.
3) If two lines are perpendicular to the same line, they are parallel.
4) If two lines are cut by a transversal and the corresponding angles are congruent, they are parallel.

14 The lateral area of a right circular cone is equal to 120π cm^2. If the base of the cone has a diameter of 24 cm, what is the length of the slant height, in centimeters?
1) 2.5
2) 5
3) 10
4) 15.7

15 A student wrote the following equations:
$$3y + 6 = 2x$$
$$2y - 3x = 6$$
The lines represented by these equations are
1) parallel
2) the same line
3) perpendicular
4) intersecting, but *not* perpendicular

16 In a coordinate plane, the locus of points 5 units from the *x*-axis is the
1) lines $x = 5$ and $x = -5$
2) lines $y = 5$ and $y = -5$
3) line $x = 5$, only
4) line $y = 5$, only

17 The sides of a triangle are 8, 12, and 15. The longest side of a similar triangle is 18. What is the ratio of the perimeter of the smaller triangle to the perimeter of the larger triangle?
1) 2:3
2) 4:9
3) 5:6
4) 25:36

18 Lines *m* and *n* are in plane $\mathcal{A}$. What is the converse of the statement "If lines *m* and *n* are parallel, then lines *m* and *n* do not intersect"?
1) If lines *m* and *n* are not parallel, then lines *m* and *n* intersect.
2) If lines *m* and *n* are not parallel, then lines *m* and *n* do not intersect
3) If lines *m* and *n* intersect, then lines *m* and *n* are not parallel.
4) If lines *m* and *n* do not intersect, then lines *m* and *n* are parallel.

19 When the system of equations $y + 2 = (x - 4)^2$ and $2x + y - 6 = 0$ is solved graphically, the solution is
1) $(-4, -2)$ and $(-2, 2)$
2) $(4, -2)$ and $(2, 2)$
3) $(-4, 2)$ and $(-6, 6)$
4) $(4, 2)$ and $(6, 6)$

20 In the diagram of $\triangle UVW$ below, *A* is the midpoint of $\overline{UV}$, *B* is the midpoint of $\overline{UW}$, *C* is the midpoint of $\overline{VW}$, and $\overline{AB}$ and $\overline{AC}$ are drawn.

If $VW = 7x - 3$ and $AB = 3x + 1$, what is the length of $\overline{VC}$?
1) 5
2) 13
3) 16
4) 32

21 Two prisms have equal heights and equal volumes. The base of one is a pentagon and the base of the other is a square. If the area of the pentagonal base is 36 square inches, how many inches are in the length of each side of the square base?
1) 6
2) 9
3) 24
4) 36

22 What is the difference between the sum of the measures of the interior angles of a regular pentagon and the sum of the measures of the exterior angles of a regular pentagon?
1) 36
2) 72
3) 108
4) 180

3

23 If line ℓ is perpendicular to distinct planes $\mathcal{P}$ and Q, then planes $\mathcal{P}$ and Q
   1) are parallel
   2) contain line ℓ
   3) are perpendicular
   4) intersect, but are *not* perpendicular

24 Which graph represents a circle whose equation is $x^2 + (y-2)^2 = 4$?

1)

2)

3)

4)

25 In the diagram below, $\overline{AC}$ and $\overline{AD}$ are tangent to circle B at points C and D, respectively, and $\overline{BC}$, $\overline{BD}$, and $\overline{BA}$ are drawn.

If $AC = 12$ and $AB = 15$, what is the length of $\overline{BD}$?
   1) 5.5
   2) 9
   3) 12
   4) 18

26 Triangle ABC shown below is a right triangle with altitude $\overline{AD}$ drawn to the hypotenuse $\overline{BC}$.

If $BD = 2$ and $DC = 10$, what is the length of $\overline{AB}$?
   1) $2\sqrt{2}$
   2) $2\sqrt{5}$
   3) $2\sqrt{6}$
   4) $2\sqrt{30}$

27 Triangle ABC has vertices $A(0,0)$, $B(6,8)$, and $C(8,4)$. Which equation represents the perpendicular bisector of $\overline{BC}$?
   1) $y = 2x - 6$
   2) $y = -2x + 4$
   3) $y = \frac{1}{2}x + \frac{5}{2}$
   4) $y = -\frac{1}{2}x + \frac{19}{2}$

4

28 Chords $\overline{AB}$ and $\overline{CD}$ intersect at point E in a circle with center at O. If $AE = 8$, $AB = 20$, and $DE = 16$, what is the length of $\overline{CE}$?
1) 6
2) 9
3) 10
4) 12

29 Triangle ABC has vertices $A(6,6)$, $B(9,0)$, and $C(3,-3)$. State and label the coordinates of $\triangle A'B'C'$, the image of $\triangle ABC$ after a dilation of $D_{\frac{1}{3}}$.

30 Using a compass and straightedge, construct the bisector of $\angle MJH$. [Leave all construction marks.]

31 Find, in simplest radical form, the length of the line segment with endpoints whose coordinates are $(-1,4)$ and $(3,-2)$.

32 In $\triangle ABC$, the measure of angle A is fifteen less than twice the measure of angle B. The measure of angle C equals the sum of the measures of angle A and angle B. Determine the measure of angle B.

33 A circle has the equation $(x-3)^2 + (y+4)^2 = 10$. Find the coordinates of the center of the circle and the length of the circle's radius.

34 Two intersecting lines are shown in the diagram below. Sketch the locus of points that are equidistant from the two lines. Sketch the locus of points that are a given distance, d, from the point of intersection of the given lines. State the number of points that satisfy both conditions.

35 Given: $\triangle ABC$, $\overline{BD}$ bisects $\angle ABC$, $\overline{BD} \perp \overline{AC}$
Prove: $\overline{AB} \cong \overline{CB}$

5

36 Quadrilateral *MATH* has coordinates $M(-6,-3)$, $A(-1,-3)$, $T(-2,-1)$, and $H(-4,-1)$. The image of quadrilateral *MATH* after the composition $r_{x\text{-axis}} \circ T_{7,5}$ is quadrilateral $M''A''T''H''$. State and label the coordinates of $M''A''T''H''$. [The use of the set of axes below is optional.]

38 Quadrilateral *ABCD* with vertices $A(-7,4)$, $B(-3,6)$, $C(3,0)$, and $D(1,-8)$ is graphed on the set of axes below. Quadrilateral *MNPQ* is formed by joining M, N, P, and Q, the midpoints of $\overline{AB}$, $\overline{BC}$, $\overline{CD}$, and $\overline{AD}$, respectively. Prove that quadrilateral *MNPQ* is a parallelogram. Prove that quadrilateral *MNPQ* is *not* a rhombus.

37 Trapezoid *TRAP*, with median $\overline{MQ}$, is shown in the diagram below. Solve algebraically for x and y.

6

0114ge

1 The midpoint of $\overline{AB}$ is $M(4, 2)$. If the coordinates of A are $(6, -4)$, what are the coordinates of B?
1) $(1, -3)$
2) $(2, 8)$
3) $(5, -1)$
4) $(14, 0)$

2 Which diagram shows the construction of a 45° angle?

1)

2)

3)

4)

3 What are the coordinates of the center and the length of the radius of the circle whose equation is $(x + 1)^2 + (y - 5)^2 = 16$?
1) $(1, -5)$ and 16
2) $(-1, 5)$ and 16
3) $(1, -5)$ and 4
4) $(-1, 5)$ and 4

4 If distinct planes $\mathcal{R}$ and $\mathcal{S}$ are both perpendicular to line ℓ, which statement must always be true?
1) Plane $\mathcal{R}$ is parallel to plane $\mathcal{S}$.
2) Plane $\mathcal{R}$ is perpendicular to plane $\mathcal{S}$.
3) Planes $\mathcal{R}$ and $\mathcal{S}$ and line ℓ are all parallel.
4) The intersection of planes $\mathcal{R}$ and $\mathcal{S}$ is perpendicular to line ℓ.

5 If $\triangle ABC$ and its image, $\triangle A'B'C'$, are graphed on a set of axes, $\triangle ABC \cong \triangle A'B'C'$ under each transformation *except*
1) D_2
2) $R_{90°}$
3) $r_{y = x}$
4) $T_{(-2, 3)}$

1

6 A rectangular right prism is shown in the diagram below.

Which pair of edges are *not* coplanar?
1) $\overline{BF}$ and $\overline{CG}$
2) $\overline{BF}$ and $\overline{DH}$
3) $\overline{EF}$ and $\overline{CD}$
4) $\overline{EF}$ and $\overline{BC}$

7 How many points in the coordinate plane are 3 units from the origin and also equidistant from both the *x*-axis and the *y*-axis?
1) 1
2) 2
3) 8
4) 4

8 As shown below, the medians of $\triangle ABC$ intersect at *D*.

If the length of $\overline{BE}$ is 12, what is the length of $\overline{BD}$?
1) 8
2) 9
3) 3
4) 4

9 The solution of the system of equations $y = x^2 - 2$ and $y = x$ is
1) $(1, 1)$ and $(-2, -2)$
2) $(2, 2)$ and $(-1, -1)$
3) $(1, 1)$ and $(2, 2)$
4) $(-2, -2)$ and $(-1, -1)$

10 Line ℓ passes through the point $(5, 3)$ and is parallel to line *k* whose equation is $5x + y = 6$. An equation of line ℓ is
1) $y = \dfrac{1}{5}x + 2$
2) $y = -5x + 28$
3) $y = \dfrac{1}{5}x - 2$
4) $y = -5x - 28$

11 In the diagram below of quadrilateral *ABCD*, *E* and *F* are points on $\overline{AB}$ and $\overline{CD}$, respectively, $\overline{BE} \cong \overline{DF}$, and $\overline{AE} \cong \overline{CF}$.

Which conclusion can be proven?
1) $\overline{ED} \cong \overline{FB}$
2) $\overline{AB} \cong \overline{CD}$
3) $\angle A \cong \angle C$
4) $\angle AED \cong \angle CFB$

2

12 In the diagram below, four pairs of triangles are shown. Congruent corresponding parts are labeled in each pair.

Using only the information given in the diagrams, which pair of triangles can *not* be proven congruent?
1) A
2) B
3) C
4) D

13 In △ABC shown below, L is the midpoint of $\overline{BC}$, M is the midpoint of $\overline{AB}$, and N is the midpoint of $\overline{AC}$.

If MN = 8, ML = 5, and NL = 6, the perimeter of trapezoid BMNC is
1) 35
2) 31
3) 28
4) 26

14 In the diagram below, $\overleftrightarrow{RCBT}$ and △ABC are shown with m∠A = 60 and m∠ABT = 125.

What is m∠ACR?
1) 125
2) 115
3) 65
4) 55

15 Which equation represents circle O shown in the graph below?

1) $x^2 + (y-2)^2 = 10$
2) $x^2 + (y+2)^2 = 10$
3) $x^2 + (y-2)^2 = 25$
4) $x^2 + (y+2)^2 = 25$

16 For which measures of the sides of △ABC is angle B the largest angle of the triangle?
1) AB = 2, BC = 6, AC = 7
2) AB = 6, BC = 12, AC = 8
3) AB = 16, BC = 9, AC = 10
4) AB = 18, BC = 14, AC = 5

3

17 What is the measure of the largest exterior angle that any regular polygon can have?
1) 60°
2) 90°
3) 120°
4) 360°

18 As shown in the diagram below, a landscaper uses a cylindrical lawn roller on a lawn. The roller has a radius of 9 inches and a width of 42 inches.

To the *nearest square inch*, the area the roller covers in one complete rotation is
1) 2,374
2) 2,375
3) 10,682
4) 10,688

19 In the diagram below, $\overline{AC}$ and $\overline{BC}$ are tangent to circle O at A and B, respectively, from external point C.

If m$\angle ACB = 38$, what is m$\angle AOB$?
1) 71
2) 104
3) 142
4) 161

20 What is the perimeter of a square whose diagonal is $3\sqrt{2}$?
1) 18
2) 12
3) 9
4) 6

21 The coordinates of point P are $(7, 1)$. What are the coordinates of the image of P after $R_{90°}$ about the origin?
1) $(1, 7)$
2) $(-7, -1)$
3) $(1, -7)$
4) $(-1, 7)$

22 Lines p and q are intersected by line r, as shown below.

If m$\angle 1 = 7x - 36$ and m$\angle 2 = 5x + 12$, for which value of x would $p \parallel q$?
1) 17
2) 24
3) 83
4) 97

23 What is the equation of the circle with its center at $(-1, 2)$ and that passes through the point $(1, 2)$?
1) $(x + 1)^2 + (y - 2)^2 = 4$
2) $(x - 1)^2 + (y + 2)^2 = 4$
3) $(x + 1)^2 + (y - 2)^2 = 2$
4) $(x - 1)^2 + (y + 2)^2 = 2$

4

24 In the diagram below, diameter $\overline{AB}$ bisects chord $\overline{CD}$ at point E in circle F.

If $AE = 2$ and $FB = 17$, then the length of $\overline{CE}$ is
1) 7
2) 8
3) 15
4) 16

25 Which quadrilateral does *not* always have congruent diagonals?
1) isosceles trapezoid
2) rectangle
3) rhombus
4) square

26 A circle with the equation $(x + 6)^2 + (y - 7)^2 = 64$ does *not* include points in Quadrant
1) I
2) II
3) III
4) IV

27 Trapezoid *QRST* is graphed on the set of axes below.

Under which transformation will there be *no* invariant points?
1) $r_{y=0}$
2) $r_{x=0}$
3) $r_{(0,0)}$
4) $r_{y=x}$

28 How many common tangent lines can be drawn to the circles shown below?

1) 1
2) 2
3) 3
4) 4

29 The diameter of a sphere is 5 inches. Determine and state the surface area of the sphere, to the *nearest hundredth of a square inch*.

5

30 Using a compass and straightedge, construct the perpendicular bisector of $\overline{AB}$. [Leave all construction marks.]

31 The endpoints of $\overline{AB}$ are $A(3,-4)$ and $B(7,2)$.

Determine and state the length of $\overline{AB}$ in simplest radical form.

32 A right prism has a square base with an area of 12 square meters. The volume of the prism is 84 cubic meters. Determine and state the height of the prism, in meters.

33 State whether the lines represented by the equations $y = \frac{1}{2}x - 1$ and $y + 4 = -\frac{1}{2}(x - 2)$ are parallel, perpendicular, or neither. Explain your answer.

34 A tree, T, is 6 meters from a row of corn, c, as represented in the diagram below. A farmer wants to place a scarecrow 2 meters from the row of corn and also 5 meters from the tree. Sketch both loci. Indicate, with an **X**, all possible locations for the scarecrow.

35 In the diagram of $\triangle BCD$ shown below, $\overline{BA}$ is drawn from vertex B to point A on $\overline{DC}$, such that $\overline{BC} \cong \overline{BA}$.

In $\triangle DAB$, m$\angle D = x$, m$\angle DAB = 5x - 30$, and m$\angle DBA = 3x - 60$. In $\triangle ABC$, $AB = 6y - 8$ and $BC = 4y - 2$. [Only algebraic solutions can receive full credit.] Find m$\angle D$. Find m$\angle BAC$. Find the length of $\overline{BC}$. Find the length of $\overline{DC}$.

36 The coordinates of the vertices of △ABC are A(−6, 5), B(−4, 8), and C(1, 6). State and label the coordinates of the vertices of △A″B″C″, the image of △ABC after the composition of transformations $T_{(−4, 5)} \circ r_{y\text{-axis}}$. [The use of the set of axes below is optional.]

37 In right triangle ABC below, $\overline{CD}$ is the altitude to hypotenuse $\overline{AB}$. If CD = 6 and the ratio of AD to AB is 1:5, determine and state the length of $\overline{BD}$. [Only an algebraic solution can receive full credit.]

38 In the diagram of circle O below, diameter $\overline{RS}$, chord $\overrightarrow{AS}$, tangent $\overrightarrow{TS}$, and secant $\overline{TAR}$ are drawn.

Complete the following proof to show $(RS)^2 = RA \cdot RT$

Statements	Reasons
1. circle O, diameter $\overline{RS}$, chord $\overline{AS}$, tangent $\overrightarrow{TS}$, and secant $\overline{TAR}$	1. Given
2. $\overline{RS} \perp \overrightarrow{TS}$	2. _____
3. ∠RST is a right angle	3. ⊥ lines form right angles
4. ∠RAS is a right angle	4. _____
5. ∠RST ≅ ∠RAS	5. _____
6. ∠R ≅ ∠R	6. Reflexive property
7. △RST ~ △RAS	7. _____
8. $\frac{RS}{RA} = \frac{RT}{RS}$	8. _____
9. $(RS)^2 = RA \cdot RT$	9. _____

fall08ge
Answer Section

1 ANS: 3
The diagonals of an isosceles trapezoid are congruent. $5x + 3 = 11x - 5$.

$$6x = 18$$
$$x = 3$$

   PTS: 2   REF: fall0801ge   STA: G.G.40   TOP: Trapezoids
2 ANS: 4   PTS: 2   REF: fall0802ge   STA: G.G.24
   TOP: Negations
3 ANS: 1
$(x, y) \rightarrow (x + 3, y + 1)$

   PTS: 2   REF: fall0803ge   STA: G.G.54   TOP: Translations
4 ANS: 3   PTS: 2   REF: fall0804ge   STA: G.G.18
   TOP: Constructions
5 ANS: 3

   PTS: 2   REF: fall0805ge   STA: G.G.70   TOP: Quadratic-Linear Systems
6 ANS: 2   PTS: 2   REF: fall0806ge   STA: G.G.9
   TOP: Planes
7 ANS: 1   PTS: 2   REF: fall0807ge   STA: G.G.19
   TOP: Constructions
8 ANS: 3
The lateral edges of a prism are parallel.

   PTS: 2   REF: fall0808ge   STA: G.G.10   TOP: Solids
9 ANS: 1
Since $\overline{AC} \cong \overline{BC}$, m$\angle A$ = m$\angle B$ under the Isosceles Triangle Theorem.

   PTS: 2   REF: fall0809ge   STA: G.G.69   TOP: Triangles in the Coordinate Plane
10 ANS: 4
Median $\overline{BF}$ bisects $\overline{AC}$ so that $\overline{CF} \cong \overline{FA}$.

   PTS: 2   REF: fall0810ge   STA: G.G.24   TOP: Statements
11 ANS: 3
Because $\overline{OC}$ is a radius, its length is 5. Since $CE = 2$ $OE = 3$. ΔEDO is a 3-4-5 triangle. If $ED = 4$, $BD = 8$.

   PTS: 2   REF: fall0811ge   STA: G.G.49   TOP: Chords

12   ANS: 2

The slope of a line in standard form is $-\dfrac{A}{B}$, so the slope of this line is $\dfrac{-2}{-1} = 2$. A parallel line would also have a slope of 2. Since the answers are in slope intercept form, find the y-intercept: $y = mx + b$

$$-11 = 2(-3) + b$$
$$-5 = b$$

   PTS: 2   REF: fall0812ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

13   ANS: 2

$M_x = \dfrac{2 + (-4)}{2} = -1.\ M_Y = \dfrac{-3 + 6}{2} = \dfrac{3}{2}.$

   PTS: 2   REF: fall0813ge   STA: G.G.66   TOP: Midpoint

14   ANS: 3   PTS: 2   REF: fall0814ge   STA: G.G.73
   TOP: Equations of Circles

15   ANS: 1

$3x^2 + 18x + 24$

$3(x^2 + 6x + 8)$

$3(x + 4)(x + 2)$

   PTS: 2   REF: fall0815ge   STA: G.G.12   TOP: Volume

16   ANS: 3   PTS: 2   REF: fall0816ge   STA: G.G.1
   TOP: Planes

17   ANS: 2

$$x^2 = 3(x + 18)$$
$$x^2 - 3x - 54 = 0$$
$$(x - 9)(x + 6) = 0$$
$$x = 9$$

   PTS: 2   REF: fall0817ge   STA: G.G.53   TOP: Segments Intercepted by Circle
   KEY: tangent and secant

18   ANS: 4   PTS: 2   REF: fall0818ge   STA: G.G.61
   TOP: Analytical Representations of Transformations

19   ANS: 2
   $7 + 18 > 6 + 12$

   PTS: 2   REF: fall0819ge   STA: G.G.33   TOP: Triangle Inequality Theorem

20   ANS: 1

$M_x = \dfrac{-2 + 6}{2} = 2.\ M_y = \dfrac{3 + 3}{2} = 3.$ The center is $(2, 3)$. $d = \sqrt{(-2 - 6)^2 + (3 - 3)^2} = \sqrt{64 + 0} = 8.$ If the diameter is 8, the radius is 4 and $r^2 = 16$.

   PTS: 2   REF: fall0820ge   STA: G.G.71   TOP: Equations of Circles

21 ANS: 1
$\triangle PRT$ and $\triangle SRQ$ share $\angle R$ and it is given that $\angle RPT \cong \angle RSQ$.

PTS: 2   REF: fall0821ge   STA: G.G.44   TOP: Similarity Proofs

22 ANS: 4
$3y + 1 = 6x + 4$. $2y + 1 = x - 9$

$\quad 3y = 6x + 3$ $\quad 2y = x - 10$

$\quad y = 2x + 1$ $\quad y = \dfrac{1}{2}x - 5$

PTS: 2   REF: fall0822ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

23 ANS: 1
After the translation, the coordinates are $A'(-1, 5)$ and $B'(3, 4)$. After the dilation, the coordinates are $A''(-2, 10)$ and $B''(6, 8)$.

PTS: 2   REF: fall0823ge   STA: G.G.58   TOP: Compositions of Transformations

24 ANS: 4   PTS: 2   REF: fall0824ge   STA: G.G.50
TOP: Tangents   KEY: common tangency

25 ANS: 3   PTS: 2   REF: fall0825ge   STA: G.G.21
TOP: Centroid, Orthocenter, Incenter and Circumcenter

26 ANS: 4
Corresponding angles of similar triangles are congruent.

PTS: 2   REF: fall0826ge   STA: G.G.45   TOP: Similarity
KEY: perimeter and area

27 ANS: 4
$(n - 2)180 = (8 - 2)180 = 1080$. $\dfrac{1080}{8} = 135$.

PTS: 2   REF: fall0827ge   STA: G.G.37   TOP: Interior and Exterior Angles of Polygons

28 ANS: 2
The slope of a line in standard form is $-\dfrac{A}{B}$ so the slope of this line is $-\dfrac{5}{3}$ Perpendicular lines have slope that are the opposite and reciprocal of each other.

PTS: 2   REF: fall0828ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines

29 ANS:
$2\sqrt{3}$. $x^2 = 3 \cdot 4$

$\quad x = \sqrt{12} = 2\sqrt{3}$

PTS: 2   REF: fall0829ge   STA: G.G.47   TOP: Similarity
KEY: altitude

30 ANS:

Translation

PTS: 2   REF: fall0830ge   STA: G.G.55   TOP: Properties of Transformations

31 ANS:

$25. d = \sqrt{(-3-4)^2 + (1-25)^2} = \sqrt{49+576} = \sqrt{625} = 25.$

PTS: 2   REF: fall0831ge   STA: G.G.67   TOP: Distance

32 ANS:

PTS: 2   REF: fall0832ge   STA: G.G.17   TOP: Constructions

33 ANS:

22.4.

$$V = \pi r^2 h$$

$$12566.4 = \pi r^2 \cdot 8$$

$$r^2 = \frac{12566.4}{8\pi}$$

$$r \approx 22.4$$

PTS: 2   REF: fall0833ge   STA: G.G.14   TOP: Volume and Lateral Area

34 ANS:

Contrapositive-If two angles of a triangle are not congruent, the sides opposite those angles are not congruent.

PTS: 2   REF: fall0834ge   STA: G.G.26   TOP: Conditional Statements

35 ANS:

PTS: 4   REF: fall0835ge   STA: G.G.42   TOP: Midsegments

36 ANS:

$\angle D$, $\angle G$ and 24° or $\angle E$, $\angle F$ and 84°. $\text{m}\overset{\frown}{FE} = \dfrac{2}{15} \times 360 = 48$. Since the chords forming $\angle D$ and $\angle G$ are intercepted by $\overset{\frown}{FE}$, their measure is 24°. $\text{m}\overset{\frown}{GD} = \dfrac{7}{15} \times 360 = 168$. Since the chords forming $\angle E$ and $\angle F$ are intercepted by $\overset{\frown}{GD}$, their measure is 84°.

PTS: 4   REF: fall0836ge   STA: G.G.51   TOP: Arcs Determined by Angles
KEY: inscribed

37 ANS:

PTS: 4   REF: fall0837ge   STA: G.G.23   TOP: Locus

38 ANS:

Because $\overline{AB} \parallel \overline{DC}$, $\overset{\frown}{AD} \cong \overset{\frown}{BC}$ since parallel chords intersect congruent arcs. $\angle BDC \cong \angle ACD$ because inscribed angles that intercept congruent arcs are congruent. $\overline{AD} \cong \overline{BC}$ since congruent chords intersect congruent arcs. $\angle DAC \cong \angle DBC$ because inscribed angles that intercept the same arc are congruent. Therefore, $\triangle ACD \cong \triangle BDC$ because of AAS.

PTS: 6   REF: fall0838ge   STA: G.G.27   TOP: Circle Proofs

0609ge
Answer Section

1 ANS: 1
If $\angle A$ is at minimum (50°) and $\angle B$ is at minimum (90°), $\angle C$ is at maximum of 40° (180° - (50° + 90°)). If $\angle A$ is at maximum (60°) and $\angle B$ is at maximum (100°), $\angle C$ is at minimum of 20° (180° - (60° + 100°)).

PTS: 2   REF: 060901ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

2 ANS: 3

PTS: 2   REF: 060902ge   STA: G.G.28   TOP: Triangle Congruency

3 ANS: 1   PTS: 2   REF: 060903ge   STA: G.G.56
TOP: Identifying Transformations

4 ANS: 4   PTS: 2   REF: 060904ge   STA: G.G.13
TOP: Solids

5 ANS: 3   PTS: 2   REF: 060905ge   STA: G.G.54
TOP: Reflections   KEY: basic

6 ANS: 2

Parallel chords intercept congruent arcs. $m\overset{\frown}{AD} = m\overset{\frown}{BC} = 60$. $m\angle CDB = \frac{1}{2} m\overset{\frown}{BC} = 30$.

PTS: 2   REF: 060906ge   STA: G.G.52   TOP: Chords

7 ANS: 2

The slope of $y = \frac{1}{2}x + 5$ is $\frac{1}{2}$. The slope of a perpendicular line is –2. $y = mx + b$.

$$5 = (-2)(-2) + b$$
$$b = 1$$

PTS: 2   REF: 060907ge   STA: G.G.64   TOP: Parallel and Perpendicular Lines

8 ANS: 3   PTS: 2   REF: 060908ge   STA: G.G.60
TOP: Identifying Transformations

9 ANS: 1
In an equilateral triangle, each interior angle is 60° and each exterior angle is 120° (180° - 120°). The sum of the three interior angles is 180° and the sum of the three exterior angles is 360°.

PTS: 2   REF: 060909ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

10 ANS: 2   PTS: 2   REF: 060910ge   STA: G.G.71
TOP: Equations of Circles

11 ANS: 2
Longest side of a triangle is opposite the largest angle. Shortest side is opposite the smallest angle.

PTS: 2   REF: 060911ge   STA: G.G.34   TOP: Angle Side Relationship

12 ANS: 4   PTS: 2   REF: 060912ge   STA: G.G.23
    TOP: Locus
13 ANS: 4   PTS: 2   REF: 060913ge   STA: G.G.26
    TOP: Conditional Statements
14 ANS: 2
    The centroid divides each median into segments whose lengths are in the ratio 2 : 1.

    PTS: 2   REF: 060914ge   STA: G.G.43   TOP: Centroid
15 ANS: 1
    $\overline{AB} = 10$ since $\triangle ABC$ is a 6-8-10 triangle. $6^2 = 10x$

    $$3.6 = x$$

    PTS: 2   REF: 060915ge   STA: G.G.47   TOP: Similarity
    KEY: leg
16 ANS: 3
    $4(x + 4) = 8^2$

    $4x + 16 = 64$

    $x = 12$

    PTS: 2   REF: 060916ge   STA: G.G.53   TOP: Segments Intercepted by Circle
    KEY: tangent and secant
17 ANS: 2

    $\angle ACB$ and $\angle ECD$ are congruent vertical angles and $\angle CAB \cong \angle CED$.

    PTS: 2   REF: 060917ge   STA: G.G.44   TOP: Similarity Proofs
18 ANS: 1   PTS: 2   REF: 060918ge   STA: G.G.2
    TOP: Planes
19 ANS: 4
    $M_x = \dfrac{-6 + 1}{2} = -\dfrac{5}{2}. \ M_y = \dfrac{1 + 8}{2} = \dfrac{9}{2}.$

    PTS: 2   REF: 060919ge   STA: G.G.66   TOP: Midpoint
20 ANS: 1   PTS: 2   REF: 060920ge   STA: G.G.74
    TOP: Graphing Circles
21 ANS: 1
    $V = \dfrac{1}{3}\pi r^2 h = \dfrac{1}{3}\pi \cdot 4^2 \cdot 12 \approx 201$

    PTS: 2   REF: 060921ge   STA: G.G.15   TOP: Volume and Lateral Area
22 ANS: 4   PTS: 2   REF: 060922ge   STA: G.G.73
    TOP: Equations of Circles

23 ANS: 1

$y = x^2 - 4x = (4)^2 - 4(4) = 0.$ (4,0) is the only intersection.

PTS: 2   REF: 060923ge   STA: G.G.70   TOP: Quadratic-Linear Systems

24 ANS: 4

(4) is not true if $\angle PQR$ is obtuse.

PTS: 2   REF: 060924ge   STA: G.G.32   TOP: Exterior Angle Theorem

25 ANS: 3   PTS: 2   REF: 060925ge   STA: G.G.17

TOP: Constructions

26 ANS: 2

The slope of $2x + 3y = 12$ is $-\dfrac{A}{B} = -\dfrac{2}{3}$. The slope of a perpendicular line is $\dfrac{3}{2}$. Rewritten in slope intercept form,

(2) becomes $y = \dfrac{3}{2}x + 3$.

PTS: 2   REF: 060926ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

27 ANS: 4

$\triangle ABC \sim \triangle DBE.$ $\dfrac{\overline{AB}}{\overline{DB}} = \dfrac{\overline{AC}}{\overline{DE}}$

$\dfrac{9}{2} = \dfrac{x}{3}$

$x = 13.5$

PTS: 2   REF: 060927ge   STA: G.G.46   TOP: Side Splitter Theorem

28 ANS: 3   PTS: 2   REF: 060928ge   STA: G.G.8

TOP: Planes

29 ANS:

20. The sides of the triangle formed by connecting the midpoints are half the sides of the original triangle.

$5 + 7 + 8 = 20.$

PTS: 2   REF: 060929ge   STA: G.G.42   TOP: Midsegments

30 ANS:

　　PTS: 2　　　　　　　REF: 060930ge　　　STA: G.G.19　　　　TOP: Constructions

31 ANS:

$y = -2x + 14.$ The slope of $2x + y = 3$ is $\dfrac{-A}{B} = \dfrac{-2}{1} = -2.$ $y = mx + b$　　.

$$4 = (-2)(5) + b$$

$$b = 14$$

　　PTS: 2　　　　　　　REF: 060931ge　　　STA: G.G.65　　　　TOP: Parallel and Perpendicular Lines

32 ANS:

　　PTS: 2　　　　　　　REF: 060932ge　　　STA: G.G.22　　　　TOP: Locus

33 ANS:

True. The first statement is true and the second statement is false. In a disjunction, if either statement is true, the disjunction is true.

　　PTS: 2　　　　　　　REF: 060933ge　　　STA: G.G.25　　　　TOP: Compound Statements
　　KEY: disjunction

34 ANS:

20. $5x + 10 = 4x + 30$

$x = 20$

PTS: 2   REF: 060934ge   STA: G.G.45   TOP: Similarity
KEY: basic

35 ANS:

18. If the ratio of *TA* to *AC* is 1:3, the ratio of *TE* to *ES* is also 1:3. $x + 3x = 24$. $3(6) = 18$.

$x = 6$

PTS: 4   REF: 060935ge   STA: G.G.50   TOP: Tangents
KEY: common tangency

36 ANS:

$15 + 5\sqrt{5}$.

PTS: 4   REF: 060936ge   STA: G.G.69   TOP: Triangles in the Coordinate Plane

37 ANS:

PTS: 4   REF: 060937ge   STA: G.G.54   TOP: Compositions of Transformations
KEY: grids

38 ANS:

$\overline{AC} \cong \overline{EC}$ and $\overline{DC} \cong \overline{BC}$ because of the definition of midpoint. $\angle ACB \cong \angle ECD$ because of vertical angles. $\triangle ABC \cong \triangle EDC$ because of SAS. $\angle CDE \cong \angle CBA$ because of CPCTC. $\overline{BD}$ is a transversal intersecting $\overline{AB}$ and

$\overline{ED}$. Therefore $\overline{AB} \parallel \overline{DE}$ because $\angle CDE$ and $\angle CBA$ are congruent alternate interior angles.

PTS: 6   REF: 060938ge   STA: G.G.27   TOP: Triangle Proofs

0809ge
Answer Section

1 ANS: 4
The marked 60º angle and the angle above it are on the same straight line and supplementary. This unmarked supplementary angle is 120º. Because the unmarked 120º angle and the marked 120º angle are alternate exterior angles and congruent, $d \parallel e$.

PTS: 2   REF: 080901ge   STA: G.G.35   TOP: Parallel Lines and Transversals

2 ANS: 3   PTS: 2   REF: 080902ge   STA: G.G.17
TOP: Constructions

3 ANS: 4
$180 - (40 + 40) = 100$

PTS: 2   REF: 080903ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

4 ANS: 2
Parallel chords intercept congruent arcs. $m\overset{\frown}{AC} = m\overset{\frown}{BD} = 30$. $180 - 30 - 30 = 120$.

PTS: 2   REF: 080904ge   STA: G.G.52   TOP: Chords

5 ANS: 4   PTS: 2   REF: 080905ge   STA: G.G.29
TOP: Triangle Congruency

6 ANS: 2
A dilation affects distance, not angle measure.

PTS: 2   REF: 080906ge   STA: G.G.60   TOP: Identifying Transformations

7 ANS: 1
$\angle DCB$ and $\angle ADC$ are supplementary adjacent angles of a parallelogram. $180 - 120 = 60$. $\angle 2 = 60 - 45 = 15$.

PTS: 2   REF: 080907ge   STA: G.G.38   TOP: Parallelograms

8 ANS: 1
Translations and reflections do not affect distance.

PTS: 2   REF: 080908ge   STA: G.G.59   TOP: Properties of Transformations

9 ANS: 3
The slope of $y = x + 2$ is 1. The slope of $y - x = -1$ is $\dfrac{-A}{B} = \dfrac{-(-1)}{1} = 1$.

PTS: 2   REF: 080909ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

10 ANS: 2
$M_x = \dfrac{-2 + 6}{2} = 2$. $M_y = \dfrac{-4 + 2}{2} = -1$

PTS: 2   REF: 080910ge   STA: G.G.66   TOP: Midpoint

11 ANS: 1   PTS: 2   REF: 080911ge   STA: G.G.73
TOP: Equations of Circles

12 ANS: 4

$y + x = 4$. $x^2 - 6x + 10 = -x + 4$. $y + x = 4$. $y + 2 = 4$

$y = -x + 4$ $x^2 - 5x + 6 = 0$ $y + 3 = 4$ $y = 2$

              $(x - 3)(x - 2) = 0$ $y = 1$

                 $x = 3$ or 2

     PTS: 2   REF: 080912ge   STA: G.G.70   TOP: Quadratic-Linear Systems

13 ANS: 3   PTS: 2   REF: 080913ge   STA: G.G.28

     TOP: Triangle Congruency

14 ANS: 4   PTS: 2   REF: 080914ge   STA: G.G.7

     TOP: Planes

15 ANS: 4   PTS: 2   REF: 080915ge   STA: G.G.56

     TOP: Identifying Transformations

16 ANS: 2

     $6 + 17 > 22$

     PTS: 2   REF: 080916ge   STA: G.G.33   TOP: Triangle Inequality Theorem

17 ANS: 4

     The slope of $y = -\frac{2}{3}x - 5$ is $-\frac{2}{3}$. Perpendicular lines have slope that are opposite reciprocals.

     PTS: 2   REF: 080917ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines

18 ANS: 1   PTS: 2   REF: 080918ge   STA: G.G.41

     TOP: Special Quadrilaterals

19 ANS: 1

     $d = \sqrt{(-4 - 2)^2 + (5 - (-5))^2} = \sqrt{36 + 100} = \sqrt{136} = \sqrt{4} \cdot \sqrt{34} = 2\sqrt{34}$.

     PTS: 2   REF: 080919ge   STA: G.G.67   TOP: Distance

20 ANS: 3

     PTS: 2   REF: 080920ge   STA: G.G.42   TOP: Midsegments

21 ANS: 2   PTS: 2   REF: 080921ge   STA: G.G.72

     TOP: Equations of Circles

22 ANS: 4

Let $\overline{AD} = x.$ $36x = 12^2$

$x = 4$

PTS: 2   REF: 080922ge   STA: G.G.47   TOP: Similarity
KEY: leg
23 ANS: 2
$4(4x - 3) = 3(2x + 8)$

$16x - 12 = 6x + 24$

$10x = 36$

$x = 3.6$

PTS: 2   REF: 080923ge   STA: G.G.53   TOP: Segments Intercepted by Circle
KEY: two chords
24 ANS: 3   PTS: 2   REF: 080924ge   STA: G.G.24
TOP: Negations
25 ANS: 4   PTS: 2   REF: 080925ge   STA: G.G.21
TOP: Centroid, Orthocenter, Incenter and Circumcenter
26 ANS: 1

$V = \pi r^2 h$

$1000 = \pi r^2 \cdot 8$

$r^2 = \dfrac{1000}{8\pi}$

$r \approx 6.3$

PTS: 2   REF: 080926ge   STA: G.G.14   TOP: Volume and Lateral Area
27 ANS: 2   PTS: 2   REF: 080927ge   STA: G.G.4
TOP: Planes
28 ANS: 3   PTS: 2   REF: 080928ge   STA: G.G.50
TOP: Tangents   KEY: common tangency
29 ANS:

3. The non-parallel sides of an isosceles trapezoid are congruent. $2x + 5 = 3x + 2$

$x = 3$

PTS: 2   REF: 080929ge   STA: G.G.40   TOP: Trapezoids
30 ANS:

2016. $V = \dfrac{1}{3} Bh = \dfrac{1}{3} s^2 h = \dfrac{1}{3} 12^2 \cdot 42 = 2016$

PTS: 2   REF: 080930ge   STA: G.G.13   TOP: Volume

31 ANS:

$y = \frac{2}{3}x - 9$. The slope of $2x - 3y = 11$ is $-\frac{A}{B} = \frac{-2}{-3} = \frac{2}{3}$. $-5 = \left(\frac{2}{3}\right)(6) + b$

$$-5 = 4 + b$$
$$b = -9$$

PTS: 2   REF: 080931ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

32 ANS:

PTS: 2   REF: 080932ge   STA: G.G.17   TOP: Constructions

33 ANS:

26. $x + 3x + 5x - 54 = 180$

$$9x = 234$$
$$x = 26$$

PTS: 2   REF: 080933ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

34 ANS:

$\overline{AC}$. $m\angle BCA = 63$ and $m\angle ABC = 80$. $\overline{AC}$ is the longest side as it is opposite the largest angle.

PTS: 2   REF: 080934ge   STA: G.G.34   TOP: Angle Side Relationship

35 ANS:

$y = \frac{4}{3}x - 6$. $M_x = \frac{-1+7}{2} = 3$ The perpendicular bisector goes through $(3, -2)$ and has a slope of $\frac{4}{3}$.

$$M_y = \frac{1 + (-5)}{2} = -2$$

$$m = \frac{1 - (-5)}{-1 - 7} = -\frac{3}{4}$$

$y - y_M = m(x - x_M)$.

$y - 1 = \frac{4}{3}(x - 2)$

PTS: 4   REF: 080935ge   STA: G.G.68   TOP: Perpendicular Bisector

36 ANS:

PTS: 4   REF: 080936ge   STA: G.G.23   TOP: Locus

37 ANS:

$D'(-1, 1)$, $E'(-1, 5)$, $G'(-4, 5)$

PTS: 4   REF: 080937ge   STA: G.G.55   TOP: Properties of Transformations

38 ANS:

$\overline{FE} \cong \overline{FE}$ (Reflexive Property); $\overline{AE} - \overline{FE} \cong \overline{FC} - \overline{EF}$ (Line Segment Subtraction Theorem); $\overline{AF} \cong \overline{CE}$ (Substitution); $\angle BFA \cong \angle DEC$ (All right angles are congruent); $\Delta BFA \cong \Delta DEC$ (AAS); $\overline{AB} \cong \overline{CD}$ and $\overline{BF} \cong \overline{DE}$ (CPCTC); $\angle BFC \cong \angle DEA$ (All right angles are congruent); $\Delta BFC \cong \Delta DEA$ (SAS); $\overline{AD} \cong \overline{CB}$ (CPCTC); *ABCD* is a parallelogram (opposite sides of quadrilateral *ABCD* are congruent)

PTS: 6   REF: 080938ge   STA: G.G.27   TOP: Quadrilateral Proofs

0110ge
Answer Section

1 ANS: 2

The length of the midsegment of a trapezoid is the average of the lengths of its bases. $\dfrac{x+30}{2} = 44.$

$$x + 30 = 88$$
$$x = 58$$

   PTS: 2   REF: 011001ge   STA: G.G.40   TOP: Trapezoids
2 ANS: 1

$$x + 2x + 2 + 3x + 4 = 180$$
$$6x + 6 = 180$$
$$x = 29$$

   PTS: 2   REF: 011002ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles
3 ANS: 2   PTS: 2   REF: 011003ge   STA: G.G.55
   TOP: Properties of Transformations
4 ANS: 2   PTS: 2   REF: 011004ge   STA: G.G.17
   TOP: Constructions
5 ANS: 1

The closer a chord is to the center of a circle, the longer the chord.

   PTS: 2   REF: 011005ge   STA: G.G.49   TOP: Chords
6 ANS: 2   PTS: 2   REF: 011006ge   STA: G.G.56
   TOP: Isometries
7 ANS: 3   PTS: 2   REF: 011007ge   STA: G.G.31
   TOP: Isosceles Triangle Theorem
8 ANS: 4

$$x^2 = (4 + 5) \times 4$$
$$x^2 = 36$$
$$x = 6$$

   PTS: 2   REF: 011008ge   STA: G.G.53   TOP: Segments Intercepted by Circle
   KEY: tangent and secant
9 ANS: 4   PTS: 2   REF: 011009ge   STA: G.G.19
   TOP: Constructions
10 ANS: 3   PTS: 2   REF: 011010ge   STA: G.G.71
   TOP: Equations of Circles
11 ANS: 2   PTS: 2   REF: 011011ge   STA: G.G.22
   TOP: Locus
12 ANS: 4   PTS: 2   REF: 011012ge   STA: G.G.1
   TOP: Planes

13 ANS: 1
Opposite sides of a parallelogram are congruent. $4x - 3 = x + 3$. $SV = (2) + 3 = 5$.

$$3x = 6$$
$$x = 2$$

   PTS: 2   REF: 011013ge   STA: G.G.38   TOP: Parallelograms
14 ANS: 3
$$m = \frac{-A}{B} = \frac{5}{2}. \quad m = \frac{-A}{B} = \frac{10}{4} = \frac{5}{2}$$

   PTS: 2   REF: 011014ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines
15 ANS: 2
$$\frac{87 + 35}{2} = \frac{122}{2} = 61$$

   PTS: 2   REF: 011015ge   STA: G.G.51   TOP: Arcs Determined by Angles
   KEY: inside circle
16 ANS: 1
$$a^2 + (5\sqrt{2})^2 = (2\sqrt{15})^2$$
$$a^2 + (25 \times 2) = 4 \times 15$$
$$a^2 + 50 = 60$$
$$a^2 = 10$$
$$a = \sqrt{10}$$

   PTS: 2   REF: 011016ge   STA: G.G.48   TOP: Pythagorean Theorem
17 ANS: 4
$$d = \sqrt{(-3 - 1)^2 + (2 - 0)^2} = \sqrt{16 + 4} = \sqrt{20} = \sqrt{4} \cdot \sqrt{5} = 2\sqrt{5}$$

   PTS: 2   REF: 011017ge   STA: G.G.67   TOP: Distance
18 ANS: 4
The slope of $y = -3x + 2$ is -3. The perpendicular slope is $\frac{1}{3}$. $-1 = \frac{1}{3}(3) + b$
$$-1 = 1 + b$$
$$b = -2$$

   PTS: 2   REF: 011018ge   STA: G.G.64   TOP: Parallel and Perpendicular Lines
19 ANS: 4   PTS: 2   REF: 011019ge   STA: G.G.44
   TOP: Similarity Proofs
20 ANS: 2   PTS: 2   REF: 011020ge   STA: G.G.74
   TOP: Graphing Circles

21 ANS: 1

$$3x + 15 + 2x - 1 = 6x + 2$$
$$5x + 14 = 6x + 2$$
$$x = 12$$

PTS: 2   REF: 011021ge   STA: G.G.32   TOP: Exterior Angle Theorem

22 ANS: 2

Because the triangles are similar, $\dfrac{m\angle A}{m\angle D} = 1$

PTS: 2   REF: 011022ge   STA: G.G.45   TOP: Similarity
KEY: perimeter and area

23 ANS: 3

. The sum of the interior angles of a pentagon is $(5 - 2)180 = 540$.

PTS: 2   REF: 011023ge   STA: G.G.36   TOP: Interior and Exterior Angles of Polygons

24 ANS: 1   PTS: 2   REF: 011024ge   STA: G.G.3
TOP: Planes

25 ANS: 3

$$m = \frac{-A}{B} = -\frac{3}{4}$$

PTS: 2   REF: 011025ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines

26 ANS: 1
$A'(2, 4)$

PTS: 2   REF: 011023ge   STA: G.G.54   TOP: Compositions of Transformations
KEY: basic

27 ANS: 3

$$V = \pi r^2 h = \pi \cdot 6^2 \cdot 27 = 972\pi$$

PTS: 2   REF: 011027ge   STA: G.G.14   TOP: Volume and Lateral Area

28 ANS: 3   PTS: 2   REF: 011028ge   STA: G.G.26
TOP: Conditional Statements

29 ANS:

67. $\dfrac{180 - 46}{2} = 67$

PTS: 2   REF: 011029ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

30 ANS:

4. $l_1 w_1 h_1 = l_2 w_2 h_2$

$10 \times 2 \times h = 5 \times w_2 \times h$

$20 = 5w_2$

$w_2 = 4$

PTS: 2   REF: 011030ge   STA: G.G.11   TOP: Volume

31 ANS:

$(6, -4).$ $C_x = \dfrac{Q_x + R_x}{2}.$ $C_y = \dfrac{Q_y + R_y}{2}.$

$3.5 = \dfrac{1 + R_x}{2}$ $2 = \dfrac{8 + R_y}{2}$

$7 = 1 + R_x$ $4 = 8 + R_y$

$6 = R_x$ $-4 = R_y$

PTS: 2   REF: 011031ge   STA: G.G.66   TOP: Midpoint

32 ANS:

PTS: 2   REF: 011032ge   STA: G.G.20   TOP: Constructions

33 ANS:

5. $\dfrac{3}{x} = \dfrac{6 + 3}{15}$

$9x = 45$

$x = 5$

PTS: 2   REF: 011033ge   STA: G.G.46   TOP: Side Splitter Theorem

34 ANS:

6. The centroid divides each median into segments whose lengths are in the ratio 2 : 1. $\overline{TD} = 6$ and $\overline{DB} = 3$

PTS: 2   REF: 011034ge   STA: G.G.43   TOP: Centroid

35 ANS:
36, because a dilation does not affect angle measure. 10, because a dilation does affect distance.

PTS: 4   REF: 011035ge   STA: G.G.59   TOP: Properties of Transformations

36 ANS:

$\overline{JK} \cong \overline{LM}$ because opposite sides of a parallelogram are congruent. $\overline{LM} \cong \overline{LN}$ because of the Isosceles Triangle Theorem. $\overline{LM} \cong \overline{JM}$ because of the transitive property. *JKLM* is a rhombus because all sides are congruent.

PTS: 4   REF: 011036ge   STA: G.G.27   TOP: Quadrilateral Proofs

37 ANS:

PTS: 4   REF: 011037ge   STA: G.G.23   TOP: Locus

38 ANS:

PTS: 6   REF: 011038ge   STA: G.G.70   TOP: Quadratic-Linear Systems

0610ge
Answer Section

1 ANS: 1
Parallel lines intercept congruent arcs.

PTS: 2   REF: 061001ge   STA: G.G.52   TOP: Chords
2 ANS: 2   PTS: 2   REF: 061002ge   STA: G.G.24
TOP: Negations
3 ANS: 4   PTS: 2   REF: 061003ge   STA: G.G.10
TOP: Solids
4 ANS: 3   PTS: 2   REF: 061004ge   STA: G.G.31
TOP: Isosceles Triangle Theorem
5 ANS: 1   PTS: 2   REF: 061005ge   STA: G.G.55
TOP: Properties of Transformations
6 ANS: 4
$L = 2\pi rh = 2\pi \cdot 5 \cdot 11 \approx 345.6$

PTS: 2   REF: 061006ge   STA: G.G.14   TOP: Volume and Lateral Area
7 ANS: 2   PTS: 2   REF: 061007ge   STA: G.G.35
TOP: Parallel Lines and Transversals
8 ANS: 4   PTS: 2   REF: 061008ge   STA: G.G.40
TOP: Trapezoids
9 ANS: 1   PTS: 2   REF: 061009ge   STA: G.G.26
TOP: Converse
10 ANS: 1   PTS: 2   REF: 061010ge   STA: G.G.34
TOP: Angle Side Relationship
11 ANS: 3

PTS: 2   REF: 061011ge   STA: G.G.70   TOP: Quadratic-Linear Systems
12 ANS: 1   PTS: 2   REF: 061012ge   STA: G.G.20
TOP: Constructions
13 ANS: 1   PTS: 2   REF: 061013ge   STA: G.G.50
TOP: Tangents   KEY: point of tangency
14 ANS: 4
The radius is 4. $r^2 = 16$.

PTS: 2   REF: 061014ge   STA: G.G.72   TOP: Equations of Circles
15 ANS: 4   PTS: 2   REF: 061015ge   STA: G.G.56
TOP: Identifying Transformations

16 ANS: 3

$\dfrac{36 - 20}{2} = 8.$ $\sqrt{17^2 - 8^2} = 15$

PTS: 2   REF: 061016ge   STA: G.G.40   TOP: Trapezoids

17 ANS: 3   PTS: 2   REF: 061017ge   STA: G.G.1
TOP: Planes

18 ANS: 4   PTS: 2   REF: 061018ge   STA: G.G.56
TOP: Identifying Transformations

19 ANS: 3

$\dfrac{36 + 20}{2} = 28$

PTS: 2   REF: 061019ge   STA: G.G.51   TOP: Arcs Determined by Angles
KEY: inside circle

20 ANS: 2   PTS: 2   REF: 061020ge   STA: G.G.19
TOP: Constructions

21 ANS: 4

$d = \sqrt{(146 - (-4))^2 + (52 - 2)^2} = \sqrt{25,000} \approx 158.1$

PTS: 2   REF: 061021ge   STA: G.G.67   TOP: Distance

22 ANS: 2   PTS: 2   REF: 061022ge   STA: G.G.62
TOP: Parallel and Perpendicular Lines

23 ANS: 2

$(d + 4)4 = 12(6)$

$4d + 16 = 72$

$d = 14$

$r = 7$

PTS: 2   REF: 061023ge   STA: G.G.53   TOP: Segments Intercepted by Circle
KEY: two secants

24 ANS: 2

$$x^2 + (x + 7)^2 = 13^2$$

$$x^2 + x^2 + 7x + 7x + 49 = 169$$

$$2x^2 + 14x - 120 = 0$$

$$x^2 + 7x - 60 = 0$$

$$(x + 12)(x - 5) = 0$$

$$x = 5$$

$$2x = 10$$

PTS: 2   REF: 061024ge   STA: G.G.48   TOP: Pythagorean Theorem

25 ANS: 4

$\overline{BG}$ is also an angle bisector since it intersects the concurrence of $\overline{CD}$ and $\overline{AE}$

PTS: 2   REF: 061025ge   STA: G.G.21
KEY: Centroid, Orthocenter, Incenter and Circumcenter

26 ANS: 2

PTS: 2   REF: 061026GE   STA: G.G.51   TOP: Arcs Determined by Angles
KEY: inscribed

27 ANS: 1

$$-2\left(-\frac{1}{2}y = 6x + 10\right)$$

$$y = -12x - 20$$

PTS: 2   REF: 061027ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

28 ANS: 2

Adjacent sides of a rectangle are perpendicular and have opposite and reciprocal slopes.

PTS: 2   REF: 061028ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

29 ANS:

452. $SA = 4\pi r^2 = 4\pi \cdot 6^2 = 144\pi \approx 452$

PTS: 2   REF: 061029ge   STA: G.G.16   TOP: Volume and Surface Area

30 ANS:

37. Since $\overline{DE}$ is a midsegment, $AC = 14$. $10 + 13 + 14 = 37$

PTS: 2   REF: 061030ge   STA: G.G.42   TOP: Midsegments

31 ANS:

34. $2x - 12 + x + 90 = 180$

$$3x + 78 = 90$$

$$3x = 102$$

$$x = 34$$

PTS: 2   REF: 061031ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

32 ANS:

PTS: 2   REF: 061032ge   STA: G.G.54   TOP: Reflections
KEY: grids

33 ANS:

PTS: 2   REF: 061033ge   STA: G.G.22   TOP: Locus

34 ANS:

18. $V = \frac{1}{3} Bh = \frac{1}{3} lwh$

$288 = \frac{1}{3} \cdot 8 \cdot 6 \cdot h$

$288 = 16h$

$18 = h$

PTS: 2   REF: 061034ge   STA: G.G.13   TOP: Volume

35 ANS:

$\overline{BD} \cong \overline{DB}$ (Reflexive Property); $\triangle ABD \cong \triangle CDB$ (SSS); $\angle BDC \cong \angle ABD$ (CPCTC).

PTS: 4   REF: 061035ge   STA: G.G.27   TOP: Quadrilateral Proofs

36 ANS:

$y = \frac{2}{3} x + 1$. $2y + 3x = 6$. $y = mx + b$

$2y = -3x + 6$ $5 = \frac{2}{3}(6) + b$

$y = -\frac{3}{2} x + 3$ $5 = 4 + b$

$m = -\frac{3}{2}$ $1 = b$

$m_\perp = \frac{2}{3}$ $y = \frac{2}{3} x + 1$

PTS: 4   REF: 061036ge   STA: G.G.64   TOP: Parallel and Perpendicular Lines

37 ANS:

Midpoint: $\left(\frac{-4+4}{2}, \frac{2+(-4)}{2} \right) = (0,-1)$. Distance: $d = \sqrt{(-4-4)^2 + (2-(-4))^2} = \sqrt{100} = 10$

$r = 5$

$r^2 = 25$

$x^2 + (y+1)^2 = 25$

PTS: 4   REF: 061037ge   STA: G.G.71   TOP: Equations of Circles

38 ANS:

$8x - 5 = 3x + 30.$ $4z - 8 = 3z.$ $9y + 8 + 5y - 2 = 90.$

$5x = 35$ $z = 8$ $14y + 6 = 90$

$x = 7$ $14y = 84$

$y = 6$

PTS: 6   REF: 061038ge   STA: G.G.39   TOP: Special Parallelograms

0810ge
Answer Section

1 ANS: 4

   PTS: 2   REF: 081001ge   STA: G.G.29   TOP: Triangle Congruency
2 ANS: 3   PTS: 2   REF: 081002ge   STA: G.G.9
   TOP: Planes
3 ANS: 1

   PTS: 2   REF: 081003ge   STA: G.G.42   TOP: Midsegments
4 ANS: 3

$$(x+3)^2 - 4 = 2x + 5$$

$$x^2 + 6x + 9 - 4 = 2x + 5$$

$$x^2 + 4x = 0$$

$$x(x+4) = 0$$

$$x = 0, -4$$

   PTS: 2   REF: 081004ge   STA: G.G.70   TOP: Quadratic-Linear Systems
5 ANS: 4   PTS: 2   REF: 081005ge   STA: G.G.18
   TOP: Constructions
6 ANS: 4
   $180 - (50 + 30) = 100$

   PTS: 2   REF: 081006ge   STA: G.G.45   TOP: Similarity
   KEY: basic

7   ANS: 2

PTS: 2   REF: 081007ge   STA: G.G.28   TOP: Triangle Congruency
8   ANS: 1   PTS: 2   REF: 081008ge   STA: G.G.3
    TOP: Planes
9   ANS: 1   PTS: 2   REF: 081009ge   STA: G.G.73
    TOP: Equations of Circles
10 ANS: 4

The slope of a line in standard form is $-\dfrac{A}{B}$, so the slope of this line is $\dfrac{-4}{2} = -2$. A parallel line would also have a

slope of -2. Since the answers are in slope intercept form, find the y-intercept: $y = mx + b$

$$3 = -2(7) + b$$
$$17 = b$$

PTS: 2   REF: 081010ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines
11 ANS: 4
Longest side of a triangle is opposite the largest angle. Shortest side is opposite the smallest angle.

PTS: 2   REF: 081011ge   STA: G.G.34   TOP: Angle Side Relationship
12 ANS: 1   PTS: 2   REF: 081012ge   STA: G.G.50
    TOP: Tangents   KEY: two tangents
13 ANS: 4

$$d = \sqrt{(-6-2)^2 + (4-(-5))^2} = \sqrt{64 + 81} = \sqrt{145}$$

PTS: 2   REF: 081013ge   STA: G.G.67   TOP: Distance
14 ANS: 2

$y + \dfrac{1}{2}x = 4$ $3x + 6y = 12$

$y = -\dfrac{1}{2}x + 4$ $6y = -3x + 12$

$m = -\dfrac{1}{2}$ $y = -\dfrac{3}{6}x + 2$

$y = -\dfrac{1}{2}x + 2$

PTS: 2   REF: 081014ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines
15 ANS: 2   PTS: 2   REF: 081015ge   STA: G.G.56
    TOP: Identifying Transformations

16 ANS: 4

sum of interior $\angle$s = sum of exterior $\angle$s

$$(n-2)180 = n\left(180 - \frac{(n-2)180}{n}\right)$$

$$180n - 360 = 180n - 180n + 360$$

$$180n = 720$$

$$n = 4$$

PTS: 2 REF: 081016ge STA: G.G.36 TOP: Interior and Exterior Angles of Polygons

17 ANS: 1

$4x = 6 \cdot 10$

$x = 15$

PTS: 2 REF: 081017ge STA: G.G.53 TOP: Segments Intercepted by Circle
KEY: two chords

18 ANS: 1

The centroid divides each median into segments whose lengths are in the ratio 2 : 1.

$$\overline{GC} = 2\overline{FG}$$

$$\overline{GC} + \overline{FG} = 24$$

$$2\overline{FG} + \overline{FG} = 24$$

$$3\overline{FG} = 24$$

$$\overline{FG} = 8$$

PTS: 2 REF: 081018ge STA: G.G.43 TOP: Centroid

19 ANS: 2

$$M_x = \frac{3x+5+x-1}{2} = \frac{4x+4}{2} = 2x+2. \quad M_Y = \frac{3y+(-y)}{2} = \frac{2y}{2} = y.$$

PTS: 2 REF: 081019ge STA: G.G.66 TOP: Midpoint

20 ANS: 4

$$SA = 4\pi r^2 \quad V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi \cdot 6^3 = 288\pi$$

$$144\pi = 4\pi r^2$$

$$36 = r^2$$

$$6 = r$$

PTS: 2　　　　REF: 081020ge　　STA: G.G.16　　TOP: Volume and Surface Area

21 ANS: 3　　　　PTS: 2　　　　REF: 081021ge　　STA: G.G.57

TOP: Properties of Transformations

22 ANS: 1

$$\angle A = \frac{(n-2)180}{n} = \frac{(5-2)180}{5} = 108 \quad \angle AEB = \frac{180-108}{2} = 36$$

PTS: 2　　　　REF: 081022ge　　STA: G.G.37　　TOP: Interior and Exterior Angles of Polygons

23 ANS: 4　　　　PTS: 2　　　　REF: 081023ge　　STA: G.G.45

TOP: Similarity　　KEY: perimeter and area

24 ANS: 3

$$2y = -6x + 8$$ Perpendicular lines have slope the opposite and reciprocal of each other.

$$y = -3x + 4$$

$$m = -3$$

$$m_\perp = \frac{1}{3}$$

PTS: 2　　　　REF: 081024ge　　STA: G.G.62　　TOP: Parallel and Perpendicular Lines

25 ANS: 2

$$\frac{140 - \overline{RS}}{2} = 40$$

$$140 - \overline{RS} = 80$$

$$\overline{RS} = 60$$

PTS: 2　　　　REF: 081025ge　　STA: G.G.51　　TOP: Arcs Determined by Angles

KEY: outside circle

26 ANS: 3　　　　PTS: 2　　　　REF: 081026ge　　STA: G.G.26

TOP: Contrapositive

27 ANS: 2

$$\frac{3}{7} = \frac{6}{x}$$

$$3x = 42$$

$$x = 14$$

PTS: 2　　　　REF: 081027ge　　STA: G.G.46　　TOP: Side Splitter Theorem

28 ANS: 1　　　　PTS: 2　　　　REF: 081028ge　　STA: G.G.21

TOP: Centroid, Orthocenter, Incenter and Circumcenter

29 ANS:
70. $3x + 5 + 3x + 5 + 2x + 2x = 180$

$$10x + 10 = 360$$

$$10x = 350$$

$$x = 35$$

$$2x = 70$$

PTS: 2   REF: 081029ge   STA: G.G.40   TOP: Trapezoids

30 ANS:
375π $L = \pi r l = \pi(15)(25) = 375\pi$

PTS: 2   REF: 081030ge   STA: G.G.15   TOP: Volume and Lateral Area

31 ANS:
110. $6x + 20 = x + 40 + 4x - 5$

$$6x + 20 = 5x + 35$$

$$x = 15$$

$$6((15) + 20 = 110$$
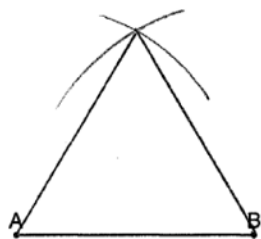
PTS: 2   REF: 081031ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

32 ANS:

PTS: 2   REF: 081032ge   STA: G.G.20   TOP: Constructions

33 ANS:

PTS: 2   REF: 081033ge   STA: G.G.22   TOP: Locus

5

34 ANS:

$(x + 1)^2 + (y - 2)^2 = 36$

PTS: 2   REF: 081034ge   STA: G.G.72   TOP: Equations of Circles

35 ANS:

Yes, m∠ABD = m∠BDC = 44 180 − (93 + 43) = 44 $x + 19 + 2x + 6 + 3x + 5 = 180$. Because alternate interior

$$6x + 30 = 180$$
$$6x = 150$$
$$x = 25$$
$$x + 19 = 44$$

angles ∠ABD and ∠CDB are congruent, $\overline{AB}$ is parallel to $\overline{DC}$.

PTS: 4   REF: 081035ge   STA: G.G.35   TOP: Parallel Lines and Transversals

36 ANS:

$A''(8, 2)$, $B''(2, 0)$, $C''(6, -8)$

PTS: 4   REF: 081036ge   STA: G.G.58   TOP: Compositions of Transformations

37 ANS:

2.4. $5a = 4^2$ $5b = 3^2$ $h^2 = ab$

$a = 3.2$ $b = 1.8$ $h^2 = 3.2 \cdot 1.8$

$h = \sqrt{5.76} = 2.4$

PTS: 4   REF: 081037ge   STA: G.G.47   TOP: Similarity
KEY: altitude

38 ANS:

$\overline{AB} \| \overline{CD}$ and $\overline{AD} \| \overline{CB}$ because their slopes are equal. ABCD is a parallelogram because opposite side are parallel. $\overline{AB} \neq \overline{BC}$. ABCD is not a rhombus because all sides are not equal. $\overline{AB} \sim \perp \overline{BC}$ because their slopes are not opposite reciprocals. ABCD is not a rectangle because ∠ABC is not a right angle.

PTS: 4   REF: 081038ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

6

0111ge
Answer Section

1 ANS: 3

 PTS: 2   REF: 011101ge   STA: G.G.53   TOP: Segments Intercepted by Circle
 KEY: two tangents
2 ANS: 1   PTS: 2   REF: 011102ge   STA: G.G.55
 TOP: Properties of Transformations
3 ANS: 2

$$\frac{4x + 10}{2} = 2x + 5$$

 PTS: 2   REF: 011103ge   STA: G.G.42   TOP: Midsegments
4 ANS: 3   PTS: 2   REF: 011104ge   STA: G.G.38
 TOP: Parallelograms
5 ANS: 3   PTS: 2   REF: 011105ge   STA: G.G.10
 TOP: Solids
6 ANS: 2

$$M_x = \frac{7 + (-3)}{2} = 2. \quad M_Y = \frac{-1 + 3}{2} = 1.$$

 PTS: 2   REF: 011106ge   STA: G.G.66   TOP: Midpoint
7 ANS: 3
 $-5 + 3 = -2$ $2 + -4 = -2$

 PTS: 2   REF: 011107ge   STA: G.G.54   TOP: Translations
8 ANS: 4   PTS: 2   REF: 011108ge   STA: G.G.27
 TOP: Angle Proofs
9 ANS: 2   PTS: 2   REF: 011109ge   STA: G.G.9
 TOP: Planes
10 ANS: 3   PTS: 2   REF: 011110ge   STA: G.G.21
 KEY: Centroid, Orthocenter, Incenter and Circumcenter
11 ANS: 3
 $8^2 + 24^2 \neq 25^2$

 PTS: 2   REF: 011111ge   STA: G.G.48   TOP: Pythagorean Theorem
12 ANS: 1   PTS: 2   REF: 011112ge   STA: G.G.39
 TOP: Special Parallelograms

13 ANS: 3

PTS: 2   REF: 011112ge   STA: G.G.49   TOP: Chords

14 ANS: 4

$y = mx + b$

$3 = \dfrac{3}{2}(-2) + b$

$3 = -3 + b$

$6 = b$

PTS: 2   REF: 011114ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

15 ANS: 4

$m\angle A = 80$

PTS: 2   REF: 011115ge   STA: G.G.34   TOP: Angle Side Relationship

16 ANS: 3   PTS: 2   REF: 011116ge   STA: G.G.71

TOP: Equations of Circles

17 ANS: 2

$V = \pi r^2 h = \pi \cdot 6^2 \cdot 15 = 540\pi$

PTS: 2   REF: 011117ge   STA: G.G.14   TOP: Volume and Lateral Area

18 ANS: 4   PTS: 2   REF: 011118ge   STA: G.G.25

TOP: Compound Statements   KEY: general

19 ANS: 4

$x + 6y = 12$ $3(x - 2) = -y - 4$

$\quad 6y = -x + 12$ $-3(x - 2) = y + 4$

$\quad\quad y = -\dfrac{1}{6}x + 2$ $m = -3$

$\quad\quad m = -\dfrac{1}{6}$

PTS: 2   REF: 011119ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

20 ANS: 1   PTS: 2   REF: 011120ge   STA: G.G.18

TOP: Constructions

21 ANS: 4

$d = \sqrt{(-5-3)^2 + (4-(-6))^2} = \sqrt{64+100} = \sqrt{164} = \sqrt{4}\sqrt{41} = 2\sqrt{41}$

PTS: 2   REF: 011121ge   STA: G.G.67   TOP: Distance
KEY: general

22 ANS: 1   PTS: 2   REF: 011122GE   STA: G.G.28
TOP: Triangle Congruency

23 ANS: 4

$6^2 = x(x+5)$

$36 = x^2 + 5x$

$0 = x^2 + 5x - 36$

$0 = (x+9)(x-4)$

$x = 4$

PTS: 2   REF: 011123ge   STA: G.G.47   TOP: Similarity
KEY: leg

24 ANS: 4   PTS: 2   REF: 011124ge   STA: G.G.51
TOP: Arcs Determined by Angles   KEY: inscribed

25 ANS: 2   PTS: 2   REF: 011125ge   STA: G.G.74
TOP: Graphing Circles

26 ANS: 3

$(3,-2) \rightarrow (2,3) \rightarrow (8,12)$

PTS: 2   REF: 011126ge   STA: G.G.54   TOP: Compositions of Transformations
KEY: basic

27 ANS: 3

$x + 2x + 15 = 5x + 15 \quad 2(5) + 15 = 25$

$3x + 15 = 5x + 5$

$10 = 2x$

$5 = x$

PTS: 2   REF: 011127ge   STA: G.G.32   TOP: Exterior Angle Theorem

28 ANS: 1   PTS: 2   REF: 011128ge   STA: G.G.2
TOP: Planes

29 ANS:

PTS: 2   REF: 011129ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

3

30 ANS:

PTS: 2 REF: 011130ge STA: G.G.54 TOP: Reflections
KEY: grids

31 ANS:

$(5-2)180 = 540.$ $\dfrac{540}{5} = 108$ interior. $180 - 108 = 72$ exterior

PTS: 2 REF: 011131ge STA: G.G.37 TOP: Interior and Exterior Angles of Polygons

32 ANS:

$x^2 = 9 \cdot 8$

$x = \sqrt{72}$

$x = \sqrt{36}\sqrt{2}$

$x = 6\sqrt{2}$

PTS: 2 REF: 011132ge STA: G.G.53 TOP: Segments Intercepted by Circle
KEY: two chords

33 ANS:

PTS: 2 REF: 011133ge STA: G.G.17 TOP: Constructions

34 ANS:

$m = \dfrac{-A}{B} = \dfrac{6}{2} = 3.$ $m_\perp = -\dfrac{1}{3}.$

PTS: 2 REF: 011134ge STA: G.G.62 TOP: Parallel and Perpendicular Lines

35 ANS:

PTS: 4   REF: 011135ge   STA: G.G.23   TOP: Locus

36 ANS:

∠*B* and ∠*E* are right angles because of the definition of perpendicular lines. ∠*B* ≅ ∠*E* because all right angles are congruent. ∠*BFD* and ∠*DFE* are supplementary and ∠*ECA* and ∠*ACB* are supplementary because of the definition of supplementary angles. ∠*DFE* ≅ ∠*ACB* because angles supplementary to congruent angles are congruent. △*ABC* ~ △*DEF* because of AA.

PTS: 4   REF: 011136ge   STA: G.G.44   TOP: Similarity Proofs

37 ANS:

32. $\dfrac{16}{20} = \dfrac{x-3}{x+5}$. $\overline{AC} = x - 3 = 35 - 3 = 32$

$16x + 80 = 20x - 60$

$140 = 4x$

$35 = x$

PTS: 4   REF: 011137ge   STA: G.G.46   TOP: Side Splitter Theorem

38 ANS:

The length of each side of quadrilateral is 5. Since each side is congruent, quadrilateral *MATH* is a rhombus. The slope of $\overline{MH}$ is 0 and the slope of $\overline{HT}$ is $-\dfrac{4}{3}$. Since the slopes are not negative reciprocals, the sides are not perpendicular and do not form rights angles. Since adjacent sides are not perpendicular, quadrilateral *MATH* is not a square.

PTS: 6   REF: 011138ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

0611ge
Answer Section

1 ANS: 2 PTS: 2 REF: 061101ge STA: G.G.18
   TOP: Constructions
2 ANS: 3 PTS: 2 REF: 061102ge STA: G.G.29
   TOP: Triangle Congruency
3 ANS: 4 PTS: 2 REF: 061103ge STA: G.G.60
   TOP: Identifying Transformations
4 ANS: 1 PTS: 2 REF: 061104ge STA: G.G.43
   TOP: Centroid
5 ANS: 1
   Parallel lines intercept congruent arcs.

   PTS: 2 REF: 061105ge STA: G.G.52 TOP: Chords
6 ANS: 2
   $7x = 5x + 30$

   $2x = 30$

   $x = 15$

   PTS: 2 REF: 061106ge STA: G.G.35 TOP: Parallel Lines and Transversals
7 ANS: 2 PTS: 2 REF: 061107ge STA: G.G.32
   TOP: Exterior Angle Theorem
8 ANS: 1 PTS: 2 REF: 061108ge STA: G.G.9
   TOP: Planes
9 ANS: 2
   $d = \sqrt{(-1 - 7)^2 + (9 - 4)^2} = \sqrt{64 + 25} = \sqrt{89}$

   PTS: 2 REF: 061109ge STA: G.G.67 TOP: Distance
   KEY: general
10 ANS: 1 PTS: 2 REF: 061110ge STA: G.G.72
    TOP: Equations of Circles
11 ANS: 3 PTS: 2 REF: 061111ge STA: G.G.38
    TOP: Parallelograms
12 ANS: 2
    $V = \dfrac{4}{3}\pi r^3 = \dfrac{4}{3}\pi \cdot 3^3 = 36\pi$

    PTS: 2 REF: 061112ge STA: G.G.16 TOP: Volume and Surface Area
13 ANS: 1 PTS: 2 REF: 061113ge STA: G.G.63
    TOP: Parallel and Perpendicular Lines
14 ANS: 4 PTS: 2 REF: 061114ge STA: G.G.73
    TOP: Equations of Circles
15 ANS: 2 PTS: 2 REF: 061115ge STA: G.G.69
    TOP: Triangles in the Coordinate Plane

16 ANS: 3

$\sqrt{5^2 + 12^2} = 13$

PTS: 2   REF: 061116ge   STA: G.G.39   TOP: Special Parallelograms

17 ANS: 4

$4(x + 4) = 8^2$

$4x + 16 = 64$

$\quad 4x = 48$

$\quad\;\; x = 12$

PTS: 2   REF: 061117ge   STA: G.G.53   TOP: Segments Intercepted by Circle
KEY: tangent and secant

18 ANS: 4   PTS: 2   REF: 061118ge   STA: G.G.1
TOP: Planes

19 ANS: 1

$3x + 5 + 4x - 15 + 2x + 10 = 180.$ m$\angle D = 3(20) + 5 = 65.$ m$\angle E = 4(20) - 15 = 65.$

$\qquad\qquad\qquad 9x = 180$

$\qquad\qquad\qquad\;\; x = 20$

PTS: 2   REF: 061119ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

20 ANS: 3

$\dfrac{7x}{4} = \dfrac{7}{x}.$ $7(2) = 14$

$7x^2 = 28$

$\;\;\; x = 2$

PTS: 2   REF: 061120ge   STA: G.G.45   TOP: Similarity
KEY: basic

21 ANS: 2   PTS: 2   REF: 061121ge   STA: G.G.22
TOP: Locus

22 ANS: 3   PTS: 2   REF: 061122ge   STA: G.G.56
TOP: Identifying Transformations

23 ANS: 2

The slope of a line in standard form is $\dfrac{-A}{B}$, so the slope of this line is $\dfrac{-4}{3}$. A parallel line would also have a slope

of $\dfrac{-4}{3}$. Since the answers are in standard form, use the point-slope formula. $y - 2 = -\dfrac{4}{3}(x + 5)$

$\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad 3y - 6 = -4x - 20$

$\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad 4x + 3y = -14$

PTS: 2   REF: 061123ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

24 ANS: 4   PTS: 2   REF: 061124ge   STA: G.G.31
TOP: Isosceles Triangle Theorem

25 ANS: 1   PTS: 2   REF: 061125ge   STA: G.G.39
    TOP: Special Parallelograms
26 ANS: 2   PTS: 2   REF: 061126ge   STA: G.G.59
    TOP: Properties of Transformations
27 ANS: 4

The slope of $3x + 5y = 4$ is $m = \dfrac{-A}{B} = \dfrac{-3}{5}$. $m_\perp = \dfrac{5}{3}$.

    PTS: 2   REF: 061127ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines
28 ANS: 1

$x^2 = 7(16 - 7)$

$x^2 = 63$

$x = \sqrt{9}\,\sqrt{7}$

$x = 3\sqrt{7}$

    PTS: 2   REF: 061128ge   STA: G.G.47   TOP: Similarity
    KEY: altitude
29 ANS:

The medians of a triangle are not concurrent. False.

    PTS: 2   REF: 061129ge   STA: G.G.24   TOP: Negations
30 ANS:

    PTS: 2   REF: 061130ge   STA: G.G.20   TOP: Constructions
31 ANS:

9.1. $(11)(8)h = 800$

$h \approx 9.1$

    PTS: 2   REF: 061131ge   STA: G.G.12   TOP: Volume

3

32 ANS:
Yes. A reflection is an isometry.

PTS: 2   REF: 061132ge   STA: G.G.55   TOP: Properties of Transformations

33 ANS:

16.7. $\dfrac{x}{25} = \dfrac{12}{18}$

    $18x = 300$

    $x \approx 16.7$

PTS: 2   REF: 061133ge   STA: G.G.46   TOP: Side Splitter Theorem

34 ANS:

$(2a-3, 3b+2).$ $\left(\dfrac{3a+a-6}{2}, \dfrac{2b-1+4b+5}{2} \right) = \left(\dfrac{4a-6}{2}, \dfrac{6b+4}{2} \right) = (2a-3, 3b+2)$

PTS: 2   REF: 061134ge   STA: G.G.66   TOP: Midpoint

35 ANS:

PTS: 4   REF: 061135ge   STA: G.G.23   TOP: Locus

36 ANS:

30. $3x + 4x + 5x = 360$. $m\overarc{LN} : m\overarc{NK} : m\overarc{KL} = 90 : 120 : 150$. $\dfrac{150-90}{2} = 30$

    $x = 20$

PTS: 4   REF: 061136ge   STA: G.G.51   TOP: Arcs Determined by Angles
KEY: outside circle

37 ANS:

PTS: 4   REF: 061137ge   STA: G.G.70   TOP: Quadratic-Linear Systems

38 ANS:

$\overline{OA} \cong \overline{OB}$ because all radii are equal. $\overline{OP} \cong \overline{OP}$ because of the reflexive property. $\overline{OA} \perp \overline{PA}$ and $\overline{OB} \perp \overline{PB}$ because tangents to a circle are perpendicular to a radius at a point on a circle. $\angle PAO$ and $\angle PBO$ are right angles because of the definition of perpendicular. $\angle PAO \cong \angle PBO$ because all right angles are congruent. $\Delta AOP \cong \Delta BOP$ because of HL. $\angle AOP \cong \angle BOP$ because of CPCTC.

PTS: 6   REF: 061138ge   STA: G.G.27   TOP: Circle Proofs

0811ge
Answer Section

1 ANS: 4   PTS: 2   REF: 081101ge   STA: G.G.25
   TOP: Compound Statements   KEY: conjunction
2 ANS: 2   PTS: 2   REF: 081102ge   STA: G.G.29
   TOP: Triangle Congruency
3 ANS: 3

$$\frac{5}{7} = \frac{10}{x}$$

$$5x = 70$$

$$x = 14$$

   PTS: 2   REF: 081103ge   STA: G.G.46   TOP: Side Splitter Theorem
4 ANS: 3   PTS: 2   REF: 081104ge   STA: G.G.55
   TOP: Properties of Transformations
5 ANS: 4

$$\sqrt{25^2 - 7^2} = 24$$

   PTS: 2   REF: 081105ge   STA: G.G.50   TOP: Tangents
   KEY: point of tangency
6 ANS: 4   PTS: 2   REF: 081106ge   STA: G.G.17
   TOP: Constructions
7 ANS: 3

$$d = \sqrt{(1-9)^2 + (-4-2)^2} = \sqrt{64+36} = \sqrt{100} = 10$$

   PTS: 2   REF: 081107ge   STA: G.G.67   TOP: Distance
   KEY: general
8 ANS: 2   PTS: 2   REF: 081108ge   STA: G.G.54
   TOP: Reflections   KEY: basic
9 ANS: 3

$$7x = 5x + 30$$

$$2x = 30$$

$$x = 15$$

   PTS: 2   REF: 081109ge   STA: G.G.35   TOP: Parallel Lines and Transversals
10 ANS: 4   PTS: 2   REF: 081110ge   STA: G.G.71
   TOP: Equations of Circles
11 ANS: 3   PTS: 2   REF: 081111ge   STA: G.G.32
   TOP: Exterior Angle Theorem

12 ANS: 2

$$m = \frac{-A}{B} = \frac{-4}{2} = -2 \quad y = mx + b$$
$$2 = -2(2) + b$$
$$6 = b$$

PTS: 2   REF: 081112ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines
13 ANS: 1   PTS: 2   REF: 081113ge   STA: G.G.54
TOP: Reflections   KEY: basic
14 ANS: 4

PTS: 2   REF: 081114ge   STA: G.G.28   TOP: Triangle Congruency
15 ANS: 1

$$1 = \frac{-4 + x}{2}. \qquad 5 = \frac{3 + y}{2}.$$
$$-4 + x = 2 \qquad 3 + y = 10$$
$$x = 6 \qquad y = 7$$

PTS: 2   REF: 081115ge   STA: G.G.66   TOP: Midpoint
16 ANS: 1   PTS: 2   REF: 081116ge   STA: G.G.7
TOP: Planes
17 ANS: 2   PTS: 2   REF: 081117ge   STA: G.G.23
TOP: Locus
18 ANS: 3

PTS: 2   REF: 081118ge   STA: G.G.70   TOP: Quadratic-Linear Systems
19 ANS: 4

$$\frac{5}{2 + 3 + 5} \times 180 = 90$$

PTS: 2   REF: 081119ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles
20 ANS: 2   PTS: 2   REF: 081120ge   STA: G.G.8
TOP: Planes

21 ANS: 1 PTS: 2 REF: 081121ge STA: G.G.39
TOP: Special Parallelograms

22 ANS: 2

The slope of $x + 2y = 3$ is $m = \dfrac{-A}{B} = \dfrac{-1}{2}$. $m_\perp = 2$.

PTS: 2 REF: 081122ge STA: G.G.62 TOP: Parallel and Perpendicular Lines

23 ANS: 3 PTS: 2 REF: 081123ge STA: G.G.12
TOP: Volume

24 ANS: 4

$\sqrt{6^2 - 2^2} = \sqrt{32} = \sqrt{16}\sqrt{2} = 4\sqrt{2}$

PTS: 2 REF: 081124ge STA: G.G.49 TOP: Chords

25 ANS: 2

$(n - 2)180 = (6 - 2)180 = 720$. $\dfrac{720}{6} = 120$.

PTS: 2 REF: 081125ge STA: G.G.37 TOP: Interior and Exterior Angles of Polygons

26 ANS: 1

$m = \left(\dfrac{8 + 0}{2}, \dfrac{2 + 6}{2}\right) = (4, 4)$ $m = \dfrac{6 - 2}{0 - 8} = \dfrac{4}{-8} = -\dfrac{1}{2}$ $m_\perp = 2$ $y = mx + b$

$4 = 2(4) + b$

$-4 = b$

PTS: 2 REF: 081126ge STA: G.G.68 TOP: Perpendicular Bisector

27 ANS: 3

$x^2 + 7^2 = (x + 1)^2$ $x + 1 = 25$

$x^2 + 49 = x^2 + 2x + 1$

$48 = 2x$

$24 = x$

PTS: 2 REF: 081127ge STA: G.G.48 TOP: Pythagorean Theorem

28 ANS: 3 PTS: 2 REF: 081128ge STA: G.G.39
TOP: Special Parallelograms

29 ANS:

$\dfrac{180 - 80}{2} = 50$

PTS: 2 REF: 081129ge STA: G.G.52 TOP: Chords

30 ANS:

PTS: 2   REF: 081130ge   STA: G.G.18   TOP: Constructions

31 ANS:

$$V = \frac{4}{3}\pi \cdot 9^3 = 972\pi$$

PTS: 2   REF: 081131ge   STA: G.G.16   TOP: Volume and Surface Area

32 ANS:

$$(x-5)^2 + (y+4)^2 = 36$$

PTS: 2   REF: 081132ge   STA: G.G.72   TOP: Equations of Circles

33 ANS:

$\angle ACB \cong \angle AED$ is given. $\angle A \cong \angle A$ because of the reflexive property. Therefore $\triangle ABC \sim \triangle ADE$ because of AA.

PTS: 2   REF: 081133ge   STA: G.G.44   TOP: Similarity Proofs

34 ANS:

$(7,5)$ $m\overline{AB} = \left(\dfrac{3+7}{2}, \dfrac{3+9}{2} \right) = (5,6)$ $m\overline{BC} = \left(\dfrac{7+11}{2}, \dfrac{9+3}{2} \right) = (9,6)$

PTS: 2   REF: 081134ge   STA: G.G.21
TOP: Centroid, Orthocenter, Incenter and Circumcenter

35 ANS:

No, $\angle KGH$ is not congruent to $\angle GKH$.

PTS: 2   REF: 081135ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

36 ANS:

$G''(3,3), H''(7,7), S''(-1,9)$

PTS: 4   REF: 081136ge   STA: G.G.58   TOP: Compositions of Transformations

37 ANS:

2 $\qquad \dfrac{x+2}{x} = \dfrac{x+6}{4}$

$$x^2 + 6x = 4x + 8$$

$$x^2 + 2x - 8 = 0$$

$$(x+4)(x-2) = 0$$

$$x = 2$$

PTS: 4   REF: 081137ge   STA: G.G.45   TOP: Similarity
KEY: basic

38 ANS:

$m\overline{AB} = \left(\dfrac{-6+2}{2}, \dfrac{-2+8}{2} \right) = D(2,3)$ $m\overline{BC} = \left(\dfrac{2+6}{2}, \dfrac{8+-2}{2} \right) = E(4,3)$ $F(0,-2)$. To prove that $ADEF$ is a

parallelogram, show that both pairs of opposite sides of the parallelogram are parallel by showing the opposite

sides have the same slope: $m\overline{AD} = \dfrac{3--2}{-2--6} = \dfrac{5}{4}$ $\overline{AF} \| \overline{DE}$ because all horizontal lines have the same slope. $ADEF$

$$m_{FE} = \dfrac{3--2}{4-0} = \dfrac{5}{4}$$

is not a rhombus because not all sides are congruent. $AD = \sqrt{5^2 + 4^2} = \sqrt{41}$ $AF = 6$

PTS: 6   REF: 081138ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

0112ge
Answer Section

1 ANS: 2
$$6x + 42 = 18x - 12$$
$$54 = 12x$$
$$x = \frac{54}{12} = 4.5$$

   PTS: 2   REF: 011201ge   STA: G.G.35   TOP: Parallel Lines and Transversals
2 ANS: 3   PTS: 2   REF: 011202ge   STA: G.G.21
   TOP: Centroid, Orthocenter, Incenter and Circumcenter
3 ANS: 2   PTS: 2   REF: 011203ge   STA: G.G.73
   TOP: Equations of Circles
4 ANS: 2
   The diagonals of a rhombus are perpendicular. $180 - (90 + 12) = 78$

   PTS: 2   REF: 011204ge   STA: G.G.39   TOP: Special Parallelograms
5 ANS: 1
$$d = \sqrt{(4-1)^2 + (7-11)^2} = \sqrt{9 + 16} = \sqrt{25} = 5$$

   PTS: 2   REF: 011205ge   STA: G.G.67   TOP: Distance
   KEY: general
6 ANS: 2   PTS: 2   REF: 011206ge   STA: G.G.32
   TOP: Exterior Angle Theorem
7 ANS: 1   PTS: 2   REF: 011207ge   STA: G.G.20
   TOP: Constructions
8 ANS: 4   PTS: 2   REF: 011208ge   STA: G.G.53
   TOP: Segments Intercepted by Circle   KEY: two tangents
9 ANS: 3   PTS: 2   REF: 011209ge   STA: G.G.44
   TOP: Similarity Proofs
10 ANS: 3
$$\frac{3}{8+3+4} \times 180 = 36$$

   PTS: 2   REF: 011210ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles
11 ANS: 2   PTS: 2   REF: 011211ge   STA: G.G.55
   TOP: Properties of Transformations
12 ANS: 4   PTS: 2   REF: 011212ge   STA: G.G.71
   TOP: Equations of Circles
13 ANS: 1   PTS: 2   REF: 011213ge   STA: G.G.24
   TOP: Negations

14 ANS: 2

$$\frac{50 + x}{2} = 34$$

$$50 + x = 68$$

$$x = 18$$

PTS: 2   REF: 011214ge   STA: G.G.51   TOP: Arcs Determined by Angles
KEY: inside circle

15 ANS: 2   PTS: 2   REF: 011215ge   STA: G.G.12
TOP: Volume

16 ANS: 4   PTS: 2   REF: 011216ge   STA: G.G.29
TOP: Triangle Congruency

17 ANS: 3   PTS: 2   REF: 011217ge   STA: G.G.64
TOP: Parallel and Perpendicular Lines

18 ANS: 1   PTS: 2   REF: 011218ge   STA: G.G.3
TOP: Planes

19 ANS: 4

$$\sqrt{25^2 - \left(\frac{26 - 12}{2}\right)^2} = 24$$

PTS: 2   REF: 011219ge   STA: G.G.40   TOP: Trapezoids

20 ANS: 1   PTS: 2   REF: 011220ge   STA: G.G.72
TOP: Equations of Circles

21 ANS: 1   PTS: 2   REF: 011221ge   STA: G.G.10
TOP: Solids

22 ANS: 4   PTS: 2   REF: 011222ge   STA: G.G.34
TOP: Angle Side Relationship

23 ANS: 3

$(n - 2)180 = (5 - 2)180 = 540$

PTS: 2   REF: 011223ge   STA: G.G.36   TOP: Interior and Exterior Angles of Polygons

24 ANS: 3

$$y = mx + b$$

$$-1 = 2(2) + b$$

$$-5 = b$$

PTS: 2   REF: 011224ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

25 ANS: 4

$\overline{AB}$ is a vertical line, so its perpendicular bisector is a horizontal line through the midpoint of $\overline{AB}$, which is $(0, 3)$.

PTS: 2   REF: 011225ge   STA: G.G.68   TOP: Perpendicular Bisector

26 ANS: 1
$7x + 4 = 2(2x + 5)$. $PM = 2(2) + 5 = 9$

$7x + 4 = 4x + 10$

$3x = 6$

$x = 2$

PTS: 2   REF: 011226ge   STA: G.G.43   TOP: Centroid
27 ANS: 4
$x \cdot 4x = 6^2$. $PQ = 4x + x = 5x = 5(3) = 15$

$4x^2 = 36$

$x = 3$

PTS: 2   REF: 011227ge   STA: G.G.47   TOP: Similarity
KEY: leg
28 ANS: 2
$5 - 3 = 2, 5 + 3 = 8$

PTS: 2   REF: 011228ge   STA: G.G.33   TOP: Triangle Inequality Theorem
29 ANS:
$2x - 20 = x + 20$. $m\overset{\frown}{AB} = x + 20 = 40 + 20 = 60$

$x = 40$

PTS: 2   REF: 011229ge   STA: G.G.52   TOP: Chords
30 ANS:

PTS: 2   REF: 011230ge   STA: G.G.22   TOP: Locus
31 ANS:

The slope of $y = 2x + 3$ is 2. The slope of $2y + x = 6$ is $\dfrac{-A}{B} = \dfrac{-1}{2}$. Since the slopes are opposite reciprocals, the

lines are perpendicular.

PTS: 2   REF: 011231ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines
32 ANS:
$R'(-3, -2), S'(-4, 4),$ and $T'(2, 2)$.

PTS: 2   REF: 011232ge   STA: G.G.54   TOP: Rotations

33 ANS:

PTS: 2   REF: 011233ge   STA: G.G.17   TOP: Constructions

34 ANS:

$EO = 6.$ $CE = \sqrt{10^2 - 6^2} = 8$

PTS: 2   REF: 011234ge   STA: G.G.49   TOP: Chords

35 ANS:

$A'(7,-4), B'(7,-1). C'(9,-4).$ The areas are equal because translations preserve distance.

PTS: 4   REF: 011235ge   STA: G.G.55   TOP: Properties of Transformations

36 ANS:

$$V = \pi r^2 h \quad . \ L = 2\pi rh = 2\pi \cdot 5\sqrt{2} \cdot 12 \approx 533.1$$

$$600\pi = \pi r^2 \cdot 12$$

$$50 = r^2$$

$$\sqrt{25}\sqrt{2} = r$$

$$5\sqrt{2} = r$$

PTS: 4   REF: 011236ge   STA: G.G.14   TOP: Volume and Lateral Area

37 ANS:

$M\left(\dfrac{-7+5}{2}, \dfrac{2+4}{2}\right) = M(-1,3).$ $N\left(\dfrac{3+5}{2}, \dfrac{-4+4}{2}\right) = N(4,0).$ $\overline{MN}$ is a midsegment.

PTS: 4   REF: 011237ge   STA: G.G.42   TOP: Midsegments

38 ANS:

Quadrilateral *ABCD*, $\overline{AD} \cong \overline{BC}$ and $\angle DAE \cong \angle BCE$ are given. $\overline{AD} \| \overline{BC}$ because if two lines are cut by a transversal so that a pair of alternate interior angles are congruent, the lines are parallel. *ABCD* is a parallelogram because if one pair of opposite sides of a quadrilateral are both congruent and parallel, the quadrilateral is a parallelogram. $\overline{AE} \cong \overline{CE}$ because the diagonals of a parallelogram bisect each other. $\angle FEA \cong \angle GEC$ as vertical angles. $\triangle AEF \cong \triangle CEG$ by ASA.

PTS: 6   REF: 011238ge   STA: G.G.27   TOP: Quadrilateral Proofs

0612ge
Answer Section

1   ANS: 2   PTS: 2   REF: 061201ge   STA: G.G.59
    TOP: Properties of Transformations

2   ANS: 2   PTS: 2   REF: 061202ge   STA: G.G.24
    TOP: Negations

3   ANS: 4   PTS: 2   REF: 061203ge   STA: G.G.9
    TOP: Planes

4   ANS: 1

$\frac{40-24}{2} = 8.$ $\sqrt{10^2 - 8^2} = 6.$

    PTS: 2   REF: 061204ge   STA: G.G.40   TOP: Trapezoids

5   ANS: 3

$\frac{180-70}{2} = 55$

    PTS: 2   REF: 061205ge   STA: G.G.52   TOP: Chords

6   ANS: 2

$\quad AC = BD$

$AC - BC = BD - BC$

$\quad AB = CD$

    PTS: 2   REF: 061206ge   STA: G.G.27   TOP: Line Proofs

7   ANS: 2

$V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi \cdot \left(\frac{15}{2}\right)^3 \approx 1767.1$

    PTS: 2   REF: 061207ge   STA: G.G.16   TOP: Volume and Surface Area

8   ANS: 2   PTS: 2   REF: 061208ge   STA: G.G.19
    TOP: Constructions

9   ANS: 1

The diagonals of a parallelogram intersect at their midpoints. $M_{\overline{AC}}\left(\frac{1+3}{2}, \frac{5+(-1)}{2}\right) = (2,2)$

    PTS: 2   REF: 061209ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

10 ANS: 3   PTS: 2   REF: 061210ge   STA: G.G.71
    TOP: Equations of Circles

11 ANS: 4

20 + 8 + 10 + 6 = 44.

PTS: 2   REF: 061211ge   STA: G.G.42   TOP: Midsegments

12 ANS: 1

PTS: 2   REF: 061211ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

13 ANS: 4   PTS: 2   REF: 061213ge   STA: G.G.5
TOP: Planes

14 ANS: 1   PTS: 2   REF: 061214ge   STA: G.G.21
TOP: Centroid, Orthocenter, Incenter and Circumcenter

15 ANS: 4

$m_\perp = -\dfrac{1}{3}$. $y = mx + b$

$$6 = -\frac{1}{3}(-9) + b$$

$$6 = 3 + b$$

$$3 = b$$

PTS: 2   REF: 061215ge   STA: G.G.64   TOP: Parallel and Perpendicular Lines

16 ANS: 3

$\dfrac{8}{2} = \dfrac{12}{x}$.

$8x = 24$

$x = 3$

PTS: 2   REF: 061216ge   STA: G.G.46   TOP: Side Splitter Theorem

17 ANS: 3

$$d = \sqrt{(-1-4)^2 + (0-(-3))^2} = \sqrt{25+9} = \sqrt{34}$$

PTS: 2   REF: 061217ge   STA: G.G.67   TOP: Distance
KEY: general

18 ANS: 3   PTS: 2   REF: 061218ge   STA: G.G.36
TOP: Interior and Exterior Angles of Polygons

19 ANS: 2

$$m = \frac{-A}{B} = \frac{-20}{-2} = 10. \quad m_\perp = -\frac{1}{10}$$

PTS: 2   REF: 061219ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines

20 ANS: 3   PTS: 2   REF: 061220ge   STA: G.G.74
TOP: Graphing Circles

21 ANS: 2

$\sqrt{17^2 - 15^2} = 8. \quad 17 - 8 = 9$

PTS: 2   REF: 061221ge   STA: G.G.49   TOP: Chords

22 ANS: 3

. Opposite sides of a parallelogram are congruent and the diagonals of a parallelogram bisect each other.

PTS: 2   REF: 061222ge   STA: G.G.28   TOP: Triangle Congruency

23 ANS: 1   PTS: 2   REF: 061223ge   STA: G.G.73
TOP: Equations of Circles

24 ANS: 3   PTS: 2   REF: 061224ge   STA: G.G.45
TOP: Similarity   KEY: basic

25 ANS: 4

$$x^2 - 6x + 2x - 3 = 9x + 27$$

$$x^2 - 4x - 3 = 9x + 27$$

$$x^2 - 13x - 30 = 0$$

$$(x-15)(x+2) = 0$$

$$x = 15, -2$$

PTS: 2   REF: 061225ge   STA: G.G.32   TOP: Exterior Angle Theorem

26 ANS: 4

$$m = \frac{-A}{B} = \frac{-3}{2}. \quad y = mx + b$$

$$-1 = \left(\frac{-3}{2}\right)(2) + b$$

$$-1 = -3 + b$$

$$2 = b$$

PTS: 2   REF: 061226ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

27 ANS: 2   PTS: 2   REF: 061227ge   STA: G.G.56
    TOP: Identifying Transformations

28 ANS: 3   PTS: 2   REF: 061228ge   STA: G.G.39
    TOP: Special Parallelograms

29 ANS:

$T'(-6, 3), A'(-3, 3), P'(-3, -1)$

PTS: 2   REF: 061229ge   STA: G.G.54   TOP: Translations

30 ANS:
    $180 - (90 + 63) = 27$

PTS: 2   REF: 061230ge   STA: G.G.35   TOP: Parallel Lines and Transversals

31 ANS:

The slope of $x + 2y = 4$ is $m = \frac{-A}{B} = \frac{-1}{2}$. The slope of $4y - 2x = 12$ is $\frac{-A}{B} = \frac{2}{4} = \frac{1}{2}$. Since the slopes are neither equal nor opposite reciprocals, the lines are neither parallel nor perpendicular.

PTS: 2   REF: 061231ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

32 ANS:

PTS: 2   REF: 061232ge   STA: G.G.17   TOP: Constructions

33 ANS:

$L = 2\pi rh = 2\pi \cdot 12 \cdot 22 \approx 1659.$ $\dfrac{1659}{600} \approx 2.8.$ 3 cans are needed.

PTS: 2   REF: 061233ge   STA: G.G.14   TOP: Volume and Lateral Area

34 ANS:

PTS: 2   REF: 061234ge   STA: G.G.23   TOP: Locus

35 ANS:

$\angle B$ and $\angle C$ are right angles because perpendicular lines form right angles. $\angle B \cong \angle C$ because all right angles are congruent. $\angle AEB \cong \angle DEC$ because vertical angles are congruent. $\triangle ABE \cong \triangle DCE$ because of ASA. $\overline{AB} \cong \overline{DC}$ because CPCTC.

PTS: 4   REF: 061235ge   STA: G.G.27   TOP: Triangle Proofs

36 ANS:

$A'(5,-4), B'(5,1), C'(2,1), D'(2,-6); A''(5,4), B''(5,-1), C''(2,-1), D''(2,6)$

PTS: 4   REF: 061236ge   STA: G.G.58   TOP: Compositions of Transformations
KEY: grids

37 ANS:

$$x(x+2) = 12 \cdot 2. \quad \overline{RT} = 6+4 = 10. \quad y \cdot y = 18 \cdot 8$$
$$x^2 + 2x - 24 = 0 \qquad\qquad\qquad y^2 = 144$$
$$(x+6)(x-4) = 0 \qquad\qquad\qquad y = 12$$
$$x = 4$$

PTS: 4 REF: 061237ge STA: G.G.53 TOP: Segments Intercepted by Circle
KEY: tangent and secant

38 ANS:

PTS: 6 REF: 061238ge STA: G.G.70 TOP: Quadratic-Linear Systems

0812ge
Answer Section

1 ANS: 4
   Parallel lines intercept congruent arcs.

   PTS: 2   REF: 081201ge   STA: G.G.52   TOP: Chords
2 ANS: 2   PTS: 2   REF: 081202ge   STA: G.G.55
   TOP: Properties of Transformations
3 ANS: 4

   $-5 = \dfrac{-3+x}{2}$. $2 = \dfrac{6+y}{2}$

   $-10 = -3 + x$ $4 = 6 + y$

   $-7 = x$ $-2 = y$

   PTS: 2   REF: 081203ge   STA: G.G.66   TOP: Midpoint
4 ANS: 3   PTS: 2   REF: 081204ge   STA: G.G.59
   TOP: Properties of Transformations
5 ANS: 2   PTS: 2   REF: 081205ge   STA: G.G.17
   TOP: Constructions
6 ANS: 4   PTS: 2   REF: 081206ge   STA: G.G.30
   TOP: Interior and Exterior Angles of Triangles
7 ANS: 1

     $AB = CD$

   $AB + BC = CD + BC$

     $AC = BD$

   PTS: 2   REF: 081207ge   STA: G.G.27   TOP: Triangle Proofs
8 ANS: 3   PTS: 2   REF: 081208ge   STA: G.G.27
   TOP: Quadrilateral Proofs
9 ANS: 3   PTS: 2   REF: 081209ge   STA: G.G.71
   TOP: Equations of Circles
10 ANS: 1

   PTS: 2   REF: 081210ge   STA: G.G.28   TOP: Triangle Congruency

11   ANS: 3

As originally administered, this question read, "Which fact is *not* sufficient to show that planes $\mathcal{R}$ and $\mathcal{S}$ are perpendicular?" The State Education Department stated that since a correct solution was not provided for Question 11, all students shall be awarded credit for this question.

   PTS: 2   REF: 081211ge   STA: G.G.5   TOP: Planes

12   ANS: 2   PTS: 2   REF: 081212ge   STA: G.G.72
   TOP: Equations of Circles

13   ANS: 3

$4x + 14 + 8x + 10 = 180$

$12x = 156$

$x = 13$

   PTS: 2   REF: 081213ge   STA: G.G.35   TOP: Parallel Lines and Transversals

14   ANS: 2   PTS: 2   REF: 081214ge   STA: G.G.50
   TOP: Tangents   KEY: point of tangency

15   ANS: 2

$$V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi \cdot \left(\frac{6}{2}\right)^3 \approx 36\pi$$

   PTS: 2   REF: 081215ge   STA: G.G.16   TOP: Volume and Surface Area

16   ANS: 4   PTS: 2   REF: 081216ge   STA: G.G.45
   TOP: Similarity   KEY: basic

17   ANS: 1

$$m = \frac{3}{2} \quad y = mx + b$$

$$2 = \frac{3}{2}(1) + b$$

$$\frac{1}{2} = b$$

   PTS: 2   REF: 081217ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines

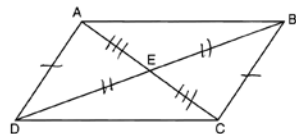18   ANS: 3   PTS: 2   REF: 081218ge   STA: G.G.1
   TOP: Planes

19   ANS: 1

   PTS: 2   REF: 081219ge   STA: G.G.34   TOP: Angle Side Relationship

20 ANS: 4
The centroid divides each median into segments whose lengths are in the ratio 2 : 1.

  PTS: 2   REF: 081220ge   STA: G.G.43   TOP: Centroid
21 ANS: 1
The length of the midsegment of a trapezoid is the average of the lengths of its bases. $\dfrac{x + 3 + 5x - 9}{2} = 2x + 2$.

$$6x - 6 = 4x + 4$$
$$2x = 10$$
$$x = 5$$

  PTS: 2   REF: 081221ge   STA: G.G.40   TOP: Trapezoids
22 ANS: 2
$3x + x + 20 + x + 20 = 180$
$$5x = 40$$
$$x = 28$$

  PTS: 2   REF: 081222ge   STA: G.G.31   TOP: Isosceles Triangle Theorem
23 ANS: 3

$$180(n - 2) = n\left(180 - \frac{180(n - 2)}{n} \right)$$

$180n - 360 = 180n - 180n + 360$
$$180n = 720$$
$$n = 4$$

  PTS: 2   REF: 081223ge   STA: G.G.36   TOP: Interior and Exterior Angles of Polygons
24 ANS: 4   PTS: 2   REF: 081224ge   STA: G.G.21
  TOP: Centroid, Orthocenter, Incenter and Circumcenter
25 ANS: 3

The slope of $9x - 3y = 27$ is $m = \dfrac{-A}{B} = \dfrac{-9}{-3} = 3$, which is the opposite reciprocal of $-\dfrac{1}{3}$.

  PTS: 2   REF: 081225ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines
26 ANS: 2   PTS: 2   REF: 081226ge   STA: G.G.69
  TOP: Triangles in the Coordinate Plane
27 ANS: 3   PTS: 2   REF: 081227ge   STA: G.G.42
  TOP: Midsegments
28 ANS: 3

The slope of $2y = x + 2$ is $\dfrac{1}{2}$, which is the opposite reciprocal of -2. $3 = -2(4) + b$
$$11 = b$$

  PTS: 2   REF: 081228ge   STA: G.G.64   TOP: Parallel and Perpendicular Lines

29 ANS:
2 is not a prime number, false.

PTS: 2　　　REF: 081229ge　　STA: G.G.24　　TOP: Negations

30 ANS:

$A'(-2, 1)$, $B'(-3, -4)$, and $C'(5, -3)$

PTS: 2　　　REF: 081230ge　　STA: G.G.54　　TOP: Rotations

31 ANS:

$V = \pi r^2 h = \pi(5)^2 \cdot 7 = 175\pi$

PTS: 2　　　REF: 081231ge　　STA: G.G.14　　TOP: Volume and Lateral Area

32 ANS:

$\sqrt{(-4-2)^2 + (3-5)^2} = \sqrt{36+4} = \sqrt{40} = \sqrt{4}\sqrt{10} = 2\sqrt{10}$.

PTS: 2　　　REF: 081232ge　　STA: G.G.67　　TOP: Distance

33 ANS:

PTS: 2　　　REF: 081233ge　　STA: G.G.19　　TOP: Constructions

34 ANS:

PTS: 2　　　REF: 081234ge　　STA: G.G.23　　TOP: Locus

35 ANS:

11. $x^2 + 6x = x + 14$. $6(2) - 1 = 11$

$x^2 + 5x - 14 = 0$

$(x + 7)(x - 2) = 0$

$x = 2$

PTS: 2   REF: 081235ge   STA: G.G.38   TOP: Parallelograms

36 ANS:

PTS: 4   REF: 081236ge   STA: G.G.58   TOP: Compositions of Transformations
KEY: grids

37 ANS:

PTS: 4   REF: 081237ge   STA: G.G.70   TOP: Quadratic-Linear Systems

38 ANS:

52, 40, 80. $360 - (56 + 112) = 192$. $\dfrac{192 - 112}{2} = 40$. $\dfrac{112 + 48}{2} = 80$

$\dfrac{1}{4} \times 192 = 48$

$\dfrac{56 + 48}{2} = 52$

PTS: 6   REF: 081238ge   STA: G.G.51   TOP: Arcs Determined by Angles
KEY: mixed

0113ge
Answer Section

1 ANS: 1   PTS: 2   REF: 011301ge   STA: G.G.29
   TOP: Triangle Congruency
2 ANS: 2

   Parallel chords intercept congruent arcs. $\dfrac{360 - (104 + 168)}{2} = 44$

   PTS: 2   REF: 011302ge   STA: G.G.52   TOP: Chords
3 ANS: 1   PTS: 2   REF: 011303ge   STA: G.G.24
   TOP: Statements
4 ANS: 3   PTS: 2   REF: 011304ge   STA: G.G.56
   TOP: Identifying Transformations
5 ANS: 3

   $6 = \dfrac{4 + x}{2}.$ $8 = \dfrac{2 + y}{2}.$

   $4 + x = 12$ $2 + y = 16$

   $x = 8$ $y = 14$

   PTS: 2   REF: 011305ge   STA: G.G.66   TOP: Midpoint
6 ANS: 4   PTS: 2   REF: 011306ge   STA: G.G.9
   TOP: Planes
7 ANS: 2

   Perimeter of ΔDEF is $5 + 8 + 11 = 24$. $\dfrac{5}{24} = \dfrac{x}{60}$

   $24x = 300$

   $x = 12.5$

   PTS: 2   REF: 011307ge   STA: G.G.45   TOP: Similarity
   KEY: perimeter and area
8 ANS: 1
   $x^2 = 3 \times 12$

   $x = 6$

   PTS: 2   REF: 011308ge   STA: G.G.47   TOP: Similarity
   KEY: altitude
9 ANS: 3   PTS: 2   REF: 011309ge   STA: G.G.20
   TOP: Constructions
10 ANS: 2

   The slope of $2x + 4y = 12$ is $m = \dfrac{-A}{B} = \dfrac{-2}{4} = -\dfrac{1}{2}$. $m_\perp = 2$.
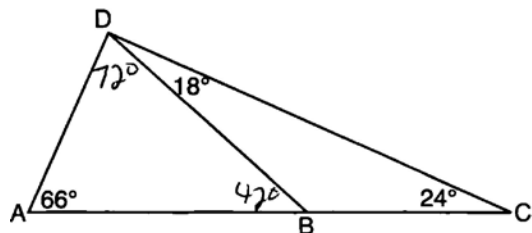
   PTS: 2   REF: 011310ge   STA: G.G.62   TOP: Parallel and Perpendicular Lines

11 ANS: 3   PTS: 2   REF: 011311ge   STA: G.G.42
     TOP: Midsegments

12 ANS: 3

$$x^2 + 5^2 = 25$$
$$x = 0$$

     PTS: 2   REF: 011312ge   STA: G.G.70   TOP: Quadratic-Linear Systems

13 ANS: 2

$$\sqrt{(-2-4)^2 + (-3-(-1))^2} = \sqrt{40} = \sqrt{4}\sqrt{10} = 2\sqrt{10}$$

     PTS: 2   REF: 011313ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

14 ANS: 1

$$\frac{180-52}{2} = 64. \quad 180 - (90+64) = 26$$

     PTS: 2   REF: 011314ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

15 ANS: 4   PTS: 2   REF: 011315ge   STA: G.G.1
     TOP: Planes

16 ANS: 2

$$2^2 + 3^2 \neq 4^2$$

     PTS: 2   REF: 011316ge   STA: G.G.48   TOP: Pythagorean Theorem

17 ANS: 2   PTS: 2   REF: 011317ge   STA: G.G.22
     TOP: Locus

18 ANS: 4   PTS: 2   REF: 011318ge   STA: G.G.73
     TOP: Equations of Circles

19 ANS: 4

$$m = \frac{2}{3} \quad . \quad 2 = -\frac{3}{2}(4) + b$$
$$m_{\perp} = -\frac{3}{2} \quad 2 = -6 + b$$
$$8 = b$$

     PTS: 2   REF: 011319ge   STA: G.G.64   TOP: Parallel and Perpendicular Lines

20 ANS: 1   PTS: 2   REF: 011320ge   STA: G.G.26
     TOP: Conditional Statements

21 ANS: 3

$$2(4x+20) + 2(3x-15) = 360. \quad \angle D = 3(25) - 15 = 60$$
$$8x + 40 + 6x - 30 = 360$$
$$14x + 10 = 360$$
$$14x = 350$$
$$x = 25$$

     PTS: 2   REF: 011321ge   STA: G.G.40   TOP: Trapezoids

22 ANS: 3   PTS: 2   REF: 011322ge   STA: G.G.49
   TOP: Chords
23 ANS: 4   PTS: 2   REF: 011323ge   STA: G.G.72
   TOP: Equations of Circles
24 ANS: 3

$$m = \frac{-A}{B} = \frac{-3}{-2} = \frac{3}{2}$$

   PTS: 2   REF: 011324ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines
25 ANS: 1

$$\frac{70 - 20}{2} = 25$$

   PTS: 2   REF: 011325ge   STA: G.G.51   TOP: Arcs Determined by Angles
   KEY: outside circle
26 ANS: 2

$$\frac{(n-2)180}{n} = 120 \ .$$

$$180n - 360 = 120n$$
$$60n = 360$$
$$n = 6$$

   PTS: 2   REF: 011326ge   STA: G.G.37   TOP: Interior and Exterior Angles of Polygons
27 ANS: 4

$2x - 8 = x + 2$. $AE = 10 + 2 = 12$. $AC = 2(AE) = 2(12) = 24$
$x = 10$

   PTS: 2   REF: 011327ge   STA: G.G.39   TOP: Special Parallelograms
28 ANS: 3

$AB = 8 - 4 = 4$. $BC = \sqrt{(-2-(-5))^2 + (8-6)^2} = \sqrt{13}$. $AC = \sqrt{(-2-(-5))^2 + (4-6)^2} = \sqrt{13}$

   PTS: 2   REF: 011328ge   STA: G.G.69   TOP: Triangles in the Coordinate Plane
29 ANS:
   Distance is preserved after the reflection. $2x + 13 = 9x - 8$
$$21 = 7x$$
$$3 = x$$

   PTS: 2   REF: 011329ge   STA: G.G.55   TOP: Properties of Transformations

30 ANS:

PTS: 2   REF: 011330ge   STA: G.G.50   TOP: Tangents
KEY: common tangency

31 ANS:

PTS: 2   REF: 011331ge   STA: G.G.23   TOP: Locus

32 ANS:

If $r = 5$, then $r^2 = 25$. $(x + 3)^2 + (y - 2)^2 = 25$

PTS: 2   REF: 011332ge   STA: G.G.71   TOP: Equations of Circles

33 ANS:

PTS: 2   REF: 011333ge   STA: G.G.19   TOP: Constructions

34 ANS:

$M = \left(\dfrac{3 + 3}{2}, \dfrac{-1 + 5}{2} \right) = (3, 2)$. $y = 2$.

PTS: 2   REF: 011334ge   STA: G.G.68   TOP: Perpendicular Bisector

35 ANS:

$L = 2\pi r h = 2\pi \cdot 3 \cdot 5 \approx 94.25$. $V = \pi r^2 h = \pi(3)^2(5) \approx 141.37$

PTS: 4   REF: 011335ge   STA: G.G.14   TOP: Volume and Lateral Area

36 ANS:

$A''(11,1)$, $B''(3,7)$, $C''(3,1)$

PTS: 4   REF: 011336ge   STA: G.G.58   TOP: Compositions of Transformations

37 ANS:

$x^2 + 12 + 11x + 5 + 13x - 17 = 180$. m$\angle A = 6^2 + 12 = 48$. $\angle B$ is the largest angle, so $\overline{AC}$ in the longest side.

$$x^2 + 24x - 180 = 0 \quad m\angle B = 11(6) + 5 = 71$$
$$(x + 30)(x - 6) = 0 \quad m\angle C = 13(6) - 7 = 61$$
$$x = 6$$

PTS: 4   REF: 011337ge   STA: G.G.34   TOP: Angle Side Relationship

38 ANS:

Rectangle $ABCD$ with points E and F on side $\overline{AB}$, segments CE and DF intersect at G, and $\angle ADG \cong \angle BCE$ are given. $\overline{AD} \cong \overline{BC}$ because opposite sides of a rectangle are congruent. $\angle A$ and $\angle B$ are right angles and congruent because all angles of a rectangle are right and congruent. $\triangle ADF \cong \triangle BCE$ by ASA. $\overline{AF} \cong \overline{BE}$ per CPCTC. $\overline{EF} \cong \overline{FE}$ under the Reflexive Property. $\overline{AF} - \overline{EF} \cong \overline{BE} - \overline{FE}$ using the Subtraction Property of Segments. $\overline{AE} \cong \overline{BF}$ because of the Definition of Segments.

PTS: 6   REF: 011338ge   STA: G.G.27   TOP: Quadrilateral Proofs

13 ANS: 2   PTS: 2   REF: 061313ge   STA: G.G.70
    TOP: Quadratic-Linear Systems
14 ANS: 1   PTS: 2   REF: 061314ge   STA: G.G.26
    TOP: Converse and Biconditional
15 ANS: 2   PTS: 2   REF: 061315ge   STA: G.G.13
    TOP: Solids
16 ANS: 1

$$V = \frac{4}{3} \pi r^3$$

$$44.6022 = \frac{4}{3} \pi r^3$$

$$10.648 \approx r^3$$

$$2.2 \approx r$$

    PTS: 2   REF: 061317ge   STA: G.G.16   TOP: Volume and Surface Area
17 ANS: 3

$$2y = 3x - 4 . \quad 1 = \frac{3}{2}(6) + b$$

$$y = \frac{3}{2} x - 2 \quad 1 = 9 + b$$

$$-8 = b$$

    PTS: 2   REF: 061316ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines
18 ANS: 4

$$m_{\overleftrightarrow{AB}} = \frac{6-3}{7-5} = \frac{3}{2} . \quad m_{\overleftrightarrow{CD}} = \frac{4-0}{6-9} = \frac{4}{-3}$$

    PTS: 2   REF: 061318ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines
19 ANS: 4   PTS: 2   REF: 061319ge   STA: G.G.73
    TOP: Equations of Circles
20 ANS: 3   PTS: 2   REF: 061320ge   STA: G.G.35
    TOP: Parallel Lines and Transversals
21 ANS: 2   PTS: 2   REF: 061321ge   STA: G.G.34
    TOP: Angle Side Relationship
22 ANS: 2   PTS: 2   REF: 061322ge   STA: G.G.51
    TOP: Arcs Determined by Angles   KEY: inscribed
23 ANS: 3

$$25 \times 9 \times 12 = 15^2 h$$

$$2700 = 15^2 h$$

$$12 = h$$

    PTS: 2   REF: 061323ge   STA: G.G.11   TOP: Volume
24 ANS: 2   PTS: 2   REF: 061324ge   STA: G.G.44
    TOP: Similarity Proofs
25 ANS: 1   PTS: 2   REF: 061325ge   STA: G.G.74
    TOP: Graphing Circles

26 ANS: 2

$$\sqrt{8^2 + 15^2} = 17$$

PTS: 2 REF: 061326ge STA: G.G.39 TOP: Special Parallelograms

27 ANS: 3

$$x^2 = 3 \times 12. \quad \sqrt{6^2 + 3^2} = \sqrt{45} = \sqrt{9}\sqrt{5} = 3\sqrt{5}$$

$$x = 6$$

PTS: 2 REF: 061327ge STA: G.G.47 TOP: Similarity

KEY: altitude

28 ANS: 1

$$12(8) = x(6)$$

$$96 = 6x$$

$$16 = x$$

PTS: 2 REF: 061328ge STA: G.G.53 TOP: Segments Intercepted by Circle

KEY: two secants

29 ANS:

$$L = 2\pi rh = 2\pi \cdot 3 \cdot 7 = 42\pi$$

PTS: 2 REF: 061329ge STA: G.G.14 TOP: Volume and Lateral Area

30 ANS:

$$(n-2)180 = (8-2)180 = 1080. \quad \frac{1080}{8} = 135.$$

PTS: 2 REF: 061330ge STA: G.G.37 TOP: Interior and Exterior Angles of Polygons

31 ANS:

$$\sqrt{(7-3)^2 + (-8-0)^2} = \sqrt{16+64} = \sqrt{80} = 4\sqrt{5}$$

PTS: 2 REF: 061331ge STA: G.G.69 TOP: Triangles in the Coordinate Plane

32 ANS:

PTS: 2 REF: 061332ge STA: G.G.20 TOP: Constructions

3

33 ANS:

PTS: 2   REF: 061333ge   STA: G.G.23   TOP: Locus

34 ANS:

$$m_{\overline{AB}} = \frac{4-1}{4-2} = \frac{3}{2}. \; m_{\overline{BC}} = -\frac{2}{3}$$

PTS: 4   REF: 061334ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

35 ANS:

$S''(5,-3), W''(3,-4), A''(2,1),$ and $N''(4,2)$

PTS: 4   REF: 061335ge   STA: G.G.58   TOP: Compositions of Transformations
KEY: grids

36 ANS:

$2(y+10) = 4y - 20.$ $\overline{DF} = y + 10 = 20 + 10 = 30.$ $\overline{OA} = \overline{OD} = \sqrt{16^2 + 30^2} = 34$

$2y + 20 = 4y - 20$

$\quad 40 = 2y$

$\quad 20 = y$

PTS: 4   REF: 061336ge   STA: G.G.49   TOP: Chords

37 ANS:

$\quad x^2 - 8x = 5x + 30.$ $m\angle C = 4(15) - 5 = 55$

$x^2 - 13x - 30 = 0$

$(x-15)(x+2) = 0$

$\quad\quad\quad x = 15$

PTS: 4   REF: 061337ge   STA: G.G.45   TOP: Similarity
KEY: basic

38 ANS:

$\triangle MAH$, $\overline{MH} \cong \overline{AH}$ and medians $\overline{AB}$ and $\overline{MT}$ are given. $\overline{MA} \cong \overline{AM}$ (reflexive property). $\triangle MAH$ is an isosceles triangle (definition of isosceles triangle). $\angle AMB \cong \angle MAT$ (isosceles triangle theorem). B is the midpoint of $\overline{MH}$ and T is the midpoint of $\overline{AH}$ (definition of median). $m\overline{MB} = \frac{1}{2} m\overline{MH}$ and $m\overline{AT} = \frac{1}{2} m\overline{AH}$ (definition of midpoint). $\overline{MB} \cong \overline{AT}$ (multiplication postulate). $\triangle MBA \cong \triangle ATM$ (SAS). $\angle MBA \cong \angle ATM$ (CPCTC).

PTS: 6   REF: 061338ge   STA: G.G.27   TOP: Triangle Proofs

0813ge
Answer Section

1 ANS: 2   PTS: 2   REF: 081301ge   STA: G.G.24
  TOP: Statements
2 ANS: 1

  Parallel chords intercept congruent arcs. $m\overset{\frown}{AC} = m\overset{\frown}{BD}$. $\dfrac{180 - 110}{2} = 35$.

  PTS: 2   REF: 081302ge   STA: G.G.52   TOP: Chords
3 ANS: 1   PTS: 2   REF: 081303ge   STA: G.G.24
  TOP: Negations
4 ANS: 4
  Distance is preserved after a rotation.

  PTS: 2   REF: 081304ge   STA: G.G.55   TOP: Properties of Transformations
5 ANS: 4   PTS: 2   REF: 081305ge   STA: G.G.71
  TOP: Equations of Circles
6 ANS: 2   PTS: 2   REF: 081306ge   STA: G.G.34
  TOP: Angle Side Relationship
7 ANS: 3
  The centroid divides each median into segments whose lengths are in the ratio 2 : 1.

  PTS: 2   REF: 081307ge   STA: G.G.43   TOP: Centroid
8 ANS: 4   PTS: 2   REF: 081308ge   STA: G.G.49
  TOP: Chords
9 ANS: 3   PTS: 2   REF: 081309ge   STA: G.G.29
  TOP: Triangle Congruency
10 ANS: 4
   $6x = x + 40 + 3x + 10$. $m\angle CAB = 25 + 40 = 65$

   $6x = 4x + 50$

   $2x = 50$

   $x = 25$

   PTS: 2   REF: 081310ge   STA: G.G.32   TOP: Exterior Angle Theorem
11 ANS: 2   PTS: 2   REF: 081311ge   STA: G.G.10
   TOP: Solids
12 ANS: 3   PTS: 2   REF: 081312ge   STA: G.G.72
   TOP: Equations of Circles
13 ANS: 4   PTS: 2   REF: 081313ge   STA: G.G.19
   TOP: Constructions
14 ANS: 3
   $120\pi = \pi(12)(l)$

   $10 = l$

   PTS: 2   REF: 081314ge   STA: G.G.15   TOP: Volume and Lateral Area

1

15 ANS: 4

$$3y + 6 = 2x \qquad 2y - 3x = 6$$

$$3y = 2x - 6 \qquad 2y = 3x + 6$$

$$y = \frac{2}{3}x - 2 \qquad y = \frac{3}{2}x + 3$$

$$m = \frac{2}{3} \qquad\qquad m = \frac{3}{2}$$

  PTS: 2   REF: 081315ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines
16 ANS: 2   PTS: 2   REF: 081316ge   STA: G.G.23
  TOP: Locus
17 ANS: 3

$$\frac{15}{18} = \frac{5}{6}$$

  PTS: 2   REF: 081317ge   STA: G.G.45   TOP: Similarity
  KEY: perimeter and area
18 ANS: 4   PTS: 2   REF: 081318ge   STA: G.G.26
  TOP: Converse and Biconditional
19 ANS: 2

$$(x - 4)^2 - 2 = -2x + 6. \quad y = -2(4) + 6 = -2$$

$$x^2 - 8x + 16 - 2 = -2x + 6 \quad y = -2(2) + 6 = 2$$

$$x^2 - 6x + 8 = 0$$

$$(x - 4)(x - 2) = 0$$

$$x = 4, 2$$

  PTS: 2   REF: 081319ge   STA: G.G.70   TOP: Quadratic-Linear Systems
20 ANS: 3   PTS: 2   REF: 081320ge   STA: G.G.42
  TOP: Midsegments
21 ANS: 1
  If two prisms have equal heights and volume, the area of their bases is equal.

  PTS: 2   REF: 081321ge   STA: G.G.11   TOP: Volume
22 ANS: 4

$$(n - 2)180 - n\left(\frac{(n-2)180}{n}\right) = 180n - 360 - 180n + 180n - 360 = 180n - 720.$$

$$180(5) - 720 = 180$$

  PTS: 2   REF: 081322ge   STA: G.G.37   TOP: Interior and Exterior Angles of Polygons
23 ANS: 1   PTS: 2   REF: 081323ge   STA: G.G.9
  TOP: Planes
24 ANS: 1   PTS: 2   REF: 081324ge   STA: G.G.74
  TOP: Graphing Circles

25 ANS: 2

$$\sqrt{15^2 - 12^2} = 9$$

PTS: 2   REF: 081325ge   STA: G.G.50   TOP: Tangents
KEY: point of tangency

26 ANS: 3

$$x^2 = 2(2 + 10)$$

$$x^2 = 24$$

$$x = \sqrt{24} = \sqrt{4}\sqrt{6} = 2\sqrt{6}$$

PTS: 2   REF: 081326ge   STA: G.G.47   TOP: Similarity
KEY: leg

27 ANS: 3

midpoint: $\left(\dfrac{6+8}{2}, \dfrac{8+4}{2} \right) = (7,6)$. slope: $\dfrac{8-4}{6-8} = \dfrac{4}{-2} = -2$; $m_\perp = \dfrac{1}{2}$. $6 = \dfrac{1}{2}(7) + b$

$$\dfrac{12}{2} = \dfrac{7}{2} + b$$

$$\dfrac{5}{12} = b$$

PTS: 2   REF: 081327ge   STA: G.G.68   TOP: Perpendicular Bisector

28 ANS: 1

$$8 \times 12 = 16x$$

$$6 = x$$

PTS: 2   REF: 081328ge   STA: G.G.53   TOP: Segments Intercepted by Circle
KEY: two chords

29 ANS:
$A'(2,2), B'(3,0), C(1,-1)$

PTS: 2   REF: 081329ge   STA: G.G.58   TOP: Dilations

30 ANS:

PTS: 2   REF: 081330ge   STA: G.G.17   TOP: Constructions

31 ANS:

$$\sqrt{(-1-3)^2 + (4-(-2))^2} = \sqrt{16+36} = \sqrt{52} = \sqrt{4}\sqrt{13} = 2\sqrt{13}$$

PTS: 2   REF: 081331ge   STA: G.G.67   TOP: Distance

32 ANS:

$A = 2B - 15$. $2B - 15 + B + 2B - 15 + B = 180$

$C = A + B$ $6B - 30 = 180$

$C = 2B - 15 + B$ $6B = 210$

            $B = 35$

PTS: 2   REF: 081332ge   STA: G.G.30   TOP: Interior and Exterior Angles of Triangles

33 ANS:

center: $(3, -4)$; radius: $\sqrt{10}$

PTS: 2   REF: 081333ge   STA: G.G.73   TOP: Equations of Circles

34 ANS:

PTS: 2   REF: 081334ge   STA: G.G.22   TOP: Locus

35 ANS:

$\triangle ABC$, $\overline{BD}$ bisects $\angle ABC$, $\overline{BD} \perp \overline{AC}$ (Given). $\angle CBD \cong \angle ABD$ (Definition of angle bisector). $\overline{BD} \cong \overline{BD}$ (Reflexive property). $\angle CDB$ and $\angle ADB$ are right angles (Definition of perpendicular). $\angle CDB \cong \angle ADB$ (All right angles are congruent). $\triangle CDB \cong \triangle ADB$ (SAS). $\overline{AB} \cong \overline{CB}$ (CPCTC).

PTS: 4   REF: 081335ge   STA: G.G.27   TOP: Triangle Proofs

36 ANS:

$M''(1, -2), A''(6, -2), T''(5, -4), H''(3, -4)$

PTS: 4   REF: 081336ge   STA: G.G.58   TOP: Compositions of Transformations
KEY: grids

37 ANS:

$$12x - 4 + 180 - 6x + 6x + 7x + 13 = 360. \quad 16y + 1 = \frac{12y + 1 + 18y + 6}{2}$$

$$19x + 189 = 360$$
$$32y + 2 = 30y + 7$$
$$19x = 171$$
$$2y = 5$$
$$x = 9$$
$$y = \frac{5}{2}$$

PTS: 4   REF: 081337ge   STA: G.G.40   TOP: Trapezoids

38 ANS:

$$M\left(\frac{-7 + -3}{2}, \frac{4 + 6}{2}\right) = M(-5, 5). \quad m_{\overline{MN}} = \frac{5 - 3}{-5 - 0} = \frac{2}{-5} \quad . \text{ Since both opposite sides have equal slopes and are}$$

$$N\left(\frac{-3 + 3}{2}, \frac{6 + 0}{2}\right) = N(0, 3) \qquad m_{\overline{PQ}} = \frac{-4 - -2}{2 - -3} = \frac{-2}{5}$$

$$P\left(\frac{3 + 1}{2}, \frac{0 + -8}{2}\right) = P(2, -4) \qquad m_{\overline{NA}} = \frac{3 - -4}{0 - 2} = \frac{7}{-2}$$

$$Q\left(\frac{-7 + 1}{2}, \frac{4 + -8}{2}\right) = Q(-3, -2) \qquad m_{\overline{QM}} = \frac{-2 - 5}{-3 - -5} = \frac{-7}{2}$$

parallel, *MNPQ* is a parallelogram. $\overline{MN} = \sqrt{(-5 - 0)^2 + (5 - 3)^2} = \sqrt{29}$. $\overline{MN}$ is not congruent to $\overline{NP}$, so *MNPQ*

$$\overline{NA} = \sqrt{(0 - 2)^2 + (3 - -4)^2} = \sqrt{53}$$

is not a rhombus since not all sides are congruent.

PTS: 6   REF: 081338ge   STA: G.G.69   TOP: Quadrilaterals in the Coordinate Plane

0114ge
Answer Section

1 ANS: 2

$$\frac{6+x}{2} = 4. \quad \frac{-4+y}{2} = 2$$

$$\quad x = 2 \qquad \quad y = 8$$

   PTS: 2   REF: 011401ge   STA: G.G.66   TOP: Midpoint
2 ANS: 3   PTS: 2   REF: 011402ge   STA: G.G.17
   TOP: Constructions
3 ANS: 4   PTS: 2   REF: 011403ge   STA: G.G.73
   TOP: Equations of Circles
4 ANS: 1   PTS: 2   REF: 011404ge   STA: G.G.9
   TOP: Planes
5 ANS: 1   PTS: 2   REF: 011405ge   STA: G.G.59
   TOP: Properties of Transformations
6 ANS: 4   PTS: 2   REF: 011406ge   STA: G.G.10
   TOP: Solids
7 ANS: 4   PTS: 2   REF: 011407ge   STA: G.G.23
   TOP: Locus
8 ANS: 1

$2x + x = 12. \quad \overline{BD} = 2(4) = 8$

$\quad 3x = 12$

$\quad\ x = 4$

   PTS: 2   REF: 011408ge   STA: G.G.43   TOP: Centroid
9 ANS: 2

$$x^2 - 2 = x$$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1) = 0$$

$$\quad x = 2, -1$$

   PTS: 2   REF: 011409ge   STA: G.G.70   TOP: Quadratic-Linear Systems
10 ANS: 2

$$m = \frac{-A}{B} = \frac{-5}{1} = -5 \quad y = mx + b$$

$$3 = -5(5) + b$$

$$28 = b$$

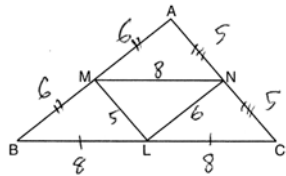   PTS: 2   REF: 011410ge   STA: G.G.65   TOP: Parallel and Perpendicular Lines
11 ANS: 2   PTS: 2   REF: 011411ge   STA: G.G.27
   TOP: Quadrilateral Proofs

12 ANS: 1   PTS: 2   REF: 011412ge   STA: G.G.28
    TOP: Triangle Congruency

13 ANS: 1

    PTS: 2   REF: 011413ge   STA: G.G.42   TOP: Midsegments

14 ANS: 2
    m$\angle ABC = 55$, so m$\angle ACR = 60 + 55 = 115$

    PTS: 2   REF: 011414ge   STA: G.G.32   TOP: Exterior Angle Theorem

15 ANS: 4   PTS: 2   REF: 011415ge   STA: G.G.72
    TOP: Equations of Circles

16 ANS: 1   PTS: 2   REF: 011416ge   STA: G.G.34
    TOP: Angle Side Relationship

17 ANS: 3
    The regular polygon with the smallest interior angle is an equilateral triangle, with 60º. 180° − 60° = 120°

    PTS: 2   REF: 011417ge   STA: G.G.37   TOP: Interior and Exterior Angles of Polygons

18 ANS: 2
    $18\pi \cdot 42 \approx 2375$

    PTS: 2   REF: 011418ge   STA: G.G.14   TOP: Volume and Lateral Area

19 ANS: 3
    $180 - 38 = 142$

    PTS: 2   REF: 011419ge   STA: G.G.50   TOP: Tangents
    KEY: two tangents

20 ANS: 2
    $s^2 + s^2 = (3\sqrt{2})^2$

    $2s^2 = 18$

    $s^2 = 9$

    $s = 3$

    PTS: 2   REF: 011420ge   STA: G.G.39   TOP: Special Parallelograms

21 ANS: 4   PTS: 2   REF: 011421ge   STA: G.G.54
    TOP: Rotations

22 ANS: 1

$7x - 36 + 5x + 12 = 180$

$12x - 24 = 180$

$12x = 204$

$x = 17$

    PTS: 2   REF: 011422ge   STA: G.G.35   TOP: Parallel Lines and Transversals

23 ANS: 1   PTS: 2   REF: 011423ge   STA: G.G.71

    TOP: Equations of Circles

24 ANS: 2

$\sqrt{17^2 - 15^2} = \sqrt{289 - 225} = \sqrt{64} = 8$

    PTS: 2   REF: 011424ge   STA: G.G.49   TOP: Chords

25 ANS: 3   PTS: 2   REF: 011425ge   STA: G.G.39

    TOP: Special Parallelograms

26 ANS: 4   PTS: 2   REF: 011426ge   STA: G.G.73

    TOP: Equations of Circles

27 ANS: 3   PTS: 2   REF: 011427ge   STA: G.G.56

    TOP: Identifying Transformations

28 ANS: 4   PTS: 2   REF: 011428ge   STA: G.G.50

    TOP: Tangents   KEY: common tangency

29 ANS:

$SA = 4\pi r^2 = 4\pi \cdot 2.5^2 = 25\pi \approx 78.54$
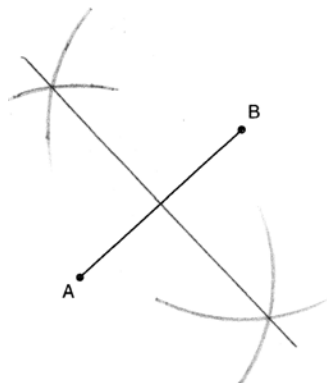
    PTS: 2   REF: 011429ge   STA: G.G.16   TOP: Volume and Surface Area

30 ANS:

    PTS: 2   REF: 011430ge   STA: G.G.18   TOP: Constructions

31 ANS:

$\sqrt{(3-7)^2 + (-4-2)^2} = \sqrt{16+36} = \sqrt{52} = \sqrt{4}\sqrt{13} = 2\sqrt{13}$.

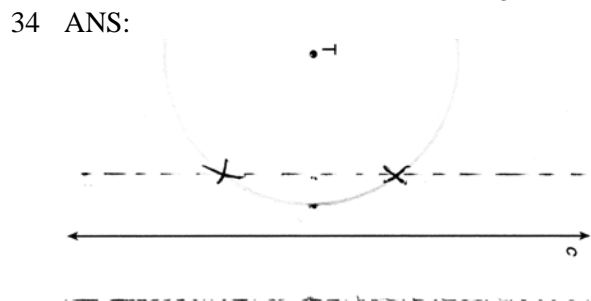   PTS: 2   REF: 011431ge   STA: G.G.67   TOP: Distance

32 ANS:

$Bh = V$

$12h = 84$

$h = 7$

PTS: 2   REF: 011432ge   STA: G.G.12   TOP: Volume
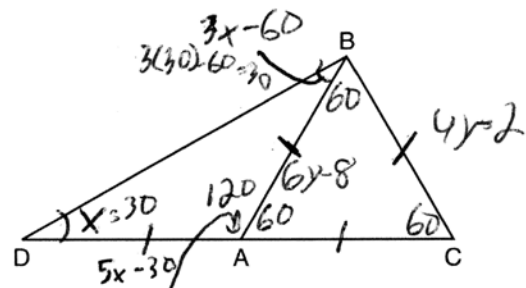
33 ANS:

Neither. The slope of $y = \frac{1}{2}x - 1$ is $\frac{1}{2}$. The slope of $y + 4 = -\frac{1}{2}(x - 2)$ is $-\frac{1}{2}$. The slopes are neither the same nor opposite reciprocals.

PTS: 2   REF: 011433ge   STA: G.G.63   TOP: Parallel and Perpendicular Lines

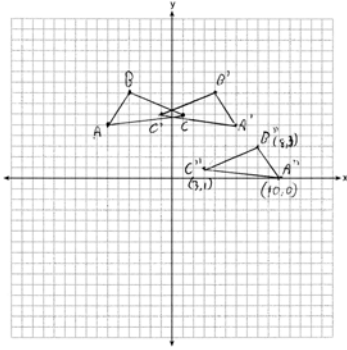34 ANS:

PTS: 2   REF: 011434ge   STA: G.G.22   TOP: Locus

35 ANS:

$x + 3x - 60 + 5x - 30 = 180$ $5(30) - 30 = 120$ $6y - 8 = 4y - 2$ $\overline{DC} = 10 + 10 = 20$

$9x - 90 = 180$ $m\angle BAC = 180 - 120 = 60$ $2y = 6$

$9x = 270$ $y = 3$

$x = 30 = m\angle D$ $4(3) - 2 = 10 = \overline{BC}$

PTS: 3   REF: 011435ge   STA: G.G.31   TOP: Isosceles Triangle Theorem

36 ANS:

PTS: 3   REF: 011436ge   STA: G.G.58   TOP: Compositions of Transformations
KEY: grids

37 ANS:

$4x \cdot x = 6^2$

$\quad 4x^2 = 36$

$\quad\quad x^2 = 9$

$\quad\quad x = 3$

$\overline{BD} = 4(3) = 12$

PTS: 4   REF: 011437ge   STA: G.G.47   TOP: Similarity
KEY: leg

38 ANS:
2. The diameter of a circle is $\perp$ to a tangent at the point of tangency. 4. An angle inscribed in a semicircle is a right angle. 5. All right angles are congruent. 7. AA. 8. Corresponding sides of congruent triangles are in proportion. 9. The product of the means equals the product of the extremes.

PTS: 6   REF: 011438ge   STA: G.G.27   TOP: Circle Proofs