

JEFFERSON MATH PROJECT REGENTS BY PERFORMANCE INDICATOR: TOPIC

NY Algebra 2/Trigonometry Regents Exam Questions
from Fall, 2009 to June, 2011 Sorted by PI: Topic

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Dear Sir

I have to acknolege the reciept of your favor of May 14. in which you mention that you have finished the 6. first books of Euclid, plane trigonometry, surveying & algebra and ask whether I think a further pursuit of that branch of science would be useful to you. there are some propositions in the latter books of Euclid, & some of Archimedes, which are useful, & I have no doubt you have been made acquainted with them. trigonometry, so far as this, is most valuable to every man, there is scarcely a day in which he will not resort to it for some of the purposes of common life. the science of calculation also is indispensable as far as the extraction of the square & cube roots; Algebra as far as the quadratic equation & the use of logarithms are often of value in ordinary cases: but all beyond these is but a luxury; a delicious luxury indeed; but not to be indulged in by one who is to have a profession to follow for his subsistence. in this light I view the conic sections, curves of the higher orders, perhaps even spherical trigonometry, Algebraical operations beyond the 2d dimension, and fluxions.

Letter from Thomas Jefferson to William G. Munford, Monticello, June 18, 1799.

Algebra 2/Trigonometry Regents Exam Questions by Performance Indicator: Topic Answer Section

1 ANS:

Controlled experiment because Howard is comparing the results obtained from an experimental sample against a control sample.

PTS: 2 REF: 081030a2 STA: A2.S.1 TOP: Analysis of Data

2 ANS: 4 PTS: 2 REF: 011127a2 STA: A2.S.1
TOP: Analysis of Data

3 ANS: 4 PTS: 2 REF: 061101a2 STA: A2.S.1
TOP: Analysis of Data

4 ANS: 4
Students entering the library are more likely to spend more time studying, creating bias.

PTS: 2 REF: fall0904a2 STA: A2.S.2 TOP: Analysis of Data

5 ANS: 4 PTS: 2 REF: 061124a2 STA: A2.S.3
TOP: Central Tendency

6 ANS: 3

1-Var Stats L1, L2	σ_x^2	67.31102041
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PTS: 2 REF: fall0924a2 STA: A2.S.4 TOP: Dispersion
KEY: variance

7 ANS:
7.4

PTS: 2 REF: 061029a2 STA: A2.S.4 TOP: Dispersion
KEY: basic, group frequency distributions

8 ANS: 3 PTS: 2 REF: 061127a2 STA: A2.S.6
TOP: Regression

9 ANS:
 $y = 2.001x^{2.298}$, 1,009. $y = 2.001(15)^{2.298} \approx 1009$

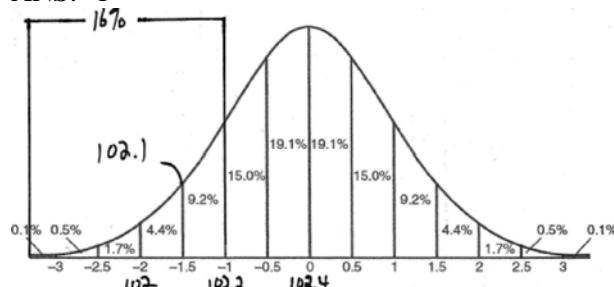
PTS: 4 REF: fall0938a2 STA: A2.S.7 TOP: Power Regression

10 ANS:
 $y = 10.596(1.586)^x$

PTS: 2 REF: 081031a2 STA: A2.S.7 TOP: Exponential Regression

11 ANS: 2 PTS: 2 REF: 061021a2 STA: A2.S.8
TOP: Correlation Coefficient

12 ANS: 1



PTS: 2

REF: fall0915a2

STA: A2.S.5

TOP: Normal Distributions

KEY: interval

13 ANS: 3

$$68\% \times 50 = 34$$

PTS: 2

REF: 081013a2

STA: A2.S.5

TOP: Normal Distributions

KEY: predict

14 ANS:

68% of the students are within one standard deviation of the mean. 16% of the students are more than one standard deviation above the mean.

PTS: 2

REF: 011134a2

STA: A2.S.5

TOP: Normal Distributions

KEY: percent

15 ANS:

no. over 20 is more than 1 standard deviation above the mean. $0.159 \cdot 82 \approx 13.038$

PTS: 2

REF: 061129a2

STA: A2.S.5

TOP: Normal Distributions

KEY: predict

16 ANS: 4

PTS: 2

REF: fall0925a2

STA: A2.S.10

TOP: Permutations

17 ANS:

$$39,916,800 \cdot \frac{^{12}P_{12}}{3! \cdot 2!} = \frac{479,001,600}{12} = 39,916,800$$

PTS: 2

REF: 081035a2

STA: A2.S.10

TOP: Permutations

18 ANS:

$$\text{No. TENNESSEE: } \frac{^9P_9}{4! \cdot 2! \cdot 2!} = \frac{362,880}{96} = 3,780. \text{ VERMONT: } {}_7P_7 = 5,040$$

PTS: 4

REF: 061038a2

STA: A2.S.10

TOP: Permutations

19 ANS: 1

$8 \times 8 \times 7 \times 1 = 448$. The first digit cannot be 0 or 5. The second digit cannot be 5 or the same as the first digit. The third digit cannot be 5 or the same as the first or second digit.

PTS: 2

REF: 011125a2

STA: A2.S.10

TOP: Permutations

20 ANS: 2
 ${}_{15}C_8 = 6,435$

PTS: 2 REF: 081012a2 STA: A2.S.11 TOP: Combinations
 21 ANS: 1
 ${}_{10}C_4 = 210$

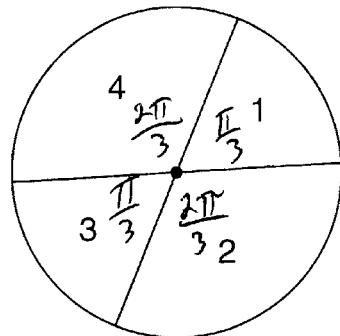
PTS: 2 REF: 061113a2 STA: A2.S.11 TOP: Combinations
 22 ANS: 3 PTS: 2 REF: 061007a2 STA: A2.S.9
 TOP: Differentiating Permutations and Combinations
 23 ANS: 1 PTS: 2 REF: 011117a2 STA: A2.S.9
 TOP: Differentiating Permutations and Combinations

24 ANS:

$9 \text{ nCr } 2 * 20 \text{ nCr } 3$
 41040

41,040.

PTS: 2 REF: fall0935a2 STA: A2.S.12 TOP: Sample Space
 25 ANS: 2



$$\frac{\frac{\pi}{3} + \frac{\pi}{3}}{2\pi} = \frac{\frac{2\pi}{3}}{2\pi} = \frac{1}{3}$$

PTS: 2 REF: 011108a2 STA: A2.S.13 TOP: Geometric Probability
 26 ANS:

$$0.167. {}_{10}C_8 \cdot 0.6^8 \cdot 0.4^2 + {}_{10}C_9 \cdot 0.6^9 \cdot 0.4^1 + {}_{10}C_{10} \cdot 0.6^{10} \cdot 0.4^0 \approx 0.167$$

PTS: 4 REF: 061036a2 STA: A2.S.15 TOP: Binomial Probability
 KEY: at least or at most

27 ANS:
 26.2%. ${}_{10}C_8 \cdot 0.65^8 \cdot 0.35^2 + {}_{10}C_9 \cdot 0.65^9 \cdot 0.35^1 + {}_{10}C_{10} \cdot 0.65^{10} \cdot 0.35^0 \approx 0.262$

PTS: 4 REF: 081038a2 STA: A2.S.15 TOP: Binomial Probability
 KEY: at least or at most

28 ANS:

$$0.468. \quad {}_8C_6 \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^2 \approx 0.27313. \quad {}_8C_7 \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^1 \approx 0.15607. \quad {}_8C_8 \left(\frac{2}{3}\right)^8 \left(\frac{1}{3}\right)^0 \approx 0.03902.$$

PTS: 4

REF: 011138a2

STA: A2.S.15

TOP: Binomial Probability

KEY: at least or at most

29 ANS:

$$\frac{51}{243} \cdot {}_5C_3 \left(\frac{1}{3}\right)^3 \left(\frac{2}{3}\right)^2 = \frac{40}{243}$$

$${}_5C_4 \left(\frac{1}{3}\right)^4 \left(\frac{2}{3}\right)^1 = \frac{10}{243}$$

$${}_5C_3 \left(\frac{1}{3}\right)^5 \left(\frac{2}{3}\right)^0 = \frac{1}{243}$$

PTS: 4

REF: 061138a2

STA: A2.S.15

TOP: Binomial Probability

KEY: at least or at most

30 ANS: 1

$$4a + 6 = 4a - 10. \quad 4a + 6 = -4a + 10. \quad \left| 4\left(\frac{1}{2}\right) + 6 \right| - 4\left(\frac{1}{2}\right) = -10$$

$$6 \neq -10 \quad 8a = 4 \quad 8 - 2 \neq -10$$

$$a = \frac{4}{8} = \frac{1}{2}$$

PTS: 2

REF: 011106a2

STA: A2.A.1

TOP: Absolute Value Equations

31 ANS: 1

$$6x - 7 \leq 5 \quad 6x - 7 \geq -5$$

$$6x \leq 12 \quad 6x \geq 2$$

$$x \leq 2 \quad x \geq \frac{1}{3}$$

PTS: 2

REF: fall0905a2

STA: A2.A.1

TOP: Absolute Value Inequalities

KEY: graph

32 ANS:

$$-3|6-x| < -15$$



$$|6-x| > 5$$

$$6-x > 5 \text{ or } 6-x < -5$$

$$1 > x \text{ or } 11 < x$$

PTS: 2

REF: 061137a2

STA: A2.A.1

TOP: Absolute Value Inequalities

KEY: graph

33 ANS:

$$\text{Sum } \frac{-b}{a} = -\frac{11}{5}. \text{ Product } \frac{c}{a} = -\frac{3}{5}$$

PTS: 2

REF: 061030a2

STA: A2.A.20

TOP: Roots of Quadratics

34 ANS: 3

$$S = \frac{-b}{a} = \frac{-(-3)}{4} = \frac{3}{4}. P = \frac{c}{a} = \frac{-8}{4} = -2$$

PTS: 2

REF: fall0912a2

STA: A2.A.21

TOP: Roots of Quadratics

KEY: basic

35 ANS: 3

$$\frac{-b}{a} = \frac{-6}{2} = -3. \frac{c}{a} = \frac{4}{2} = 2$$

PTS: 2

REF: 011121a2

STA: A2.A.21

TOP: Roots of Quadratics

KEY: basic

36 ANS:

$$x^2 - 6x - 27 = 0, \frac{-b}{a} = 6. \frac{c}{a} = -27. \text{ If } a = 1 \text{ then } b = -6 \text{ and } c = -27$$

PTS: 4

REF: 061130a2

STA: A2.A.21

TOP: Roots of Quadratics

KEY: basic

37 ANS: 4

$$6x - x^3 - x^2 = -x(x^2 + x - 6) = -x(x + 3)(x - 2)$$

PTS: 2

REF: fall0917a2

STA: A2.A.7

TOP: Factoring Polynomials

KEY: single variable

38 ANS: 4

$$12x^4 + 10x^3 - 12x^2 = 2x^2(6x^2 + 5x - 6) = 2x^2(2x + 3)(3x - 2)$$

PTS: 2

REF: 061008a2

STA: A2.A.7

TOP: Factoring Polynomials

KEY: single variable

39 ANS:

$$10ax^2 - 23ax - 5a = a(10x^2 - 23x - 5) = a(5x + 1)(2x - 5)$$

PTS: 2

REF: 081028a2

STA: A2.A.7

TOP: Factoring Polynomials

KEY: multiple variables

40 ANS:

$$12t^8 - 75t^4 = 3t^4(4t^4 - 25) = 3t^4(2t^2 + 5)(2t^2 - 5)$$

PTS: 2

REF: 061133a2

STA: A2.A.7

TOP: Factoring the Difference of Perfect Squares

KEY: binomial

41 ANS: 4

$$\frac{3 \pm \sqrt{(-3)^2 - 4(1)(-9)}}{2(1)} = \frac{3 \pm \sqrt{45}}{2} = \frac{3 \pm 3\sqrt{5}}{2}$$

PTS: 2

REF: 061009a2

STA: A2.A.25

TOP: Quadratic Formula

42 ANS: 3

$$\frac{-7 \pm \sqrt{7^2 - 4(2)(-3)}}{2(2)} = \frac{-7 \pm \sqrt{73}}{4}$$

PTS: 2

REF: 081009a2

STA: A2.A.25

TOP: Quadratic Formula

43 ANS: 4

$$b^2 - 4ac = 3^2 - 4(9)(-4) = 9 + 144 = 153$$

PTS: 2

REF: 081016a2

STA: A2.A.2

TOP: Using the Discriminant

KEY: determine nature of roots given equation

44 ANS: 3

$$b^2 - 4ac = (-10)^2 - 4(1)(25) = 100 - 100 = 0$$

PTS: 2

REF: 011102a2

STA: A2.A.2

TOP: Using the Discriminant

KEY: determine nature of roots given equation

45 ANS:

$$b^2 - 4ac = 0$$

$$k^2 - 4(1)(4) = 0$$

$$k^2 - 16 = 0$$

$$(k + 4)(k - 4) = 0$$

$$k = \pm 4$$

PTS: 2

REF: 061028a2

STA: A2.A.2

TOP: Using the Discriminant

KEY: determine equation given nature of roots

46 ANS: 2

PTS: 2

REF: 061122a2

STA: A2.A.24

TOP: Completing the Square

47 ANS: 2

$$x^2 + 2 = 6x$$

$$x^2 - 6x = -2$$

$$x^2 - 6x + 9 = -2 + 9$$

$$(x - 3)^2 = 7$$

PTS: 2

REF: 011116a2

STA: A2.A.24

TOP: Completing the Square

48 ANS:

$$3 \pm \sqrt{7}, \quad 2x^2 - 12x + 4 = 0$$

$$x^2 - 6x + 2 = 0$$

$$x^2 - 6x = -2$$

$$x^2 - 6x + 9 = -2 + 9$$

$$(x - 3)^2 = 7$$

$$x - 3 = \pm \sqrt{7}$$

$$x = 3 \pm \sqrt{7}$$

PTS: 4

REF: fall0936a2

STA: A2.A.24

TOP: Completing the Square

49 ANS: 1

$$y \geq x^2 - x - 6$$

$$y \geq (x - 3)(x + 2)$$

PTS: 2

REF: 061017a2

STA: A2.A.4

TOP: Quadratic Inequalities

KEY: two variables

50 ANS: 3

$$x^2 - 3x - 10 > 0 \quad \text{or}$$

$$(x - 5)(x + 2) > 0 \quad x - 5 < 0 \text{ and } x + 2 < 0$$

$$x - 5 > 0 \text{ and } x + 2 > 0 \quad x < 5 \text{ and } x < -2$$

$$x > 5 \text{ and } x > -2 \quad x < -2$$

$$x > 5$$

PTS: 2

REF: 011115a2

STA: A2.A.4

TOP: Quadratic Inequalities

KEY: one variable

51 ANS: 2

$$x^2 - x - 6 = 3x - 6$$

$$x^2 - 4x = 0$$

$$x(x - 4) = 0$$

$$x = 0, 4$$

PTS: 2

REF: 081015a2

STA: A2.A.3

TOP: Quadratic-Linear Systems

KEY: equations

52 ANS:

$$\left(-\frac{9}{2}, \frac{1}{2}\right) \text{ and } \left(\frac{1}{2}, \frac{11}{2}\right). \quad y = x + 5 \quad . \quad 4x^2 + 17x - 4 = x + 5$$

$$y = 4x^2 + 17x - 4 \quad 4x^2 + 16x - 9 = 0$$

$$(2x + 9)(2x - 1) = 0$$

$$x = -\frac{9}{2} \text{ and } x = \frac{1}{2}$$

$$y = -\frac{9}{2} + 5 = \frac{1}{2} \text{ and } y = \frac{1}{2} + 5 = \frac{11}{2}$$

PTS: 6 REF: 061139a2 STA: A2.A.3 TOP: Quadratic-Linear Systems
 KEY: equations

53 ANS: 2 PTS: 2 REF: 011114a2 STA: A2.N.3
 TOP: Operations with Polynomials

54 ANS:

$$\frac{4}{9}x^2 - \frac{4}{3}x + 1. \quad \left(\frac{2}{3}x - 1\right)^2 = \left(\frac{2}{3}x - 1\right)\left(\frac{2}{3}x - 1\right) = \frac{4}{9}x^2 - \frac{2}{3}x - \frac{2}{3}x + 1 = \frac{4}{9}x^2 - \frac{4}{3}x + 1$$

PTS: 2 REF: 081034a2 STA: A2.N.3 TOP: Operations with Polynomials
 55 ANS:

$$6y^3 - \frac{37}{10}y^2 - \frac{1}{5}y. \quad \left(\frac{1}{2}y^2 - \frac{1}{3}y\right)\left(12y + \frac{3}{5}\right) = 6y^3 + \frac{3}{10}y^2 - 4y^2 - \frac{1}{5}y = 6y^3 - \frac{37}{10}y^2 - \frac{1}{5}y$$

PTS: 2 REF: 061128a2 STA: A2.N.3 TOP: Operations with Polynomials
 56 ANS: 1 PTS: 2 REF: fall0914a2 STA: A2.A.8
 TOP: Negative and Fractional Exponents

57 ANS: 3

$$\frac{3^{-2}}{(-2)^{-3}} = \frac{\frac{1}{9}}{-\frac{1}{8}} = -\frac{8}{9}$$

PTS: 2 REF: 061003a2 STA: A2.A.8 TOP: Negative and Fractional Exponents
 58 ANS: 2

$$\left(\frac{w^{-5}}{w^{-9}}\right)^{\frac{1}{2}} = (w^4)^{\frac{1}{2}} = w^2$$

PTS: 2 REF: 081011a2 STA: A2.A.8 TOP: Negative and Fractional Exponents

59 ANS: 2

$$\frac{x^{-1} - 1}{x - 1} = \frac{\frac{1}{x} - 1}{x - 1} = \frac{1 - x}{x(x - 1)} = \frac{-(x - 1)}{x(x - 1)} = -\frac{1}{x}$$

PTS: 2 REF: 081018a2 STA: A2.A.9 TOP: Negative Exponents

60 ANS:

$$\frac{12x^2}{y^9} \cdot \frac{3x^{-4}y^5}{(2x^3y^{-7})^{-2}} = \frac{3y^5(2x^3y^{-7})^2}{x^4} = \frac{3y^5(4x^6y^{-14})}{x^4} = \frac{12x^6y^{-9}}{x^4} = \frac{12x^2}{y^9}$$

PTS: 2 REF: 061134a2 STA: A2.A.9 TOP: Negative Exponents

61 ANS:


2,298.65.

PTS: 2 REF: fall0932a2 STA: A2.A.12 TOP: Evaluating Exponential Expressions

62 ANS:

$$e^{3\ln 2} = e^{\ln 2^3} = e^{\ln 8} = 8$$

PTS: 2 REF: 061131a2 STA: A2.A.12 TOP: Evaluating Exponential Expressions

63 ANS: 2

$$8^2 = 64$$

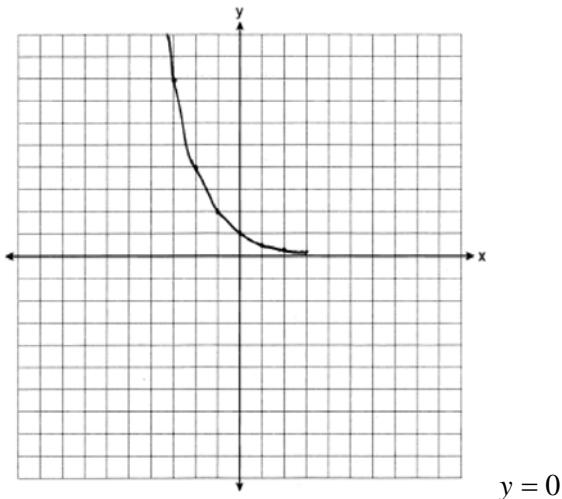
PTS: 2 REF: fall0909a2 STA: A2.A.18 TOP: Evaluating Logarithmic Expressions

64 ANS: 4

PTS: 2 REF: 011124a2 STA: A2.A.18

TOP: Evaluating Logarithmic Expressions

65 ANS:



PTS: 2

REF: 061031a2

STA: A2.A.53

TOP: Graphing Exponential Functions

66 ANS: 2

$$f^{-1}(x) = \log_4 x$$

PTS: 2

REF: fall0916a2

STA: A2.A.54

TOP: Graphing Logarithmic Functions

67 ANS: 1

$$2\log x - (3\log y + \log z) = \log x^2 - \log y^3 - \log z = \log \frac{x^2}{y^3 z}$$

PTS: 2

REF: 061010a2

STA: A2.A.19

TOP: Properties of Logarithms

68 ANS: 4

PTS: 2

REF: 061120a2

STA: A2.A.19

TOP: Properties of Logarithms

KEY: splitting logs

69 ANS: 3

$$x = 5^4 = 625$$

PTS: 2

REF: 061106a2

STA: A2.A.28

TOP: Logarithmic Equations

KEY: basic

70 ANS: 4

$$2\log_4(5x) = 3$$

$$\log_4(5x) = \frac{3}{2}$$

$$5x = 4^{\frac{3}{2}}$$

$$5x = 8$$

$$x = \frac{8}{5}$$

PTS: 2

REF: fall0921a2

STA: A2.A.28

TOP: Logarithmic Equations

KEY: advanced

71 ANS:

$$x = -\frac{1}{3}, -1 \quad \log_{x+3} \frac{x^3 + x - 2}{x} = 2$$

$$\frac{x^3 + x - 2}{x} = (x+3)^2$$

$$\frac{x^3 + x - 2}{x} = x^2 + 6x + 9$$

$$x^3 + x - 2 = x^3 + 6x^2 + 9x$$

$$0 = 6x^2 + 8x + 2$$

$$0 = 3x^2 + 4x + 1$$

$$0 = (3x+1)(x+1)$$

$$x = -\frac{1}{3}, -1$$

PTS: 6

REF: 081039a2

STA: A2.A.28

TOP: Logarithmic Equations

KEY: basic

72 ANS:

$$\ln(T - T_0) = -kt + 4.718 \quad . \quad \ln(T - 68) = -0.104(10) + 4.718.$$

$$\ln(150 - 68) = -k(3) + 4.718 \quad \ln(T - 68) = 3.678$$

$$4.407 \approx -3k + 4.718 \quad T - 68 \approx 39.6$$

$$k \approx 0.104$$

$$T \approx 108$$

PTS: 6

REF: 011139a2

STA: A2.A.28

TOP: Logarithmic Equations

KEY: advanced

73 ANS: 3

$$4^{x^2 + 4x} = 2^{-6}. \quad 2x^2 + 8x = -6$$

$$(2^2)^{x^2 + 4x} = 2^{-6} \quad 2x^2 + 8x + 6 = 0$$

$$2^{2x^2 + 8x} = 2^{-6} \quad x^2 + 4x + 3 = 0 \\ (x+3)(x+1) = 0$$

$$x = -3 \quad x = -1$$

PTS: 2

REF: 061015a2

STA: A2.A.27

TOP: Exponential Equations

KEY: common base shown

74 ANS: 2

$$4^{2x+5} = 8^{3x}$$

$$(2^2)^{2x+5} = (2^3)^{3x}$$

$$2^{4x+10} = 2^{9x}$$

$$4x + 10 = 9x$$

$$10 = 5x$$

$$2 = x$$

PTS: 2

REF: 061105a2

STA: A2.A.27

TOP: Exponential Equations

KEY: common base not shown

75 ANS: 4

$$9^{3x+1} = 27^{x+2}$$

$$(3^2)^{3x+1} = (3^3)^{x+2}$$

$$3^{6x+2} = 3^{3x+6}$$

$$6x + 2 = 3x + 6$$

$$3x = 4$$

$$x = \frac{4}{3}$$

PTS: 2

REF: 081008a2

STA: A2.A.27

TOP: Exponential Equations

KEY: common base not shown

76 ANS:

$$16^{2x+3} = 64^{x+2}$$

$$(4^2)^{2x+3} = (4^3)^{x+2}$$

$$4x + 6 = 3x + 6$$

$$x = 0$$

PTS: 2

REF: 011128a2

STA: A2.A.27

TOP: Exponential Equations

KEY: common base not shown

77 ANS: 3

$$75000 = 25000e^{.0475t}$$

$$3 = e^{.0475t}$$

$$\ln 3 = \ln e^{.0475t}$$

$$\frac{\ln 3}{.0475} = \frac{.0475t \cdot \ln e}{.0475}$$

$$23.1 \approx t$$

PTS: 2 REF: 061117a2 STA: A2.A.6 TOP: Exponential Growth

78 ANS: 1

$${}_9C_3 a^6 (-4b)^3 = -5376a^6 b^3$$

PTS: 2 REF: 061126a2 STA: A2.A.36 TOP: Binomial Expansions

79 ANS: 1

$${}_5C_3 (3x)^2 (-2)^3 = 10 \cdot 9x^2 \cdot -8 = -720x^2$$

PTS: 2 REF: fall0919a2 STA: A2.A.36 TOP: Binomial Expansions

80 ANS:

$$32x^5 - 80x^4 + 80x^3 - 40x^2 + 10x - 1. {}_5C_0 (2x)^5 (-1)^0 = 32x^5. {}_5C_1 (2x)^4 (-1)^1 = -80x^4. {}_5C_2 (2x)^3 (-1)^2 = 80x^3.$$

$${}_5C_3 (2x)^2 (-1)^3 = -40x^2. {}_5C_4 (2x)^1 (-1)^4 = 10x. {}_5C_5 (2x)^0 (-1)^5 = -1$$

PTS: 4 REF: 011136a2 STA: A2.A.36 TOP: Binomial Expansions

81 ANS: 2

$$x^3 + x^2 - 2x = 0$$

$$x(x^2 + x - 2) = 0$$

$$x(x + 2)(x - 1) = 0$$

$$x = 0, -2, 1$$

PTS: 2 REF: 011103a2 STA: A2.A.26 TOP: Solving Polynomial Equations

82 ANS:

$$\pm\frac{3}{2}, -\frac{1}{2}. \quad 8x^3 + 4x^2 - 18x - 9 = 0$$

$$4x^2(2x+1) - 9(2x+1) = 0$$

$$(4x^2 - 9)(2x+1) = 0$$

$$4x^2 - 9 = 0 \text{ or } 2x+1 = 0$$

$$(2x+3)(2x-3) = 0 \quad x = -\frac{1}{2}$$

$$x = \pm\frac{3}{2}$$

PTS: 4

REF: fall0937a2

STA: A2.A.26

TOP: Solving Polynomial Equations

83 ANS: 2

The roots are $-1, 2, 3$.

PTS: 2

REF: 081023a2

STA: A2.A.50

TOP: Solving Polynomial Equations

84 ANS: 4

PTS: 2

REF: 061005a2

STA: A2.A.50

TOP: Solving Polynomial Equations

85 ANS: 4

$$(3 + \sqrt{5})(3 - \sqrt{5}) = 9 - \sqrt{25} = 4$$

PTS: 2

REF: 081001a2

STA: A2.N.2

TOP: Operations with Radicals

86 ANS: 4

$$4ab\sqrt{2b} - 3a\sqrt{9b^2}\sqrt{2b} + 7ab\sqrt{6b} = 4ab\sqrt{2b} - 9ab\sqrt{2b} + 7ab\sqrt{6b} = -5ab\sqrt{2b} + 7ab\sqrt{6b}$$

PTS: 2

REF: fall0918a2

STA: A2.A.14

TOP: Operations with Radicals

KEY: with variables | index = 2

87 ANS:

$$\frac{\sqrt{108x^5y^8}}{\sqrt{6xy^5}} = \sqrt{18x^4y^3} = 3x^2y\sqrt{2y}$$

PTS: 2

REF: 011133a2

STA: A2.A.14

TOP: Operations with Radicals

KEY: with variables | index = 2

88 ANS:

$$5\sqrt{3x^3} - 2\sqrt{27x^3} = 5\sqrt{x^2}\sqrt{3x} - 2\sqrt{9x^2}\sqrt{3x} = 5x\sqrt{3x} - 6x\sqrt{3x} = -x\sqrt{3x}$$

PTS: 2

REF: 061032a2

STA: A2.N.2

TOP: Operations with Radicals

89 ANS: 3

$$\frac{3}{\sqrt{3a^2b}} = \frac{3}{a\sqrt{3b}} \cdot \frac{\sqrt{3b}}{\sqrt{3b}} = \frac{3\sqrt{3b}}{3ab} = \frac{\sqrt{3b}}{ab}$$

PTS: 2 REF: 081019a2 STA: A2.A.15 TOP: Rationalizing Denominators
 KEY: index = 2

90 ANS: 4

$$\frac{2x+4}{\sqrt{x+2}} \cdot \frac{\sqrt{x+2}}{\sqrt{x+2}} = \frac{2(x+2)\sqrt{x+2}}{x+2} = 2\sqrt{x+2}$$

PTS: 2 REF: 011122a2 STA: A2.A.15 TOP: Rationalizing Denominators
 KEY: index = 2

91 ANS: 1

$$\frac{\sqrt{3}+5}{\sqrt{3}-5} \cdot \frac{\sqrt{3}+5}{\sqrt{3}+5} = \frac{3+5\sqrt{3}+5\sqrt{3}+25}{3-25} = \frac{28+10\sqrt{3}}{-22} = -\frac{14+5\sqrt{3}}{11}$$

PTS: 2 REF: 061012a2 STA: A2.N.5 TOP: Rationalizing Denominators

92 ANS: 3

$$\frac{4}{5-\sqrt{13}} \cdot \frac{5+\sqrt{13}}{5+\sqrt{13}} = \frac{4(5+\sqrt{13})}{25-13} = \frac{5+\sqrt{13}}{3}$$

PTS: 2 REF: 061116a2 STA: A2.N.5 TOP: Rationalizing Denominators

93 ANS:

$$\frac{5(3+\sqrt{2})}{7} \cdot \frac{5}{3-\sqrt{2}} \times \frac{3+\sqrt{2}}{3+\sqrt{2}} = \frac{5(3+\sqrt{2})}{9-2} = \frac{5(3+\sqrt{2})}{7}$$

PTS: 2 REF: fall0928a2 STA: A2.N.5 TOP: Rationalizing Denominators

94 ANS: 1

PTS: 2 REF: 061018a2 STA: A2.A.22

TOP: Solving Radicals

KEY: extraneous solutions

95 ANS: 3

$$3x+16=(x+2)^2 \quad . \quad -4 \text{ is an extraneous solution.}$$

$$3x+16=x^2+4x+4$$

$$0=x^2+x-12$$

$$0=(x+4)(x-3)$$

$$x=-4 \quad x=3$$

PTS: 2 REF: 061121a2 STA: A2.A.22 TOP: Solving Radicals
 KEY: extraneous solutions

96 ANS: 4

$$x^{-\frac{2}{5}} = \frac{1}{x^{\frac{2}{5}}} = \frac{1}{\sqrt[5]{x^2}}$$

- PTS: 2 REF: 011118a2 STA: A2.A.10 TOP: Fractional Exponents as Radicals
 97 ANS: 2 PTS: 2 REF: 061011a2 STA: A2.A.10
 TOP: Fractional Exponents as Radicals

98 ANS: 1

$$\sqrt[4]{16x^2y^7} = 16^{\frac{1}{4}}x^{\frac{2}{4}}y^{\frac{7}{4}} = 2x^{\frac{1}{2}}y^{\frac{7}{4}}$$

- PTS: 2 REF: 061107a2 STA: A2.A.11 TOP: Radicals as Fractional Exponents
 99 ANS: 3
 $\sqrt{-300} = \sqrt{100}\sqrt{-1}\sqrt{3}$

- PTS: 2 REF: 061006a2 STA: A2.N.6 TOP: Square Roots of Negative Numbers
 100 ANS: 1 PTS: 2 REF: 061019a2 STA: A2.N.7
 TOP: Imaginary Numbers

101 ANS: 1

$$2i^2 + 3i^3 = 2(-1) + 3(-i) = -2 - 3i$$

- PTS: 2 REF: 081004a2 STA: A2.N.7 TOP: Imaginary Numbers
 102 ANS: 2 PTS: 2 REF: 081024a2 STA: A2.N.8
 TOP: Conjugates of Complex Numbers
 103 ANS: 4 PTS: 2 REF: 011111a2 STA: A2.N.8
 TOP: Conjugates of Complex Numbers

104 ANS: 2

$$(3 - 7i)(3 - 7i) = 9 - 21i - 21i + 49i^2 = 9 - 42i - 49 = -40 - 42i$$

- PTS: 2 REF: fall0901a2 STA: A2.N.9
 TOP: Multiplication and Division of Complex Numbers
 105 ANS:

no solution. $\frac{4x}{x-3} = 2 + \frac{12}{x-3}$

$$\frac{4x-12}{x-3} = 2$$

$$\frac{4(x-3)}{x-3} = 2$$

$$4 \neq 2$$

- PTS: 2 REF: fall0930a2 STA: A2.A.23 TOP: Solving Rationals
 KEY: rational solutions

106 ANS:

$$\frac{1}{3} - \frac{1}{x+3} - \frac{2}{3-x} = \frac{4}{x^2-9}$$

$$\frac{1}{x+3} + \frac{2}{x-3} = \frac{4}{x^2-9}$$

$$\frac{x-3+2(x+3)}{(x+3)(x-3)} = \frac{4}{(x+3)(x-3)}$$

$$x-3+2x+6=4$$

$$3x=1$$

$$x=\frac{1}{3}$$

PTS: 4

REF: 081036a2

STA: A2.A.23

TOP: Solving Rationals

KEY: rational solutions

107 ANS: 2

$$\frac{\frac{x}{4}-\frac{1}{x}}{\frac{1}{2x}+\frac{1}{4}} = \frac{\frac{x^2-4}{4x}}{\frac{8x}{8x}} = \frac{(x+2)(x-2)}{4x} \times \frac{8x}{2(x+2)} = x-2$$

PTS: 2

REF: fall0920a2

STA: A2.A.17

TOP: Complex Fractions

108 ANS:

$$\frac{\frac{1}{2}-\frac{4}{d}}{\frac{1}{d}+\frac{3}{2d}} = \frac{\frac{d-8}{2d}}{\frac{2d+3d}{2d^2}} = \frac{d-8}{2d} \times \frac{2d^2}{5d} = \frac{d-8}{5}$$

PTS: 2

REF: 061035a2

STA: A2.A.17

TOP: Complex Fractions

109 ANS:

$$12 \cdot 6 = 9w$$

$$8 = w$$

PTS: 2

REF: 011130a2

STA: A2.A.5

TOP: Inverse Variation

110 ANS: 4

$$y - 2 \sin \theta = 3$$

$$y = 2 \sin \theta + 3$$

$$f(\theta) = 2 \sin \theta + 3$$

PTS: 2

REF: fall0927a2

STA: A2.A.40

TOP: Functional Notation

111 ANS: 2

$$f(10) = \frac{-10}{(-10)^2 - 16} = \frac{-10}{84} = -\frac{5}{42}$$

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|-----|---|---|--|--|
| 111 | ANS: 2
PTS: 2
TOP: Families of Functions | REF: 061102a2
PTS: 2
TOP: Identifying the Equation of a Graph | STA: A2.A.41
REF: 011119a2
TOP: Identifying the Equation of a Graph | TOP: Functional Notation
STA: A2.A.52 |
| 112 | ANS: 3
TOP: Defining Functions | PTS: 2
TOP: Defining Functions | REF: 061004a2
REF: 061108a2
TOP: Defining Functions | STA: A2.A.52
STA: A2.A.52
TOP: Defining Functions |
| 113 | ANS: 1
TOP: Identifying the Equation of a Graph | PTS: 2
TOP: Identifying the Equation of a Graph | REF: 061004a2
REF: 061108a2
TOP: Identifying the Equation of a Graph | STA: A2.A.52
STA: A2.A.52
TOP: Identifying the Equation of a Graph |
| 114 | ANS: 2
TOP: Defining Functions | PTS: 2
TOP: Defining Functions | REF: 061108a2
REF: 061101a2
TOP: Defining Functions | STA: A2.A.52
STA: A2.A.38
KEY: graphs |
| 115 | ANS: 4
TOP: Defining Functions | PTS: 2
TOP: Defining Functions | REF: fall0908a2
REF: 061114a2
TOP: Defining Functions | STA: A2.A.38
STA: A2.A.38
KEY: graphs |
| 116 | ANS: 4
TOP: Defining Functions | PTS: 2
TOP: Defining Functions | REF: 011101a2
REF: 061013a2
TOP: Defining Functions | STA: A2.A.38
STA: A2.A.38
KEY: graphs |
| 117 | ANS: 3
TOP: Defining Functions | PTS: 2
TOP: Defining Functions | REF: 061114a2
REF: 061013a2
TOP: Defining Functions | STA: A2.A.38
STA: A2.A.38
KEY: graphs |
| 118 | ANS: 1
TOP: Defining Functions | PTS: 2
TOP: Defining Functions | REF: 061013a2
REF: fall0906a2
TOP: Defining Functions | STA: A2.A.38
STA: A2.A.43
TOP: Defining Functions |
| 119 | ANS: 4
(4) fails the horizontal line test. Not every element of the range corresponds to only one element of the domain. | | | |

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|-----|---|--|------------------------------|
| 120 | ANS: 3
(1) and (4) fail the horizontal line test and are not one-to-one. Not every element of the range corresponds to only one element of the domain. (2) fails the vertical line test and is not a function. Not every element of the domain corresponds to only one element of the range. | PTS: 2
REF: fall0906a2
TOP: Defining Functions | STA: A2.A.43
STA: A2.A.39 |
|-----|---|--|------------------------------|

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|-----|---|---------------------------------|---|---|
| 121 | ANS: 3
TOP: Domain and Range | PTS: 2
TOP: Domain and Range | REF: 081020a2
REF: fall0923a2
TOP: Domain and Range | STA: A2.A.43
STA: A2.A.39
KEY: real domain |
| 122 | ANS: 4
TOP: Domain and Range | PTS: 2
TOP: Domain and Range | REF: 061112a2
REF: 081003a2
TOP: Domain and Range | STA: A2.A.39
STA: A2.A.51 |
| 123 | ANS: 2
TOP: Domain and Range | PTS: 2
TOP: Domain and Range | REF: 081003a2
REF: 011132a2
TOP: Domain and Range | STA: A2.A.51
STA: A2.A.51
TOP: Domain and Range |
| 124 | ANS:
D: $-5 \leq x \leq 8$. R: $-3 \leq y \leq 2$ | | | |

- | | | | |
|-----|--|--|------------------------------|
| 125 | ANS: 3
$f(4) = \frac{1}{2}(4) - 3 = -1$. $g(-1) = 2(-1) + 5 = 3$ | PTS: 2
REF: 011132a2
TOP: Domain and Range | STA: A2.A.51
STA: A2.A.51 |
|-----|--|--|------------------------------|

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|-----|--|---|------------------------------|
| 125 | ANS: 3
$f(4) = \frac{1}{2}(4) - 3 = -1$. $g(-1) = 2(-1) + 5 = 3$ | PTS: 2
REF: fall0902a2
TOP: Compositions of Functions | STA: A2.A.42
KEY: numbers |
|-----|--|---|------------------------------|

126 ANS: 2

$$6(x^2 - 5) = 6x^2 - 30$$

PTS: 2 REF: 011109a2 STA: A2.A.42 TOP: Compositions of Functions
 KEY: variables

127 ANS:

$$7. f(-3) = (-3)^2 - 6 = 3. g(x) = 2^3 - 1 = 7.$$

PTS: 2 REF: 061135a2 STA: A2.A.42 TOP: Compositions of Functions
 KEY: numbers

128 ANS: 3 PTS: 2

REF: 081027a2 STA: A2.A.44

TOP: Inverse of Functions

KEY: equations

129 ANS:

$$y = x^2 - 6. f^{-1}(x) \text{ is not a function.}$$

$$x = y^2 - 6$$

$$x + 6 = y^2$$

$$\pm\sqrt{x+6} = y$$

PTS: 2 REF: 061132a2 STA: A2.A.44 TOP: Inverse of Functions
 KEY: equations

130 ANS: 2 PTS: 2 REF: fall0926a2 STA: A2.A.46

TOP: Transformations with Functions and Relations

131 ANS: 1 PTS: 2 REF: 081022a2 STA: A2.A.46

TOP: Transformations with Functions and Relations

132 ANS: 4 PTS: 2 REF: 061026a2 STA: A2.A.29
 TOP: Sequences

133 ANS: 1

common difference is 2. $b_n = x + 2n$

$$10 = x + 2(1)$$

$$8 = x$$

PTS: 2 REF: 081014a2 STA: A2.A.29 TOP: Sequences

134 ANS: 3 PTS: 2 REF: 061001a2 STA: A2.A.30
 TOP: Sequences135 ANS: 3 PTS: 2 REF: 011110a2 STA: A2.A.30
 TOP: Sequences

136 ANS: 3

$$27r^{4-1} = 64$$

$$r^3 = \frac{64}{27}$$

$$r = \frac{4}{3}$$

PTS: 2 REF: 081025a2 STA: A2.A.31 TOP: Conjugates of Complex Numbers
 137 ANS: 3

$$a_n = 5(-2)^{n-1}$$

$$a_{15} = 5(-2)^{15-1} = 81,920$$

PTS: 2 REF: 011105a2 STA: A2.A.32 TOP: Sequences
 138 ANS: 1

$$a_n = -\sqrt{5}(-\sqrt{2})^{n-1}$$

$$a_{15} = -\sqrt{5}(-\sqrt{2})^{15-1} = -\sqrt{5}(-\sqrt{2})^{14} = -\sqrt{5} \cdot 2^7 = -128\sqrt{5}$$

PTS: 2 REF: 061109a2 STA: A2.A.32 TOP: Sequences
 139 ANS:

$$-3, -5, -8, -12$$

PTS: 2 REF: fall0934a2 STA: A2.A.33 TOP: Recursive Sequences
 140 ANS: 1

n	3	4	5	Σ
$-r^2 + r$	$-3^2 + 3 = -6$	$-4^2 + 4 = -12$	$-5^2 + 5 = -20$	-38

PTS: 2 REF: 061118a2 STA: A2.N.10 TOP: Sigma Notation
 KEY: basic

141 ANS: 3

n	0	1	2	Σ
$n^2 + 2^n$	$0^2 + 2^0 = 1$	$1^2 + 2^1 = 3$	$2^2 + 2^2 = 8$	12

$$2 \times 12 = 24$$

PTS: 2 REF: fall0911a2 STA: A2.N.10 TOP: Sigma Notation
 KEY: basic

142 ANS:

$$230. \quad 10 + (1^3 - 1) + (2^3 - 1) + (3^3 - 1) + (4^3 - 1) + (5^3 - 1) = 10 + 0 + 7 + 26 + 63 + 124 = 230$$

PTS: 2 REF: 011131a2 STA: A2.N.10 TOP: Sigma Notation
 KEY: basic

143 ANS: 1 PTS: 2 REF: 061025a2 STA: A2.A.34
 TOP: Sigma Notation

144 ANS:

$$\sum_{n=1}^{15} 7n$$

PTS: 2

REF: 081029a2

STA: A2.A.34

TOP: Sigma Notation

145 ANS: 4

$$S_n = \frac{n}{2} [2a + (n-1)d] = \frac{21}{2} [2(18) + (21-1)2] = 798$$

PTS: 2

REF: 061103a2

STA: A2.A.35

TOP: Series

KEY: arithmetic

146 ANS: 1

$\cos^{-1}(5/6)$
33.55730976
Ans DMS
33°33'26.315"

$$\cos K = \frac{5}{6}$$

$$K = \cos^{-1} \frac{5}{6}$$

$$K \approx 33^\circ 33'$$

PTS: 2

REF: 061023a2

STA: A2.A.55

TOP: Trigonometric Ratios

147 ANS: 2

PTS: 2

REF: 081010a2

STA: A2.A.55

TOP: Trigonometric Ratios

148 ANS: 1

$$\sqrt{12^2 - 6^2} = \sqrt{108} = \sqrt{36}\sqrt{3} = 6\sqrt{3}. \cot J = \frac{A}{O} = \frac{6}{6\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$

PTS: 2

REF: 011120a2

STA: A2.A.55

TOP: Trigonometric Ratios

149 ANS: 3

$$2\pi \cdot \frac{5}{12} = \frac{10\pi}{12} = \frac{5\pi}{6}$$

PTS: 2

REF: 061125a2

STA: A2.M.1

TOP: Radian Measure

150 ANS: 1

$$-420 \left(\frac{\pi}{180} \right) = -\frac{7\pi}{3}$$

PTS: 2

REF: 081002a2

STA: A2.M.2

TOP: Radian Measure

KEY: radians

151 ANS: 2

$$\frac{11\pi}{12} \cdot \frac{180}{\pi} = 165$$

PTS: 2

REF: 061002a2

STA: A2.M.2

TOP: Radian Measure

KEY: degrees

152 ANS:

$3.45 \times \frac{180}{\pi}$
 197.6704393
Ans \rightarrow $197^\circ 40' 13.582''$

$$197^\circ 40'. \quad 3.45 \times \frac{180}{\pi} \approx 197^\circ 40'.$$

PTS: 2

REF: fall0931a2

STA: A2.M.2

TOP: Radian Measure

KEY: degrees

153 ANS:

$$2.5 \cdot \frac{180}{\pi} \approx 143.2^\circ$$

PTS: 2

REF: 011129a2

STA: A2.M.2

TOP: Radian Measure

KEY: degrees

154 ANS: 4

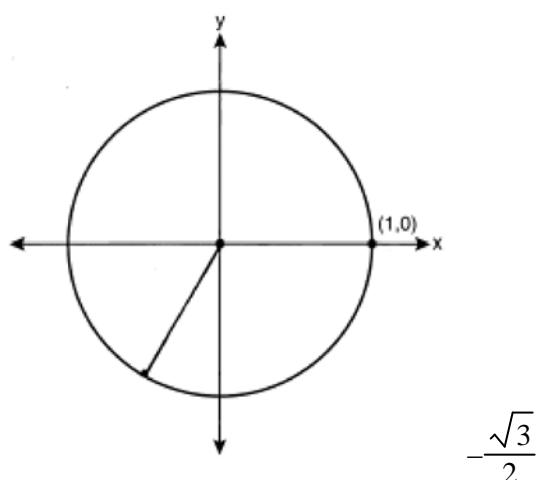
PTS: 2

REF: 081005a2

STA: A2.A.60

TOP: Unit Circle

155 ANS:



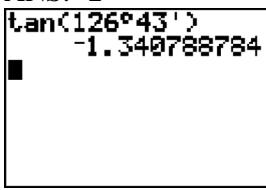
$$-\frac{\sqrt{3}}{2}$$

PTS: 2

REF: 061033a2

STA: A2.A.60

TOP: Unit Circle

- 156 ANS: 2

 PTS: 2 REF: 061115a2 STA: A2.A.66 TOP: Determining Trigonometric Functions
- 157 ANS:

$$\frac{\sqrt{13}}{2} \cdot \sin \theta = \frac{y}{\sqrt{x^2 + y^2}} = \frac{2}{\sqrt{(-3)^2 + 2^2}} = \frac{2}{\sqrt{13}}. \csc \theta = \frac{\sqrt{13}}{2}.$$
- PTS: 2 REF: fall0933a2 STA: A2.A.62 TOP: Determining Trigonometric Functions
 158 ANS: 3 PTS: 2 REF: 081007a2 STA: A2.A.64
 TOP: Using Inverse Trigonometric Functions KEY: basic
 159 ANS: 3 PTS: 2 REF: 011104a2 STA: A2.A.64
 TOP: Using Inverse Trigonometric Functions KEY: unit circle
 160 ANS: 1 PTS: 2 REF: 011112a2 STA: A2.A.64
 TOP: Using Inverse Trigonometric Functions KEY: advanced
 161 ANS: 2
 $\cos(-305^\circ + 360^\circ) = \cos(55^\circ)$
- PTS: 2 REF: 061104a2 STA: A2.A.57 TOP: Reference Angles
 162 ANS: 4
 $s = \theta r = 2 \cdot 4 = 8$
- PTS: 2 REF: fall0922a2 STA: A2.A.61 TOP: Arc Length
 KEY: arc length
- 163 ANS: 3
 Cofunctions tangent and cotangent are complementary
- PTS: 2 REF: 061014a2 STA: A2.A.58 TOP: Cofunction Trigonometric Relationships
 164 ANS: 3

$$\frac{\sin^2 \theta + \cos^2 \theta}{1 - \sin^2 \theta} = \frac{1}{\cos^2 \theta} = \sec^2 \theta$$
- PTS: 2 REF: 061123a2 STA: A2.A.58 TOP: Reciprocal Trigonometric Relationships
 165 ANS:

$$\frac{\sin^2 A}{\cos^2 A} + \frac{\cos^2 A}{\cos^2 A} = \frac{1}{\cos^2 A}$$

 $\tan^2 A + 1 = \sec^2 A$
- PTS: 2 REF: 011135a2 STA: A2.A.67 TOP: Proving Trigonometric Identities
 166 ANS: 3 PTS: 2 REF: fall0910a2 STA: A2.A.76
 TOP: Angle Sum and Difference Identities KEY: simplifying

167 ANS:

$$\begin{aligned} \frac{23}{2} \quad \cos^2 B + \sin^2 B &= 1 \quad \tan B = \frac{\sin B}{\cos B} = \frac{\frac{5}{\sqrt{41}}}{\frac{4}{\sqrt{41}}} = \frac{5}{4} \quad \tan(A+B) = \frac{\frac{2}{3} + \frac{5}{4}}{1 - \left(\frac{2}{3}\right)\left(\frac{5}{4}\right)} = \frac{\frac{8+15}{12}}{\frac{12}{12} - \frac{10}{12}} = \frac{\frac{23}{12}}{\frac{2}{12}} = \frac{23}{2} \\ \cos^2 B + \left(\frac{5}{\sqrt{41}}\right)^2 &= 1 \\ \cos^2 B + \frac{25}{41} &= \frac{41}{41} \\ \cos^2 B &= \frac{16}{41} \\ \cos B &= \frac{4}{\sqrt{41}} \end{aligned}$$

PTS: 4 REF: 081037a2 STA: A2.A.76 TOP: Angle Sum and Difference Identities
 KEY: evaluating

168 ANS:

$$\sin(45 + 30) = \sin 45 \cos 30 + \cos 45 \sin 30$$

$$= \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{\sqrt{2}}{2} \cdot \frac{1}{2} = \frac{\sqrt{6}}{4} + \frac{\sqrt{2}}{4} = \frac{\sqrt{6} + \sqrt{2}}{4}$$

PTS: 4 REF: 061136a2 STA: A2.A.76 TOP: Angle Sum and Difference Identities
 KEY: evaluating

169 ANS: 1

$$\cos^2 \theta - \cos 2\theta = \cos^2 \theta - (\cos^2 \theta - \sin^2 \theta) = \sin^2 \theta$$

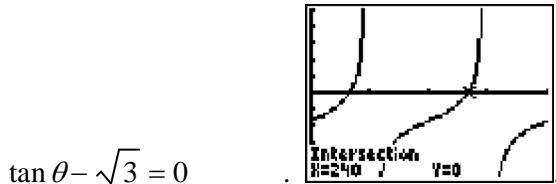
PTS: 2 REF: 061024a2 STA: A2.A.77 TOP: Double Angle Identities
 KEY: simplifying

170 ANS: 3

$$\begin{aligned} \left(\frac{2}{3}\right)^2 + \cos^2 A &= 1 \quad \sin 2A = 2 \sin A \cos A \\ \cos^2 A &= \frac{5}{9} \quad = 2\left(\frac{2}{3}\right)\left(\frac{\sqrt{5}}{3}\right) \\ \cos A &= \pm \frac{\sqrt{5}}{3}, \text{ sin } A \text{ is acute.} \quad = \frac{4\sqrt{5}}{9} \end{aligned}$$

PTS: 2 REF: 011107a2 STA: A2.A.77 TOP: Double Angle Identities
 KEY: evaluating

171 ANS: 1



$$\tan \theta - \sqrt{3} = 0$$

$$\tan \theta = \sqrt{3}$$

$$\theta = \tan^{-1} \sqrt{3}$$

$$\theta = 60, 240$$

PTS: 2 REF: fall0903a2 STA: A2.A.68 TOP: Trigonometric Equations
KEY: basic

172 ANS:

$$45, 225 \quad 2\tan C - 3 = 3\tan C - 4$$

$$1 = \tan C$$

$$\tan^{-1} 1 = C$$

$$C = 45, 225$$

PTS: 2 REF: 081032a2 STA: A2.A.68 TOP: Trigonometric Equations
KEY: basic

173 ANS:

$$0, 60, 180, 300. \quad \sin 2\theta = \sin \theta$$

$$\sin 2\theta - \sin \theta = 0$$

$$2\sin \theta \cos \theta - \sin \theta = 0$$

$$\sin \theta(2\cos \theta - 1) = 0$$

$$\sin \theta = 0 \quad 2\cos \theta - 1 = 0$$

$$\theta = 0, 180 \quad \cos \theta = \frac{1}{2}$$

$$\theta = 60, 300$$

PTS: 4 REF: 061037a2 STA: A2.A.68 TOP: Trigonometric Equations
KEY: double angle identities

174 ANS: 2

$$\frac{2\pi}{b} = \frac{2\pi}{3}$$

PTS: 2 REF: 061111a2 STA: A2.A.69
TOP: Properties of Graphs of Trigonometric Functions

KEY: period

175 ANS: 4

$$\frac{2\pi}{b} = \frac{2\pi}{\frac{1}{3}} = 6\pi$$

PTS: 2 REF: 061027a2 STA: A2.A.69

TOP: Properties of Graphs of Trigonometric Functions

KEY: period

176 ANS: 3

$$\text{period} = \frac{2\pi}{b} = \frac{2\pi}{3\pi} = \frac{2}{3}$$

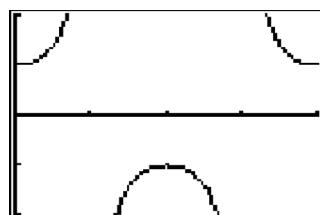
PTS: 2 REF: 081026a2 STA: A2.A.70 TOP: Graphing Trigonometric Functions

KEY: recognize

177 ANS: 3

```
Plot1 Plot2 Plot3
Y1=1/cos(X)
Y2=
Y3=
Y4=
Y5=
Y6=
Y7=
```

```
WINDOW
Xmin=0
Xmax=6.2831853...
Xscl=1.5707963...
Ymin=-2
Ymax=2
Yscl=1
Xres=1
```

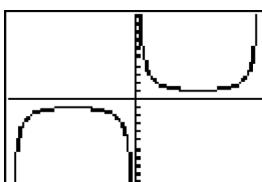


PTS: 2 REF: 061020a2 STA: A2.A.71 TOP: Graphing Trigonometric Functions

178 ANS: 1

```
Plot1 Plot2 Plot3
Y1=sin(X)
Y2=
Y3=
Y4=
Y5=
Y6=
Y7=
```

```
WINDOW
Xmin=-3.141592...
Xmax=3.1415926...
Xscl=0
Ymin=-10
Ymax=10
Yscl=1
Xres=1
```



PTS: 2 REF: 011123a2 STA: A2.A.71 TOP: Graphing Trigonometric Functions

179 ANS: 3

PTS: 2

REF: fall0913a2

STA: A2.A.65

TOP: Graphing Trigonometric Functions

180 ANS: 3

PTS: 2

REF: 061119a2

STA: A2.A.65

TOP: Graphing Trigonometric Functions

181 ANS: 3

PTS: 2

REF: 061022a2

STA: A2.A.63

TOP: Domain and Range

182 ANS: 2

$$K = \frac{1}{2}(10)(18)\sin 120 = 45\sqrt{3} \approx 78$$

PTS: 2 REF: fall0907a2 STA: A2.A.74 TOP: Using Trigonometry to Find Area

KEY: basic

183 ANS: 3

$$K = (10)(18)\sin 46 \approx 129$$

PTS: 2 REF: 081021a2 STA: A2.A.74 TOP: Using Trigonometry to Find Area

KEY: parallelograms

184 ANS:

$$K = ab \sin C = 24 \cdot 30 \sin 57 \approx 604$$

PTS: 2 REF: 061034a2 STA: A2.A.74 TOP: Using Trigonometry to Find Area

KEY: parallelograms

185 ANS:

$$\frac{12}{\sin 32} = \frac{10}{\sin B} \quad . \quad C \approx 180 - (32 + 26.2) \approx 121.8. \quad \frac{12}{\sin 32} = \frac{c}{\sin 121.8}$$

$$B = \sin^{-1} \frac{10 \sin 32}{12} \approx 26.2$$

$$c = \frac{12 \sin 121.8}{\sin 32} \approx 19.2$$

PTS: 4 REF: 011137a2 STA: A2.A.73 TOP: Law of Sines

KEY: basic

186 ANS: 2

$$\frac{10}{\sin 35} = \frac{13}{\sin B} \quad . \quad 35 + 48 < 180$$

$$B \approx 48, 132 \quad 35 + 132 < 180$$

PTS: 2 REF: 011113a2 STA: A2.A.75 TOP: Law of Sines - The Ambiguous Case

187 ANS: 3

$$\frac{59.2}{\sin 74} = \frac{60.3}{\sin C} \quad 180 - 78.3 = 101.7$$

$$C \approx 78.3$$

PTS: 2 REF: 081006a2 STA: A2.A.75 TOP: Law of Sines - The Ambiguous Case

188 ANS: 1

$$13^2 = 15^2 + 14^2 - 2(15)(14) \cos C$$

$$169 = 421 - 420 \cos C$$

$$-252 = -420 \cos C$$

$$\frac{252}{420} = \cos C$$

$$53 \approx C$$

PTS: 2 REF: 061110a2 STA: A2.A.73 TOP: Law of Cosines

KEY: find angle

189 ANS: 4

$$7^2 = 3^2 + 5^2 - 2(3)(5)\cos A$$

$$49 = 34 - 30\cos A$$

$$15 = -30\cos A$$

$$-\frac{1}{2} = \cos A$$

$$120 = \cos A$$

PTS: 2 REF: 081017a2 STA: A2.A.73 TOP: Law of Cosines

KEY: angle, without calculator

190 ANS:

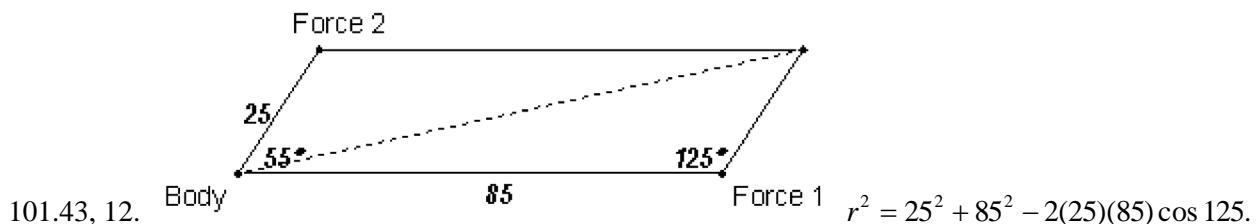
33. $a = \sqrt{10^2 + 6^2 - 2(10)(6)\cos 80} \approx 10.7$. $\angle C$ is opposite the shortest side. $\frac{6}{\sin C} = \frac{10.7}{\sin 80}$

$$C \approx 33$$

PTS: 6 REF: 061039a2 STA: A2.A.73 TOP: Law of Cosines

KEY: advanced

191 ANS:



$$r^2 = 25^2 + 85^2 - 2(25)(85)\cos 125.$$

$$r^2 \approx 10287.7$$

$$r \approx 101.43$$

$$\frac{2.5}{\sin x} = \frac{101.43}{\sin 125}$$

$$x \approx 12$$

PTS: 6 REF: fall0939a2 STA: A2.A.73 TOP: Vectors

192 ANS: 2

$$x^2 - 2x + y^2 + 6y = -3$$

$$x^2 - 2x + 1 + y^2 + 6y + 9 = -3 + 1 + 9$$

$$(x - 1)^2 + (y + 3)^2 = 7$$

PTS: 2 REF: 061016a2 STA: A2.A.47 TOP: Equations of Circles

193 ANS:

$$(x + 3)^2 + (y - 4)^2 = 25$$

PTS: 2 REF: fall0929a2 STA: A2.A.49 TOP: Writing Equations of Circles

194 ANS:

$$(x + 5)^2 + (y - 3)^2 = 32$$

PTS: 2

REF: 081033a2

STA: A2.A.49

TOP: Writing Equations of Circles

195 ANS: 2

PTS: 2

REF: 011126a2

STA: A2.A.49

TOP: Equations of Circles