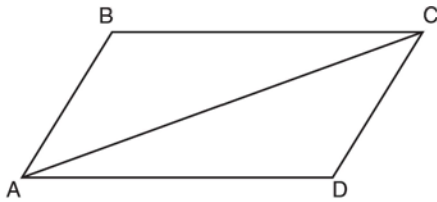


**G.SRT.B.5: Quadrilateral Proofs**

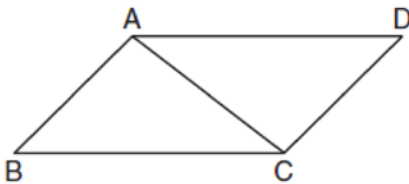
- 1 Given that  $ABCD$  is a parallelogram, a student wrote the proof below to show that a pair of opposite angles are congruent.



Statement	Reason
1. $ABCD$ is a parallelogram.	1. Given
2. $\overline{BC} \cong \overline{AD}$ $\overline{AB} \cong \overline{DC}$	2. Opposite sides of a parallelogram are congruent.
3. $\overline{AC} \cong \overline{CA}$	3. Reflexive Postulate of Congruency
4. $\triangle ABC \cong \triangle CDA$	4. Side-Side-Side
5. $\angle B \cong \angle D$	5. _____

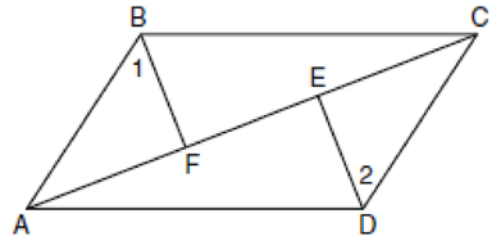
What is the reason justifying that  $\angle B \cong \angle D$ ?

- 1) Opposite angles in a quadrilateral are congruent.
  - 2) Parallel lines have congruent corresponding angles.
  - 3) Corresponding parts of congruent triangles are congruent.
  - 4) Alternate interior angles in congruent triangles are congruent.
- 2 Given: Parallelogram  $ABCD$  with diagonal  $\overline{AC}$  drawn

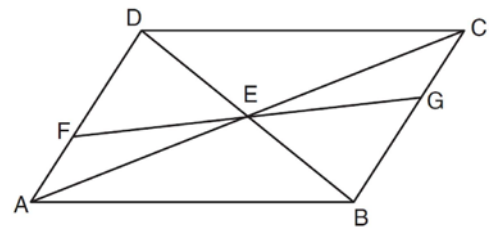


Prove:  $\triangle ABC \cong \triangle CDA$

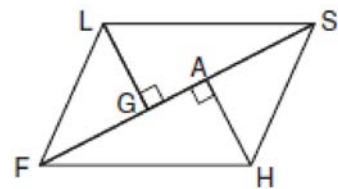
- 3 Given: Quadrilateral  $ABCD$ , diagonal  $\overline{AFEC}$ ,  $\overline{AE} \cong \overline{FC}$ ,  $\overline{BF} \perp \overline{AC}$ ,  $\overline{DE} \perp \overline{AC}$ ,  $\angle 1 \cong \angle 2$   
Prove:  $ABCD$  is a parallelogram.



- 4 In the diagram below of quadrilateral  $ABCD$ ,  $\overline{AD} \cong \overline{BC}$  and  $\angle DAE \cong \angle BCE$ . Line segments  $\overline{AC}$ ,  $\overline{DB}$ , and  $\overline{FG}$  intersect at  $E$ . Prove:  $\triangle AEF \cong \triangle CEG$

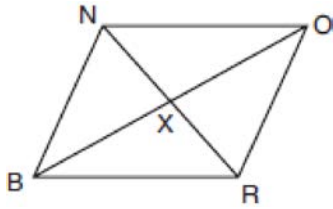


- 5 Given: parallelogram  $FLSH$ , diagonal  $\overline{FGAS}$ ,  $\overline{LG} \perp \overline{FS}$ ,  $\overline{HA} \perp \overline{FS}$



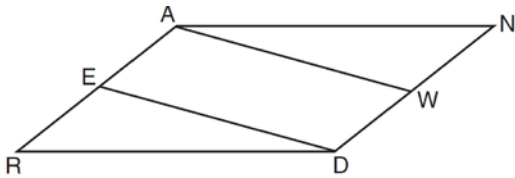
Prove:  $\triangle LGS \cong \triangle HAF$

- 6 The accompanying diagram shows quadrilateral  $BRON$ , with diagonals  $\overline{NR}$  and  $\overline{BO}$ , which bisect each other at  $X$ .



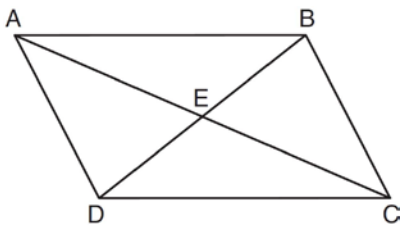
Prove:  $\triangle BNX \cong \triangle ORX$

- 7 Given: Parallelogram  $ANDR$  with  $\overline{AW}$  and  $\overline{DE}$  bisecting  $\overline{NWD}$  and  $\overline{REA}$  at points  $W$  and  $E$ , respectively



Prove that  $\triangle ANW \cong \triangle DRE$ . Prove that quadrilateral  $AWDE$  is a parallelogram.

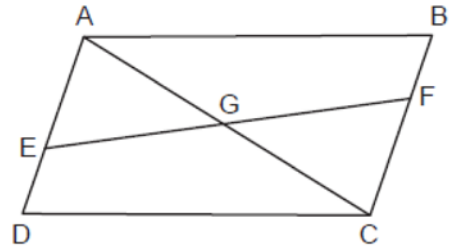
- 8 Given: Quadrilateral  $ABCD$  is a parallelogram with diagonals  $\overline{AC}$  and  $\overline{BD}$  intersecting at  $E$



Prove:  $\triangle AED \cong \triangle CEB$

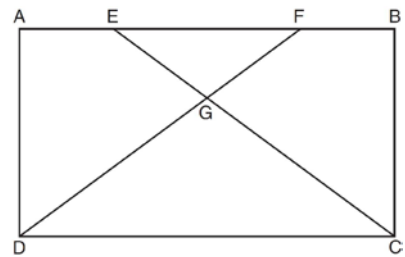
Describe a single rigid motion that maps  $\triangle AED$  onto  $\triangle CEB$ .

- 9 Given: Quadrilateral  $ABCD$ ,  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AB} \parallel \overline{CD}$ , diagonal  $\overline{AC}$  intersects  $\overline{EF}$  at  $G$ , and  $\overline{DE} \cong \overline{BF}$

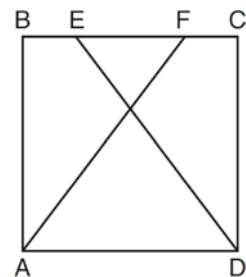


Prove:  $G$  is the midpoint of  $\overline{EF}$

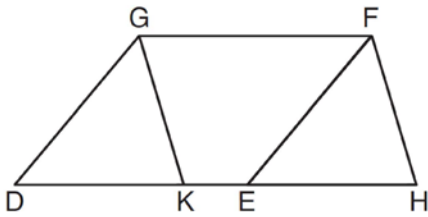
- 10 The diagram below shows rectangle  $ABCD$  with points  $E$  and  $F$  on side  $\overline{AB}$ . Segments  $\overline{CE}$  and  $\overline{DF}$  intersect at  $G$ , and  $\angle ADG \cong \angle BCG$ . Prove:  $\overline{AE} \cong \overline{BF}$



- 11 The diagram below shows square  $ABCD$  where  $E$  and  $F$  are points on  $\overline{BC}$  such that  $\overline{BE} \cong \overline{FC}$ , and segments  $\overline{AF}$  and  $\overline{DE}$  are drawn. Prove that  $\overline{AF} \cong \overline{DE}$ .

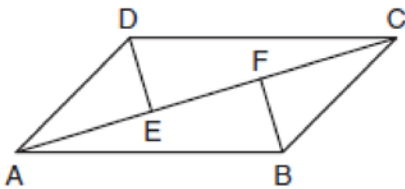


- 12 Given: Parallelogram  $DEFG$ ,  $K$  and  $H$  are points on  $\overline{DE}$  such that  $\angle DGK \cong \angle EFH$  and  $\overline{GK}$  and  $\overline{FH}$  are drawn.



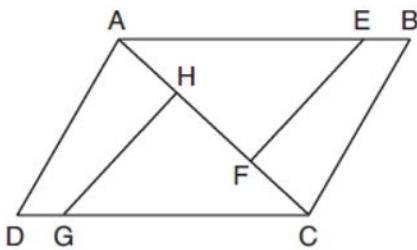
Prove:  $\overline{DK} \cong \overline{EH}$

- 13 In quadrilateral  $ABCD$ ,  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AB} \parallel \overline{CD}$ , and  $\overline{BF}$  and  $\overline{DE}$  are perpendicular to diagonal  $\overline{AC}$  at points  $F$  and  $E$ .



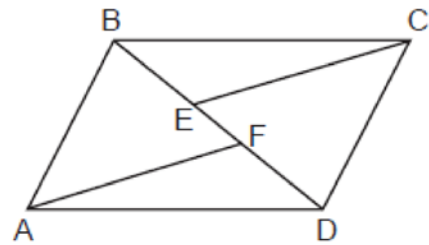
Prove:  $\overline{AE} \cong \overline{CF}$

- 14 In the diagram of quadrilateral  $ABCD$  with diagonal  $\overline{AC}$  shown below, segments  $\overline{GH}$  and  $\overline{EF}$  are drawn,  $\overline{AE} \cong \overline{CG}$ ,  $\overline{BE} \cong \overline{DG}$ ,  $\overline{AH} \cong \overline{CF}$ , and  $\overline{AD} \cong \overline{CB}$ .



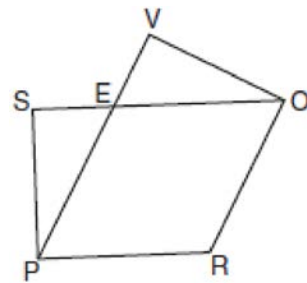
Prove:  $\overline{EF} \cong \overline{GH}$

- 15 In the diagram of quadrilateral  $ABCD$  below,  $\overline{AB} \cong \overline{CD}$ , and  $\overline{AB} \parallel \overline{CD}$ . Segments  $\overline{CE}$  and  $\overline{AF}$  are drawn to diagonal  $\overline{BD}$  such that  $\overline{BE} \cong \overline{DF}$ .



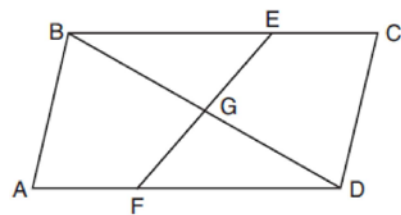
Prove:  $\overline{CE} \cong \overline{AF}$

- 16 Given:  $PROE$  is a rhombus,  $\overline{SEO}$ ,  $\overline{PEV}$ ,  $\angle SPR \cong \angle VOR$



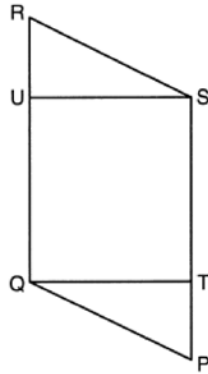
Prove:  $\overline{SE} \cong \overline{EV}$

- 17 In quadrilateral  $ABCD$ ,  $E$  and  $F$  are points on  $\overline{BC}$  and  $\overline{AD}$ , respectively, and  $\overline{BGD}$  and  $\overline{EGF}$  are drawn such that  $\angle ABG \cong \angle CDG$ ,  $\overline{AB} \cong \overline{CD}$ , and  $\overline{CE} \cong \overline{AF}$ .



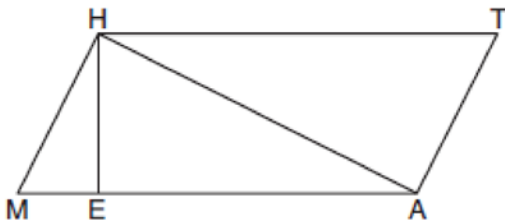
Prove:  $\overline{FG} \cong \overline{EG}$

- 18 Given: Parallelogram  $PQRS$ ,  $\overline{QT} \perp \overline{PS}$ ,  $\overline{SU} \perp \overline{QR}$



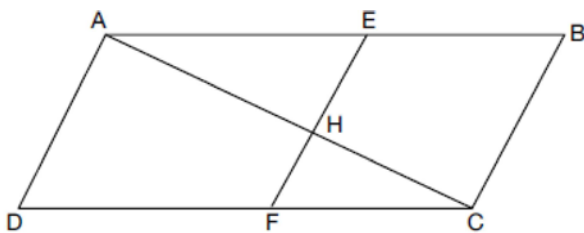
Prove:  $\overline{PT} \cong \overline{RU}$

- 19 Given: Quadrilateral  $MATH$ ,  $\overline{HM} \cong \overline{AT}$ ,  $\overline{HT} \cong \overline{AM}$ ,  $\overline{HE} \perp \overline{ME}$ , and  $\overline{HA} \perp \overline{AT}$



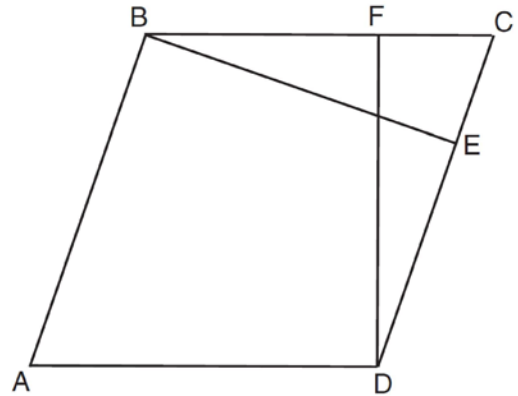
Prove:  $TA \cdot HA = HE \cdot TH$

- 20 Given: Quadrilateral  $ABCD$ ,  $\overline{AC}$  and  $\overline{EF}$  intersect at  $H$ ,  $\overline{EF} \parallel \overline{AD}$ ,  $\overline{EF} \parallel \overline{BC}$ , and  $\overline{AD} \cong \overline{BC}$ .



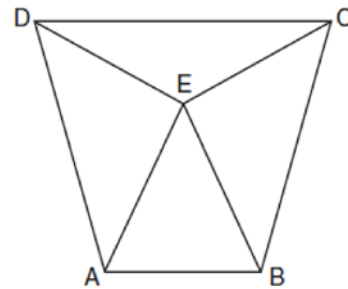
Prove:  $(EH)(CH) = (FH)(AH)$

- 21 In the diagram of parallelogram  $ABCD$  below,  $\overline{BE} \perp \overline{CED}$ ,  $\overline{DF} \perp \overline{BFC}$ ,  $\overline{CE} \cong \overline{CF}$ .



Prove  $ABCD$  is a rhombus.

- 22 Isosceles trapezoid  $ABCD$  has bases  $\overline{DC}$  and  $\overline{AB}$  with nonparallel legs  $\overline{AD}$  and  $\overline{BC}$ . Segments  $\overline{AE}$ ,  $\overline{BE}$ ,  $\overline{CE}$ , and  $\overline{DE}$  are drawn in trapezoid  $ABCD$  such that  $\angle CDE \cong \angle DCE$ ,  $\overline{AE} \perp \overline{DE}$ , and  $\overline{BE} \perp \overline{CE}$ .



Prove  $\triangle ADE \cong \triangle BCE$  and prove  $\triangle AEB$  is an isosceles triangle.

- 23 Given: Quadrilateral  $ABCD$  with  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AD} \cong \overline{BC}$ , and diagonal  $\overline{BD}$  is drawn  
Prove:  $\angle BDC \cong \angle ABD$

- 24 Prove that the diagonals of a parallelogram bisect each other.

- 25 A tricolored flag is made out of a rectangular piece of cloth whose corners are labeled  $A$ ,  $B$ ,  $C$ , and  $D$ . The colored regions are separated by two line segments,  $\overline{BM}$  and  $\overline{CM}$ , that meet at point  $M$ , the midpoint of side  $\overline{AD}$ . Prove that the two line segments that separate the regions will always be equal in length, regardless of the size of the flag.

## G.SRT.B.5: Quadrilateral Proofs

## Answer Section

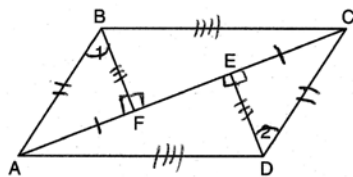
1 ANS: 3 REF: 081208ge

2 ANS:

Parallelogram  $ABCD$  with diagonal  $\overline{AC}$  drawn (given).  $\overline{AC} \cong \overline{AC}$  (reflexive property).  $\overline{AD} \cong \overline{CB}$  and  $\overline{BA} \cong \overline{DC}$  (opposite sides of a parallelogram are congruent).  $\triangle ABC \cong \triangle CDA$  (SSS).

REF: 011825geo

3 ANS:



$\overline{FE} \cong \overline{FE}$  (Reflexive Property);  $\overline{AE} - \overline{FE} \cong \overline{FC} - \overline{EF}$  (Line Segment Subtraction Theorem);  $\overline{AF} \cong \overline{CE}$  (Substitution);  $\angle BFA \cong \angle DEC$  (All right angles are congruent);  $\triangle BFA \cong \triangle DEC$  (AAS);  $\overline{AB} \cong \overline{CD}$  and  $\overline{BF} \cong \overline{DE}$  (CPCTC);  $\angle BFC \cong \angle DEA$  (All right angles are congruent);  $\triangle BFC \cong \triangle DEA$  (SAS);  $\overline{AD} \cong \overline{CB}$  (CPCTC);  $ABCD$  is a parallelogram (opposite sides of quadrilateral  $ABCD$  are congruent)

REF: 080938ge

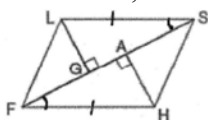
4 ANS:

Quadrilateral  $ABCD$ ,  $\overline{AD} \cong \overline{BC}$  and  $\angle DAE \cong \angle BCE$  are given.  $\overline{AD} \parallel \overline{BC}$  because if two lines are cut by a transversal so that a pair of alternate interior angles are congruent, the lines are parallel.  $ABCD$  is a parallelogram because if one pair of opposite sides of a quadrilateral are both congruent and parallel, the quadrilateral is a parallelogram.  $\overline{AE} \cong \overline{CE}$  because the diagonals of a parallelogram bisect each other.  $\angle FEA \cong \angle GEC$  as vertical angles.  $\triangle AEF \cong \triangle CEG$  by ASA.

REF: 011238ge

5 ANS:

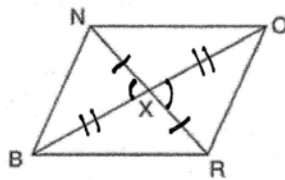
Because  $FLSH$  is a parallelogram,  $\overline{FH} \cong \overline{SL}$ . Because  $FLSH$  is a parallelogram,  $\overline{FH} \parallel \overline{SL}$  and since  $\overline{FGAS}$  is a transversal,  $\angle AFH$  and  $\angle LSG$  are alternate interior angles and congruent. Therefore  $\triangle LGS \cong \triangle HAF$  by AAS.



REF: 010634b

6 ANS:

Because diagonals  $\overline{NR}$  and  $\overline{BO}$  bisect each other,  $\overline{NX} \cong \overline{RX}$  and  $\overline{BX} \cong \overline{OX}$ .  $\angle BXN$  and  $\angle OXR$  are congruent



vertical angles. Therefore  $\triangle BNX \cong \triangle ORX$  by SAS.

REF: 080731b

7 ANS:

Parallelogram  $ANDR$  with  $\overline{AW}$  and  $\overline{DE}$  bisecting  $\overline{NWD}$  and  $\overline{REA}$  at points  $W$  and  $E$  (Given).  $\overline{AN} \cong \overline{RD}$ ,  $\overline{AR} \cong \overline{DN}$  (Opposite sides of a parallelogram are congruent).  $AE = \frac{1}{2}AR$ ,  $WD = \frac{1}{2}DN$ , so  $\overline{AE} \cong \overline{WD}$  (Definition of bisect and division property of equality).  $\overline{AR} \parallel \overline{DN}$  (Opposite sides of a parallelogram are parallel).  $AWDE$  is a parallelogram (Definition of parallelogram).  $RE = \frac{1}{2}AR$ ,  $NW = \frac{1}{2}DN$ , so  $\overline{RE} \cong \overline{NW}$  (Definition of bisect and division property of equality).  $\overline{ED} \cong \overline{AW}$  (Opposite sides of a parallelogram are congruent).  $\triangle ANW \cong \triangle DRE$  (SSS).

REF: 011635geo

8 ANS:

Quadrilateral  $ABCD$  is a parallelogram with diagonals  $\overline{AC}$  and  $\overline{BD}$  intersecting at  $E$  (Given).  $\overline{AD} \cong \overline{BC}$  (Opposite sides of a parallelogram are congruent).  $\angle AED \cong \angle CEB$  (Vertical angles are congruent).  $\overline{BC} \parallel \overline{DA}$  (Definition of parallelogram).  $\angle DBC \cong \angle BDA$  (Alternate interior angles are congruent).  $\triangle AED \cong \triangle CEB$  (AAS).  $180^\circ$  rotation of  $\triangle AED$  around point  $E$ .

REF: 061533geo

9 ANS:

Quadrilateral  $ABCD$ ,  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AB} \parallel \overline{CD}$ , diagonal  $\overline{AC}$  intersects  $\overline{EF}$  at  $G$ , and  $\overline{DE} \cong \overline{BF}$  (given);  $ABCD$  is a parallelogram (a quadrilateral with a pair of opposite sides  $\parallel$  is a parallelogram);  $\overline{AD} \cong \overline{CB}$  (opposite side of a parallelogram are congruent);  $\overline{AE} \cong \overline{CF}$  (subtraction postulate);  $\overline{AD} \parallel \overline{CB}$  (opposite side of a parallelogram are parallel);  $\angle EAG \cong \angle FCG$  (if parallel sides are cut by a transversal, the alternate interior angles are congruent);  $\angle AGE \cong \angle CGF$  (vertical angles);  $\triangle AEG \cong \triangle CFG$  (AAS);  $\overline{EG} \cong \overline{FG}$  (CPCTC):  $G$  is the midpoint of  $\overline{EF}$  (since  $G$  divides  $\overline{EF}$  into two equal parts,  $G$  is the midpoint of  $\overline{EF}$ ).

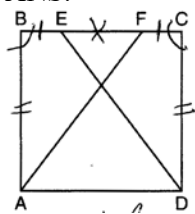
REF: 062335geo

10 ANS:

Rectangle  $ABCD$  with points  $E$  and  $F$  on side  $\overline{AB}$ , segments  $\overline{CE}$  and  $\overline{DF}$  intersect at  $G$ , and  $\angle ADG \cong \angle BCE$  are given.  $\overline{AD} \cong \overline{BC}$  because opposite sides of a rectangle are congruent.  $\angle A$  and  $\angle B$  are right angles and congruent because all angles of a rectangle are right and congruent.  $\triangle ADF \cong \triangle BCE$  by ASA.  $\overline{AF} \cong \overline{BE}$  per CPCTC.  $\overline{EF} \cong \overline{FE}$  under the Reflexive Property.  $\overline{AF} - \overline{EF} \cong \overline{BE} - \overline{FE}$  using the Subtraction Property of Segments.  $\overline{AE} \cong \overline{BF}$  because of the Definition of Segments.

REF: 011338ge

11 ANS:

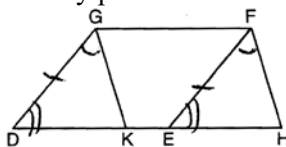


Square  $ABCD$ ;  $E$  and  $F$  are points on  $\overline{BC}$  such that  $\overline{BE} \cong \overline{FC}$ ;  $\overline{AF}$  and  $\overline{DE}$  drawn (Given).  
 $\overline{AB} \cong \overline{CD}$  (All sides of a square are congruent).  $\angle ABF \cong \angle DCE$  (All angles of a square are equiangular).  
 $\overline{EF} \cong \overline{FE}$  (Reflexive property).  $\overline{BE} + \overline{EF} \cong \overline{FC} + \overline{FE}$  (Additive property of line segments).  $\overline{BF} \cong \overline{CE}$  (Angle addition).  $\triangle ABF \cong \triangle DCE$  (SAS).  $\overline{AF} \cong \overline{DE}$  (CPCTC).

REF: 061538ge

12 ANS:

Parallelogram  $DEFG$ ,  $K$  and  $H$  are points on  $\overline{DE}$  such that  $\angle DGK \cong \angle EFH$  and  $\overline{GK}$  and  $\overline{FH}$  are drawn (given).  
 $\overline{DG} \cong \overline{EF}$  (opposite sides of a parallelogram are congruent).  $\overline{DG} \parallel \overline{EF}$  (opposite sides of a parallelogram are parallel).  $\angle D \cong \angle FEH$  (corresponding angles formed by parallel lines and a transversal are congruent).



$\triangle DGK \cong \triangle EFH$  (ASA).  $\overline{DK} \cong \overline{EH}$  (CPCTC).

REF: 081538ge

13 ANS:

Quadrilateral  $ABCD$ ,  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AB} \parallel \overline{CD}$ , and  $\overline{BF}$  and  $\overline{DE}$  are perpendicular to diagonal  $\overline{AC}$  at points  $F$  and  $E$  (given).  $\angle AED$  and  $\angle CFB$  are right angles (perpendicular lines form right angles).  $\angle AED \cong \angle CFB$  (All right angles are congruent).  $ABCD$  is a parallelogram (A quadrilateral with one pair of sides congruent and parallel is a parallelogram).  $\overline{AD} \parallel \overline{BC}$  (Opposite sides of a parallelogram are parallel).  $\angle DAE \cong \angle BCF$  (Parallel lines cut by a transversal form congruent alternate interior angles).  $\overline{DA} \cong \overline{BC}$  (Opposite sides of a parallelogram are congruent).  $\triangle ADE \cong \triangle CBF$  (AAS).  $\overline{AE} \cong \overline{CF}$  (CPCTC).

REF: 011735geo

14 ANS:

Quadrilateral  $ABCD$  with diagonal  $\overline{AC}$ , segments  $\overline{GH}$  and  $\overline{EF}$ ,  $\overline{AE} \cong \overline{CG}$ ,  $\overline{BE} \cong \overline{DG}$ ,  $\overline{AH} \cong \overline{CF}$ , and  $\overline{AD} \cong \overline{CB}$  (given);  $\overline{HF} \cong \overline{HF}$ ,  $\overline{AC} \cong \overline{AC}$  (reflexive property);  $\overline{AH} + \overline{HF} \cong \overline{CF} + \overline{HF}$ ,  $\overline{AE} + \overline{BE} \cong \overline{CG} + \overline{DG}$  (segment

$$\overline{AF} \cong \overline{CH} \qquad \overline{AB} \cong \overline{CD}$$

addition);  $\triangle ABC \cong \triangle CDA$  (SSS);  $\angle EAF \cong \angle GCH$  (CPCTC);  $\triangle AEF \cong \triangle CGH$  (SAS);  $\overline{EF} \cong \overline{GH}$  (CPCTC).

REF: 011935geo

15 ANS:

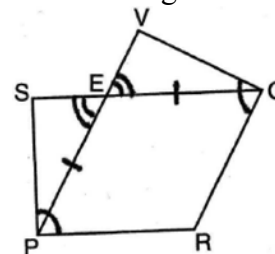
In quadrilateral  $ABCD$ ,  $\overline{AB} \cong \overline{CD}$  and  $\overline{AB} \parallel \overline{CD}$ , segments  $\overline{CE}$  and  $\overline{AF}$  are drawn to diagonal  $\overline{BD}$  such that  $\overline{BE} \cong \overline{DF}$  (Given);  $\angle ABF \cong \angle CDE$  (Parallel lines cut by a transversal form congruent interior angles);  $\overline{EF} \cong \overline{FE}$  (Reflexive);  $\overline{BE} + \overline{EF} \cong \overline{DF} + \overline{FE}$  (Addition);  $\triangle AFB \cong \triangle CED$  (SAS);  $\overline{CE} \cong \overline{AF}$  (CPCTC).

$$\overline{BF} \cong \overline{DE}$$

REF: 012434geo

16 ANS:

Because  $PROE$  is a rhombus,  $\overline{PE} \cong \overline{OE}$ .  $\angle SEP \cong \angle VEO$  are congruent vertical angles.  $\angle EPR \cong \angle EOR$  because opposite angles of a rhombus are congruent.  $\angle SPE \cong \angle VOE$  because of the Angle Subtraction



Theorem.  $\triangle SEP \cong \triangle VEO$  because of ASA.  $\overline{SE} \cong \overline{EV}$  because of CPCTC.

REF: 010934b

17 ANS:

Quadrilateral  $ABCD$ ,  $E$  and  $F$  are points on  $\overline{BC}$  and  $\overline{AD}$ , respectively, and  $\overline{BGD}$  and  $\overline{EGF}$  are drawn such that  $\angle ABG \cong \angle CDG$ ,  $\overline{AB} \cong \overline{CD}$ , and  $\overline{CE} \cong \overline{AF}$  (given);  $\overline{BD} \cong \overline{BD}$  (reflexive);  $\triangle ABD \cong \triangle CDB$  (SAS);  $\overline{BC} \cong \overline{DA}$  (CPCTC);  $\overline{BE} + \overline{CE} \cong \overline{AF} + \overline{DF}$  (segment addition);  $\overline{BE} \cong \overline{DF}$  (segment subtraction);  $\angle BGE \cong \angle DGF$  (vertical angles are congruent);  $\angle CBD \cong \angle ADB$  (CPCTC);  $\triangle EBG \cong \triangle FDG$  (AAS);  $\overline{FG} \cong \overline{EG}$  (CPCTC).

REF: 012035geo

18 ANS:

Parallelogram  $PQRS$ ,  $\overline{QT} \perp \overline{PS}$ ,  $\overline{SU} \perp \overline{QR}$  (given);  $\overline{QR} \cong \overline{PS}$  (opposite sides of a parallelogram are parallel); Quadrilateral  $QUST$  is a rectangle (quadrilateral with parallel opposite sides and opposite right angles is a rectangle);  $\overline{SU} \cong \overline{QT}$  (opposite sides of a rectangle are congruent);  $\overline{RS} \cong \overline{PQ}$  (opposite sides of a parallelogram are congruent);  $\angle RUS$  and  $\angle PTQ$  are right angles (the supplement of a right angle is a right angle),  $\triangle RSU \cong \triangle PQT$  (HL);  $\overline{PT} \cong \overline{RU}$  (CPCTC)

REF: 062233geo

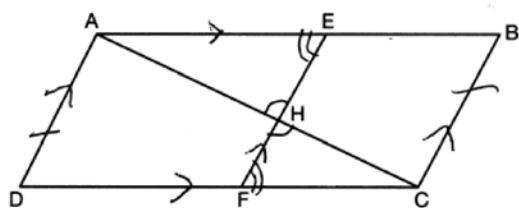
19 ANS:

Quadrilateral  $MATH$ ,  $\overline{HM} \cong \overline{AT}$ ,  $\overline{HT} \cong \overline{AM}$ ,  $\overline{HE} \perp \overline{MEA}$ , and  $\overline{HA} \perp \overline{AT}$  (given);  $\angle HEA$  and  $\angle TAH$  are right angles (perpendicular lines form right angles);  $\angle HEA \cong \angle TAH$  (all right angles are congruent);  $MATH$  is a parallelogram (a quadrilateral with two pairs of congruent opposite sides is a parallelogram);  $\overline{MA} \parallel \overline{TH}$  (opposite sides of a parallelogram are parallel);  $\angle THA \cong \angle EAH$  (alternate interior angles of parallel lines and a transversal are congruent);  $\triangle HEA \sim \triangle TAH$  (AA);  $\frac{HA}{TH} = \frac{HE}{TA}$  (corresponding sides of similar triangles are in proportion);  $TA \cdot HA = HE \cdot TH$  (product of means equals product of extremes).

REF: 061935geo



20 ANS:



1) Quadrilateral  $ABCD$ ,  $\overline{AC}$  and  $\overline{EF}$  intersect at  $H$ ,  $\overline{EF} \parallel \overline{AD}$ ,  $\overline{EF} \parallel \overline{BC}$ , and  $\overline{AD} \cong \overline{BC}$  (Given); 2)  $\angle EHA \cong \angle FHC$  (Vertical angles are congruent); 3)  $\overline{AD} \parallel \overline{BC}$  (Transitive property of parallel lines); 4)  $ABCD$  is a parallelogram (Quadrilateral with a pair of sides both parallel and congruent); 5)  $\overline{AB} \parallel \overline{CD}$  (Opposite sides of a parallelogram); 6)  $\angle AEH \cong \angle CFH$  (Alternate interior angles formed by parallel lines and a transversal); 7)  $\triangle AEH \sim \triangle CFH$  (AA); 8)  $\frac{EH}{FH} = \frac{AH}{CH}$  (Corresponding sides of similar triangles are proportional); 8)  $(EH)(CH) = (FH)(AH)$  (Product of means equals product of extremes).

REF: 082235geo

21 ANS:

Parallelogram  $ABCD$ ,  $\overline{BE} \perp \overline{CED}$ ,  $\overline{DF} \perp \overline{BFC}$ ,  $\overline{CE} \cong \overline{CF}$  (given).  $\angle BEC \cong \angle DFC$  (perpendicular lines form right angles, which are congruent).  $\angle FCD \cong \angle BCE$  (reflexive property).  $\triangle BEC \cong \triangle DFC$  (ASA).  $\overline{BC} \cong \overline{CD}$  (CPCTC).  $ABCD$  is a rhombus (a parallelogram with consecutive congruent sides is a rhombus).

REF: 081535geo

22 ANS:

Isosceles trapezoid  $ABCD$ ,  $\angle CDE \cong \angle DCE$ ,  $\overline{AE} \perp \overline{DE}$ , and  $\overline{BE} \perp \overline{CE}$  (given);  $\overline{AD} \cong \overline{BC}$  (congruent legs of isosceles trapezoid);  $\angle DEA$  and  $\angle CEB$  are right angles (perpendicular lines form right angles);  $\angle DEA \cong \angle CEB$  (all right angles are congruent);  $\angle CDA \cong \angle DCB$  (base angles of an isosceles trapezoid are congruent);  $\angle CDA - \angle CDE \cong \angle DCB - \angle DCE$  (subtraction postulate);  $\triangle ADE \cong \triangle BCE$  (AAS);  $\overline{EA} \cong \overline{EB}$  (CPCTC);

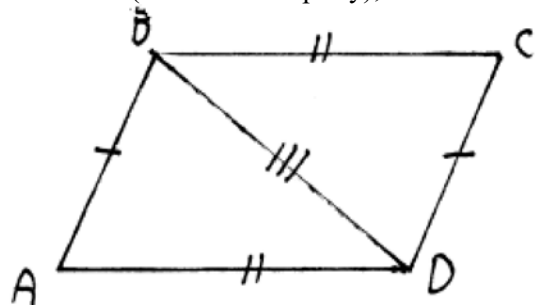
$$\angle EDA \cong \angle ECB$$

$\triangle AEB$  is an isosceles triangle (an isosceles triangle has two congruent sides).

REF: 081735geo

23 ANS:

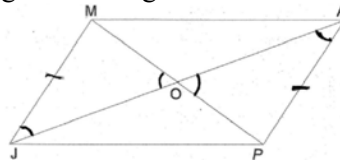
$\overline{BD} \cong \overline{DB}$  (Reflexive Property);  $\triangle ABD \cong \triangle CDB$  (SSS);  $\angle BDC \cong \angle ABD$  (CPCTC).



REF: 061035ge

24 ANS:

Assume parallelogram  $JMAP$  with diagonals intersecting at  $O$ . Opposite sides of a parallelogram are congruent, so  $\overline{JM} \cong \overline{AP}$ .  $\angle JOM$  and  $\angle AOP$  are congruent vertical angles. Because  $JMAP$  is a parallelogram,  $\overline{JM} \parallel \overline{AP}$  and since  $\overline{JOA}$  is a transversal,  $\angle MJO$  and  $\angle PAO$  are alternate interior angles and congruent. Therefore  $\triangle MJO \cong \triangle PAO$  by AAS. Corresponding parts of congruent triangles are congruent. Therefore  $\overline{JO} \cong \overline{AO}$  and

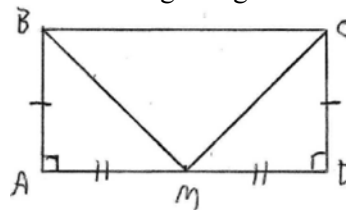


$\overline{MO} \cong \overline{PO}$  and the diagonals of a parallelogram bisect each other.

REF: 010233b

25 ANS:

$\overline{AB} \cong \overline{CD}$ , because opposite sides of a rectangle are congruent.  $\overline{AM} \cong \overline{DM}$ , because of the definition of midpoint.  $\angle A$  and  $\angle D$  are right angles because a rectangle has four right angles.  $\angle A \cong \angle D$ , because all right angles are



congruent.  $\triangle ABM \cong \triangle DCM$ , because of SAS.  $\overline{BM} \cong \overline{CM}$  because of CPCTC.

REF: 080834b